

$X =$
 6×6

7	5	0	0	3	2
6	4	5	1	4	8
9	0	2	2	5	4
6	3	4	7	9	8
5	7	5	6	9	0
7	9	0	8	2	3

$$F = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

3×3

3.1) Dimensions of input: $6 \times 6 \times 1$

Dimensions of kernel: 3×3

$$\# \text{ parameters} = (\text{kernel width})^2 \times (\# \text{ input channels}) \times (\# \text{ kernels}) + (\# \text{ biases})$$

kernel width = 3

$\#$ input channels = 1

$\#$ kernels = 1

$\#$ biases = $\#$ kernels = 1

$$\text{So, } \# \text{ parameters} = (3^2 \times 1 \times 1) + 1 = 10 \text{ parameters in kernel } f$$

$$3.2) (1 \times 7) + (0 \times 5) + (-1 \times 0) \\ + (2 \times 6) + (0 \times 4) + (-2 \times 5) \\ + (1 \times 9) + (0 \times 0) + (-1 \times 2) = 16$$

$$(1 \times 5) + (0 \times 0) + (-1 \times 0) \\ + (2 \times 4) + (0 \times 5) + (-2 \times 1) \\ + (1 \times 0) + (0 \times 2) + (-1 \times 2) = 9$$

$$(1 \times 0) + (0 \times 6) + (-1 \times 3) \\ + (2 \times 5) + (0 \times 1) + (-2 \times 4) \\ + (1 \times 2) + (0 \times 2) + (-1 \times 5) = -4$$

$$(1 \times 6) + (0 \times 3) + (-1 \times 2) \\ + (2 \times 1) + (0 \times 4) + (-2 \times 8) \\ + (1 \times 2) + (0 \times 5) + (-1 \times 4) = -18$$

$$(1 \times 6) + (0 \times 4) + (-1 \times 9) \\ + (2 \times 9) + (0 \times 0) + (-2 \times 2) \\ + (1 \times 6) + (0 \times 3) + (-1 \times 4) = 17$$

$$X = \begin{bmatrix} 7 & 5 & 0 & 0 & 3 & 2 \\ 6 & 4 & 5 & 1 & 4 & 8 \\ 9 & 0 & 2 & 2 & 5 & 4 \\ 6 & 3 & 4 & 7 & 9 & 8 \\ 5 & 7 & 5 & 6 & 9 & 0 \\ 7 & 9 & 0 & 8 & 2 & 3 \end{bmatrix}$$

$$F = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\begin{aligned} & (1 \times 4) + (0 \times 5) + (-1 \times 1) \\ & + (2 \times 0) + (0 \times 2) + (-2 \times 2) \\ & + (1 \times 3) + (0 \times 4) + (-1 \times 7) = -5 \end{aligned}$$

$$\begin{aligned} & (1 \times 5) + (0 \times 1) + (-1 \times 4) \\ & + (2 \times 2) + (0 \times 2) + (-2 \times 5) \\ & + (1 \times 4) + (0 \times 7) + (-1 \times 9) = -10 \end{aligned}$$

$$\begin{aligned} & (1 \times 1) + (0 \times 4) + (-1 \times 8) \\ & + (2 \times 2) + (0 \times 5) + (-2 \times 4) \\ & + (1 \times 7) + (0 \times 9) + (-1 \times 8) = -12 \end{aligned}$$

next row

$$\begin{aligned} & (1 \times 9) + (0 \times 0) + (-1 \times 2) \\ & + (2 \times 6) + (0 \times 3) + (-2 \times 4) \\ & + (1 \times 5) + (0 \times 7) + (-1 \times 5) = 11 \end{aligned}$$

$$\begin{aligned} & (1 \times 6) + (0 \times 2) + (-1 \times 2) \\ & + (2 \times 3) + (0 \times 4) + (-2 \times 7) \\ & + (1 \times 7) + (0 \times 5) + (-1 \times 6) = -9 \end{aligned}$$

$$\begin{aligned} & (1 \times 2) + (0 \times 2) + (-1 \times 5) \\ & + (2 \times 4) + (0 \times 7) + (-2 \times 9) \\ & + (1 \times 5) + (0 \times 6) + (-1 \times 9) = -17 \end{aligned}$$

$$\begin{aligned} & (1 \times 2) + (0 \times 5) + (-1 \times 4) \\ & + (2 \times 7) + (0 \times 9) + (-2 \times 8) \\ & + (1 \times 6) + (0 \times 9) + (-1 \times 0) = 2 \end{aligned}$$

next row

$$(1 \times 6) + (0 \times 3) + (-1 \times 4) \\ + (2 \times 5) + (0 \times 7) + (-2 \times 5) \\ + (1 \times 7) + (0 \times 9) + (-1 \times 0) = 9$$

$$(1 \times 3) + (0 \times 4) + (-1 \times 7) \\ + (2 \times 7) + (0 \times 5) + (-2 \times 6) \\ + (1 \times 9) + (0 \times 0) + (-1 \times 8) = -1$$

$$(1 \times 4) + (0 \times 7) + (-1 \times 9) \\ + (2 \times 5) + (0 \times 6) + (-2 \times 9) \\ + (1 \times 0) + (0 \times 8) + (-1 \times 2) = -15$$

$$(1 \times 7) + (0 \times 9) + (-1 \times 8) \\ + (2 \times 6) + (0 \times 9) + (-2 \times 0) \\ + (1 \times 8) + (0 \times 2) + (-1 \times 3) = 16$$

Output activation map:

$$\begin{bmatrix} 16 & 9 & -4 & -18 \\ 17 & -5 & -10 & -12 \\ 11 & -9 & -17 & 2 \\ 9 & -1 & -15 & 16 \end{bmatrix}$$

$$3.3) \max \begin{bmatrix} 16 & 9 \\ 17 & -5 \end{bmatrix} = 17, \max \begin{bmatrix} -4 & -18 \\ -10 & -12 \end{bmatrix} = -4$$

$$\max \begin{bmatrix} 11 & -9 \\ 9 & -1 \end{bmatrix} = 11, \max \begin{bmatrix} -17 & 2 \\ -15 & 16 \end{bmatrix} = 16$$

$$\text{max pool result: } \begin{bmatrix} 17 & -4 \\ 11 & 16 \end{bmatrix}$$