# Programming Languages and Compilers (CS 421)

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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

## Using Ocamlyacc

- Input attribute grammar is put in file < grammar>.mly
- Execute

ocamlyacc < grammar>.mly

Produces code for parser in

< grammar>.ml

and interface (including type declaration for tokens) in

< grammar>.mli



- < grammar>.ml defines one parsing function per entry point
- Parsing function takes a lexing function (lexer buffer to token) and a lexer buffer as arguments
- Returns semantic attribute of corresponding entry point

### Ocamlyacc Input

File format:

```
%{
   <header>
%}
   <declarations>
%%
   <rules>
%%
   <trailer>
```



- Contains arbitrary Ocaml code
- Typically used to give types and functions needed for the semantic actions of rules and to give specialized error recovery
- May be omitted
- <footer> similar. Possibly used to call parser

## Ocamlyacc <declarations>

- %token symbol ... symbol
- Declare given symbols as tokens
- %token <type> symbol ... symbol
- Declare given symbols as token constructors, taking an argument of type <type>
- %start symbol ... symbol
- Declare given symbols as entry points; functions of same names in < grammar>.ml

### Ocamlyacc < declarations>

- %type <type> symbol ... symbol
   Specify type of attributes for given symbols.
   Mandatory for start symbols
- %left symbol ... symbol
- %right symbol ... symbol
- %nonassoc symbol ... symbol
   Associate precedence and associativity to given symbols. Same line, same precedence; earlier line, lower precedence (broadest scope)

## Ocamlyacc < rules>

```
nonterminal:
    symbol ... symbol { semantic_action }
    ...
    symbol ... symbol { semantic_action }
    ;
```

- Semantic actions are arbitrary Ocamle expressions
- Must be of same type as declared (or inferred) for nonterminal
- Access semantic attributes (values) of symbols by position: \$1 for first symbol, \$2 to second ...

### Example - Base types

```
(* File: expr.ml *)
type expr =
  Term_as_Expr of term
 | Plus Expr of (term * expr)
 | Minus Expr of (term * expr)
and term =
   Factor as Term of factor
  Mult_Term of (factor * term)
  Div Term of (factor * term)
and factor =
  Id as Factor of string
  Parenthesized Expr as Factor of expr
```

### Example - Lexer (exprlex.mll)

```
{ (*open Exprparse*) }
let numeric = \lceil '0' - '9' \rceil
let letter = ['a' - 'z' 'A' - 'Z']
rule token = parse
 | "+" {Plus token}
 | "-" {Minus_token}
 | "*" {Times_token}
 | "/" {Divide token}
  "(" {Left_parenthesis}
  ")" {Right parenthesis}
  | letter (letter|numeric|"_")* as id {Id_token id}
  [' ' '\t' '\n'] {token lexbuf}
  eof {EOL}
```

### Example - Parser (exprparse.mly)

```
%{ open Expr
%}
%token <string> Id_token
%token Left_parenthesis Right_parenthesis
%token Times token Divide token
%token Plus token Minus token
%token EOL
%start main
%type <expr> main
%%
```

### Example - Parser (exprparse.mly)

```
term
     term_as_Expr $1 }
| term Plus_token expr
     { Plus_Expr ($1, $3) }
| term Minus_token expr
     { Minus_Expr ($1, $3) }
```

### Example - Parser (exprparse.mly)

### 

{ Div Term (\$1, \$3) }

### Example - Parser (exprparse.mly)

```
factor:
  Id token
    { Id_as_Factor $1 }
| Left_parenthesis expr Right_parenthesis
    {Parenthesized_Expr_as_Factor $2 }
main:
expr EOL
     { $1 }
```

### Example - Using Parser

```
# #use "expr.ml";;
# #use "exprparse.ml";;
# #use "exprlex.ml";;
# let test s =
 let lexbuf = Lexing.from_string (s^"\n") in
     main token lexbuf;;
```

#### Example - Using Parser

```
# test "a + b";;
-: expr =
Plus_Expr
(Factor_as_Term (Id_as_Factor "a"),
  Term_as_Expr (Factor_as_Term
  (Id_as_Factor "b")))
```

## LR Parsing

- Read tokens left to right (L)
- Create a rightmost derivation (R)
- How is this possible?
- Start at the bottom (left) and work your way up
- Last step has only one non-terminal to be replaced so is right-most
- Working backwards, replace mixed strings by non-terminals
- Always proceed so that there are no nonterminals to the right of the string to be replaced

$$=$$
 (0 + 1) + 0 shift

= 
$$(0 + 1) + 0$$
 shift  
=  $(0 + 1) + 0$  shift

$$=> (0 + 1) + 0$$
 reduce  
=  $(0 + 1) + 0$  shift  
=  $(0 + 1) + 0$  shift

```
=> ( <Sum> + <Sum> ) + 0 reduce

=> ( <Sum> + 1 ) + 0 reduce

= ( <Sum> + 1 ) + 0 shift

= ( <Sum> + 1 ) + 0 shift

=> ( 0 + 1 ) + 0 reduce

= ( 0 + 1 ) + 0 shift

= ( 0 + 1 ) + 0 shift
```

<Sum> =>

```
=> ( <Sum > ) - + 0
                         reduce
shift
=> ( <Sum> + <Sum> ● ) + 0 reduce
=> ( <Sum > + 1   ) + 0
                     reduce
= ( <Sum > +   1 ) + 0
                        shift
= ( <Sum >   + 1 ) + 0
                        shift
=> (0   + 1) + 0
                         reduce
= (00 + 1) + 0
                         shift
= (0+1)+0
                         shift
```

<Sum> =>

```
= <Sum> + 0
                        shift
=> ( <Sum > ) - + 0
                        reduce
shift
=> ( <Sum> + <Sum> ● ) + 0 reduce
=> ( <Sum > + 1   ) + 0
                     reduce
= ( <Sum > +   1 ) + 0
                        shift
= ( <Sum >   + 1 ) + 0
                        shift
=> (0   + 1) + 0
                        reduce
= (00 + 1) + 0
                        shift
= (0+1)+0
                        shift
```

<Sum> =>

```
= <Sum> + 0
                        shift
= <Sum> + 0
                        shift
=> ( <Sum > ) - + 0
                       reduce
shift
=> ( <Sum> + <Sum> ● ) + 0 reduce
=> ( <Sum > + 1   ) + 0
                     reduce
= ( <Sum > +   1 ) + 0
                        shift
= ( <Sum >   + 1 ) + 0
                        shift
=> (0   + 1) + 0
                        reduce
= (00 + 1) + 0
                        shift
= (0+1)+0
                        shift
```

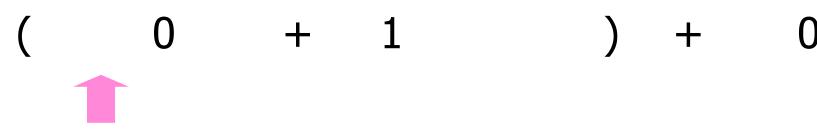
## E

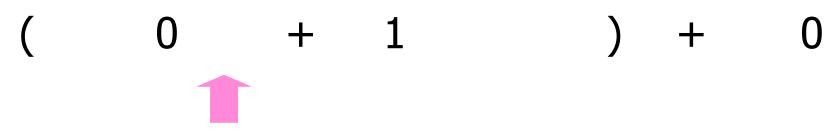
```
<Sum>
       =>
         => <Sum> + 0
                                 reduce
         = <Sum> + 0
                                 shift
         = <Sum> + 0
                                 shift
         => ( <Sum > ) - + 0
                                reduce
         shift
         => ( <Sum> + <Sum> ● ) + 0 reduce
         => ( <Sum > + 1   ) + 0
                             reduce
         = ( <Sum > +   1 ) + 0
                                 shift
         = ( <Sum >   + 1 ) + 0
                                 shift
         => (0   + 1) + 0
                                 reduce
         = (00 + 1) + 0
                                 shift
         = (0+1)+0
                                 shift
```

```
<Sum> => <Sum> + <Sum > • reduce
        => <Sum> + 0
                                reduce
         = <Sum> + 0
                                shift
                                shift
         = <Sum> + 0
         => ( <Sum > ) - + 0
                                reduce
         shift
         => ( <Sum> + <Sum> ● ) + 0 reduce
         => ( <Sum > + 1   ) + 0
                             reduce
         = ( <Sum > +   1 ) + 0
                                 shift
         = ( <Sum >   + 1 ) + 0
                                 shift
         => (0   + 1) + 0
                                 reduce
         = (00 + 1) + 0
                                 shift
         = (0+1)+0
                                 shift
```

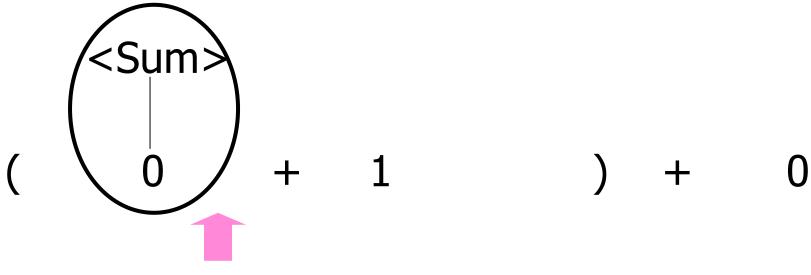
```
<Sum> => <Sum> + <Sum > =
                                reduce
        => <Sum> + 0
                                reduce
         = <Sum> + 0
                                shift
                                shift
         = <Sum> + 0
         => ( <Sum > ) - + 0
                                reduce
         shift
         => ( <Sum> + <Sum> ● ) + 0 reduce
         => ( <Sum > + 1   ) + 0
                             reduce
         = ( <Sum > +   1 ) + 0
                                shift
         = ( <Sum >   + 1 ) + 0
                                 shift
         => (0   + 1) + 0
                                 reduce
         = (00 + 1) + 0
                                 shift
         = (0+1)+0
                                 shift
```

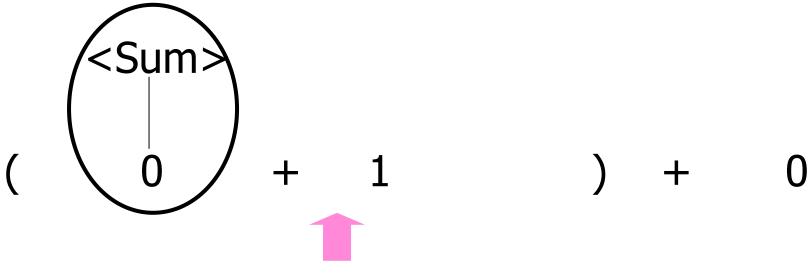
( 0 + 1 ) + 0



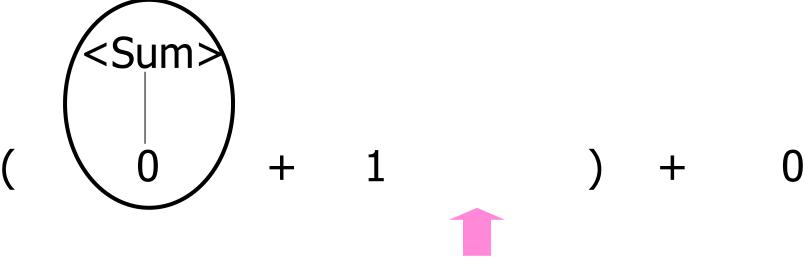




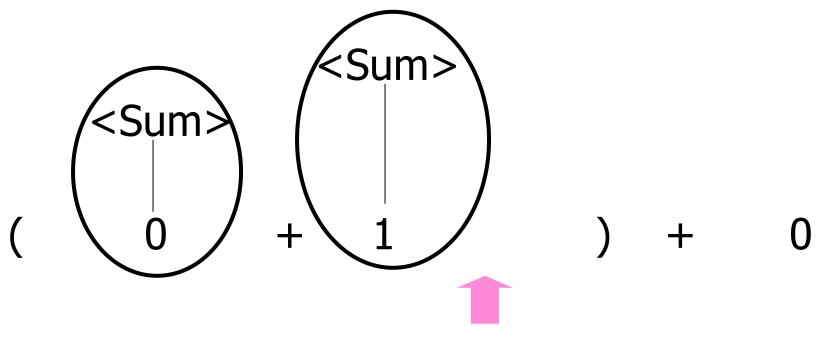




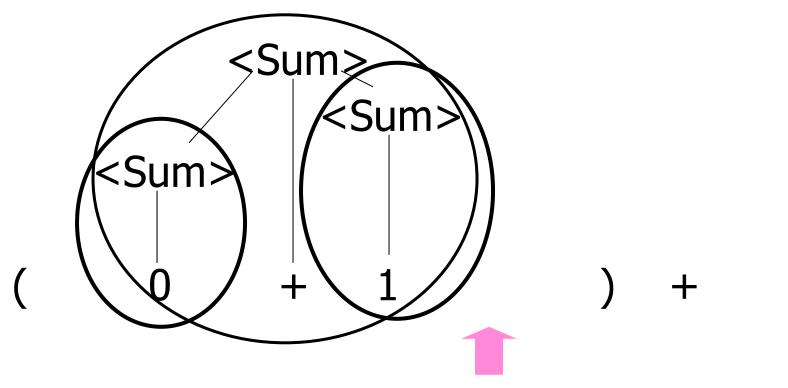
# Example



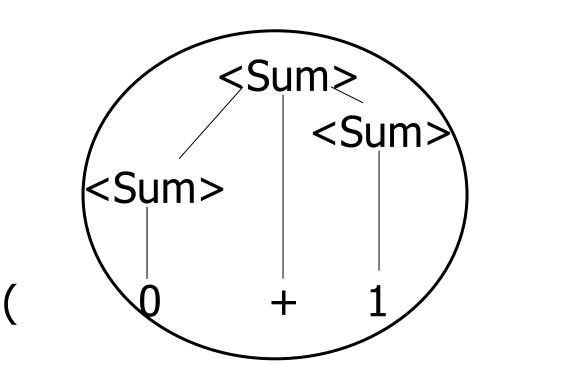






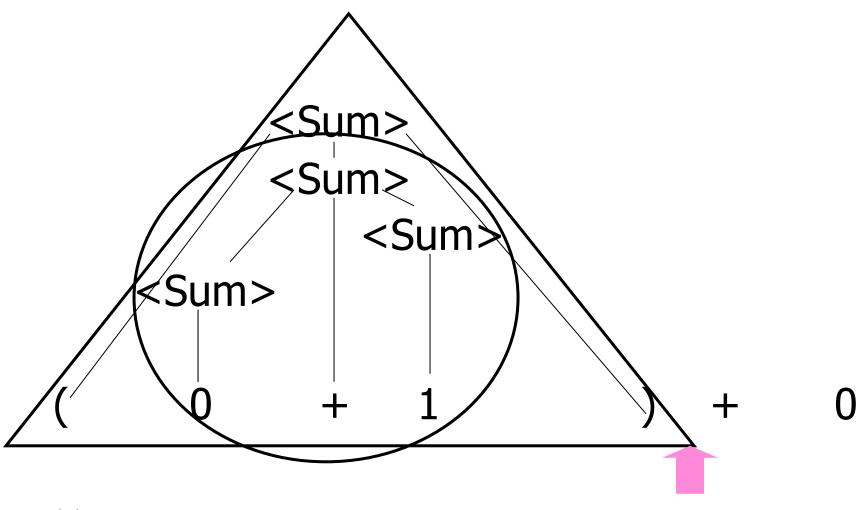




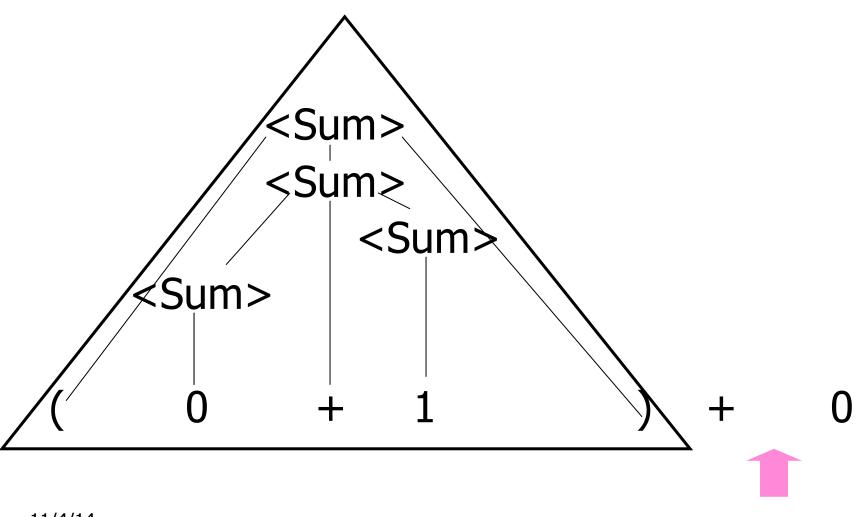




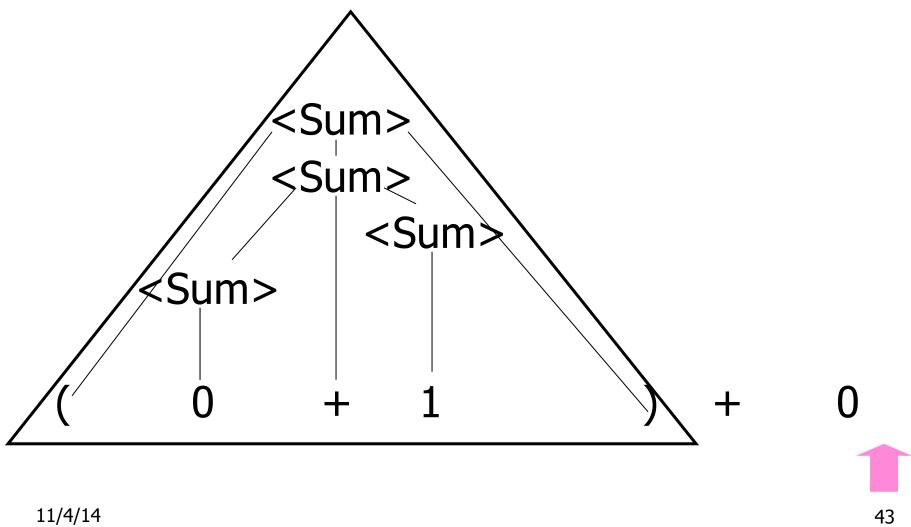




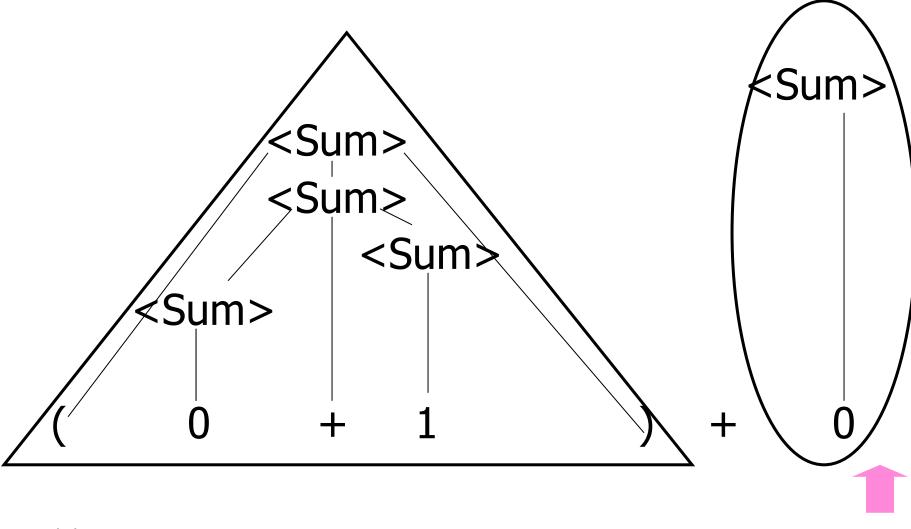




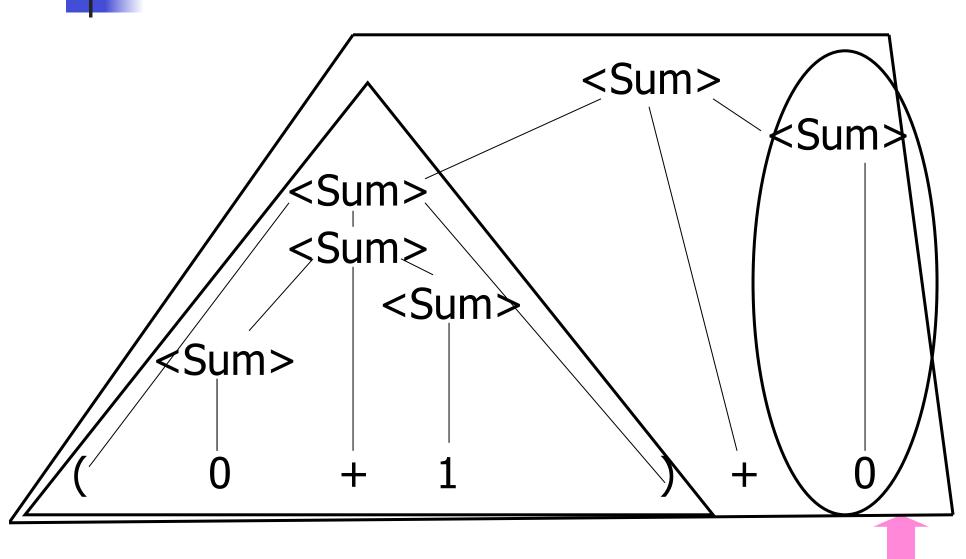




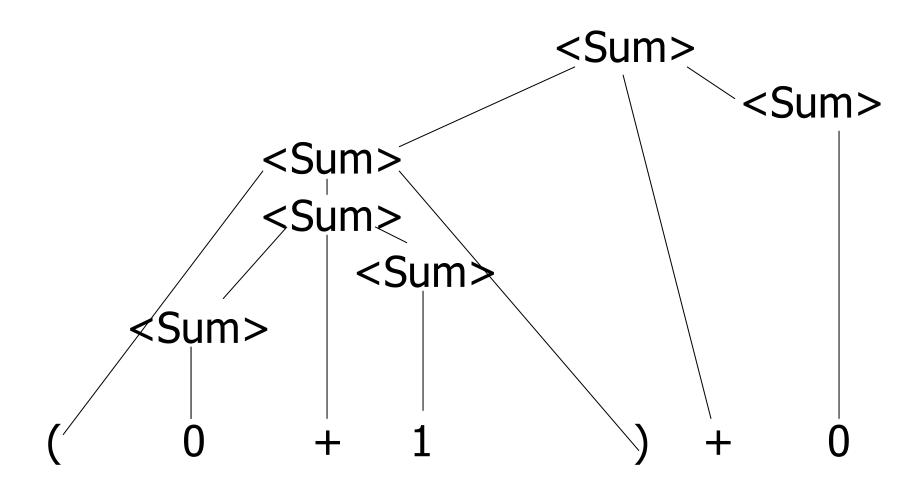












# LR Parsing Tables

- Build a pair of tables, Action and Goto, from the grammar
  - This is the hardest part, we omit here
  - Rows labeled by states
  - For Action, columns labeled by terminals and "end-of-tokens" marker
    - (more generally strings of terminals of fixed length)
  - For Goto, columns labeled by nonterminals



#### **Action and Goto Tables**

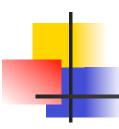
- Given a state and the next input, Action table says either
  - shift and go to state n, or
  - reduce by production k (explained in a bit)
  - accept or error
- Given a state and a non-terminal, Goto table says
  - go to state m



- Based on push-down automata
- Uses states and transitions (as recorded in Action and Goto tables)
- Uses a stack containing states, terminals and non-terminals



- O. Insure token stream ends in special "endof-tokens" symbol
- 1. Start in state 1 with an empty stack
- 2. Push **state**(1) onto stack
- →3. Look at next *i* tokens from token stream (toks) (don't remove yet)
  - 4. If top symbol on stack is **state**(*n*), look up action in Action table at (*n*, *toks*)



# 5. If action = **shift** m,

- a) Remove the top token from token stream and push it onto the stack
- b) Push **state**(*m*) onto stack
- c) Go to step 3

- 6. If action = **reduce** k where production k is E := u
  - a) Remove 2 \* length(u) symbols from stack (u and all the interleaved states)
  - b) If new top symbol on stack is **state**(*m*), look up new state *p* in Goto(*m*,E)
  - c) Push E onto the stack, then push **state**(*p*) onto the stack
  - d) Go to step 3



- 7. If action = accept
  - Stop parsing, return success
- 8. If action = error,
  - Stop parsing, return failure



### Adding Synthesized Attributes

- Add to each reduce a rule for calculating the new synthesized attribute from the component attributes
- Add to each non-terminal pushed onto the stack, the attribute calculated for it
- When performing a reduce,
  - gather the recorded attributes from each nonterminal popped from stack
  - Compute new attribute for non-terminal pushed onto stack



#### **Shift-Reduce Conflicts**

- Problem: can't decide whether the action for a state and input character should be shift or reduce
- Caused by ambiguity in grammar
- Usually caused by lack of associativity or precedence information in grammar

### Example: <Sum> = 0 | 1 | (<Sum>) | <Sum> + <Sum>



Problem: shift or reduce?

 You can shift-shift-reduce-reduce or reduce-shift-shift-reduce

- Shift first right associative
- Reduce first- left associative



#### Reduce - Reduce Conflicts

- Problem: can't decide between two different rules to reduce by
- Again caused by ambiguity in grammar
- Symptom: RHS of one production suffix of another
- Requires examining grammar and rewriting it
- Harder to solve than shift-reduce errors

# Example

- abc shift
- a bc shift
- ab c shift
- abc •
- Problem: reduce by B ::= bc then by
  - S ::= aB, or by A ::= abc then S ::A?



- Expresses the meaning of syntax
- Static semantics
  - Meaning based only on the form of the expression without executing it
  - Usually restricted to type checking / type inference



### Dynamic semantics

- Method of describing meaning of executing a program
- Several different types:
  - Operational Semantics
  - Axiomatic Semantics
  - Denotational Semantics



# **Dynamic Semantics**

- Different languages better suited to different types of semantics
- Different types of semantics serve different purposes



# **Operational Semantics**

- Start with a simple notion of machine
- Describe how to execute (implement)
   programs of language on virtual machine, by
   describing how to execute each program
   statement (ie, following the structure of the
   program)
- Meaning of program is how its execution changes the state of the machine
- Useful as basis for implementations



#### **Axiomatic Semantics**

- Also called Floyd-Hoare Logic
- Based on formal logic (first order predicate calculus)
- Axiomatic Semantics is a logical system built from axioms and inference rules
- Mainly suited to simple imperative programming languages



#### **Axiomatic Semantics**

- Used to formally prove a property (post-condition) of the state (the values of the program variables) after the execution of program, assuming another property (pre-condition) of the state before execution
- Written:{Precondition} Program {Postcondition}
- Source of idea of loop invariant



### **Denotational Semantics**

- Construct a function M assigning a mathematical meaning to each program construct
- Lambda calculus often used as the range of the meaning function
- Meaning function is compositional: meaning of construct built from meaning of parts
- Useful for proving properties of programs

#### **Natural Semantics**

- Aka Structural Operational Semantics, aka "Big Step Semantics"
- Provide value for a program by rules and derivations, similar to type derivations
- Rule conclusions look like

```
(C, m) ↓ m'
or
(E, m) ↓ v
```



### Simple Imperative Programming Language

- $I \in Identifiers$
- $\blacksquare$   $N \in Numerals$
- B::= true | false | B & B | B or B | not B
   | E < E | E = E</li>
- E::= N | I | E + E | E \* E | E E | E
- C::= skip | C; C | I ::= E
   | if B then C else C fi | while B do C od



#### **Natural Semantics of Atomic Expressions**

- Identifiers:  $(I,m) \Downarrow m(I)$
- Numerals are values: (N,m) ↓ N
- Booleans: (true, m) ↓ true(false, m) ↓ false

# **Booleans:**

$$(B, m)$$
 ↓ false  $(B \& B', m)$  ↓ false

$$(B, m)$$
 

 | false |  $(B, m)$  

 | true  $(B', m)$  

 |  $(B \& B', m)$  
 | false |  $(B \& B', m)$  
 |  $(B \& B', m)$  
 |  $(B \& B', m)$  
 |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$  |  $(B \& B', m)$ 

$$(B, m)$$
 ↓ true  
 $(B \text{ or } B', m)$  ↓ true

$$(B, m)$$
 ↓ true  $(B, m)$  ↓ false  $(B', m)$  ↓ b  $(B \text{ or } B', m)$  ↓ true  $(B \text{ or } B', m)$  ↓ b

$$(B, m)$$
  $\Downarrow$  true $(B, m)$   $\Downarrow$  false(not  $B, m)$   $\Downarrow$  false(not  $B, m)$   $\Downarrow$  true

# Relations

$$(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \sim V = b$$
$$(E \sim E', m) \Downarrow b$$

- By U ~ V = b, we mean does (the meaning of) the relation ~ hold on the meaning of U and V
- May be specified by a mathematical expression/equation or rules matching *U* and *V*



# **Arithmetic Expressions**

$$(E, m) \Downarrow U \quad (E', m) \Downarrow V \quad U \text{ op } V = N$$

$$(E \text{ op } E', m) \Downarrow N$$
where  $N$  is the specified value for  $U \text{ op } V$ 

## Commands

(skip, 
$$m$$
)  $\Downarrow m$ 

$$\frac{(E,m) \downarrow V}{(I::=E,m) \downarrow m[I <-- V]}$$

Sequencing: 
$$(C,m) \Downarrow m'$$
  $(C',m') \Downarrow m''$   $(C;C',m) \Downarrow m''$ 



### If Then Else Command

(B,m) ↓ true (C,m) ↓ m'(if B then C else C' fi, m) ↓ m'

(B,m) 

↓ false (C',m) 

↓ m'(if B then C else C' fi, m) 

↓ m'

## While Command

$$(B,m)$$
 ↓ false  
(while  $B$  do  $C$  od,  $m$ ) ↓  $m$ 

$$(B,m)$$
  $\Downarrow$  true  $(C,m)$   $\Downarrow$   $m'$  (while  $B$  do  $C$  od,  $m'$ )  $\Downarrow$   $m'$  (while  $B$  do  $C$  od,  $m$ )  $\Downarrow$   $m'$ 

### Example: If Then Else Rule

(if 
$$x > 5$$
 then  $y := 2 + 3$  else  $y := 3 + 4$  fi,  $\{x -> 7\}$ )  $\downarrow$  ?

# 4

### Example: If Then Else Rule

$$(x > 5, \{x -> 7\}) \Downarrow ?$$
  
(if x > 5 then y:= 2 + 3 else y:=3 + 4 fi,  $\{x -> 7\}) \Downarrow ?$ 

### Example: Arith Relation

```
? > ? = ?

\frac{(x,(x->7)) \|? (5,(x->7)) \|?}{(x > 5, (x -> 7)) \|?}
(if x > 5 then y:= 2 + 3 else y:= 3 + 4 fi, (x -> 7)) \|?
```

### Example: Identifier(s)

7 > 5 = true  

$$(x,(x->7))$$
 | 7 | (5,(x->7)) | 5  
 $(x > 5, (x -> 7))$  | 7  
(if x > 5 then y:= 2 + 3 else y:=3 + 4 fi,  
 $(x -> 7)$  | 1 | 7

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### Example: Arith Relation

$$7 > 5 = \text{true}$$
  
 $(x,(x->7)) \downarrow 7 \quad (5,(x->7)) \downarrow 5$   
 $(x > 5, (x -> 7)) \downarrow \text{true}$   
 $(\text{if } x > 5 \text{ then } y := 2 + 3 \text{ else } y := 3 + 4 \text{ fi},$   
 $(x -> 7) \downarrow ?$ 

### Example: If Then Else Rule

$$7 > 5 = \text{true}$$

$$(x,(x->7)) \parallel 7 \quad (5,(x->7)) \parallel 5 \quad (y:= 2 + 3, \{x-> 7\})$$

$$(x > 5, \{x -> 7\}) \parallel \text{true} \qquad \parallel ? \qquad .$$

$$(\text{if } x > 5 \text{ then } y:= 2 + 3 \text{ else } y:= 3 + 4 \text{ fi,}$$

$$(x -> 7) \parallel ?$$

### Example: Assignment

```
7 > 5 = \text{true} (2+3, \{x->7\}) \parallel ? (x,\{x->7\}) \parallel 7 (5,\{x->7\}) \parallel 5 (y:= 2+3, \{x->7\}) (x > 5, \{x -> 7\}) \parallel \text{true} (\text{if } x > 5 \text{ then } y:= 2+3 \text{ else } y:=3+4 \text{ fi}, \{x->7\}) \parallel ?
```

### Example: Arith Op

### **Example: Numerals**

```
2 + 3 = 5
(2,\{x->7\}) \downarrow 2 \quad (3,\{x->7\}) \downarrow 3
7 > 5 = \text{true} \qquad (2+3,\{x->7\}) \downarrow ?
(x,\{x->7\}) \downarrow 7 \quad (5,\{x->7\}) \downarrow 5 \qquad (y:=2+3,\{x->7\})
(x > 5,\{x->7\}) \downarrow \text{true} \qquad \downarrow ?
(if x > 5 \text{ then } y:=2+3 \text{ else } y:=3+4 \text{ fi},
\{x -> 7\}) \downarrow ?
```

### Example: Arith Op

```
2 + 3 = 5

(2,\{x->7\}) \downarrow 2 \quad (3,\{x->7\}) \downarrow 3

7 > 5 = \text{true} \qquad (2+3,\{x->7\}) \downarrow 5

(x,\{x->7\}) \downarrow 7 \quad (5,\{x->7\}) \downarrow 5 \qquad (y:= 2+3,\{x->7\})

(x > 5, \{x -> 7\}) \downarrow \text{true} \qquad \downarrow ?

(if x > 5 \text{ then } y:= 2+3 \text{ else } y:=3+4 \text{ fi,}

\{x -> 7\}) \downarrow ?
```

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### Example: Assignment



### Example: If Then Else Rule

```
2 + 3 = 5
(2,\{x->7\}) \downarrow 2 \quad (3,\{x->7\}) \downarrow 3
7 > 5 = \text{true} \qquad (2+3,\{x->7\}) \downarrow 5
(x,\{x->7\}) \downarrow 7 \quad (5,\{x->7\}) \downarrow 5 \qquad (y:=2+3,\{x->7\})
(x > 5,\{x->7\}) \downarrow \text{true} \qquad \downarrow \{x->7,y->5\}
(if x > 5 \text{ then } y:=2+3 \text{ else } y:=3+4 \text{ fi},
\{x ->7\}) \downarrow \{x->7,y->5\}
```



### Let in Command

$$\frac{(E,m) \Downarrow v \ (C,m[I <-v]) \Downarrow m'}{(\text{let } I = E \text{ in } C, m) \Downarrow m'}$$

Where m''(y) = m'(y) for  $y \ne I$  and m''(I) = m(I) if m(I) is defined, and m''(I) is undefined otherwise

# Example

$$\frac{(x,\{x->5\}) \downarrow 5 \quad (3,\{x->5\}) \downarrow 3}{(x+3,\{x->5\}) \downarrow 8}$$
$$\frac{(5,\{x->17\}) \downarrow 5 \quad (x:=x+3,\{x->5\}) \downarrow \{x->8\}}{(\text{let } x = 5 \text{ in } (x:=x+3), \{x->17\}) \downarrow ?}$$

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# Example

$$\frac{(x,\{x->5\}) \downarrow 5 \quad (3,\{x->5\}) \downarrow 3}{(x+3,\{x->5\}) \downarrow 8}$$
$$\frac{(5,\{x->17\}) \downarrow 5 \quad (x:=x+3,\{x->5\}) \downarrow \{x->8\}}{(\text{let } x = 5 \text{ in } (x:=x+3), \{x->17\}) \downarrow \{x->17\}}$$

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- Simple Imperative Programming Language introduces variables implicitly through assignment
- The let-in command introduces scoped variables explictly
- Clash of constructs apparent in awkward semantics



### Interpretation Versus Compilation

- A compiler from language L1 to language L2 is a program that takes an L1 program and for each piece of code in L1 generates a piece of code in L2 of same meaning
- An interpreter of L1 in L2 is an L2 program that executes the meaning of a given L1 program
- Compiler would examine the body of a loop once; an interpreter would examine it every time the loop was executed

## Interpreter

- An *Interpreter* represents the operational semantics of a language L1 (source language) in the language of implementation L2 (target language)
- Built incrementally
  - Start with literals
  - Variables
  - Primitive operations
  - Evaluation of expressions
  - Evaluation of commands/declarations

## Interpreter

- Takes abstract syntax trees as input
  - In simple cases could be just strings
- One procedure for each syntactic category (nonterminal)
  - eg one for expressions, another for commands
- If Natural semantics used, tells how to compute final value from code
- If Transition semantics used, tells how to compute next "state"
  - To get final value, put in a loop

### Natural Semantics Example

- compute\_exp (Var(v), m) = look\_up v m
- compute\_exp (Int(n), \_) = Num (n)
- ...
- compute\_com(IfExp(b,c1,c2),m) =
   if compute\_exp (b,m) = Bool(true)
   then compute\_com (c1,m)
   else compute\_com (c2,m)



### Natural Semantics Example

```
    compute_com(While(b,c), m) =
        if compute_exp (b,m) = Bool(false)
        then m
        else compute_com
        (While(b,c), compute_com(c,m))
```

- May fail to terminate exceed stack limits
- Returns no useful information then