

Inductive Step continued

$$= k + \underbrace{\sum_{i=1}^k \frac{1}{k(k+1)} + \frac{1}{(k+1)(k+2)}}_{\text{...}}$$

$$= \frac{k}{(k+1)} + \frac{1}{(k+1)(k+2)}$$

$$= \frac{k(k+2) + 1}{(k+1)(k+2)}$$

$$= \frac{k^2 + 2k + 1}{(k+1)(k+2)} = \frac{k^2 + k + k + 1}{(k+1)(k+2)}$$

$$= \frac{k(k+1) + 1(k+1)}{(k+1)(k+2)} = \frac{\cancel{(k+1)}(k+1)}{\cancel{(k+1)}(k+2)}$$

$$= \frac{k+1}{k+2} = \text{A.H.S.}$$

Therefore, proved, It is true for all $n \in \mathbb{Z}^+$