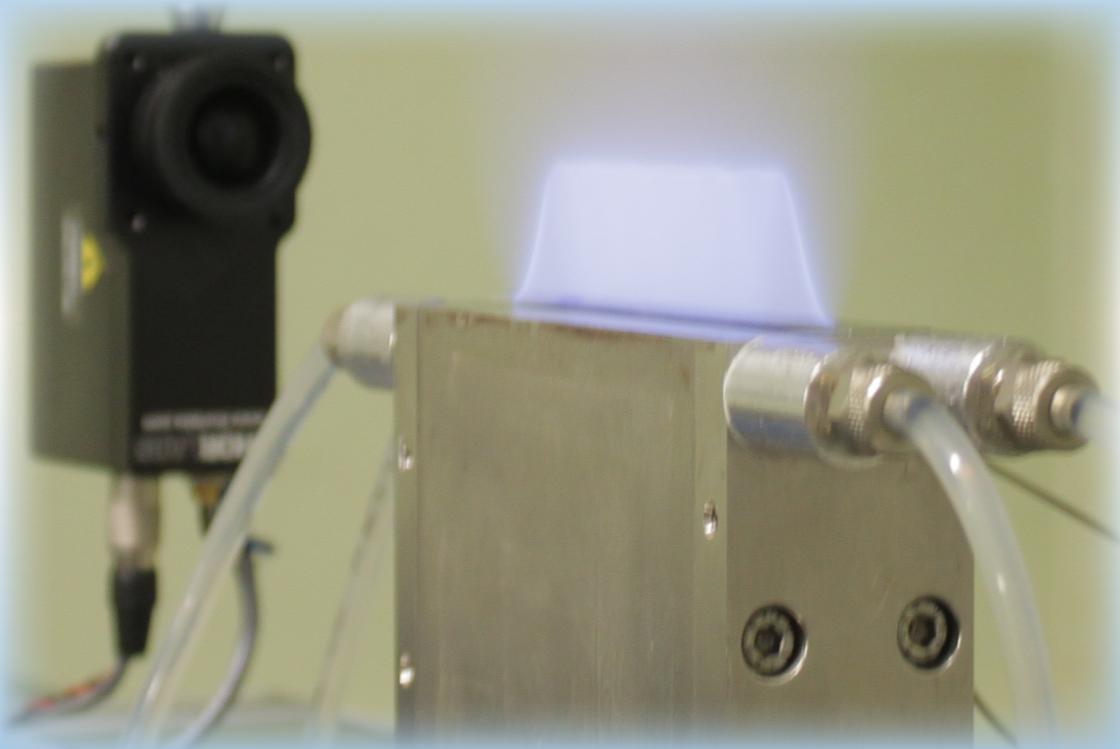


Ph.D Defense

Wall-Temperature Effects on Flame Response to Acoustic Oscillations



Daniel MEJIA

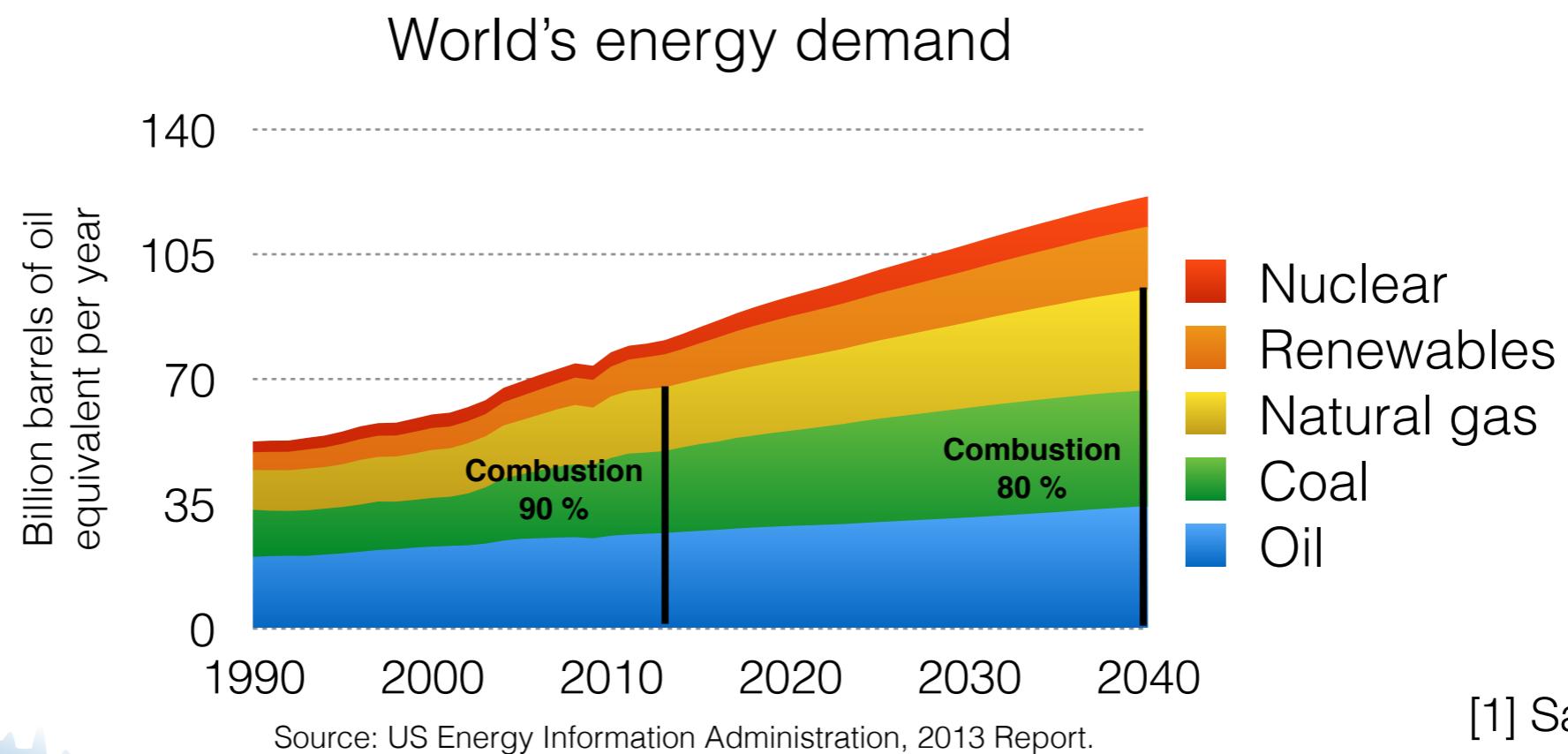
Advisers: Rudy BAZILE
Laurent SELLE



Tuesday 20 Mai 2014
Toulouse, France
 dmejia@imft.fr 

Context

- ★ **Energy production** constitutes one of the major challenges of the new era and comprises electricity generation, industrial processes, transportation and alimentation.
- ★ Despite the growth of renewable energies, **combustion is up to date, responsible for 90 % of the total energy generated on earth**, and it will remain the main source for a long time (up to 80 % in 2040).



★ Combustion systems come in a wide range of scales:



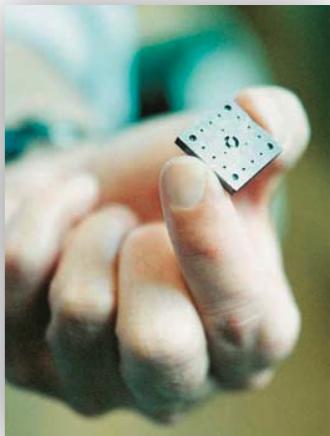
Gaz central power station
~ 1 GW



Turbofan engine
~ 100 MW



Domestic boiler
~ 10 kW



Micro turbine
~ 1 W

★ But... Combustion is also responsible for:

Air pollution (CO, NOx...)

Solution?

Lower flame temperature

How?

Lean premixed combustion

Global warming (CO₂)

Solution?

Increase efficiency

How?

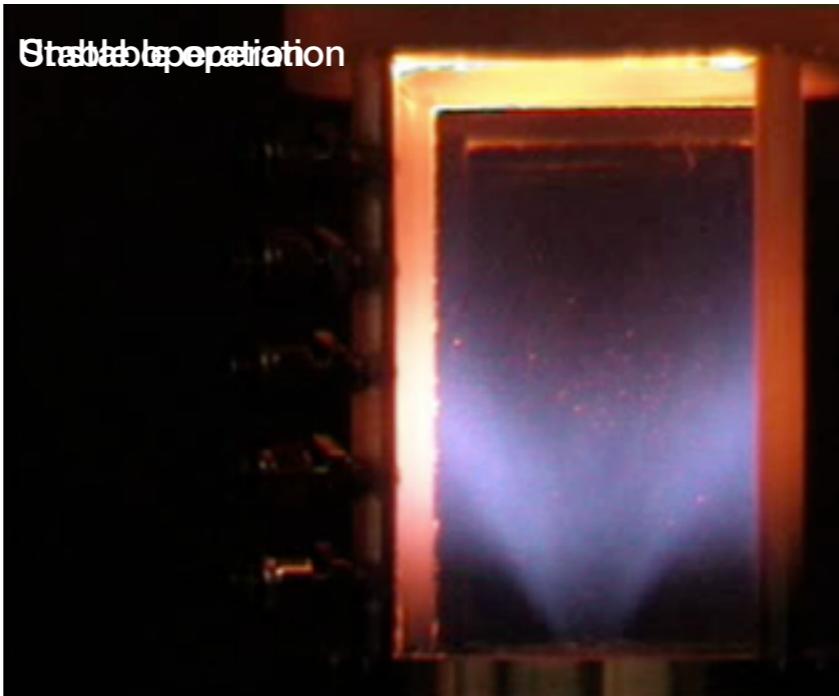
High pressures and compact design systems

New technologies are very sensitive to combustion instabilities !

[1] Penner et al. 1999



★ **Combustion instabilities (CI's)** are a major problem in the operation of many power-generation systems.

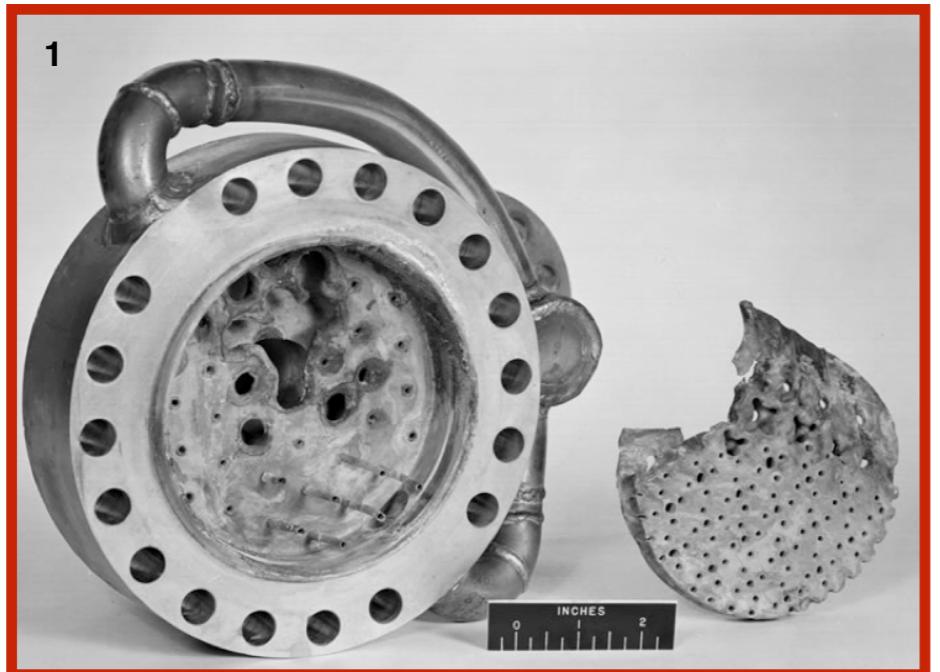


Source: PRECCINSTA burner DLR

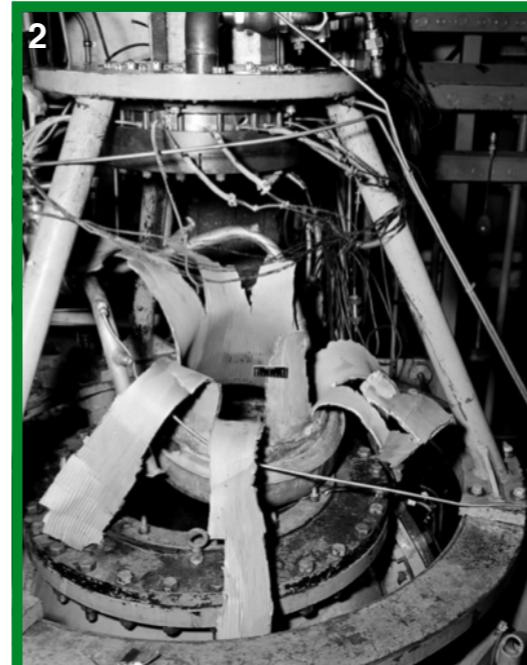
CI's consequences:

- Flame flash-back,
- Flame blow-off,
- High pressure fluctuations,
- High heat fluxes,
- Mechanical vibrations.

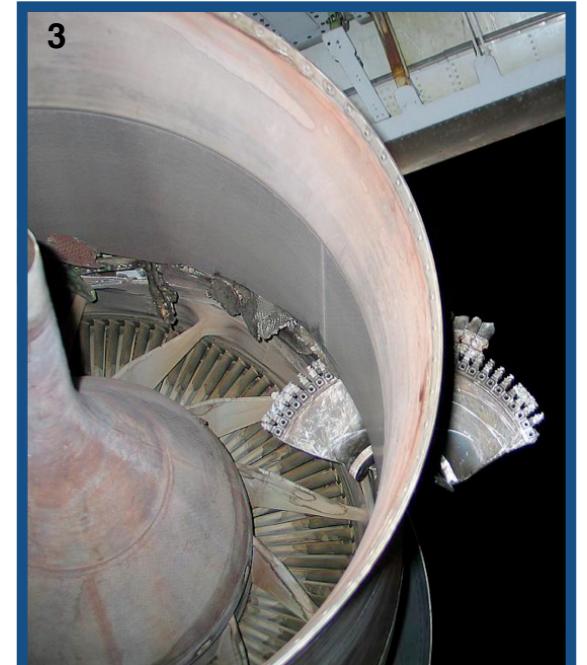
★ In some cases CI's can cause a **catastrophic failure** of the system:



1. Burner injectors of NASA rocket engine.



2. Rocket engine NASA damaged by CI's.



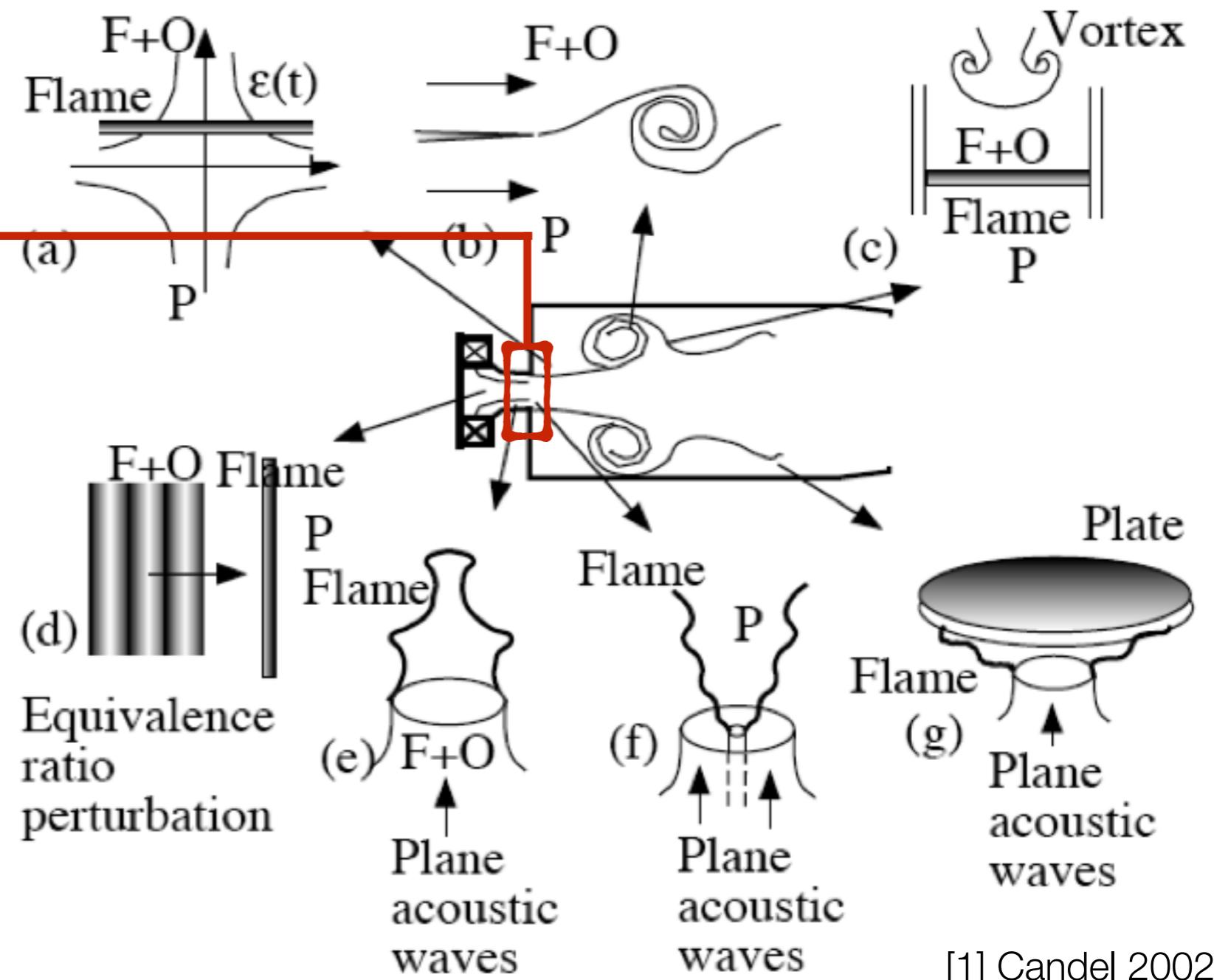
3. Turbine disk detached from a turbofan engine after CI's.



- ★ The ultimate goal of CI's is to **anticipate when a combustion chamber will be unstable** at the design stage, avoiding the high costs and reducing time of prototype testing.
- ★ The challenge for understanding and predicting CI's lies in the **multiplicity of physical phenomena** involved:

Wall temperature

Most systems behave differently at cold start and in permanent regime.



[1] Candel 2002 *pci*.

- ★ One of the canonical configurations for the study of CI's is the **laminar premixed flame**, for which, there already exist analytical solutions for the flame response to acoustic perturbation.



Laminar Premixed Flame

$$\phi = 0.92$$

$$U_b = 1.6 \text{ m/s}$$

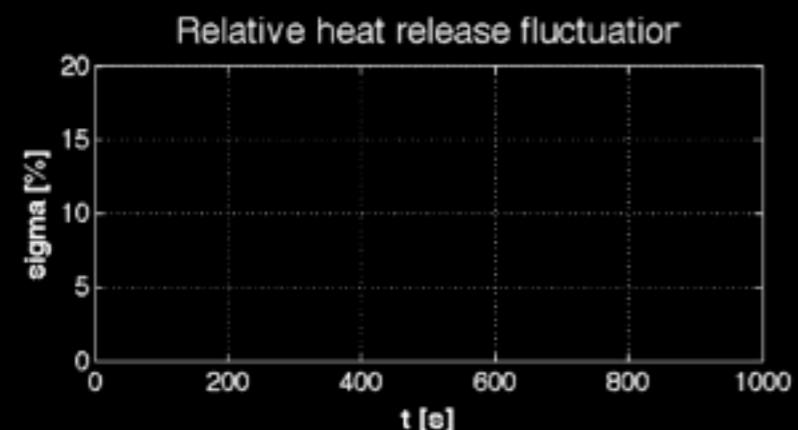
$$P = 0.96 \text{ bar}$$

$$T_{fg} = 293 \text{ K}$$

Cooling System : **OFF**

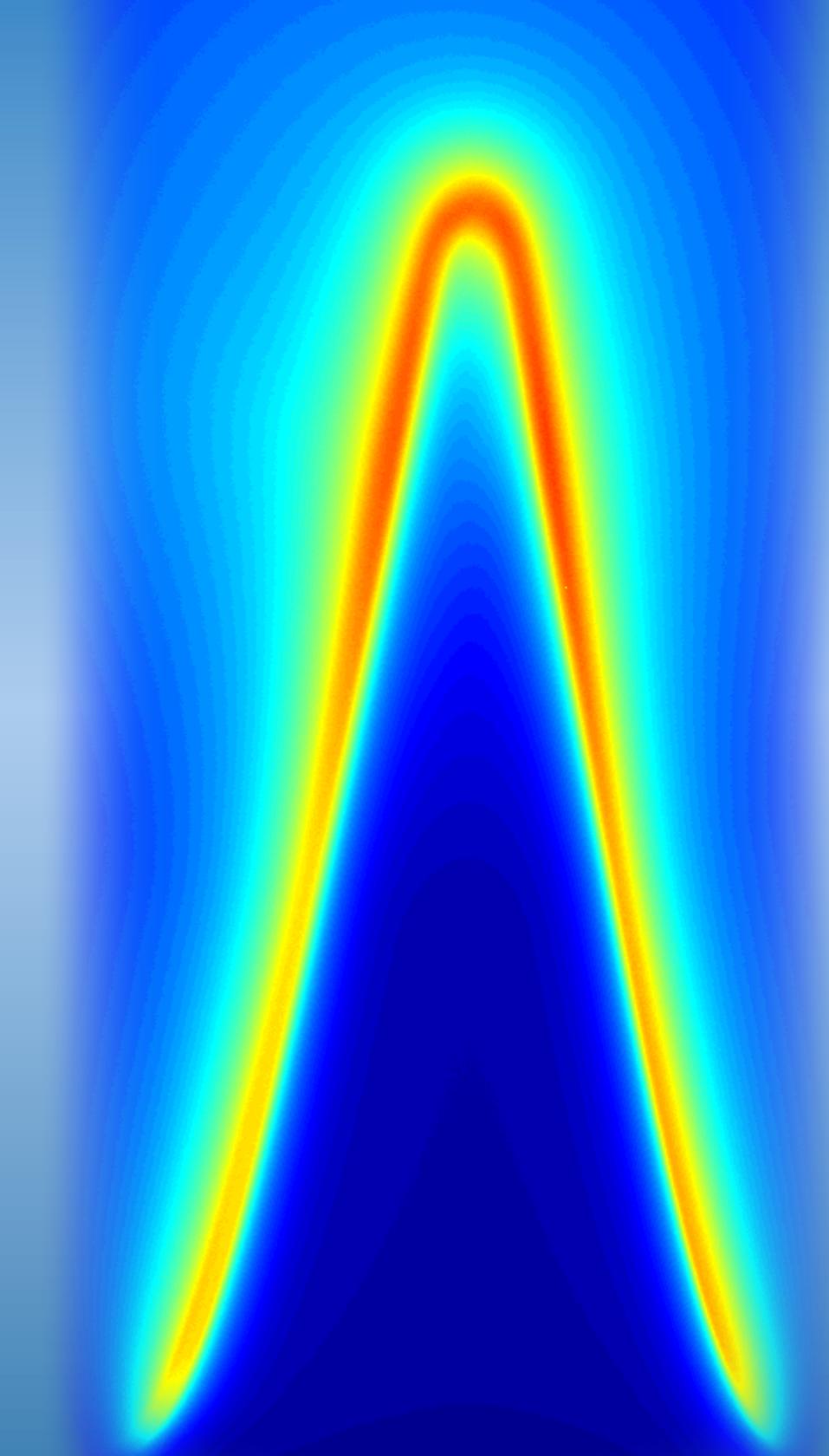


▶ 1X



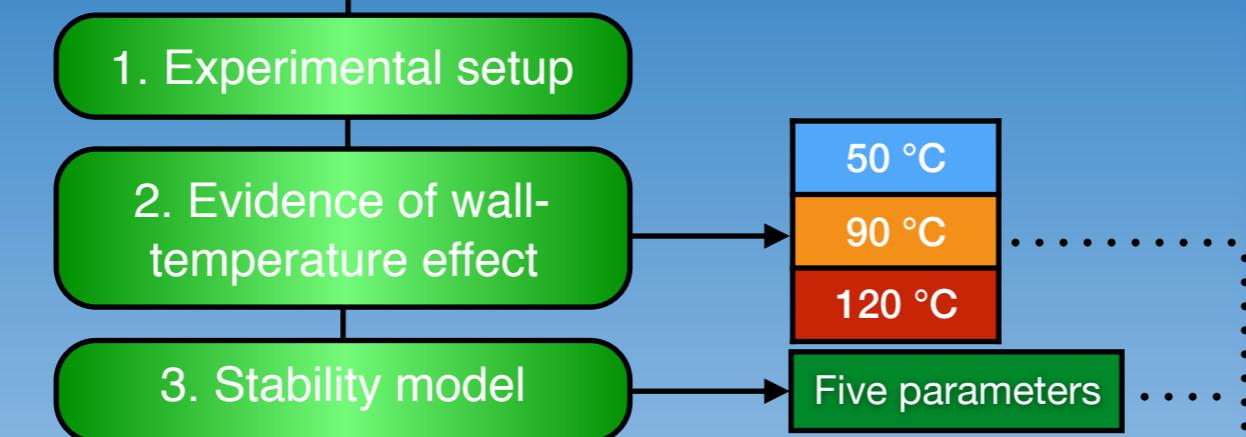
Objectives

1. Derive a stability model which can predict the experimental observations.
2. Determine which mechanism(s) is/are responsible for stabilizing the flame.
3. Understand how this mechanism(s) work(s).



Outline

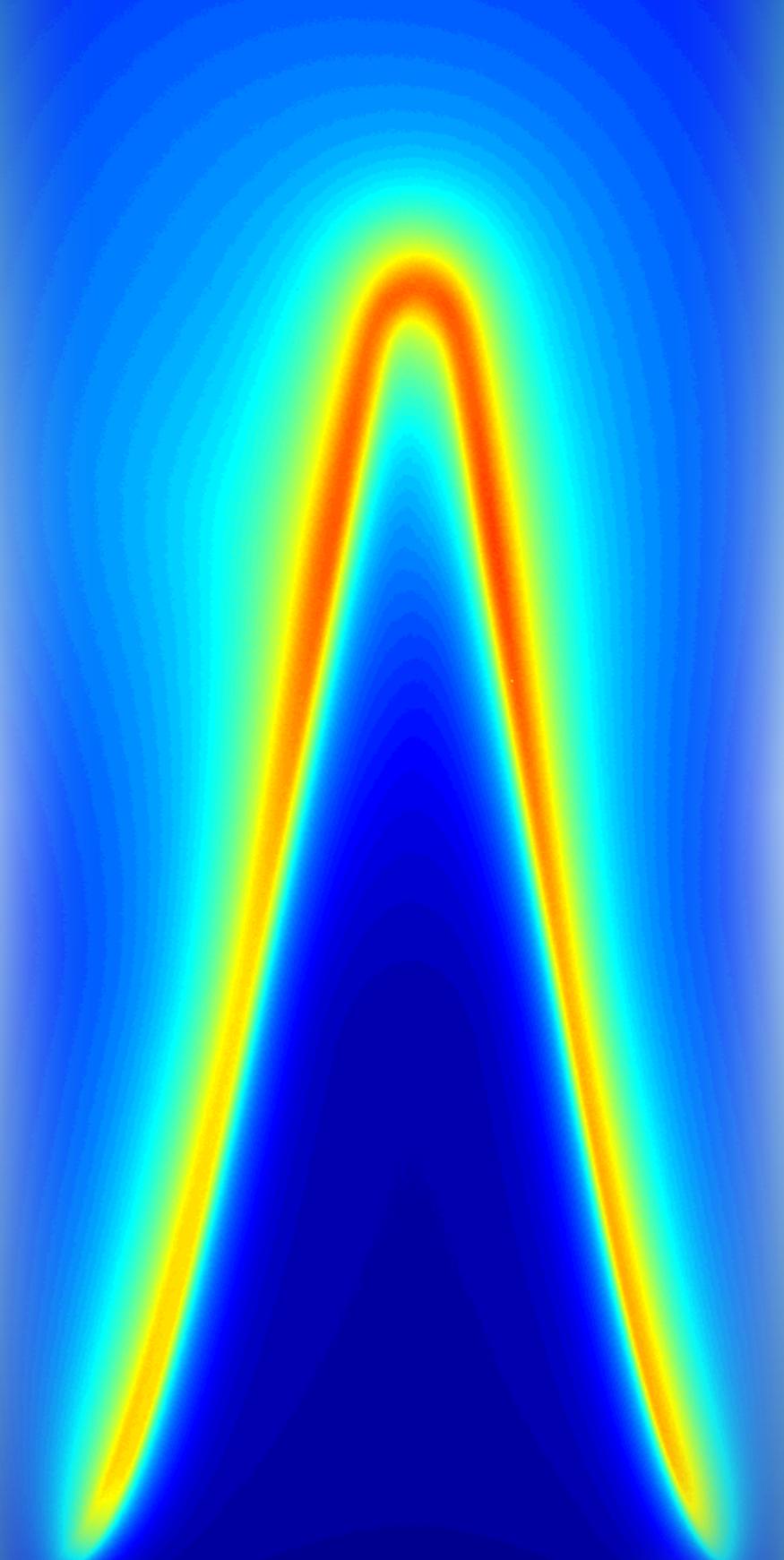
Part I: The Slot Burner



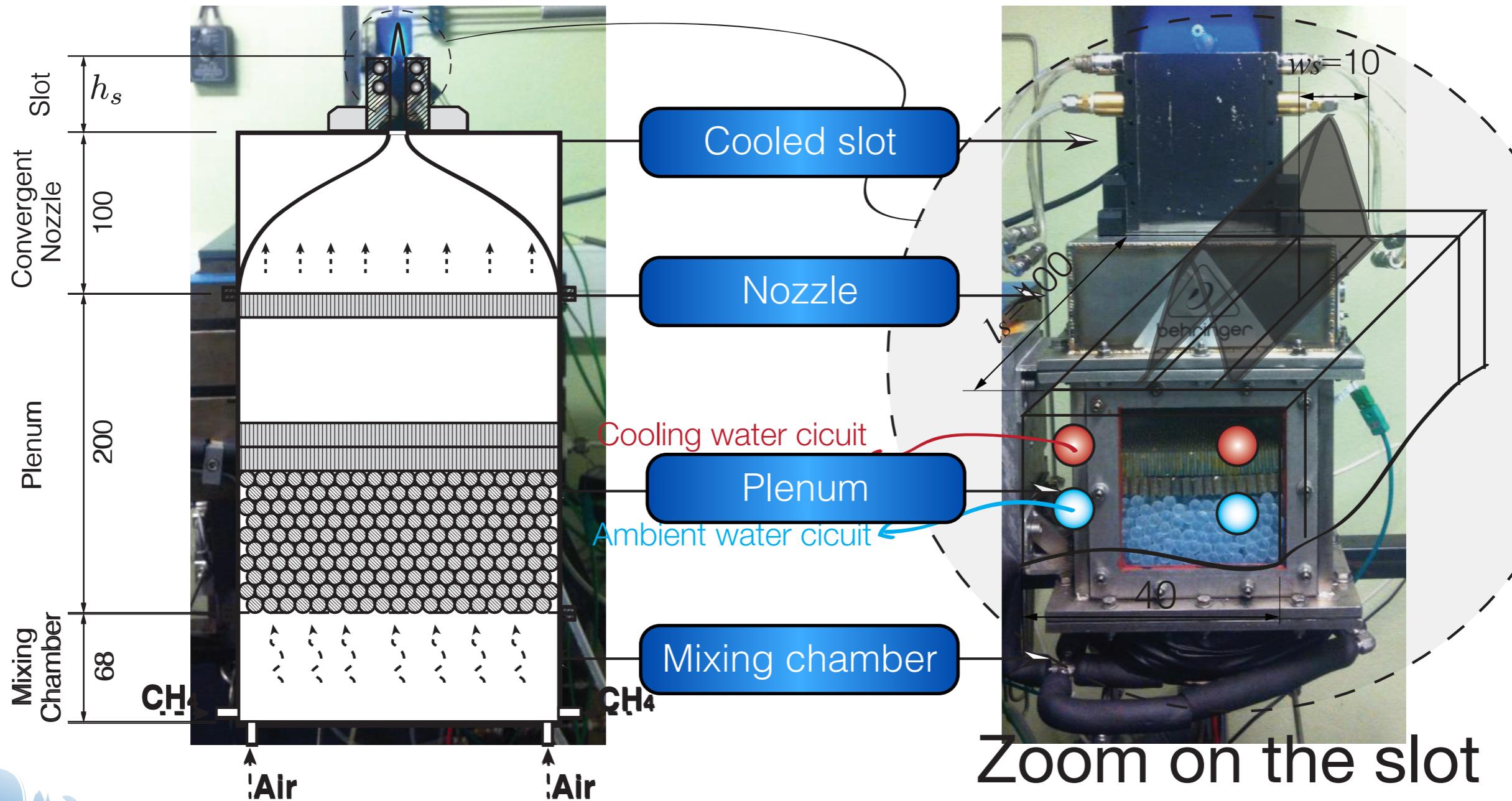
Part II: Experimental Measurements



Part III: Flame Dynamics



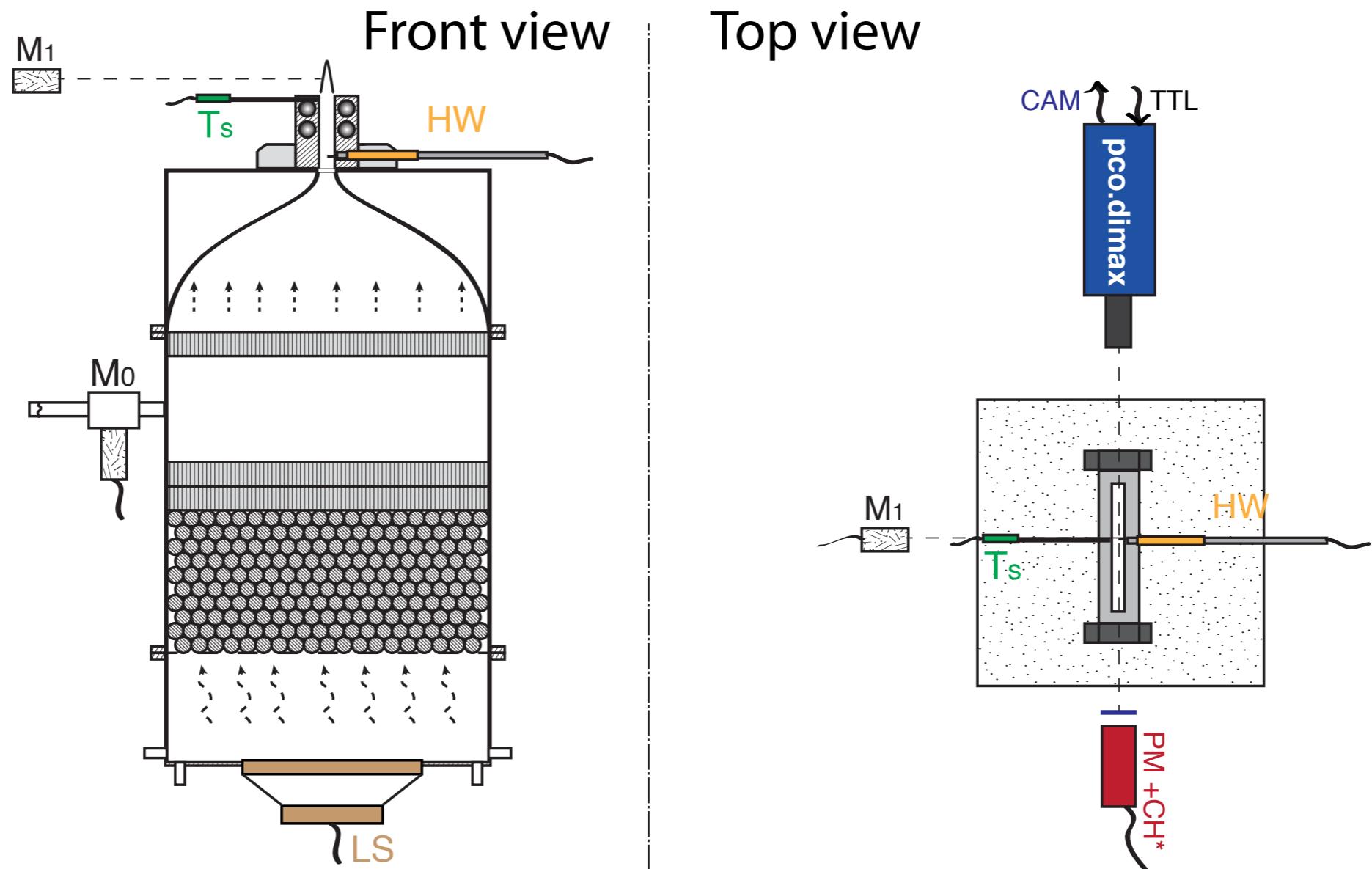
1. Experimental set-up



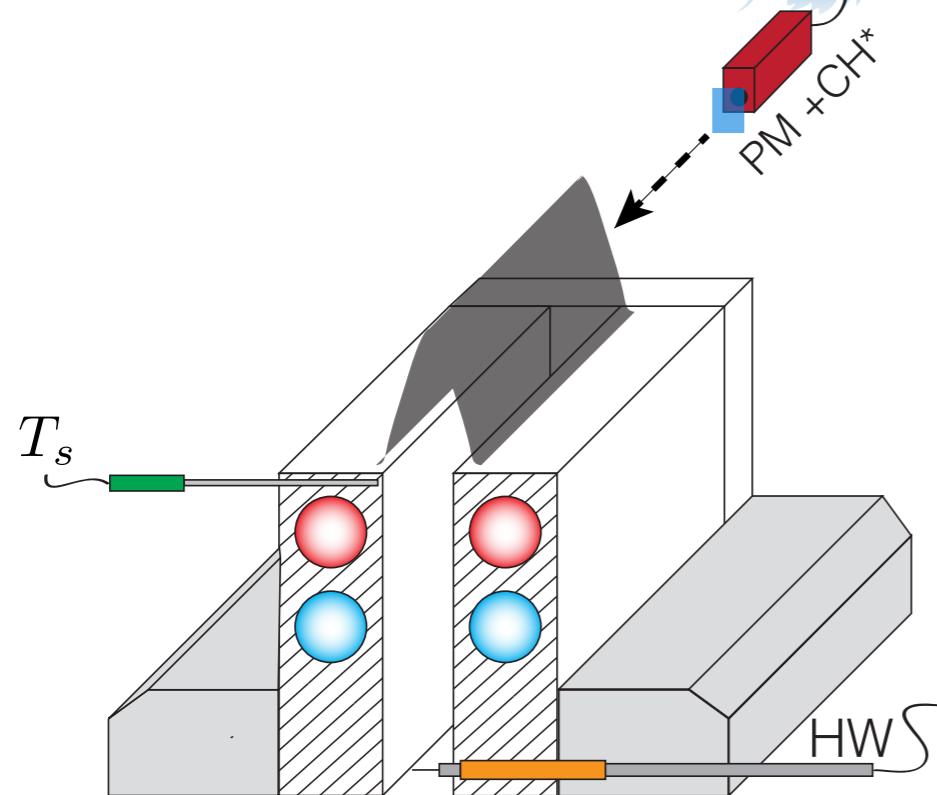
[1] Selle et al. 2011 cf.

Diagnostics

- ★ Acoustic pressure (two microphones),
- ★ velocity (hot-wire),
- ★ heat release rate (photomultiplier + CH* filter),
- ★ temperature (k -thermocouple),
- ★ flame visualization (high speed camera),
- ★ flow modulation (loud-speaker).



2. Description of the unstable behavior



Two type of analysis

Transient

UWT
(Uncontrolled wall temperature)

Cooling OFF

$$f_r = 58 \text{ Hz}$$

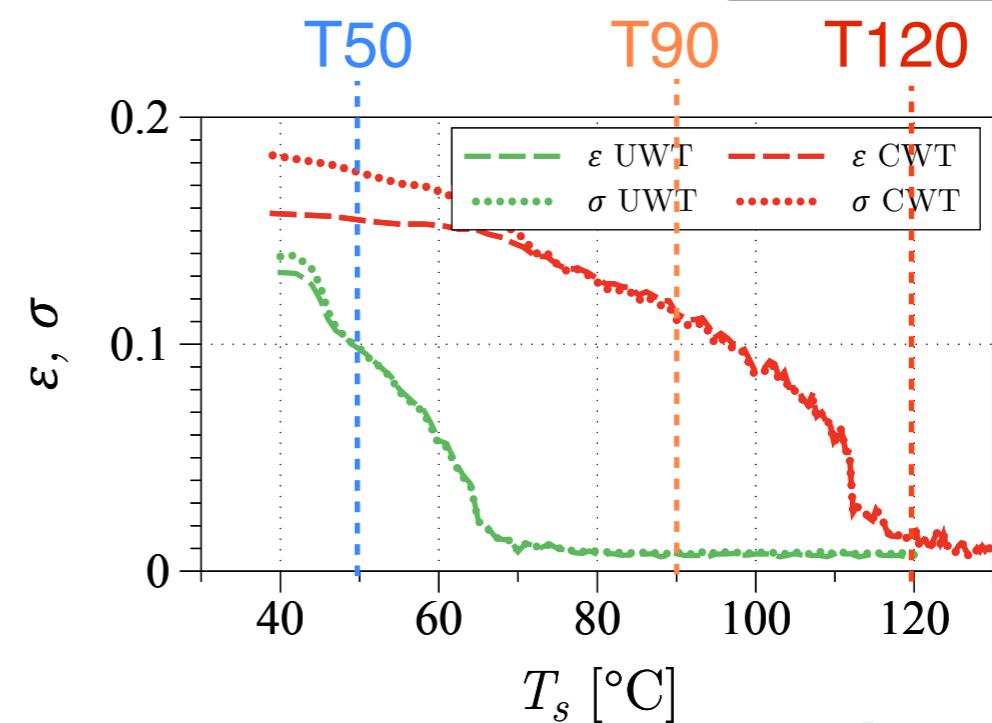
Steady-state

CWT
(Controlled wall temperature)

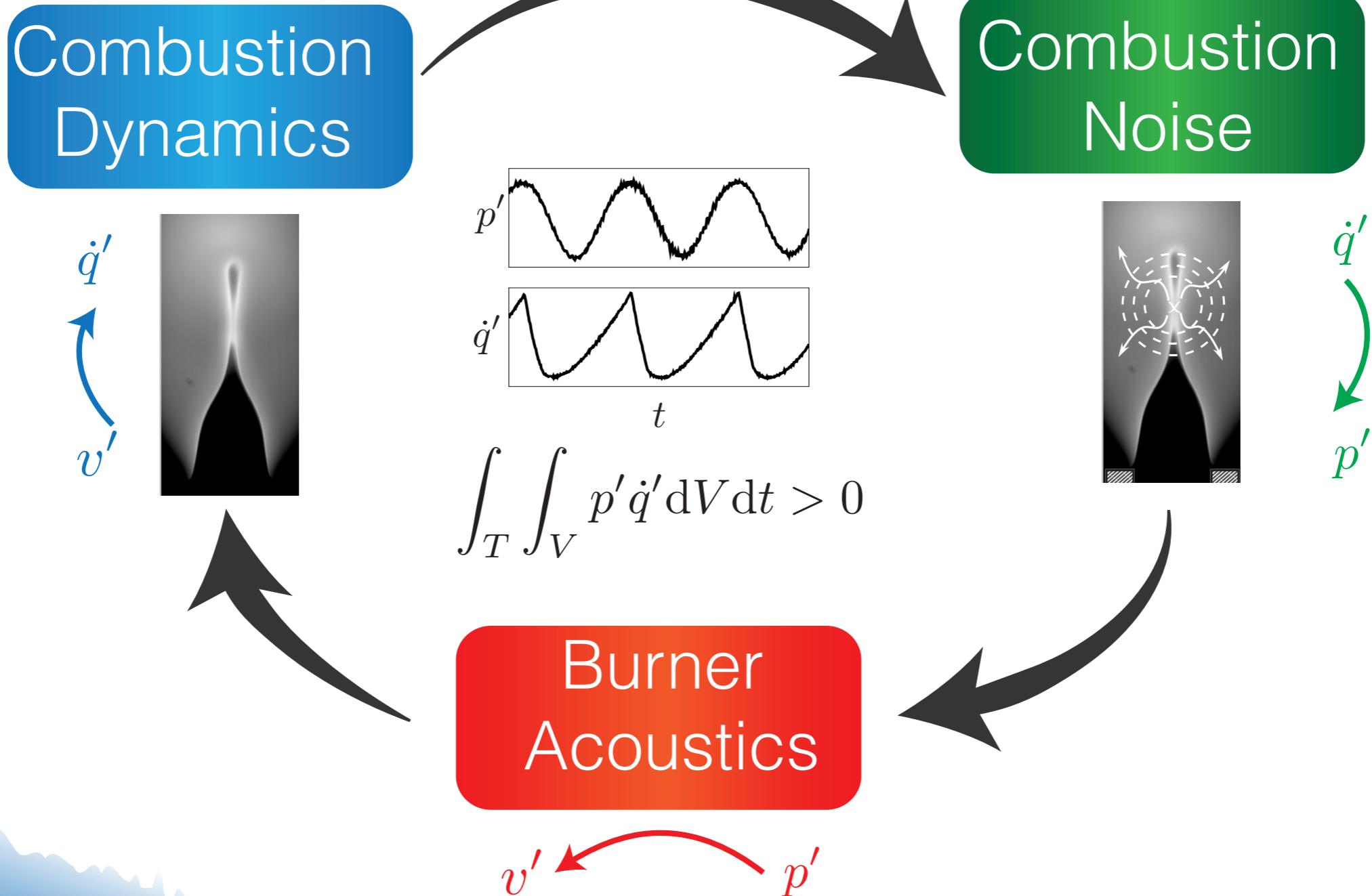
Cooling ON
 $T_{H_2O} = 1 - 99 \text{ }^{\circ}\text{C}$
 $\Delta T_{H_2O} = 1 \text{ }^{\circ}\text{C}$

Measurements

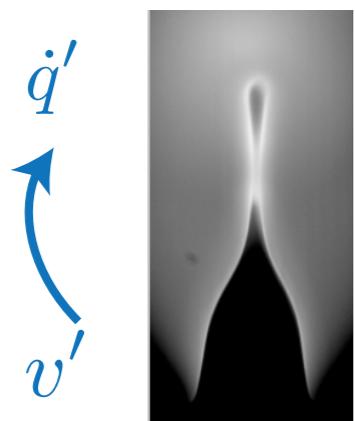
Slot temperature	T_s
RMS Heat release fluctuation magnitude	$\sigma = \frac{I_{CH^*}^{rms}}{\bar{I}_{CH^*}}$
RMS Velocity fluctuation magnitude	$\varepsilon = \frac{v_1^{rms}}{\bar{v}}$



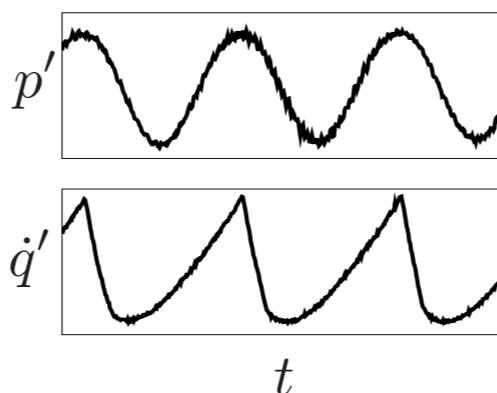
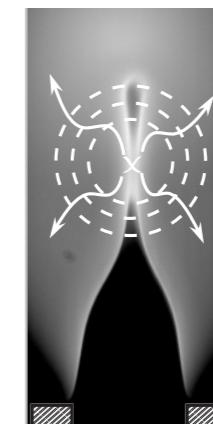
3. Stability model



Combustion
Dynamics



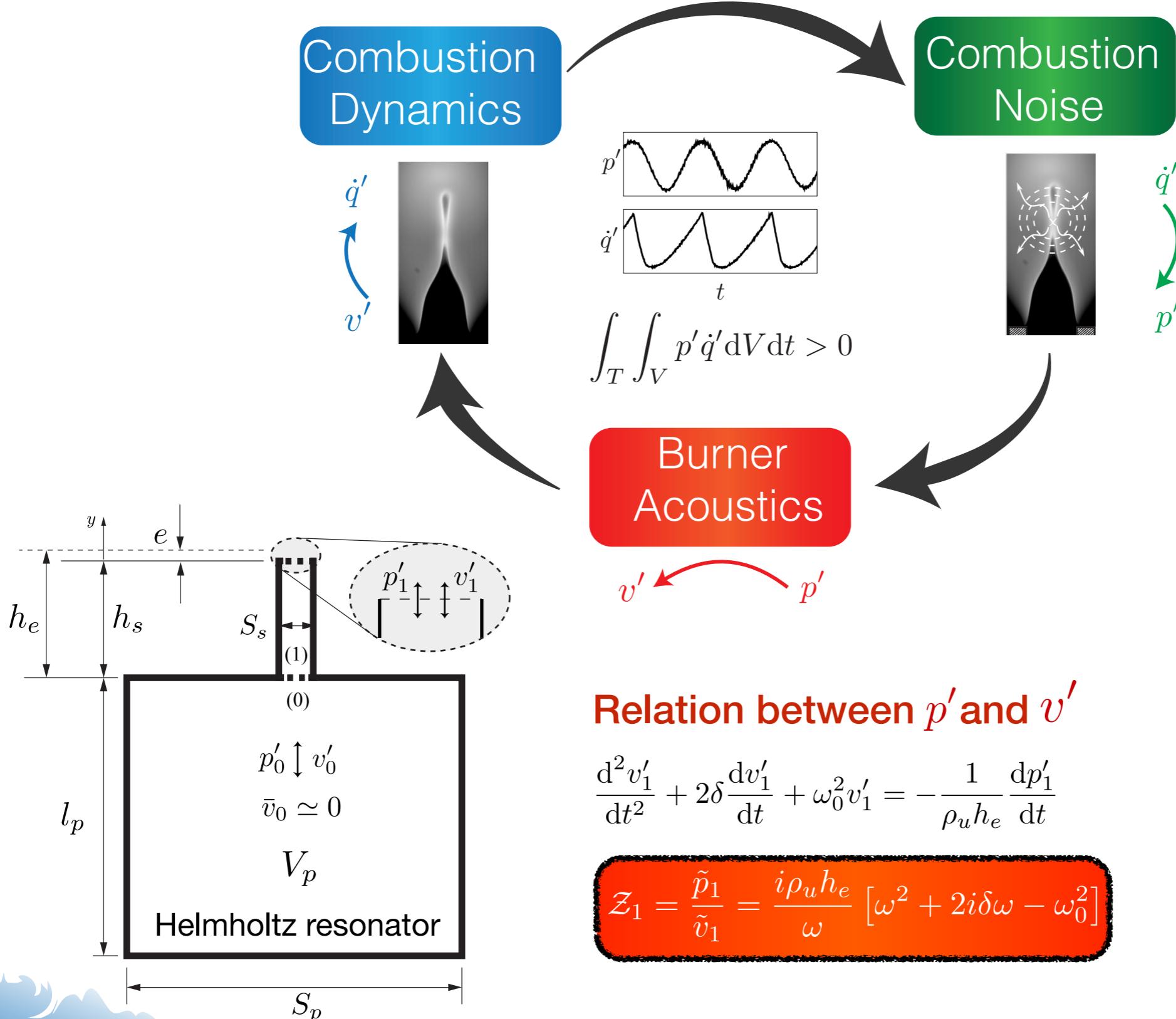
Combustion
Noise



$$\int_T \int_V p' \dot{q}' dV dt > 0$$

Burner
Acoustics

$$v' \leftarrow p'$$



Relation between p' and v'

$$\frac{d^2 v'_1}{dt^2} + 2\delta \frac{dv'_1}{dt} + \omega_0^2 v'_1 = -\frac{1}{\rho_u h_e} \frac{dp'_1}{dt}$$

$$Z_1 = \frac{\tilde{p}_1}{\tilde{v}_1} = \frac{i\rho_u h_e}{\omega} [\omega^2 + 2i\delta\omega - \omega_0^2]$$

- [1] Pierce 1981.
- [2] Rienstra 1983 *jsv*.
- [3] Durox *et al.* 2002 *pci*.

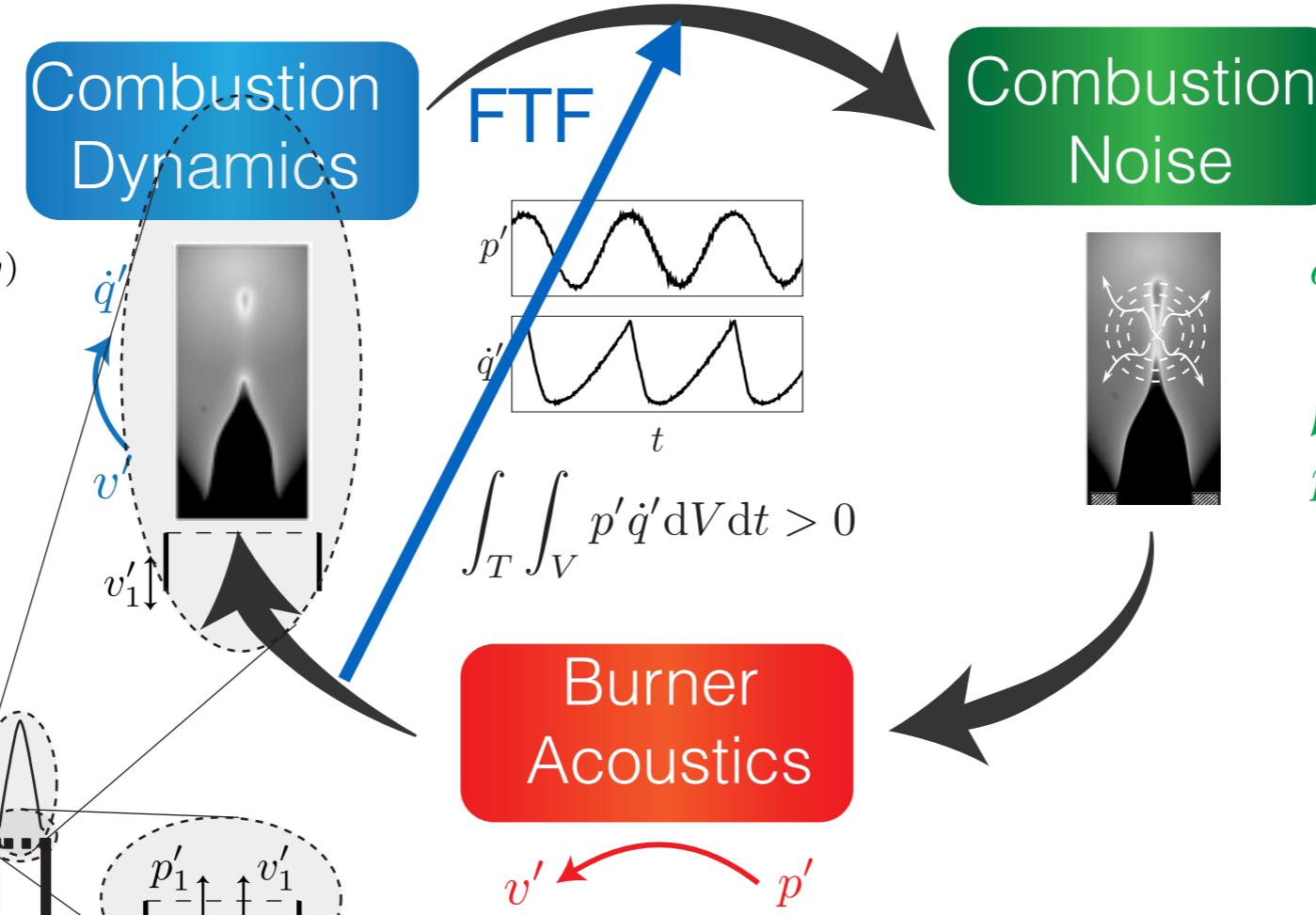
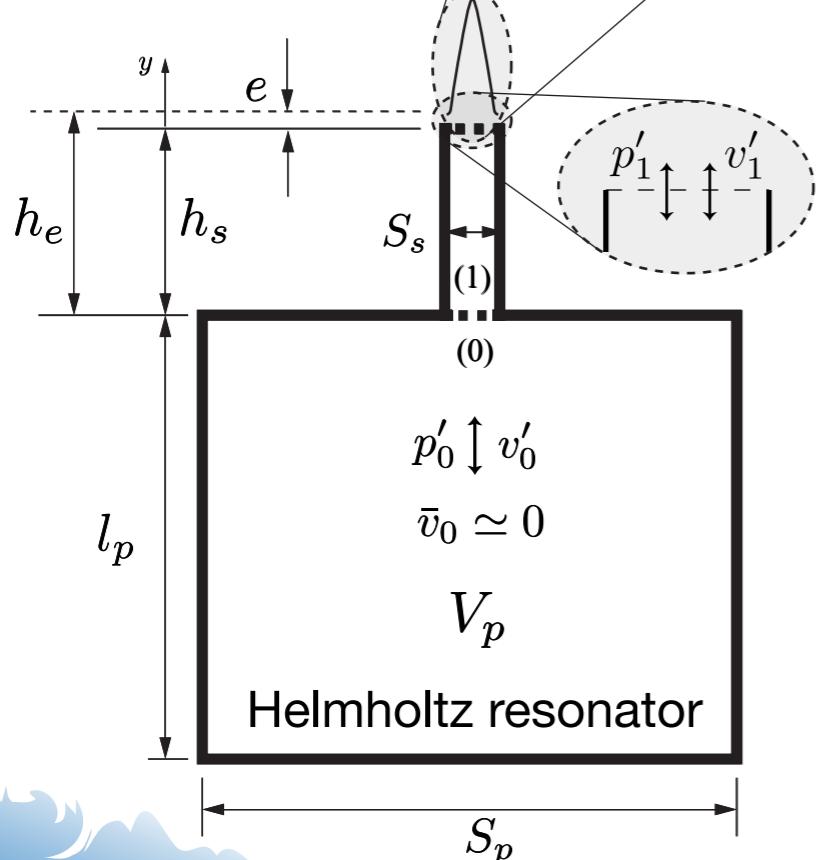
[4] Crocco 1951 jars.

[5] Keller and Saito 1987 cst.

Relation between v' and \dot{q}'

$$\mathcal{F}(\omega) = \frac{\dot{q}'/\bar{q}}{v'_1/\bar{v}} = \mathcal{G}(\omega)e^{i\varphi(\omega)}$$

$$\tilde{\mathcal{A}} = \frac{S_s}{s_L} \mathcal{G}(\omega)e^{i\varphi(\omega)} \tilde{v}_1$$



Relation between p' and v'

$$\frac{d^2 v'_1}{dt^2} + 2\delta \frac{dv'_1}{dt} + \omega_0^2 v'_1 = -\frac{1}{\rho_u h_e} \frac{dp'_1}{dt}$$

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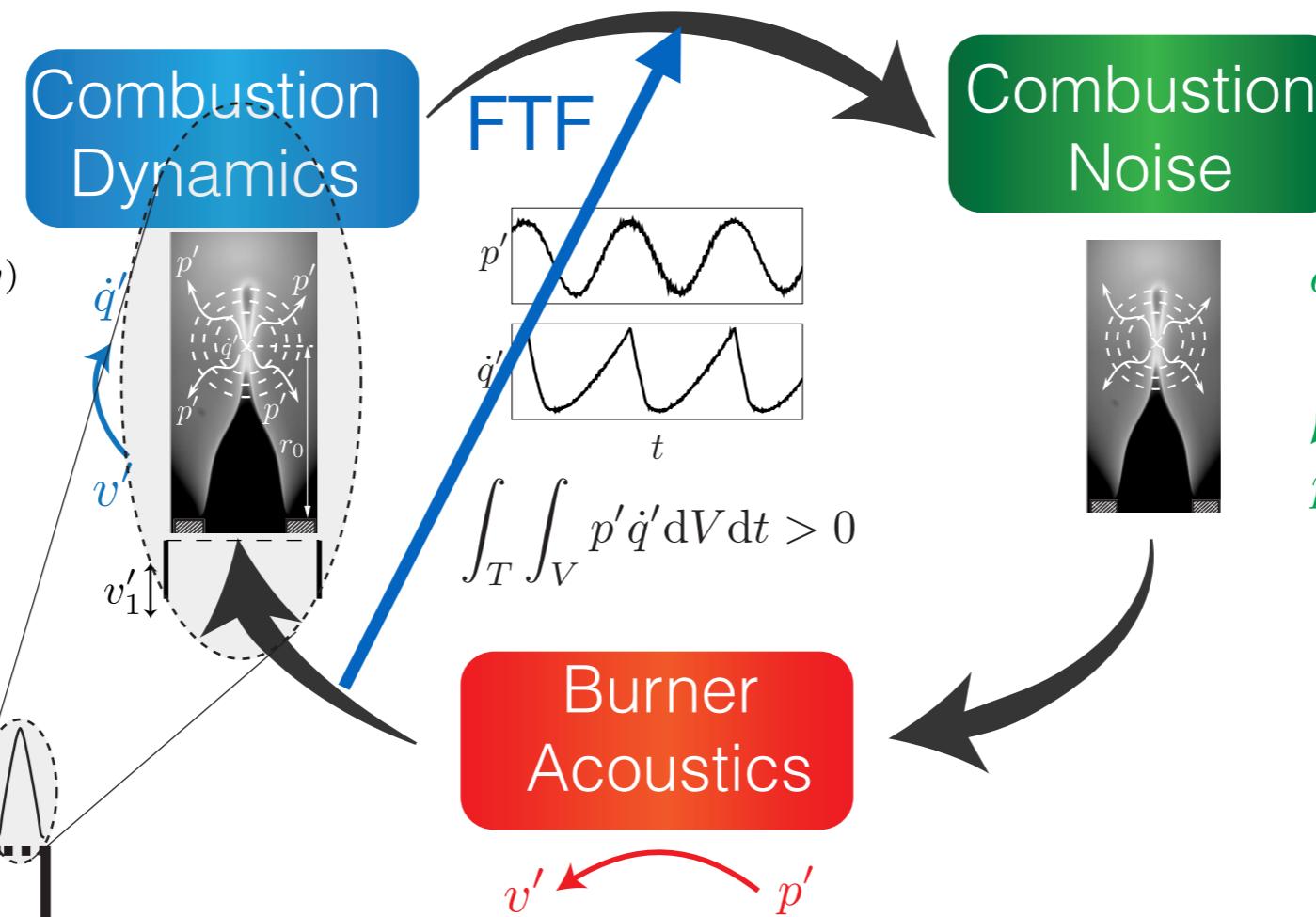
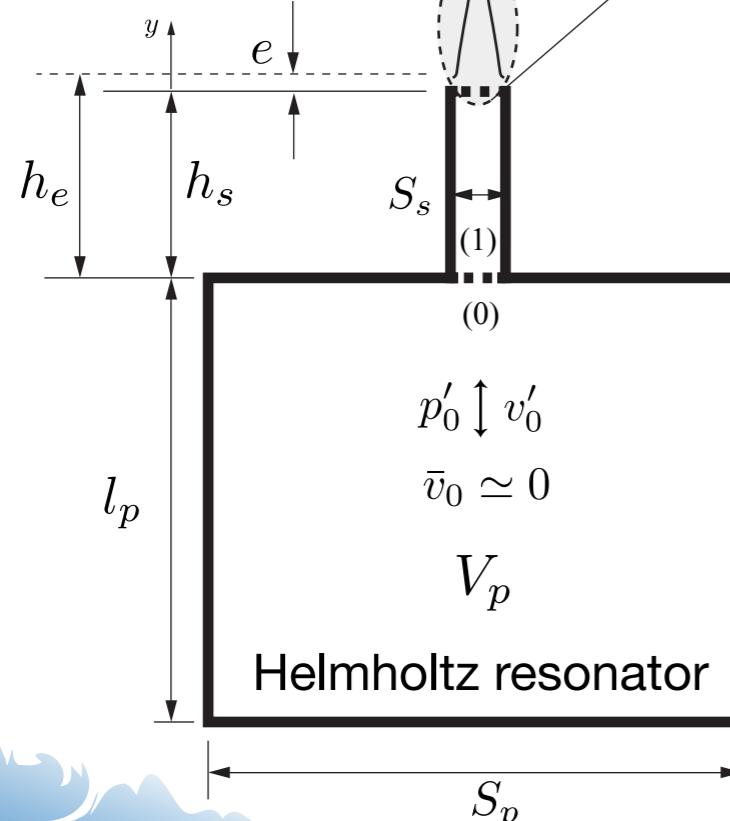
[6] Strahke 1971 *jfm.*

[7] Clavin and Siggia 1991 *cst.*

Relation between v' and \dot{q}'

$$\mathcal{F}(\omega) = \frac{\dot{q}'/\bar{q}}{v'_1/\bar{v}} = \mathcal{G}(\omega)e^{i\varphi(\omega)}$$

$$\tilde{\mathcal{A}} = \frac{S_s}{s_L} \mathcal{G}(\omega)e^{i\varphi(\omega)} \tilde{v}_1$$



Relation between \dot{q}' and p'

$$p'_1(t) = \frac{\rho_u(E-1)s_L}{4\pi r_0} \left[\frac{d\mathcal{A}}{dt} \right]_{t-\tau_{ac}}$$

$$\tilde{p}_1 = -\frac{\rho_u(E-1)s_L}{4\pi r_0} i\omega \tilde{\mathcal{A}}$$

Relation between p' and v'

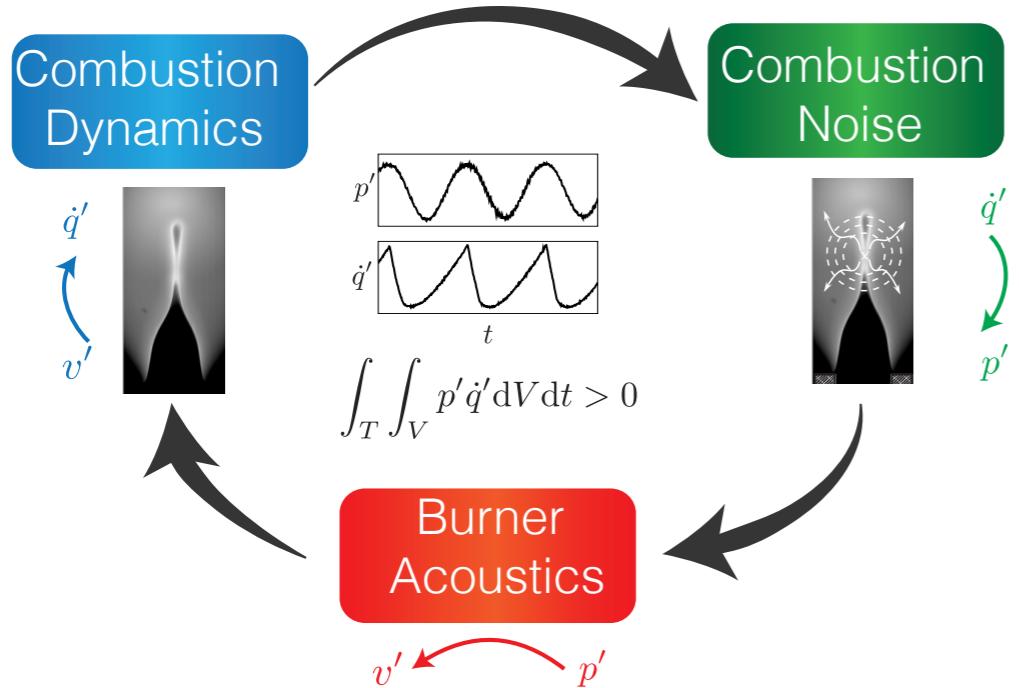
$$\frac{d^2v'_1}{dt^2} + 2\delta \frac{dv'_1}{dt} + \omega_0^2 v'_1 = -\frac{1}{\rho_u h_e} \frac{dp'_1}{dt}$$

$$\mathcal{Z}_1 = \frac{\tilde{p}_1}{\tilde{v}_1} = \frac{i\rho_u h_e}{\omega} [\omega^2 + 2i\delta\omega - \omega_0^2]$$

[1] Pierce 1981.

[2] Rienstra 1983 *jsv.*

[3] Durox *et al.* 2002 *pci.*



Dispersion relation:

$$[1 + \mathcal{N} e^{i\varphi(\omega)}] \omega^2 + 2i\delta\omega - \omega_0^2 = 0$$

Interaction index:

$$\mathcal{N} = \frac{1}{4\pi} \frac{S_s(E-1)}{h_e} \frac{\mathcal{G}(\omega)}{r_0}$$

The solution of the system is:

$$\omega = \omega_r + i\omega_i$$

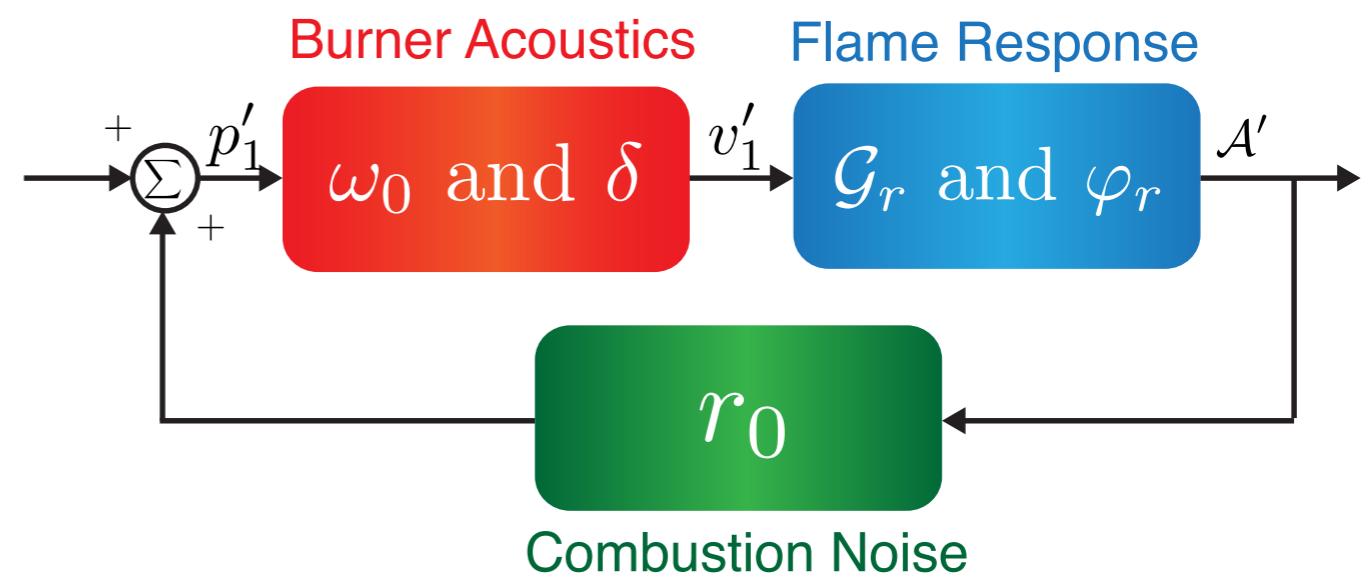
$\Re(\omega) = \omega_r \rightarrow$ Resonance frequency

$\Im(\omega) = \omega_i \rightarrow$ Growth rate

The system will develop combustion instabilities if:

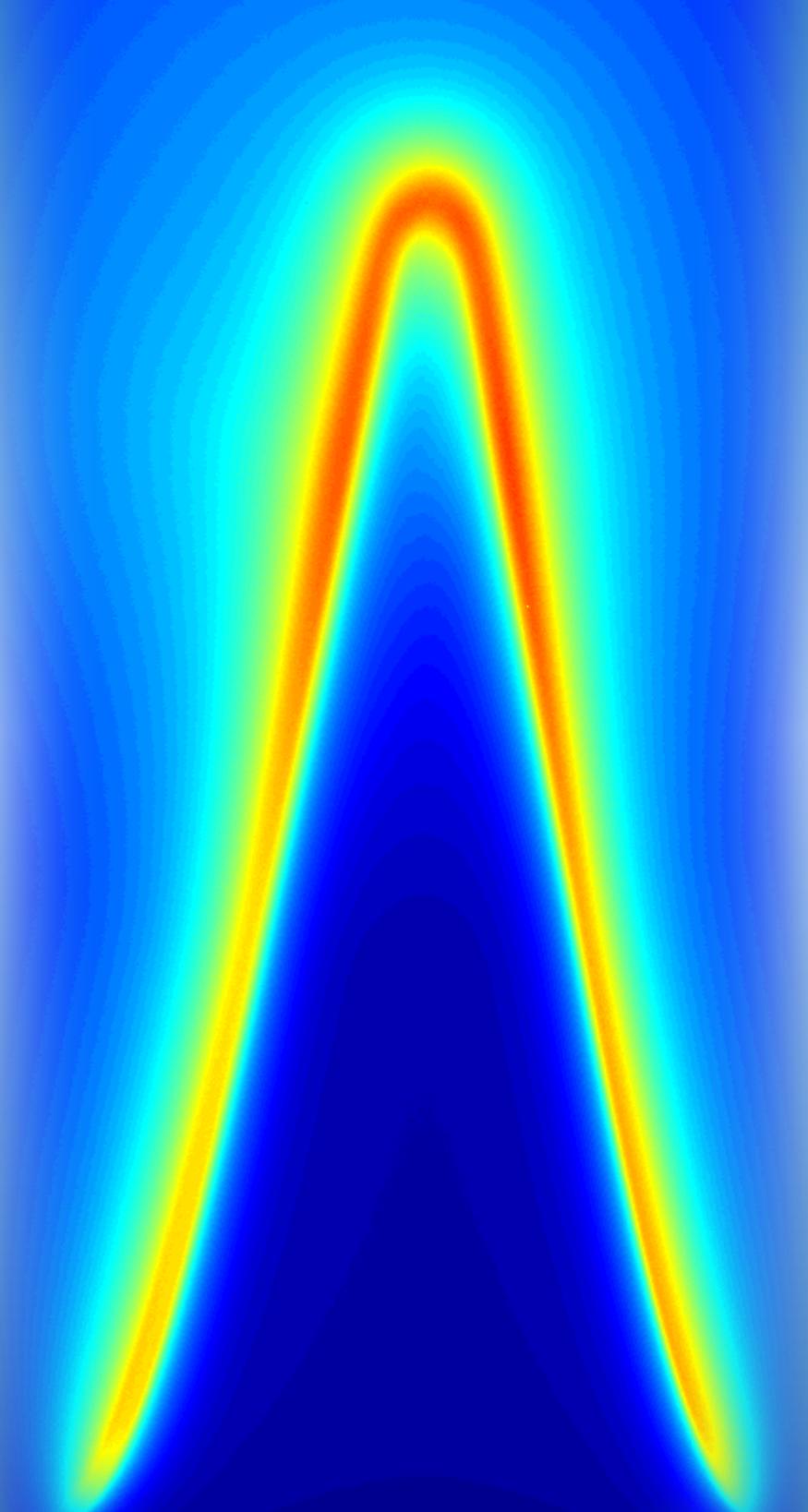
$$\omega_i > 0$$

The stability of the system depends on five parameters:



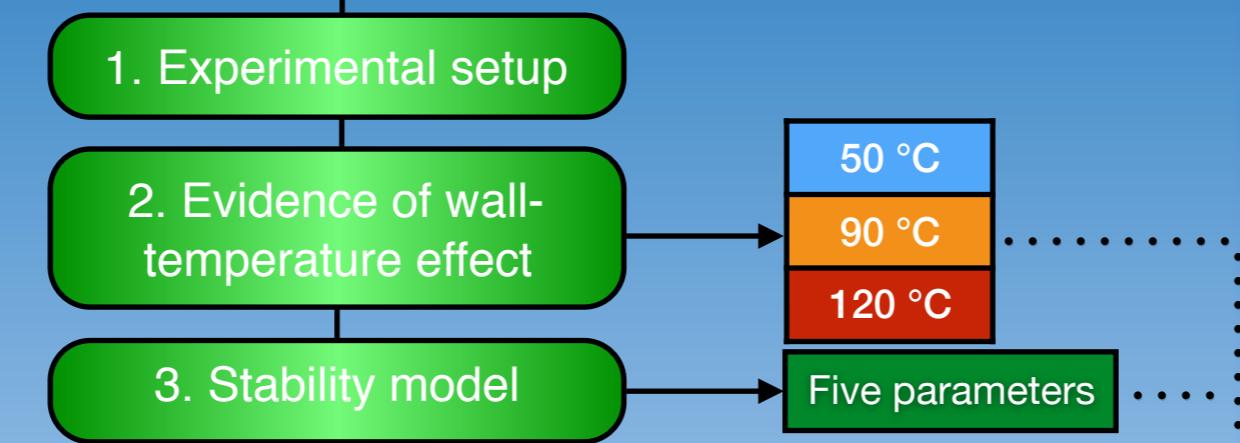
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1. Derive a stability model able to predict the experimental observations.
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Outline

Part I: The Slot Burner



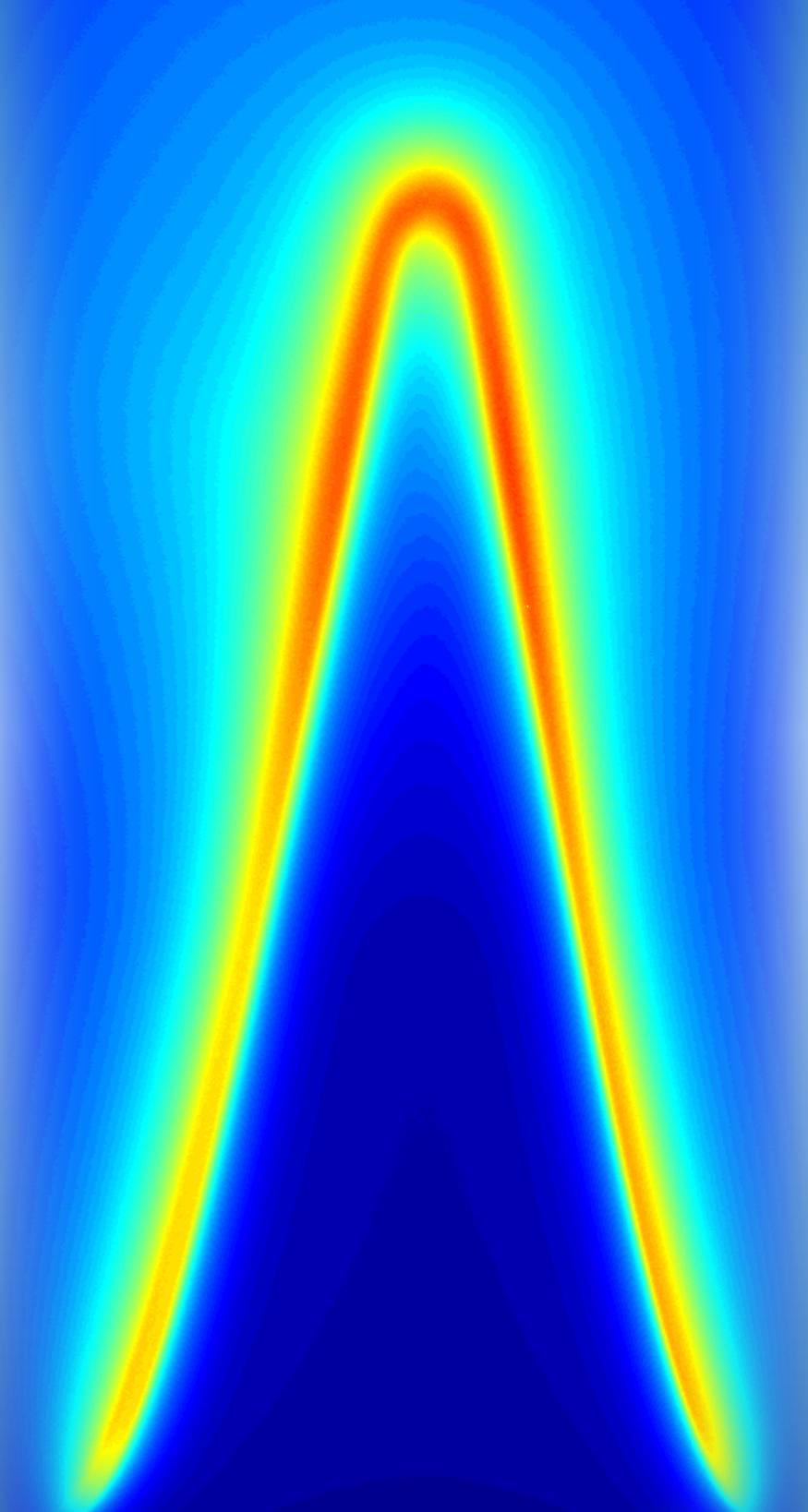
Part II: Experimental Measurements



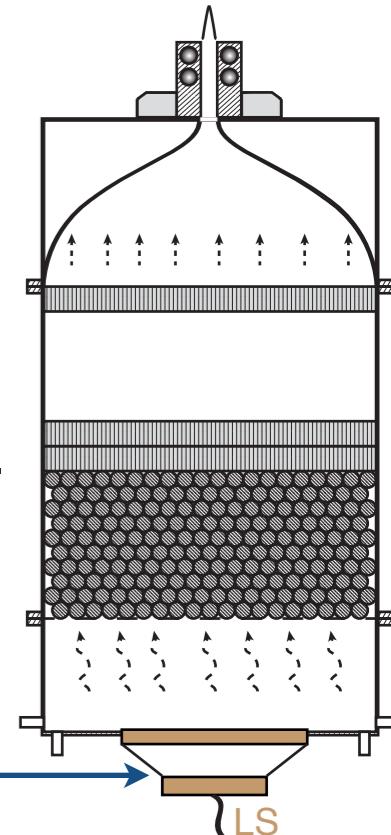
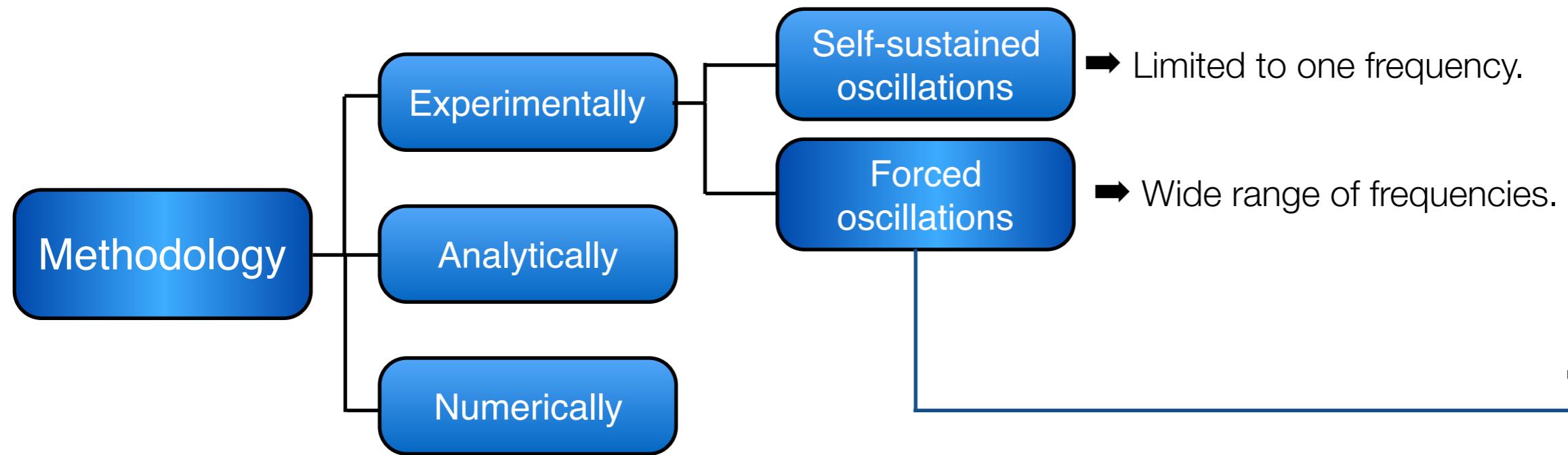
Part III: Flame Dynamics

8. Flame front dynamics

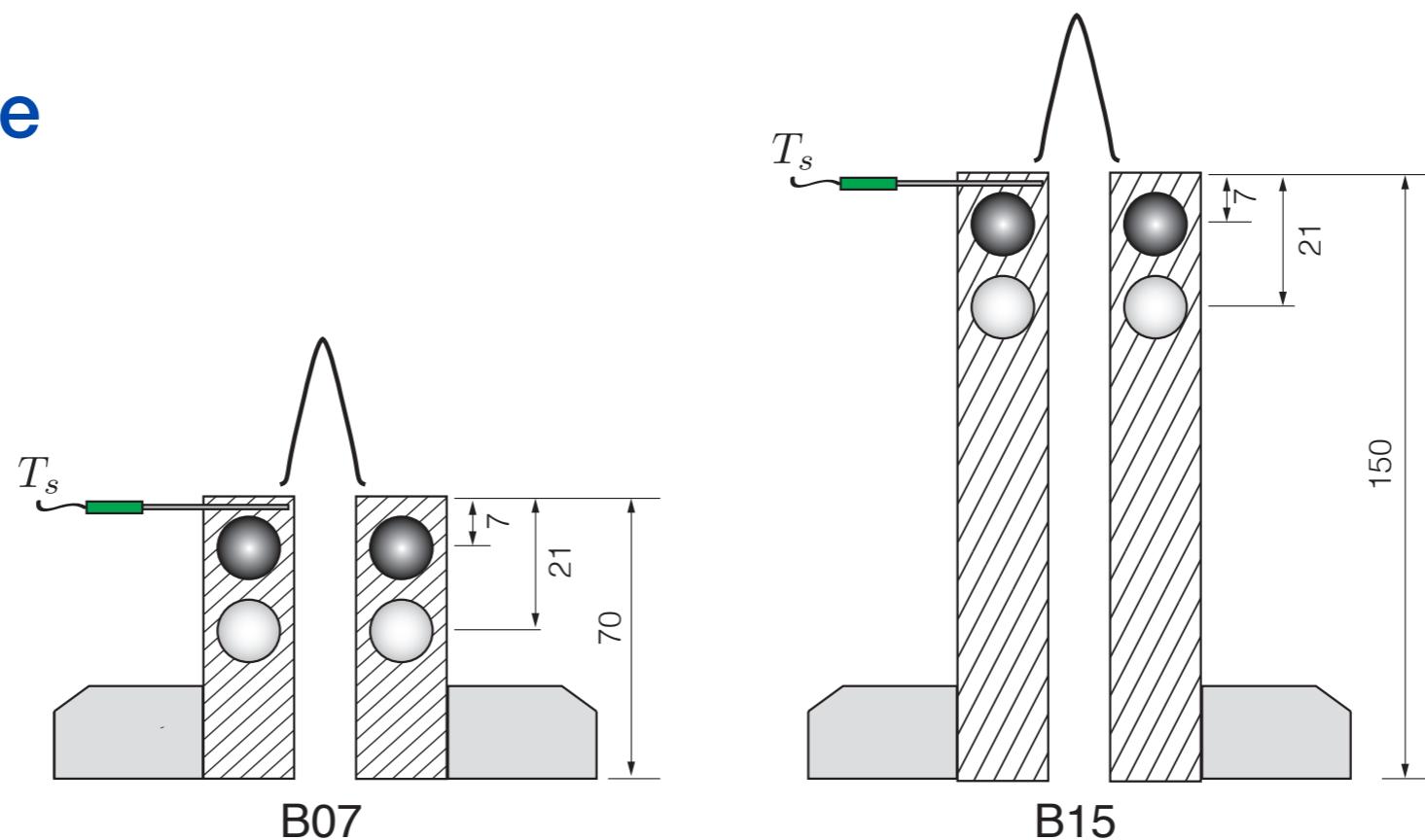
9. Flame root dynamics



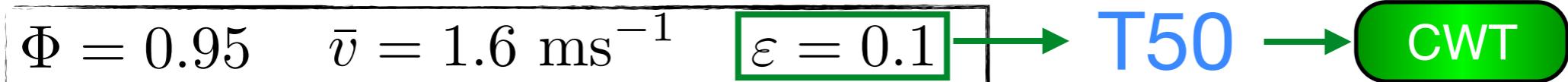
Methodology:



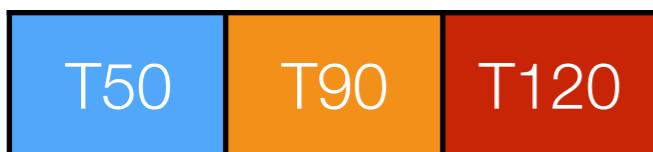
Stabilizing the flame



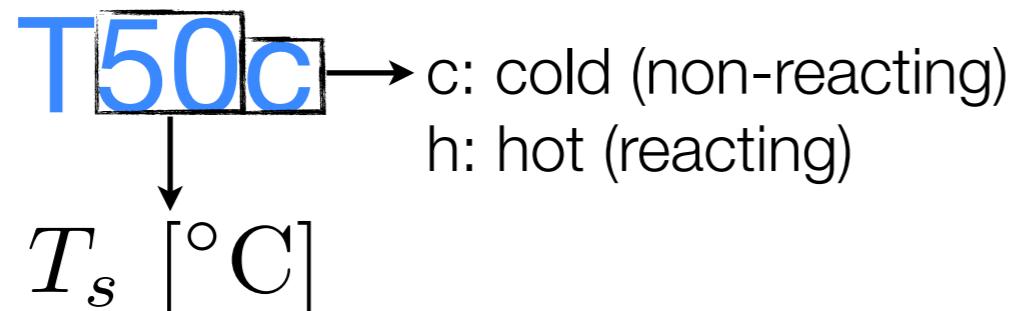
- ★ In all cases, the operating conditions are kept constant



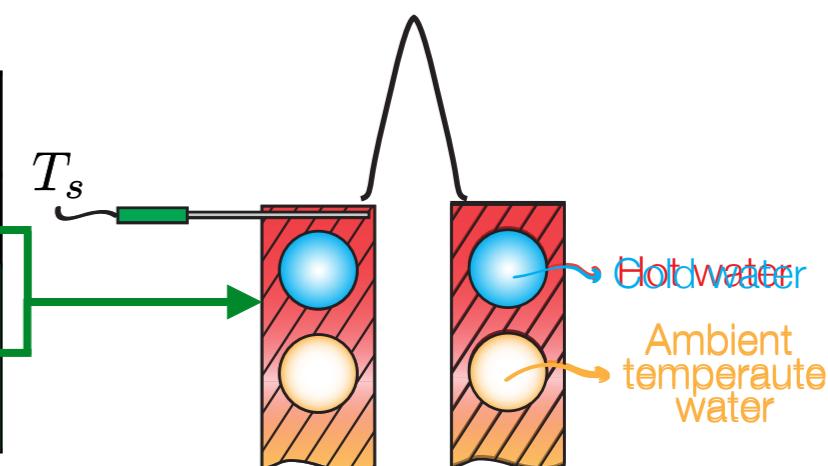
- ★ In all cases, the wall temperature is controlled and it is parametrized here by T_s
- ★ Three temperature reference cases with three different dynamic behaviors:



- ★ Code for the experiments:



	Measure	Burner	Wall temperature			Configuration
Burner Acoustics	ω_0	B07	T50c	T90c		Non-reacting
Combustion Noise	r_0	B15	T50h	T90h	T120h	Reacting
Flame Response	\mathcal{G}_r	φ_r	B15			



Outline

Part I: The Slot Burner

1. Experimental setup

2. Evidence of wall-temperature effect

3. Stability model

50 °C

90 °C

120 °C

Five parameters

Part II: Experimental Measurements

4. Burner acoustics

Do they depend on the
wall temperature?

5. Combustion noise

Do they depend on the
wall temperature?

6. Flame response

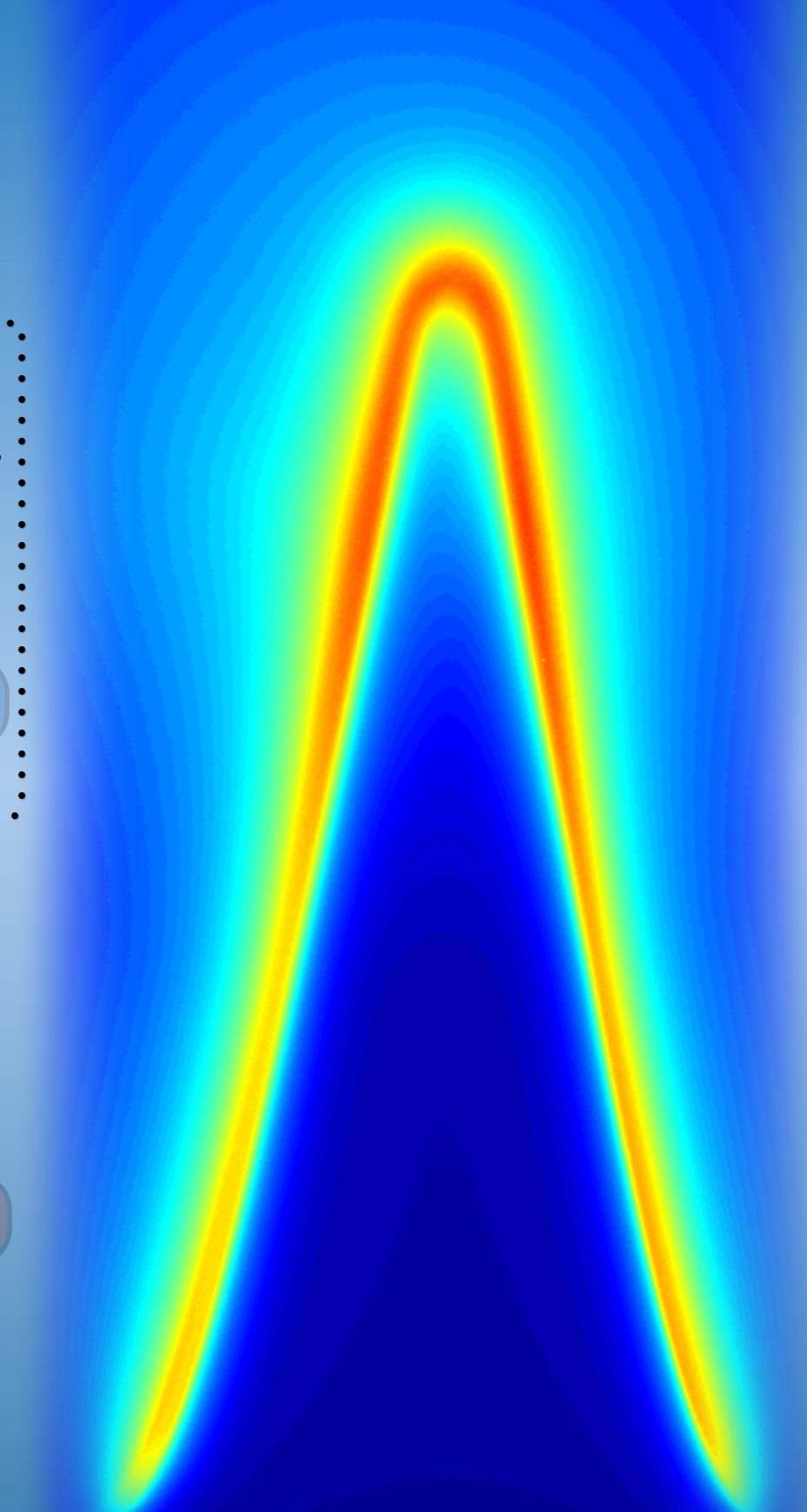
Do they depend on the
wall temperature?

7. Burner stability

Part III: Flame Dynamics

8. Flame front dynamics

9. Flame root dynamics



4. Burner acoustics

1. How to measure the natural ω_0 pulsation and the dissipation δ of the burner?
2. Do they depend on wall temperature T_s ?

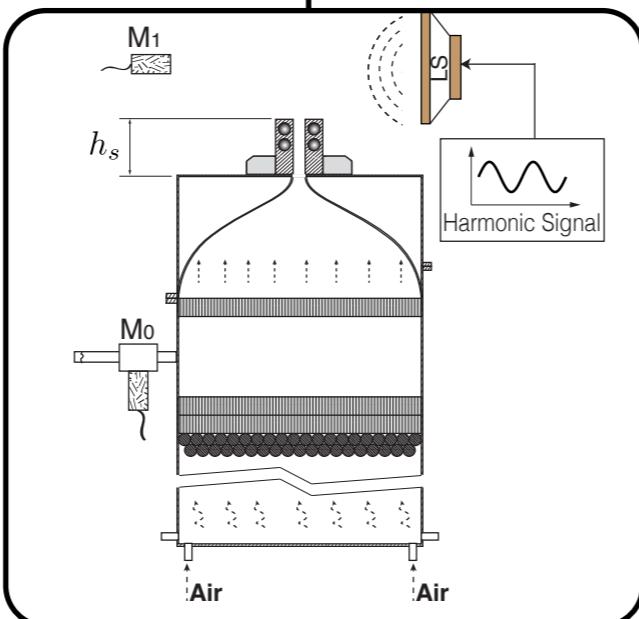
Burner acoustics

Non-reacting

Reacting

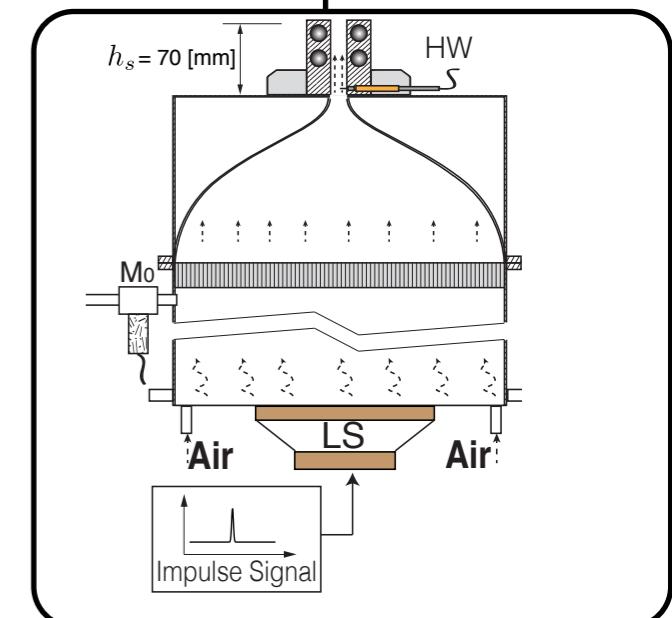
Harmonic response

$$\frac{d^2 p'_0}{dt^2} + 2\delta \frac{dp'_0}{dt} + \omega_0^2 p'_0 = \omega_0^2 p'_1$$

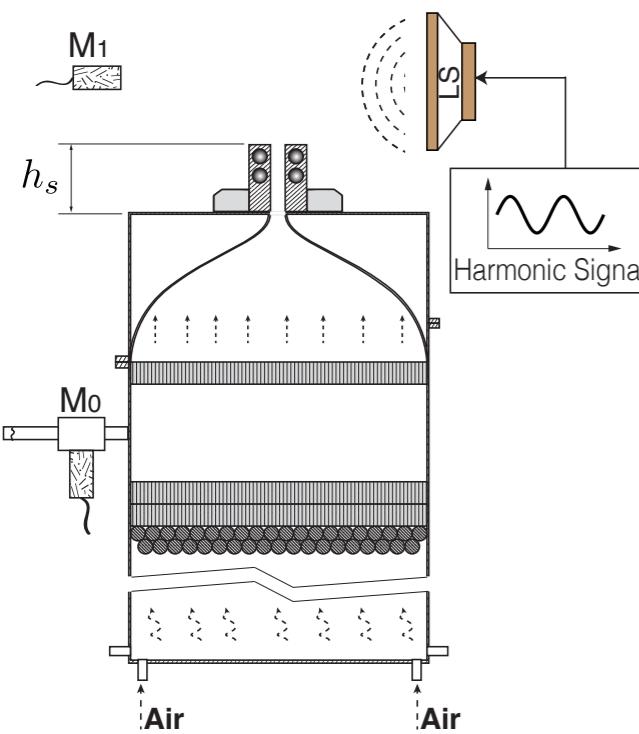


Impulse response

$$\frac{d^2 v'_1}{dt^2} + 2\delta \frac{dv'_1}{dt} + \omega_0^2 v'_1 = 0$$

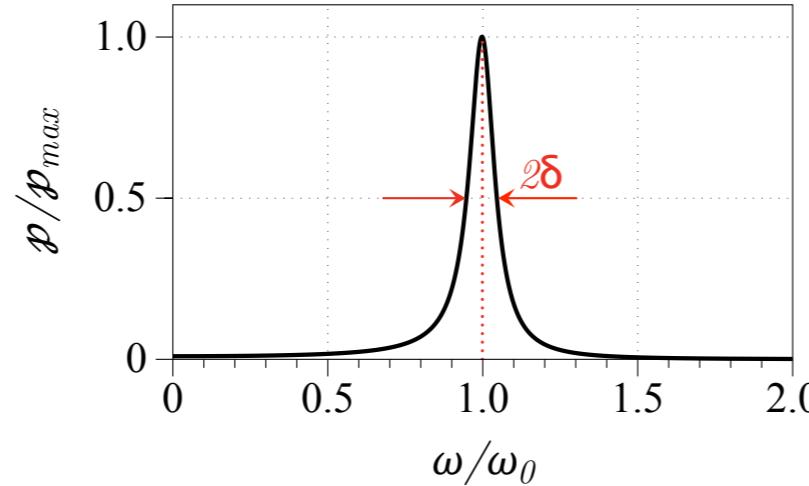


1. Harmonic response:

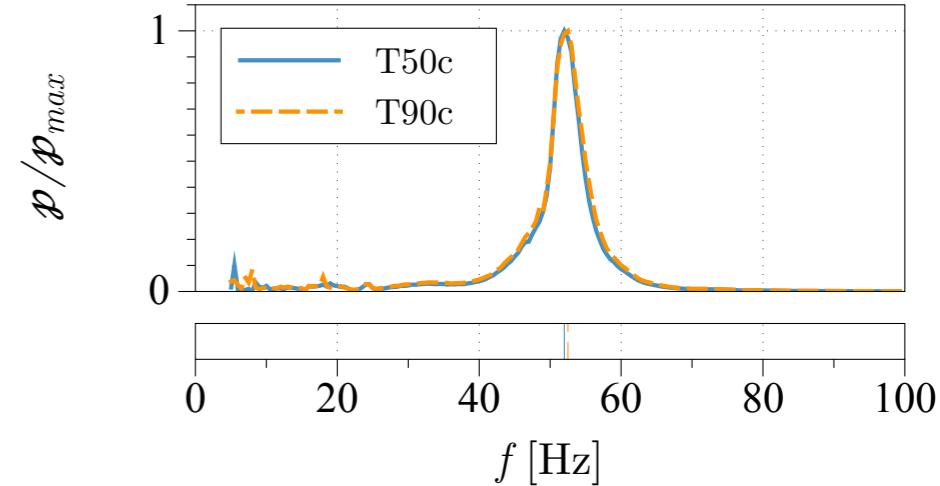


$$\frac{d^2 p'_0}{dt^2} + 2\delta \frac{dp'_0}{dt} + \omega_0^2 p'_0 = \omega_0^2 p'_1$$

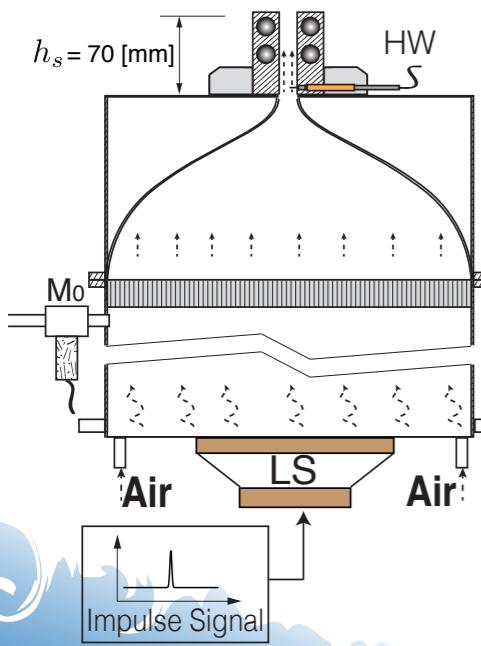
$$\mathcal{P} = \left(\frac{\tilde{p}_0}{\tilde{p}_1} \right)^2$$



	HR	
	$\omega_0/2\pi$ [Hz]	δ [s ⁻¹]
T50c	52.0	14.5
T90c	52.5	15.7

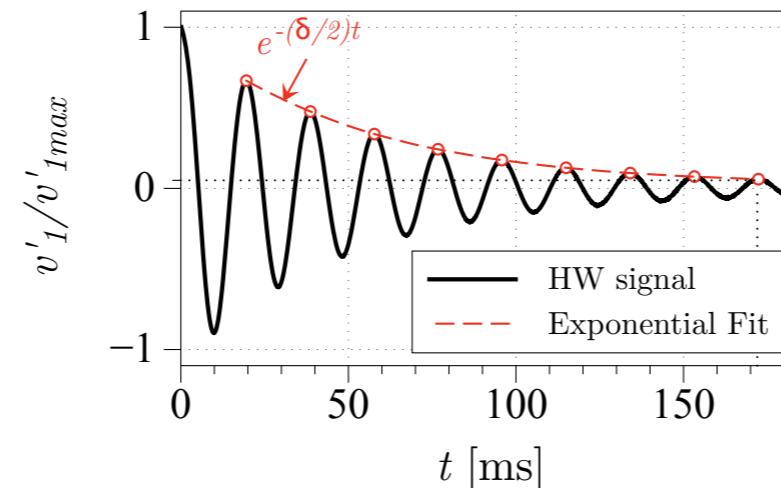


2. Impulse response:

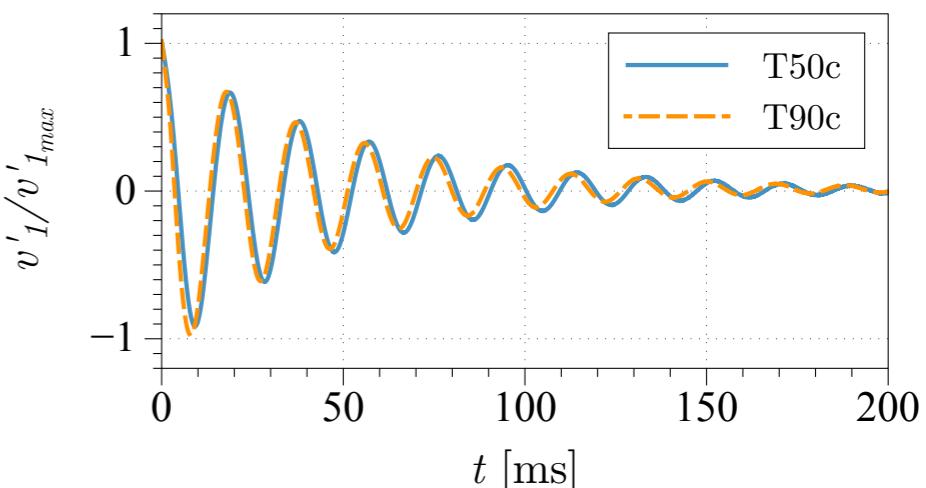


$$\frac{d^2 v'_1}{dt^2} + 2\delta \frac{dv'_1}{dt} + \omega_0^2 v'_1 = 0$$

$$v'_1(t)/v'_{1max} = e^{-(\delta/2)t} \cos(\omega_0 t)$$



	IR	
	$\omega_0/2\pi$ [Hz]	δ [s ⁻¹]
T50c	52.4	16.3
T90c	53.1	16.8



Outline

Part I: The Slot Burner

1. Experimental setup

2. Evidence of wall-temperature effect

3. Stability model

50 °C

90 °C

120 °C

Five parameters

Part II: Experimental Measurements

4. Burner acoustics

5. Combustion noise

6. Flame response

No Ts dependency

.....

Do they depend on the
wall temperature?

.....

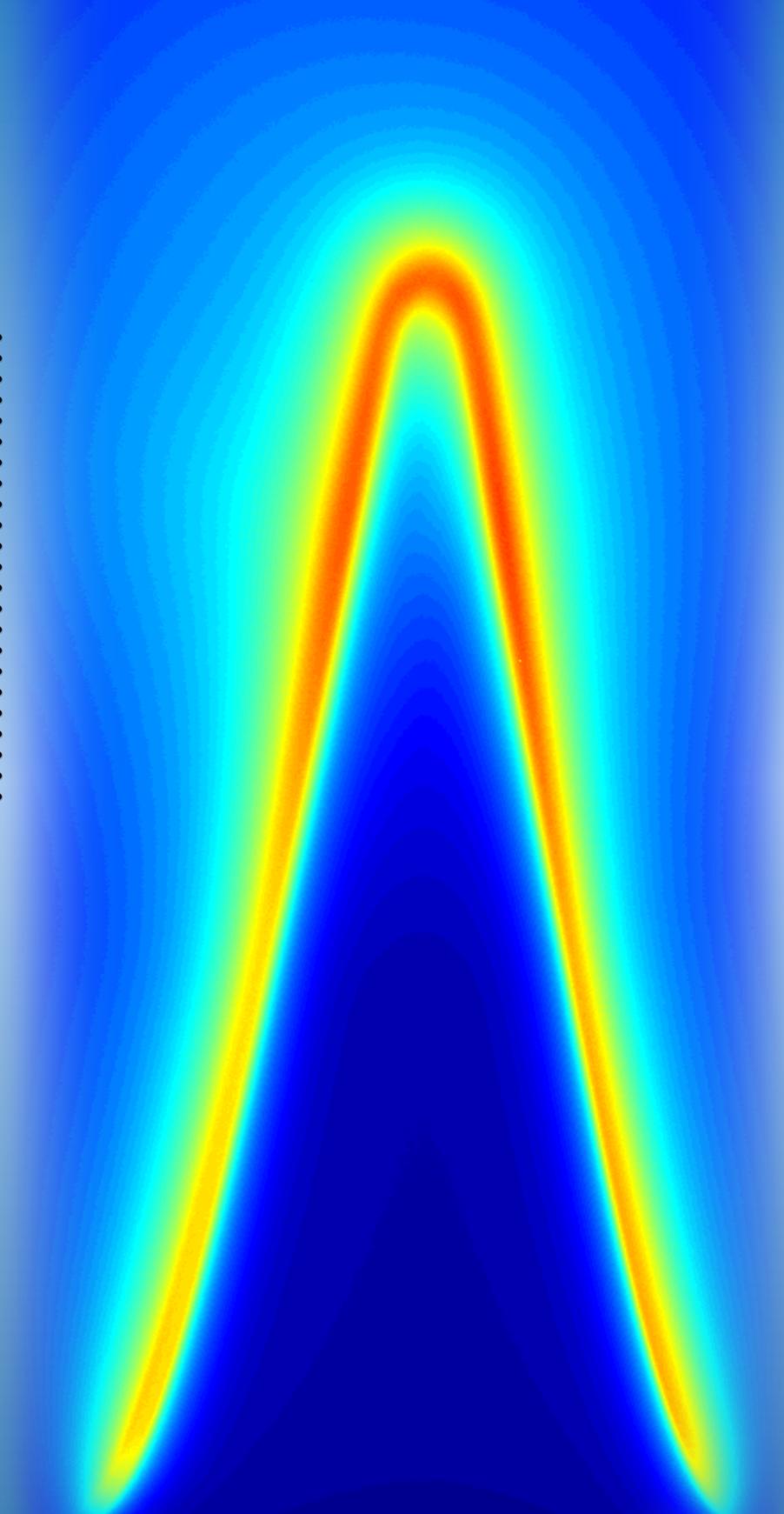
Do they depend on the
wall temperature?

7. Burner stability

Part III: Flame Dynamics

8. Flame front dynamics

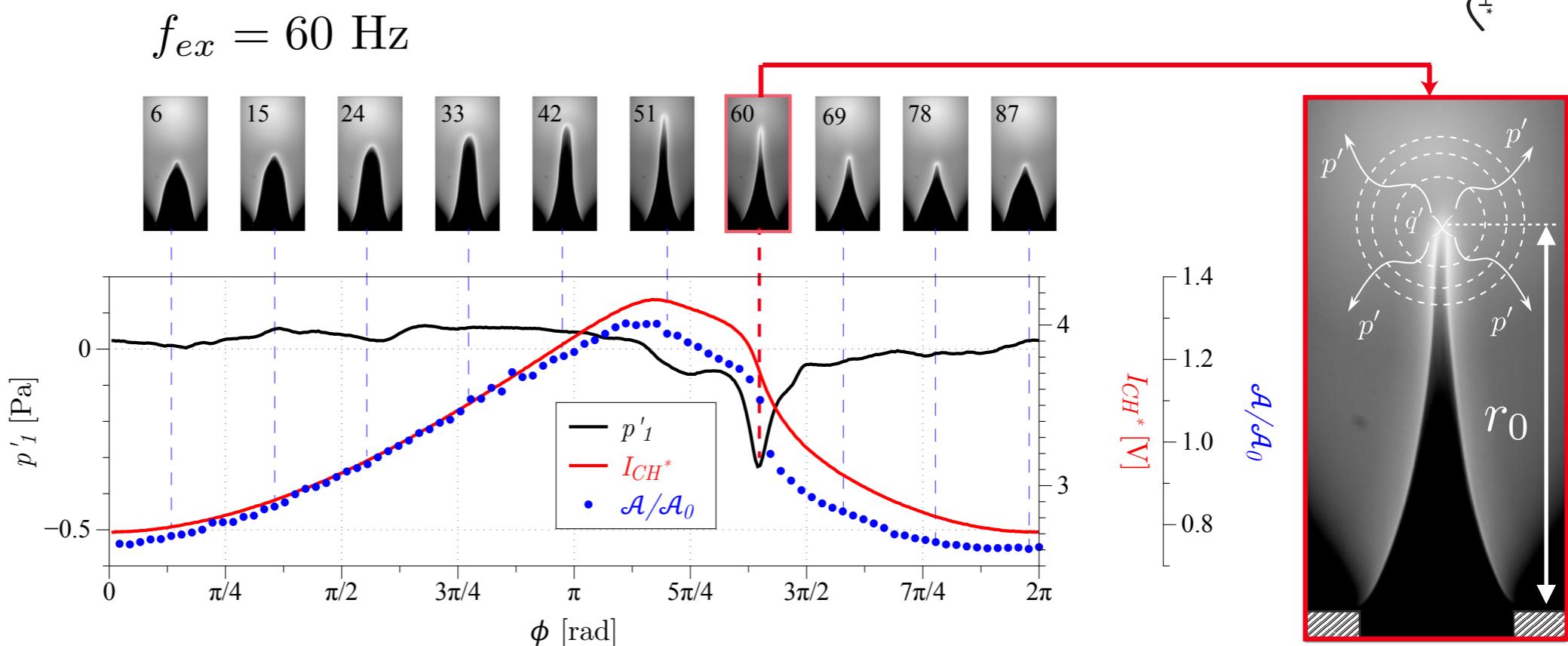
9. Flame root dynamics



5. Combustion noise

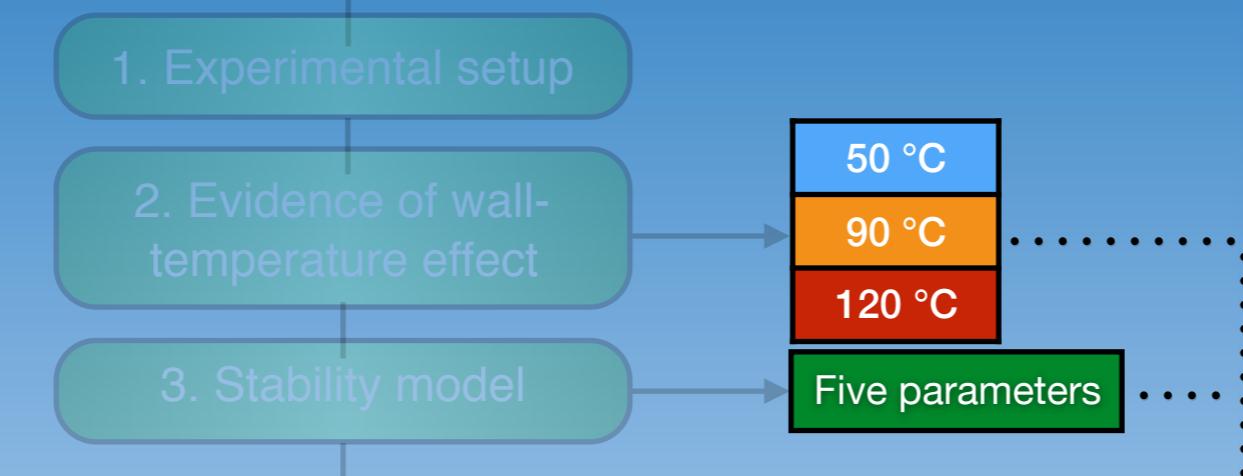
1. Can we reproduce the far-field pressure from the PM signal?
2. How to measure the pinching distance r_0 ?
3. Does r_0 depend on the wall temperature T_s ?

	r_0 [mm]
T50h	22.5
T90h	21.8
T120h	20.1
Mean	21.5

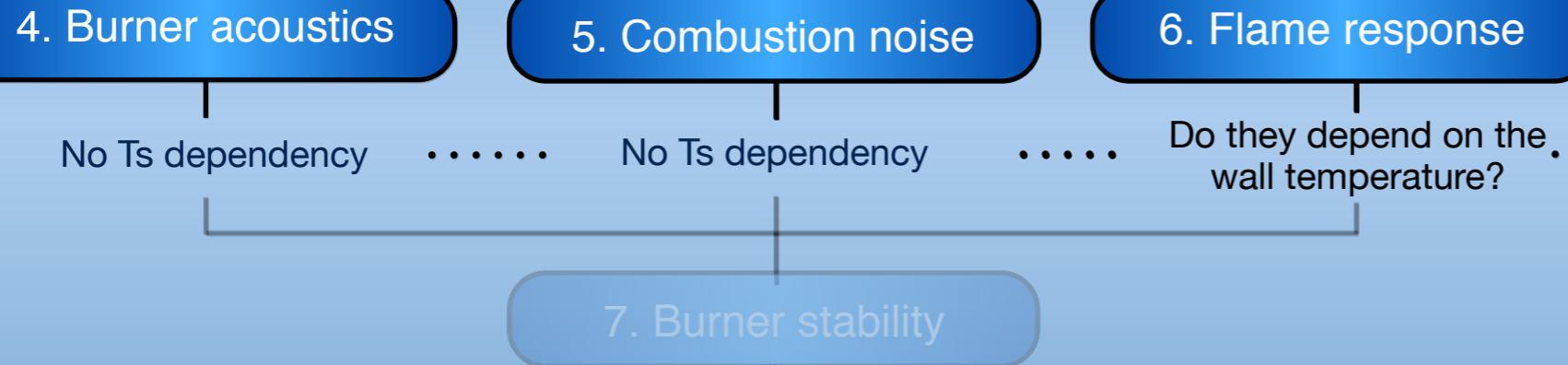


Outline

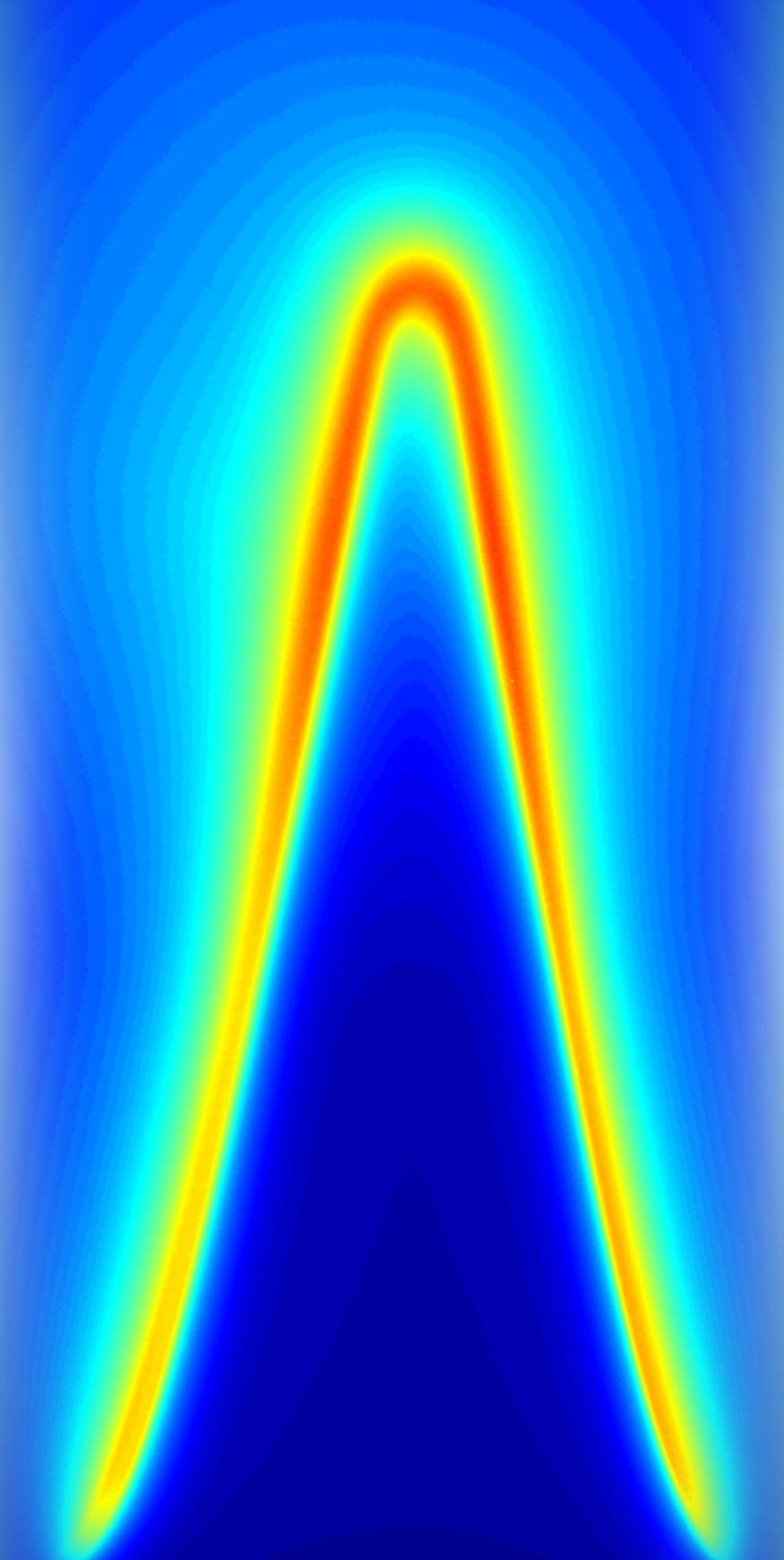
Part I: The Slot Burner



Part II: Experimental Measurements

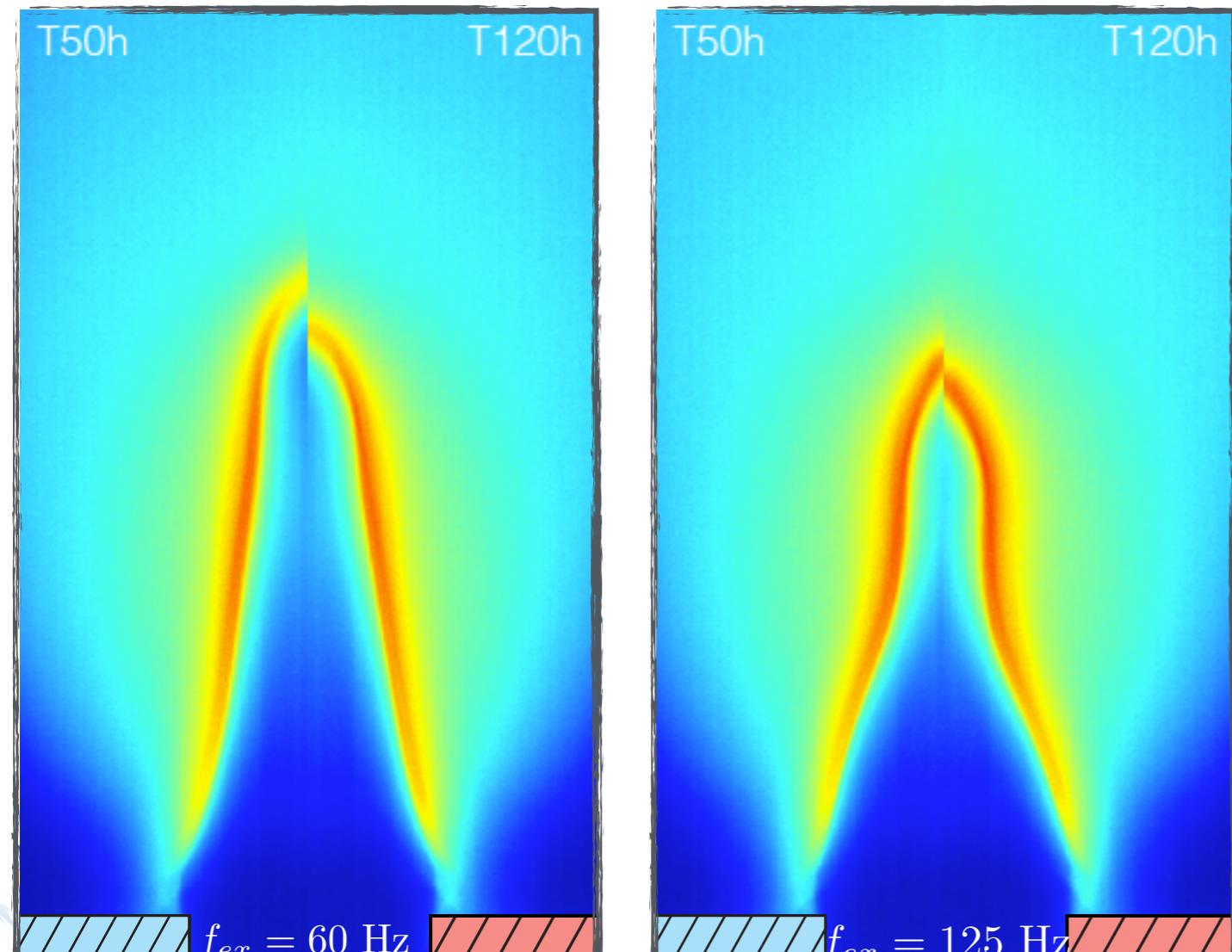


Part III: Flame Dynamics

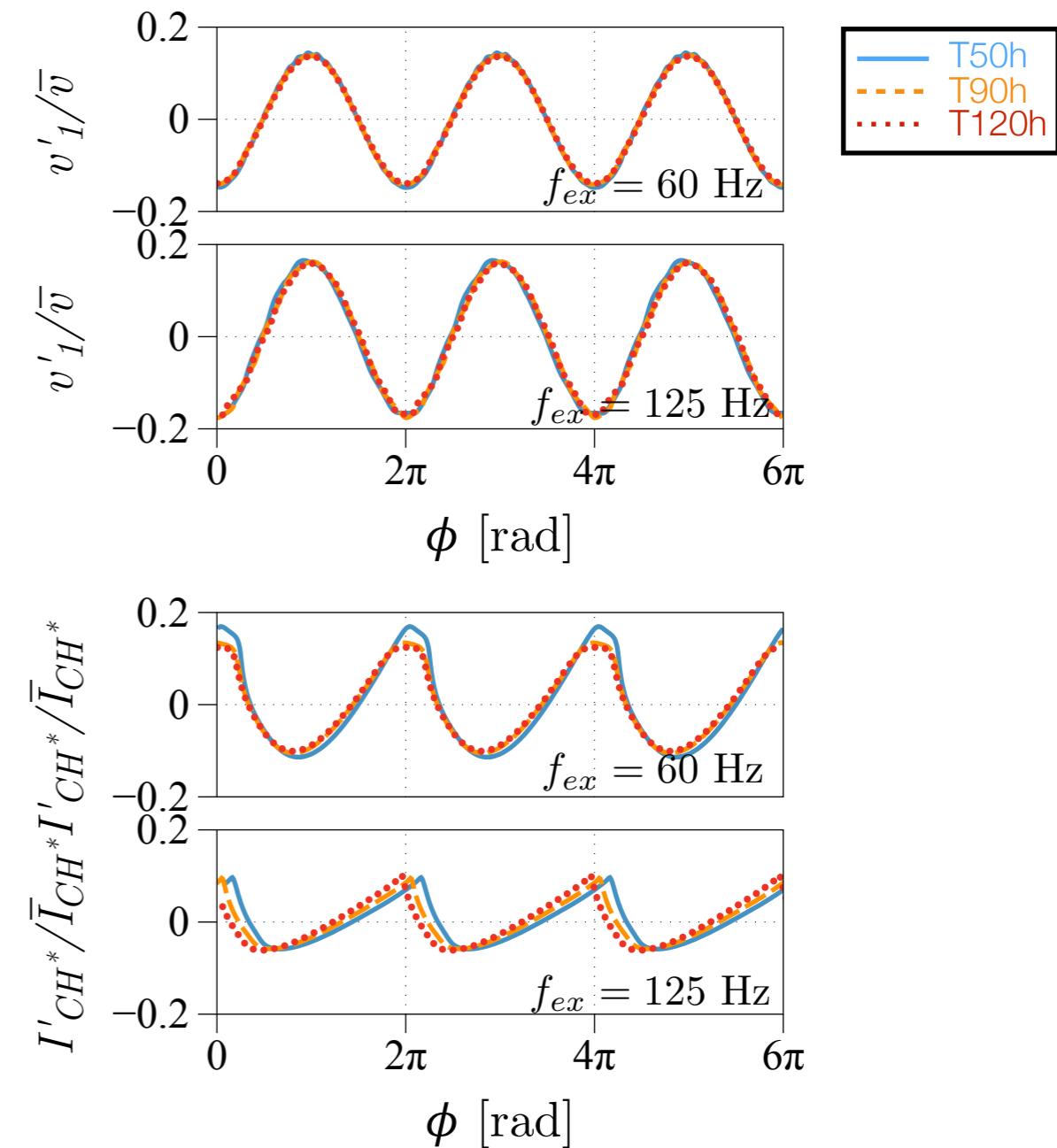


6. Flame response

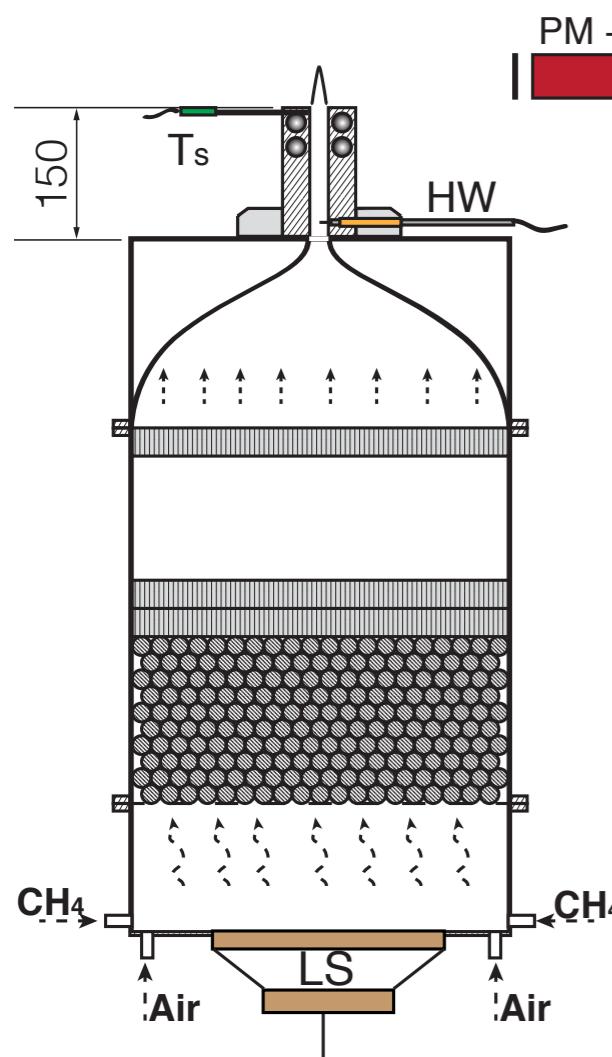
1. Is the flame response affected by the wall temperature T_s ?



2. Is the velocity fluctuation the same for all cases?



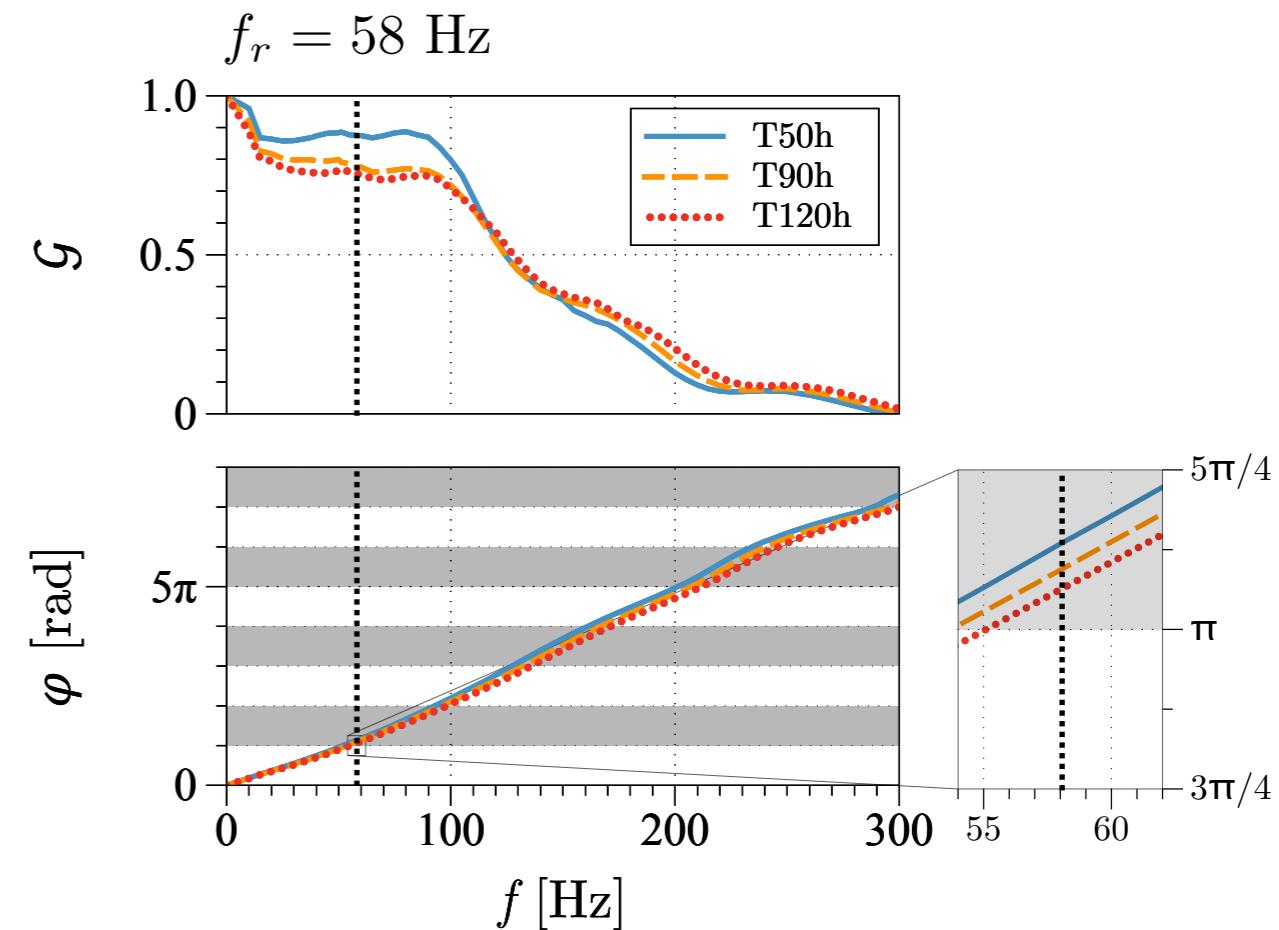
3. How does it affect the FTF?



$$\mathcal{F}(\omega, T_s) = \frac{\dot{q}' / \bar{q}}{v' / \bar{v}}$$

$$\mathcal{G} = |\mathcal{F}(\omega, T_s)|$$

$$\varphi = \arg(\mathcal{F}(\omega, T_s))$$



* Instability bands are determined for an idealized case without dissipation: $\varphi \in [\pi, 2\pi]$ modulo 2π

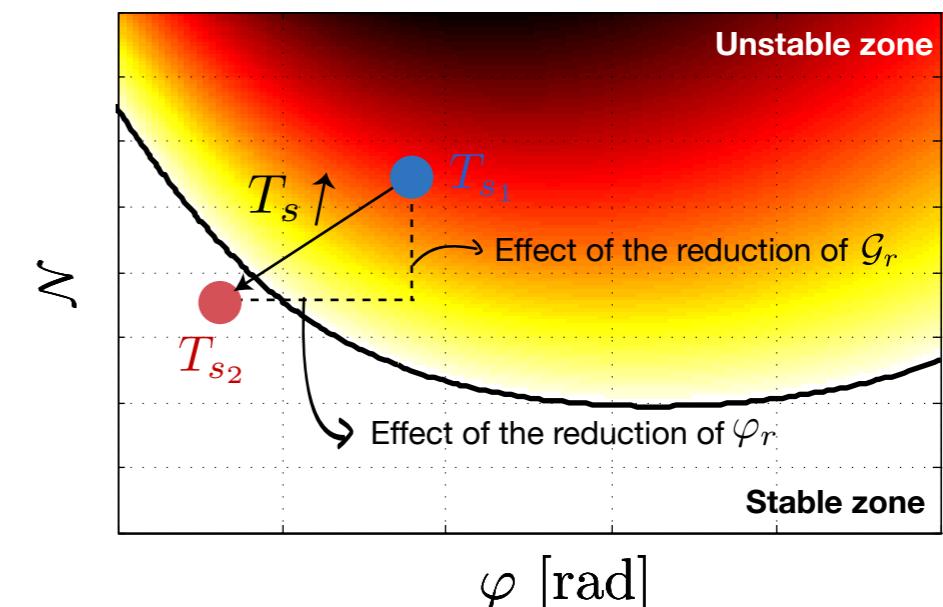
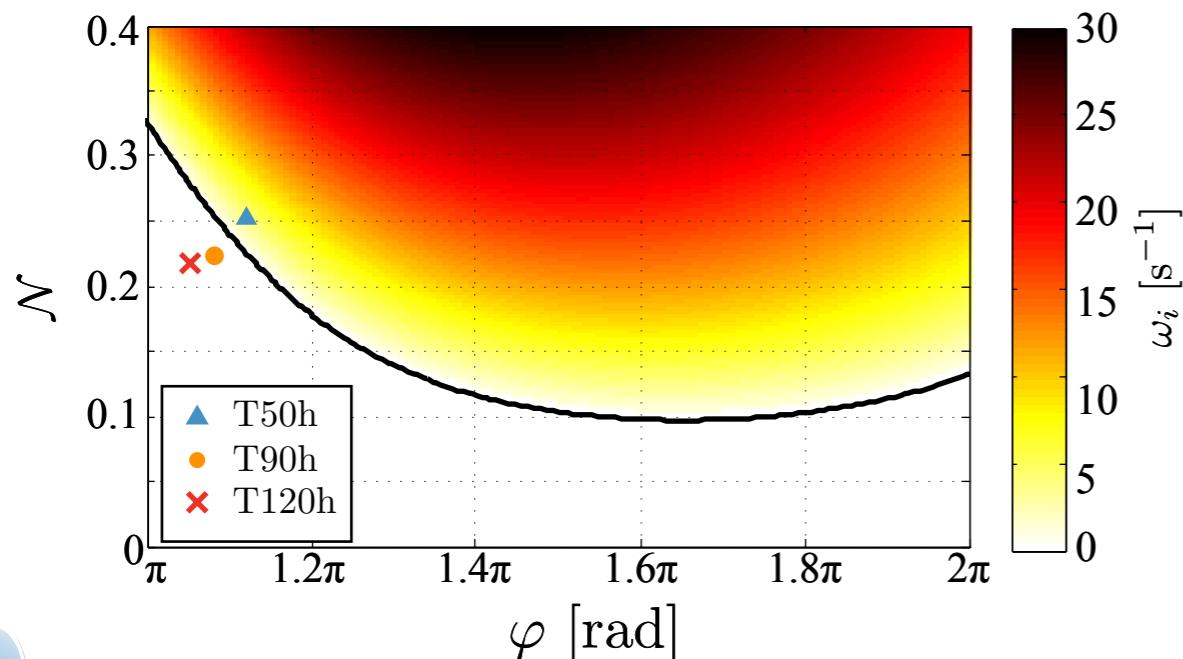
	\mathcal{G}_r	$\varphi_r [\text{rad}]$
T50h	0.88	1.13π
T90h	0.78	1.09π
T120h	0.75	1.06π
T50h-T120h	14 %	6 %

7. Burner Stability

Do the changes on the FTF explain the stability variations?

$$\left[1 + \mathcal{N}e^{i\varphi(\omega)}\right] \omega^2 + 2i\delta\omega - \omega_0^2 = 0$$

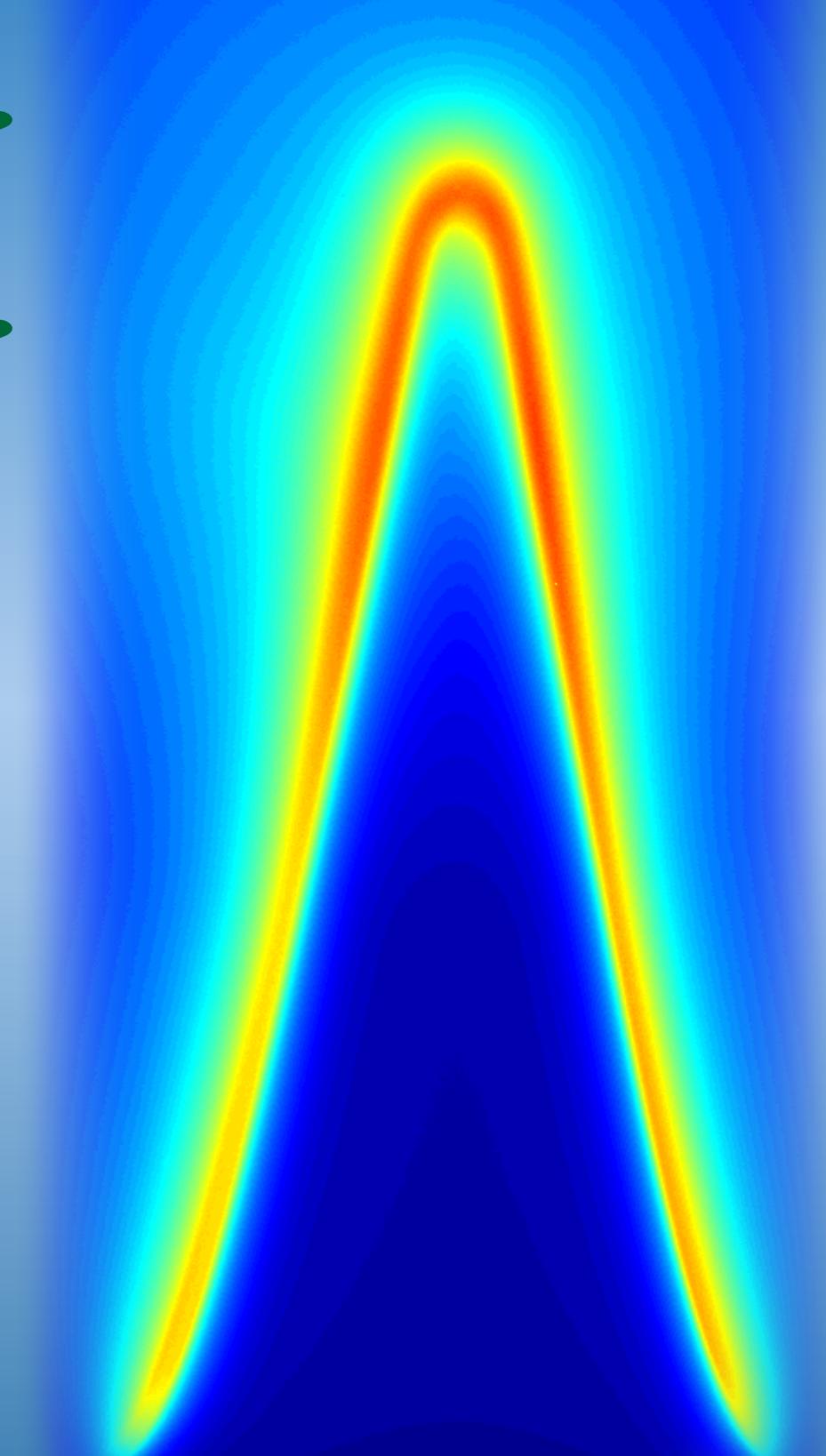
	Acoustics		Noise	Flame response		\mathcal{N}	Solution DR		Experimental observation
	$\omega_0/2\pi$ [Hz]	δ [s^{-1}]		\mathcal{G}_r	φ_r [rad]		$\omega_r/2\pi$ [Hz]	ω_i [s^{-1}]	
	T50			0.87	1.12π		59.1	2.4	Unstable
T90	52.5	15.8	21.5	0.77	1.08π	0.23	59.4	-6.9	Stable
T120				0.75	1.05π	0.22	59.3	-12.0	Stable



The flame's natural instability can be suppressed by increasing T_s by just 40 K. This 40 K variation changes the gain from 0.87 to 0.77 and the phase from 1.12π rad to 1.08π rad; This is sufficient to stabilize the system.

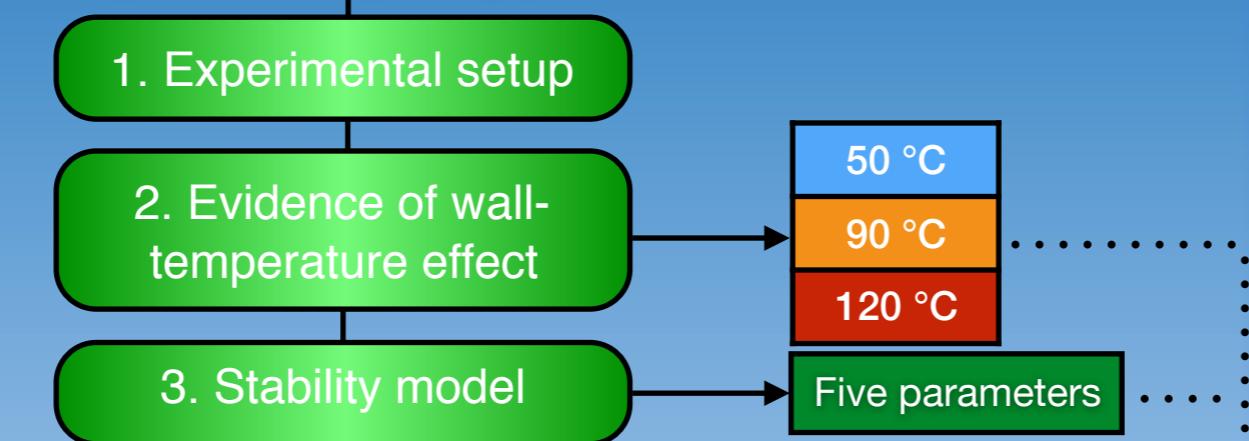
Objectives

1. Derive a stability model able to predict the experimental observations.
2. Determine which mechanism(s) is/are responsible for stabilizing the flame.
3. Understand how this mechanism(s) work(s).



Outline

Part I: The Slot Burner



Part II: Experimental Measurements



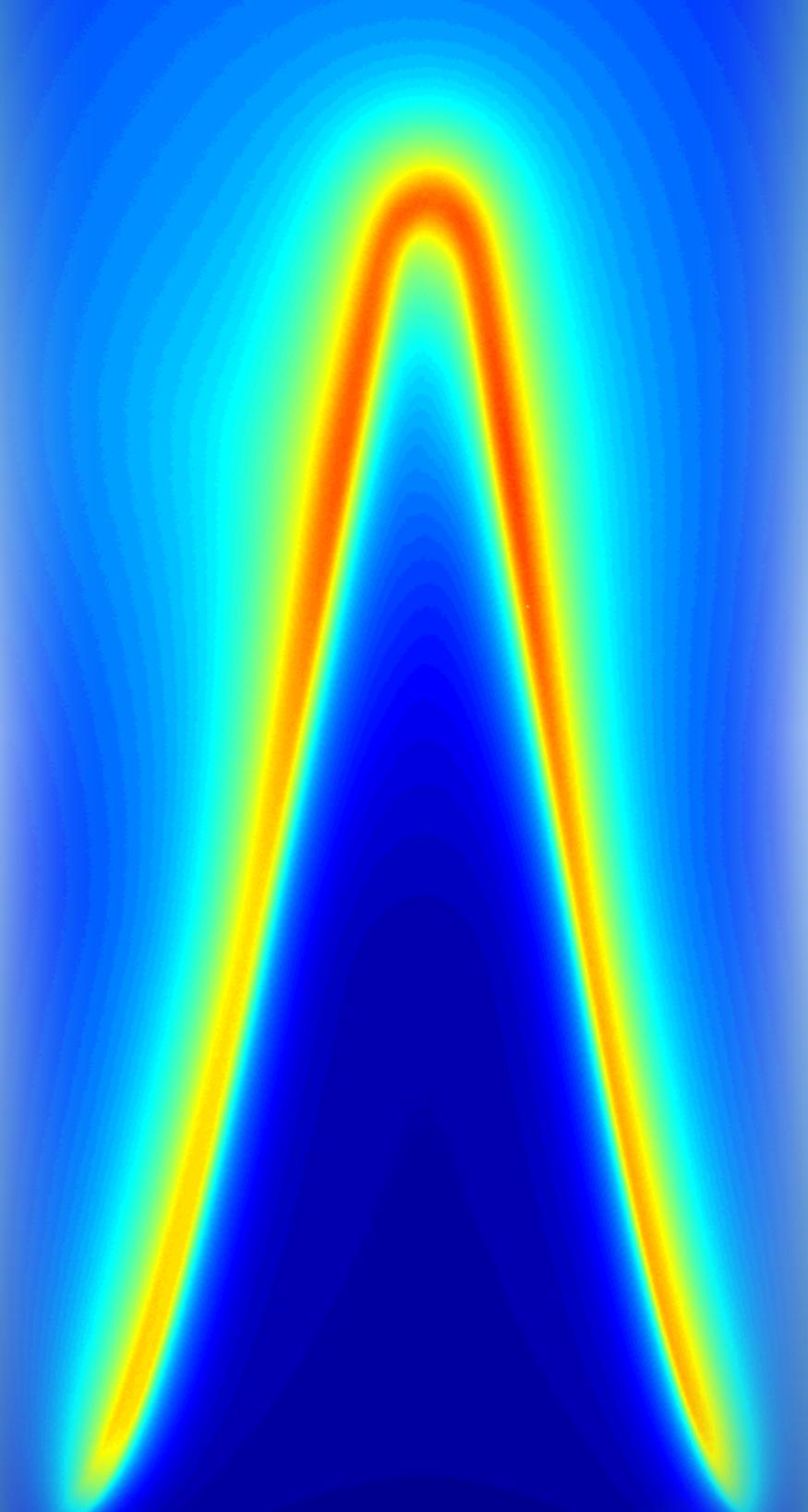
No Ts dependency No Ts dependency Very sensitive to Ts

7. Burner stability

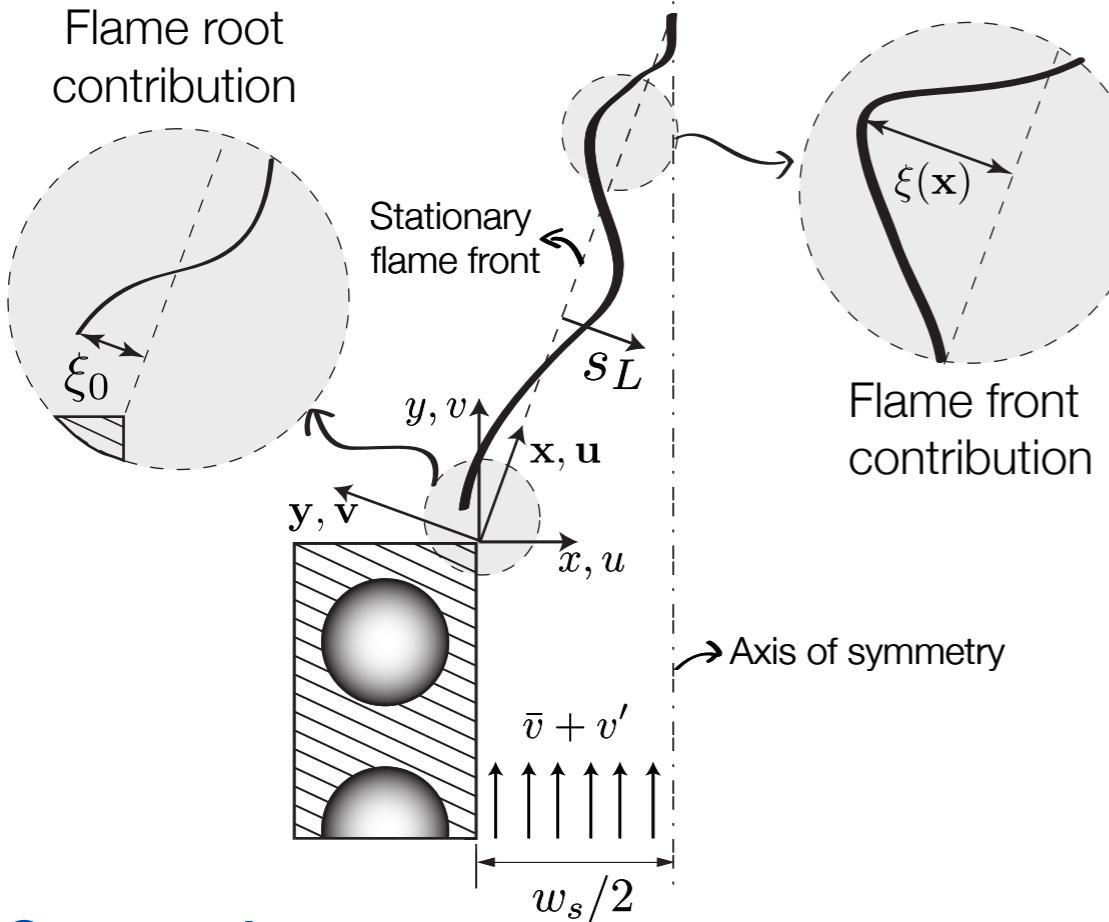
Part III: Flame Dynamics

8. Flame front dynamics

9. Flame root dynamics



Brief review of flame dynamics theory:

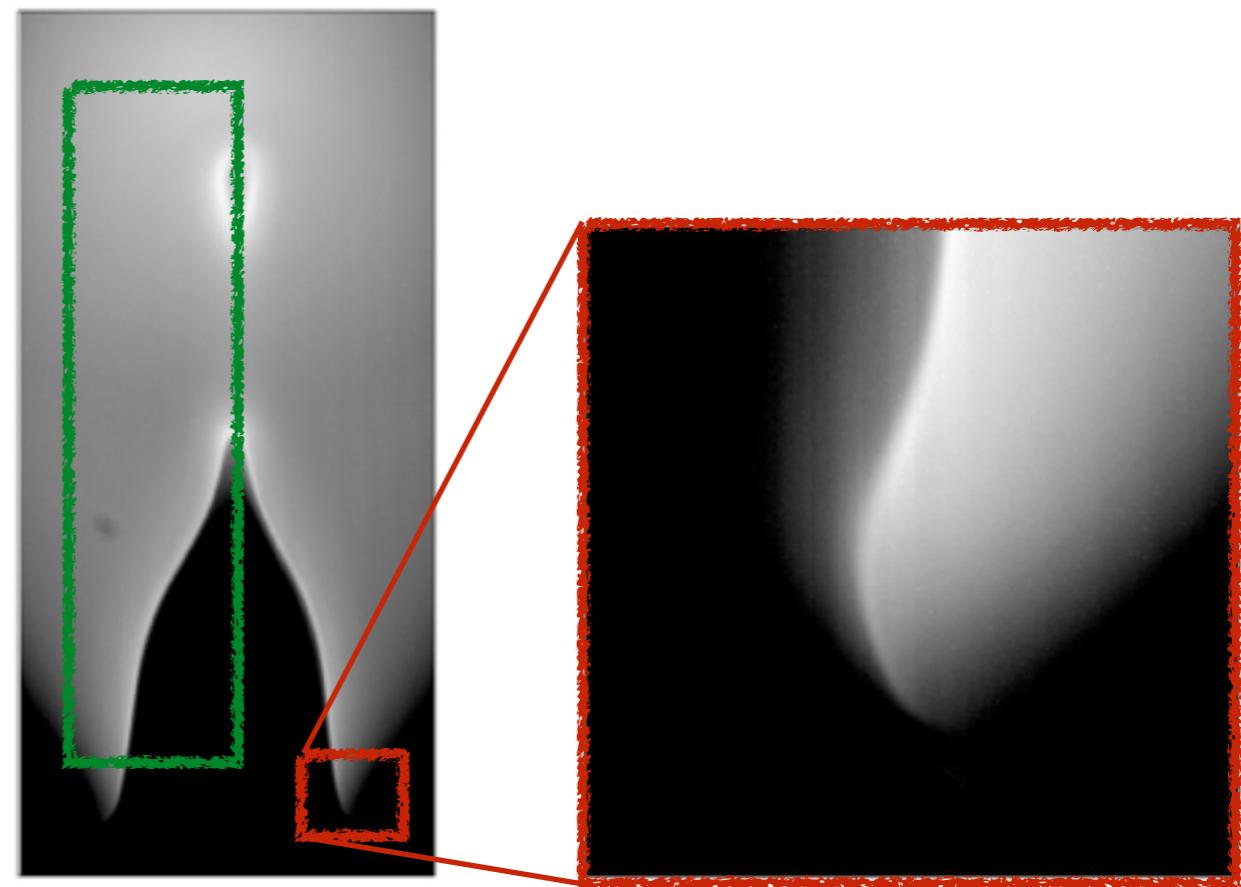


G-equation:

$$\frac{\partial G}{\partial t} + \vec{v} \cdot \nabla G = s_L |\nabla G|$$

In the reference frame attached to the steady flame front:

$$\frac{\partial \xi}{\partial t} + \bar{\mathbf{u}} \cdot \nabla \xi = \mathbf{v}'(\mathbf{x}, t)$$



Solution:

$$\tilde{\xi}(\mathbf{x}) = \frac{e^{i\kappa\mathbf{x}}}{\bar{\mathbf{u}}} \int_0^{\mathbf{x}} \tilde{\mathbf{v}}(\mathbf{x}') e^{-i\kappa\mathbf{x}'} d\mathbf{x}' + \tilde{\xi}_0 e^{i\kappa\mathbf{x}}$$

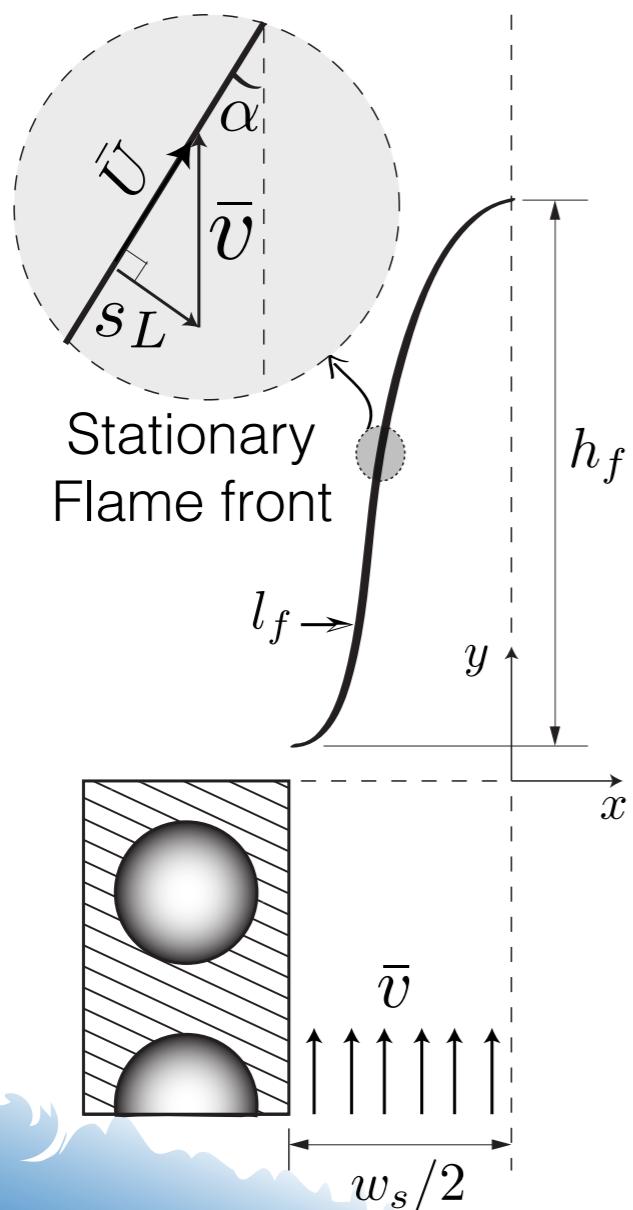
Two contributions to the FTF

$$\mathcal{F} = \boxed{\mathcal{F}_A} + \boxed{\mathcal{F}_B}$$

- [1] Boyer and Quinard 1990 *cf.*
- [2] Fleifil *et al.* 1996 *cf.*
- [3] Lee and Lieuwen 2003 *jpp.*

8. Flame Front Dynamics

1. Does the theory predict a change in the flame front response when wall temperature T_s changes?



Flame front dynamics is controlled to the first order by two parameters:

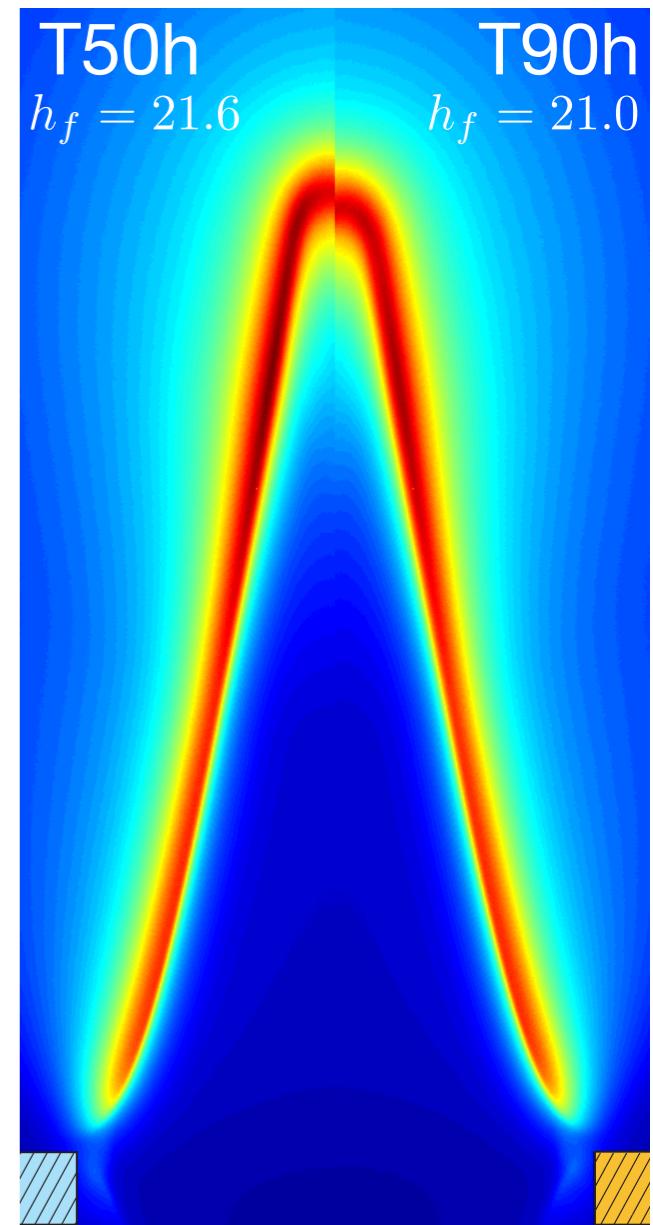
$$\mathcal{F}_A = f(\omega_*, k_*)$$

$$\omega_* = \frac{\omega}{\bar{v} \cos(\alpha)} l_f$$

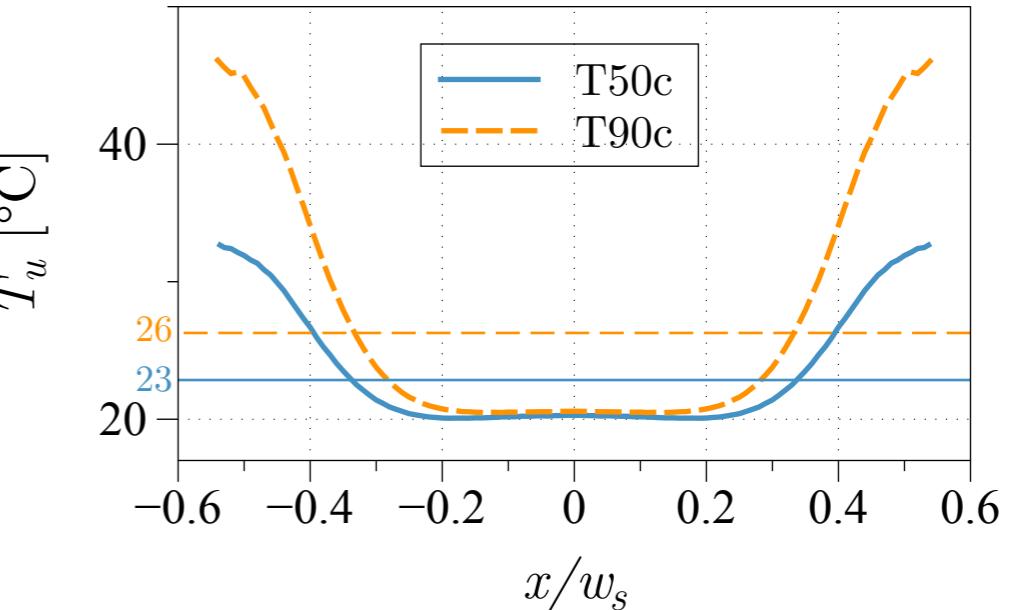
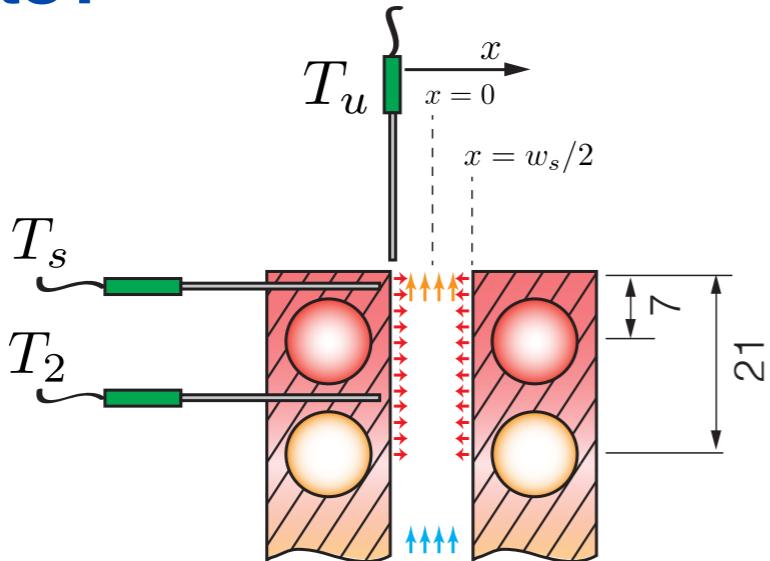
$$k_* = \frac{\omega}{\bar{v}} h_f$$

2. Is the flame geometry affected by the wall temperature T_s ?

- [1] Baillot *et al.* 1992 *cf.*
- [2] Fleifil *et al.* 1996 *cf.*
- [3] Ducruix *et al.* 2000 *pci.*
- [4] Schuller *et al.* 2003 *cf.*
- [5] Birbaud *et al.* 2006 *cf.*
- [6] Cuquel *et al.* 2011 *mcs.*



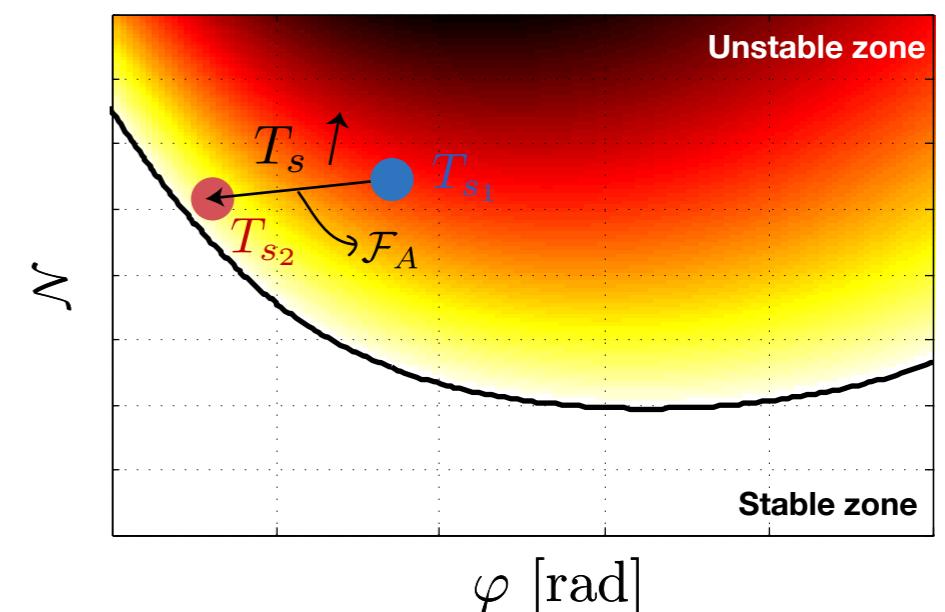
3. Does wall temperature modify the temperature profile of the reactants?



$$s_L = f(T_u)$$

4. Does the increase in s_L explain the changes in the FTF ?

T50h-T90h		s_L Impact on the FTF	
ΔT_u [°]	Δs_L [cm s ⁻¹]	\mathcal{G}_r	φ_r
3	1	3.4 %	2.2 %
		11.5 %	3.6 %
Actual FTF difference T50h-T90h			



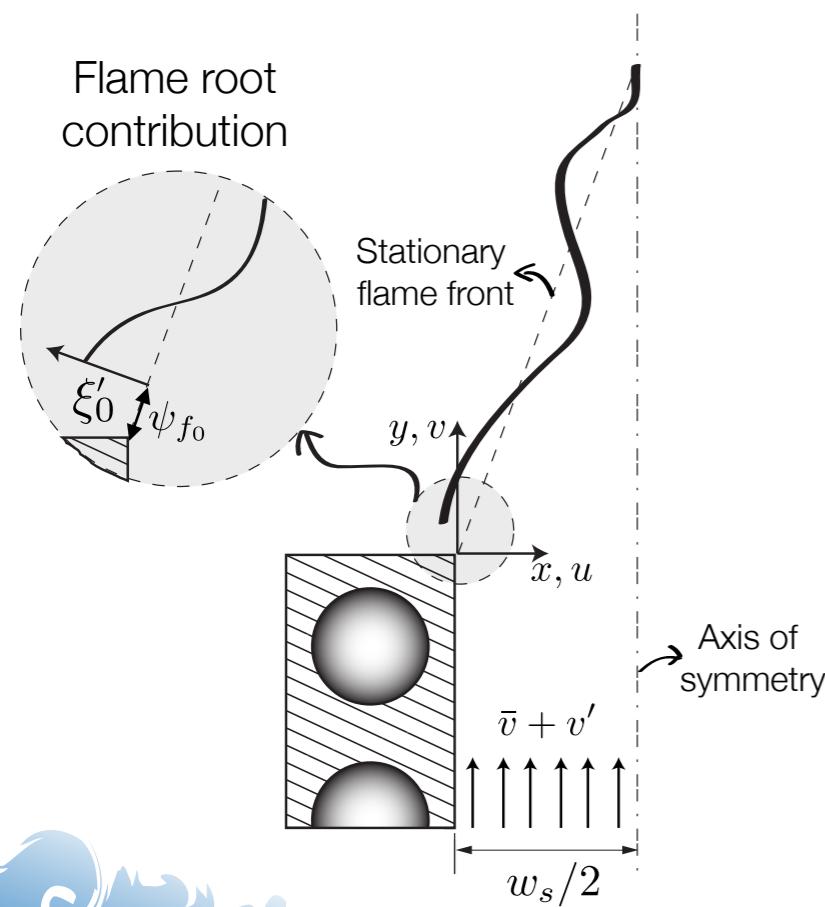
9. Flame Root Dynamics

1. Does the theory predicts a change in the flame root response when T_s changes?

Flame root dynamics is controlled to the first order by the heat transfer between the burner and the flame anchoring point.

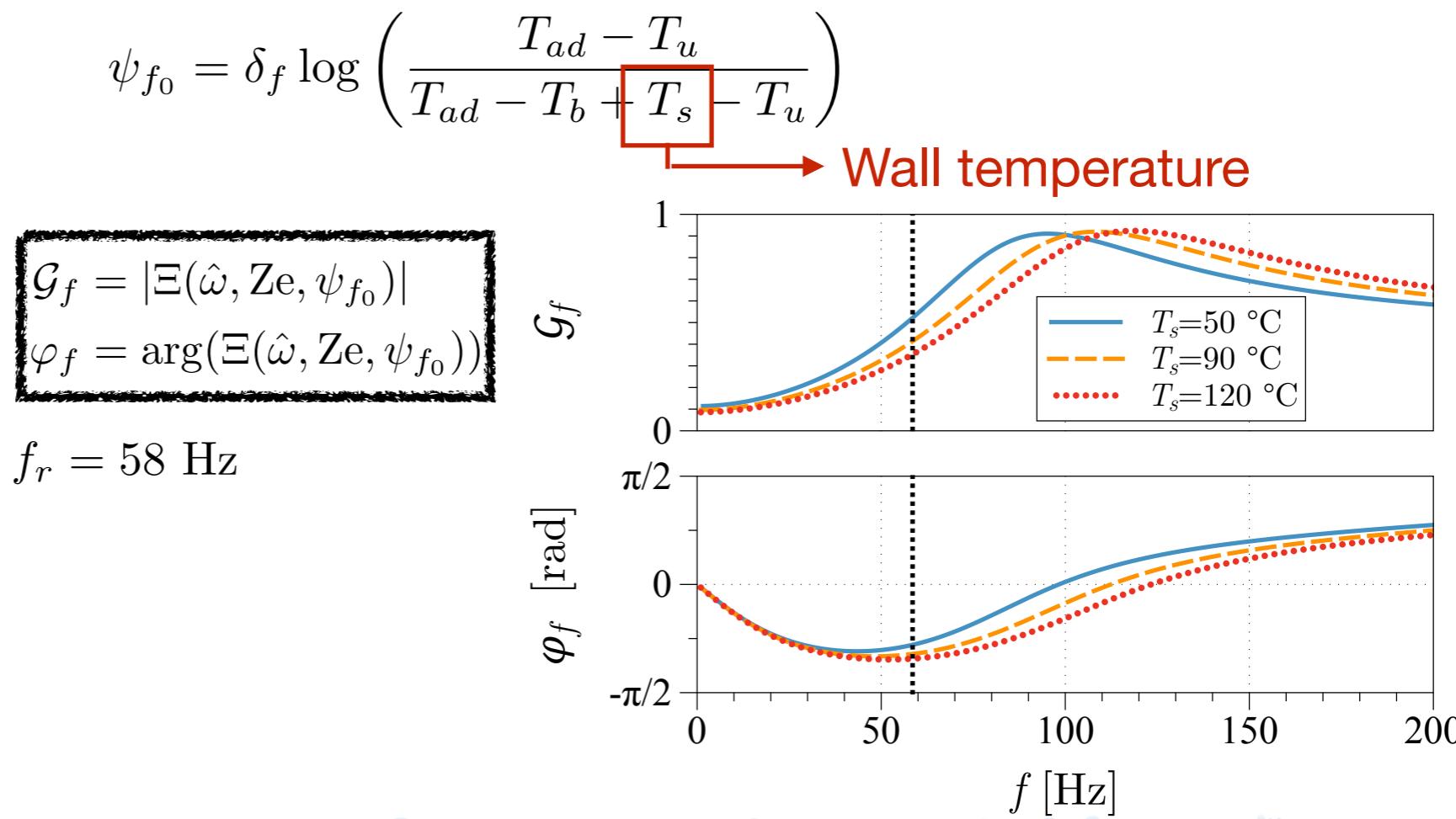
Flame root contribution

$$\mathcal{F}_B \propto \Xi$$



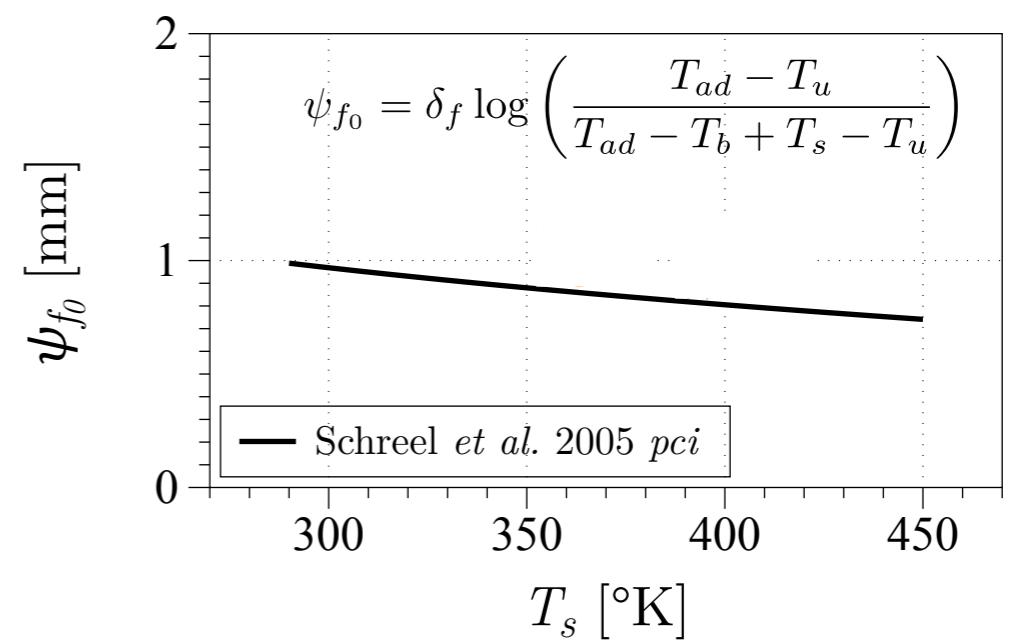
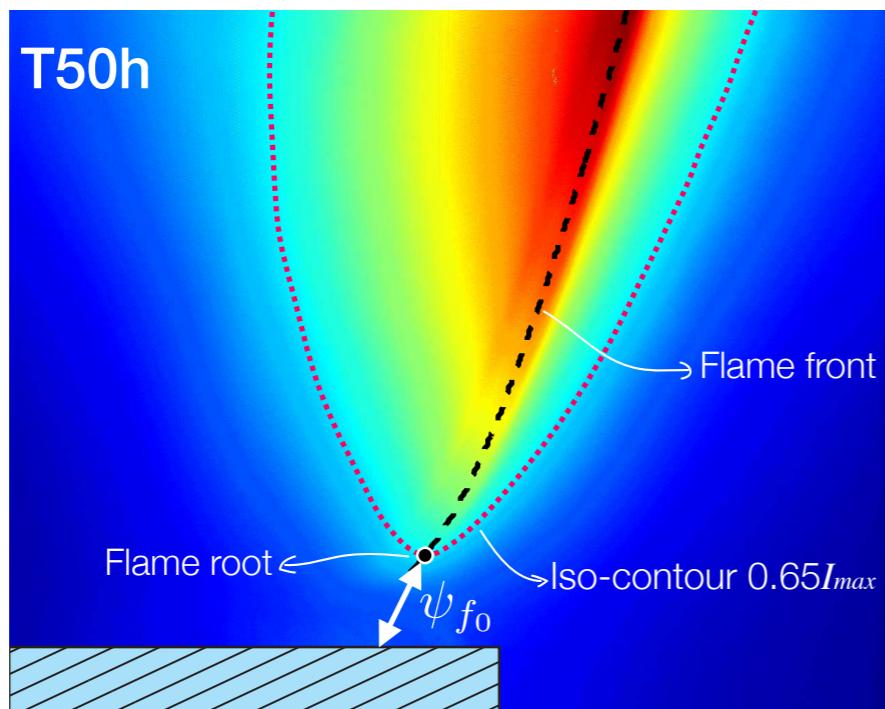
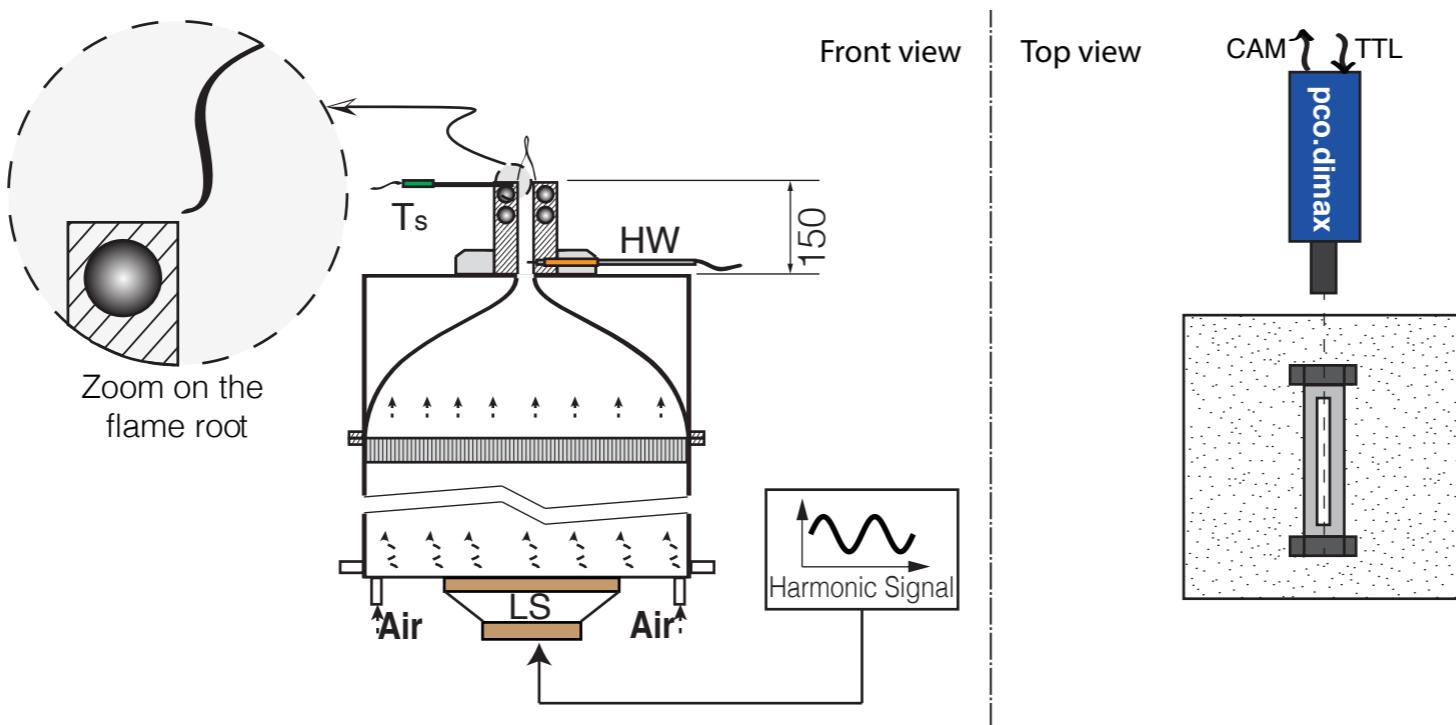
Flame root transfer function

$$\Xi = \frac{\xi'_0 / (w_s/2)}{v'/\bar{v}}$$

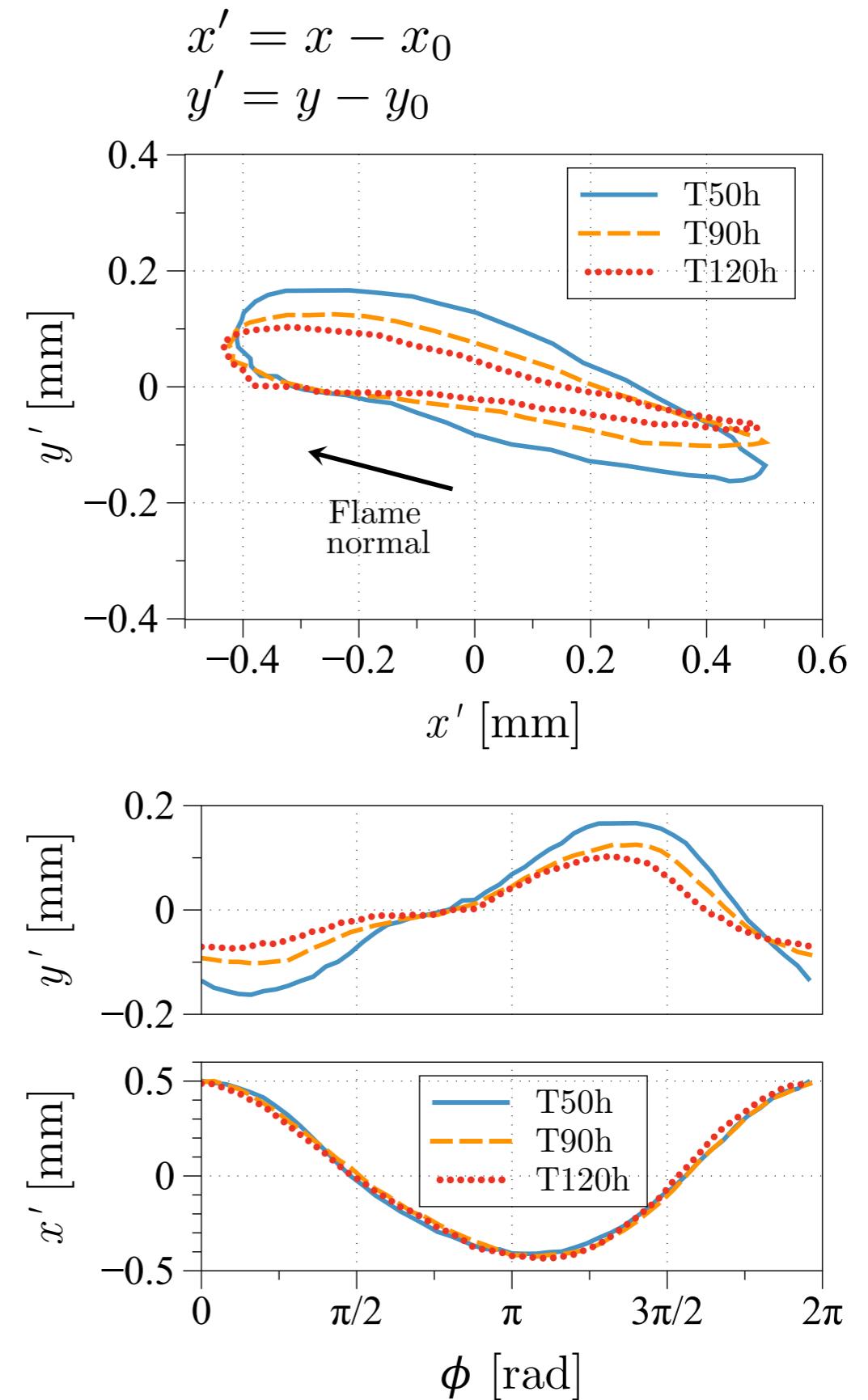
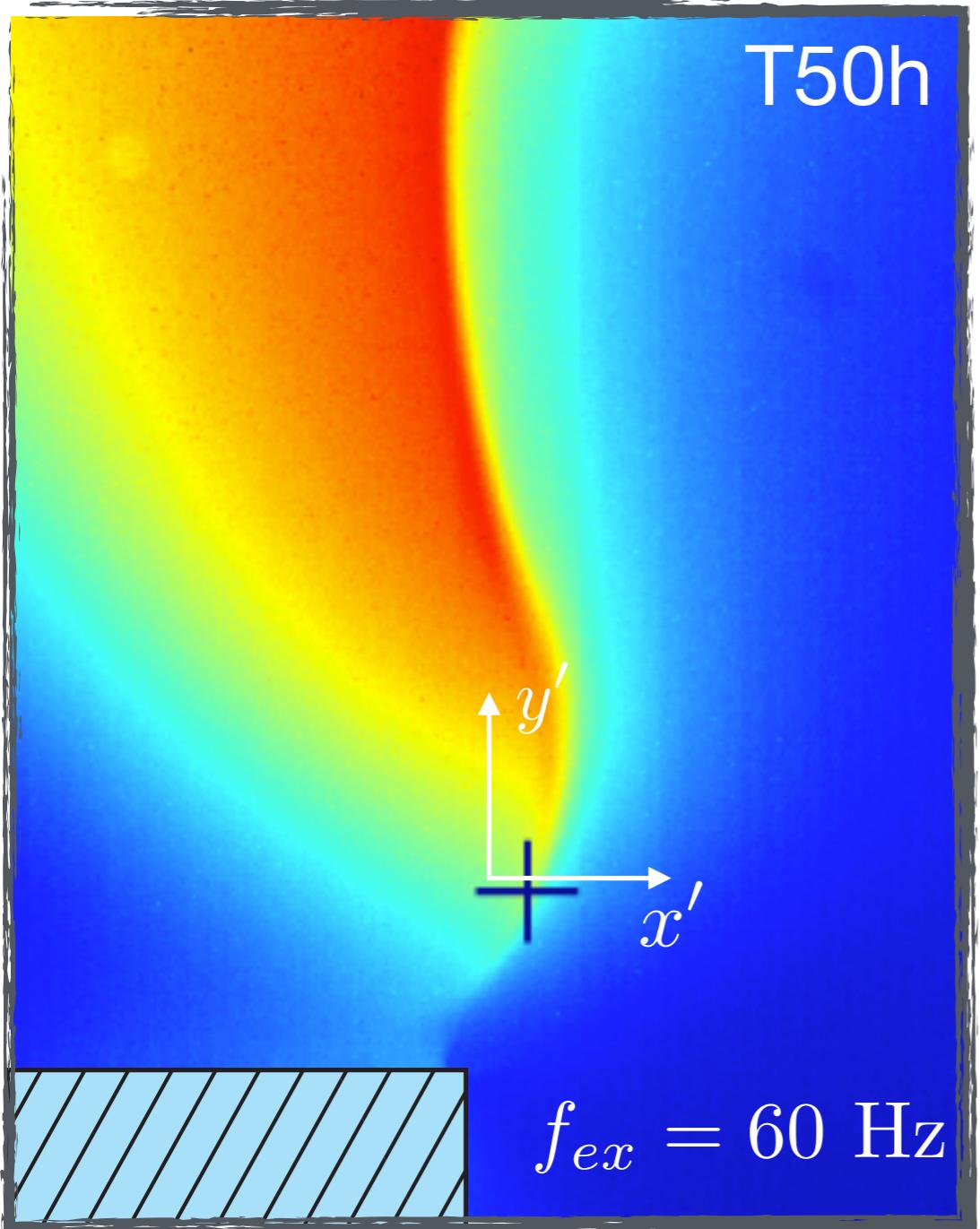


- [1] Kornilov et al. 2007 *pci*.
- [3] Cuquel et al. 2013 *crm*.
- [4] Rook et al. 2002 *ctm*.
- [5] Schreel et al. 2005 *pci*.
- [6] Altay et al. 2009 *pci*.

2. Does the experiment predict a change in the flame root response when T_s changes?



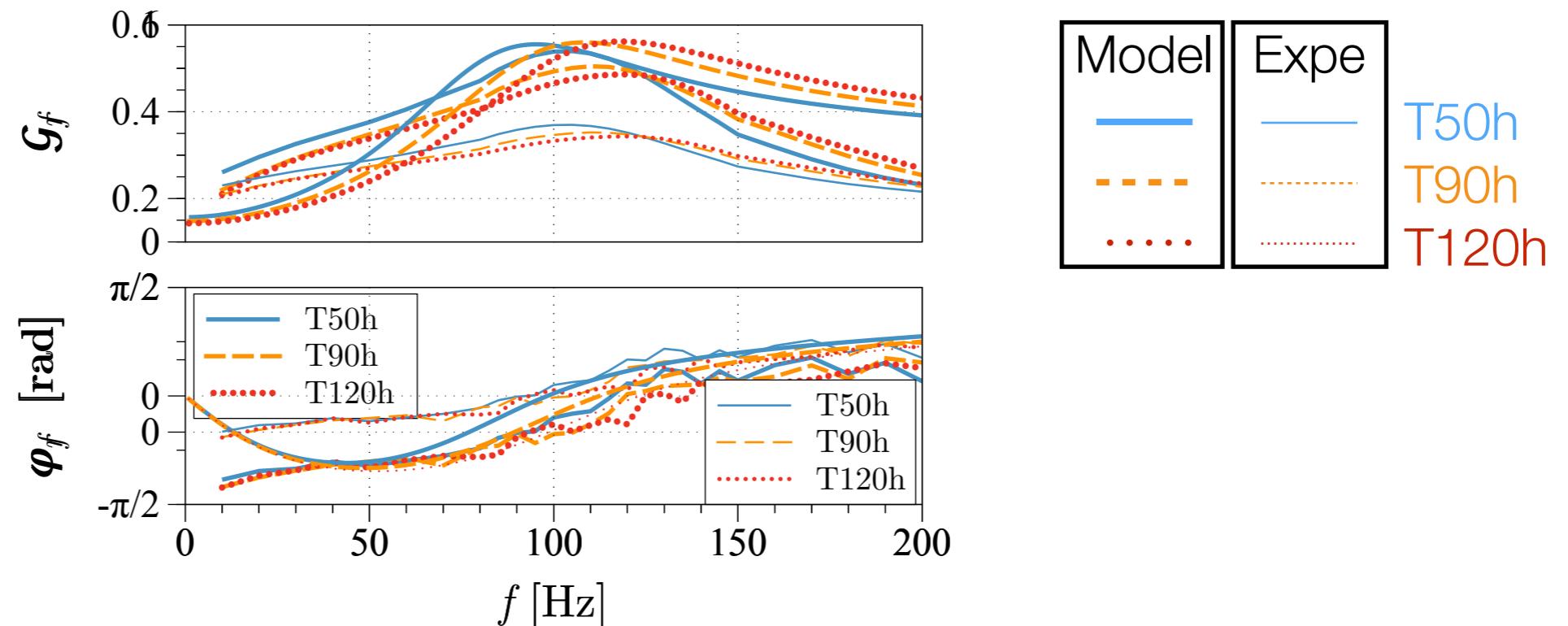
Flame root trajectoires



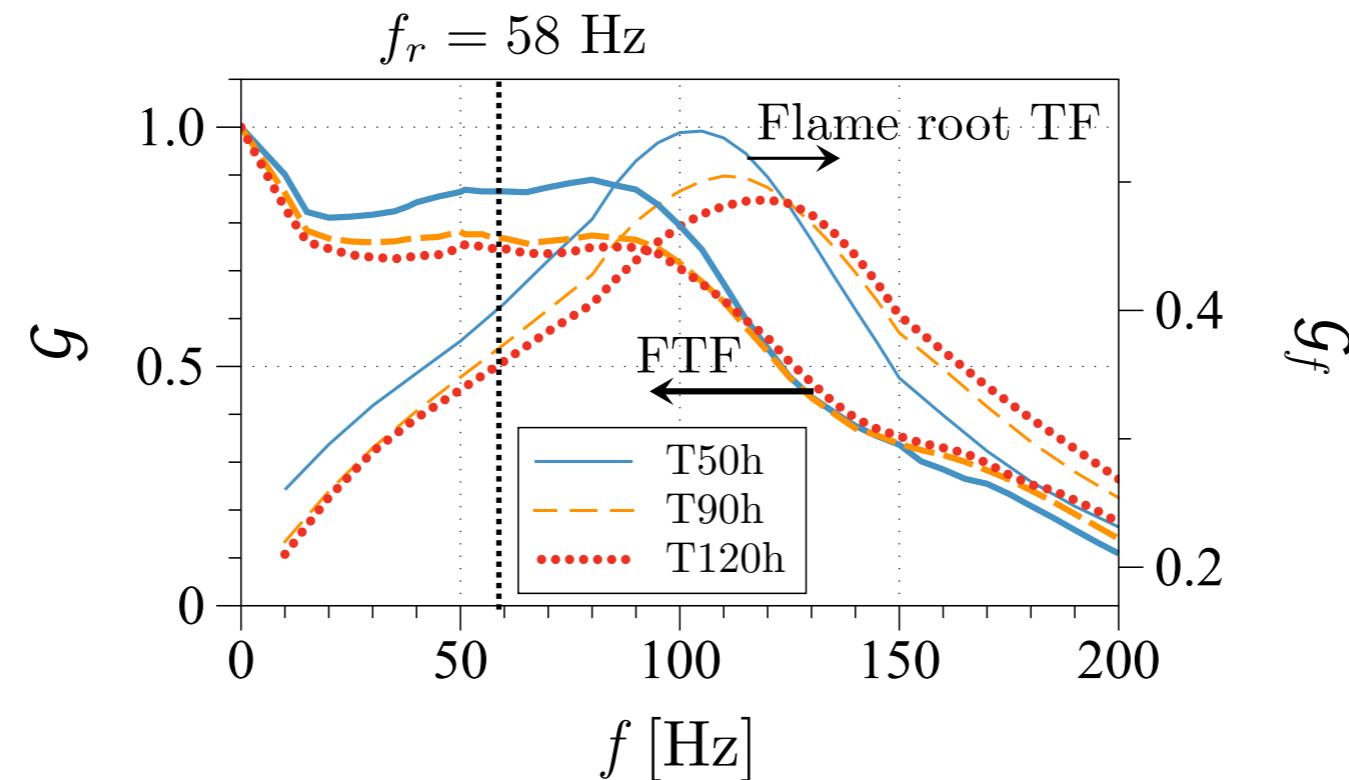
Experimental flame root transfer function

$$\mathcal{G}_r = |\Xi(\omega, T_s)|$$

$$\varphi_r = \arg(\Xi(\omega, T_s))$$

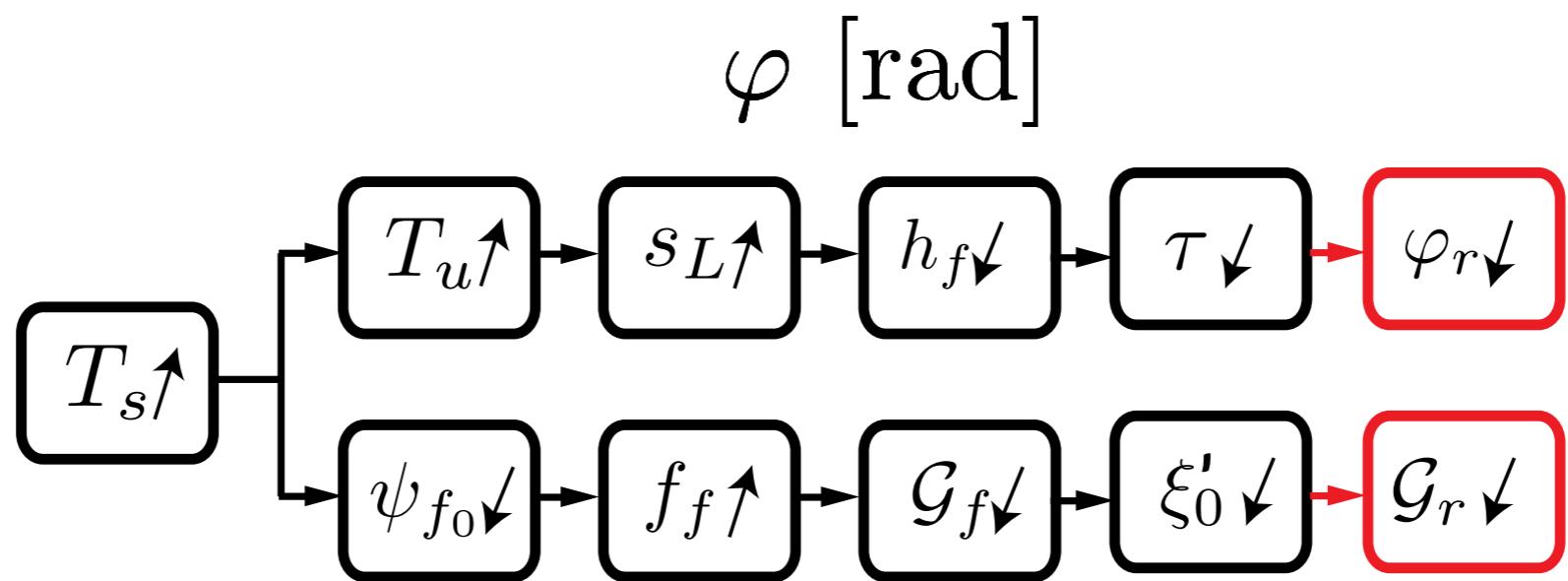
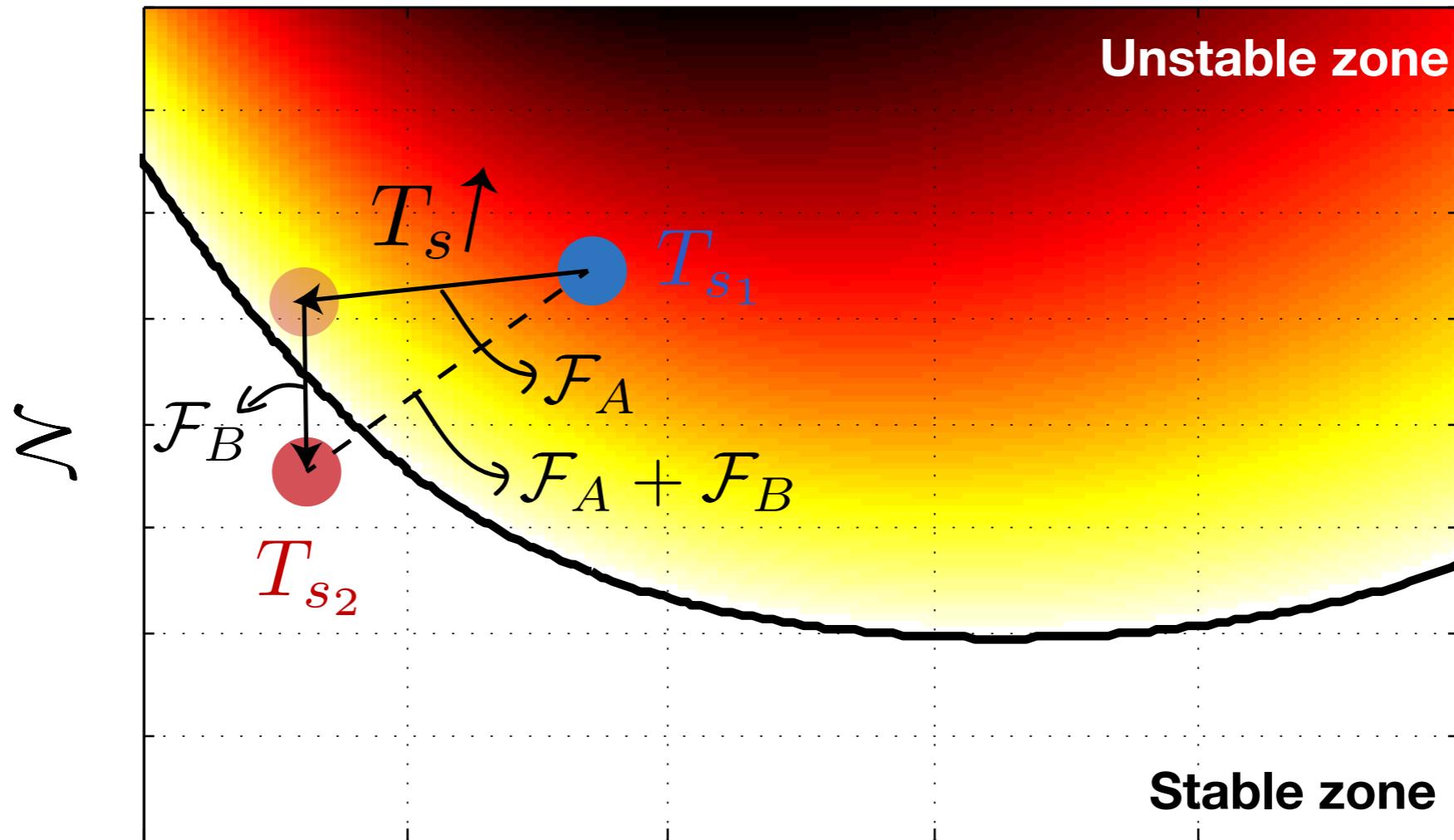


Comparison with the FTF:



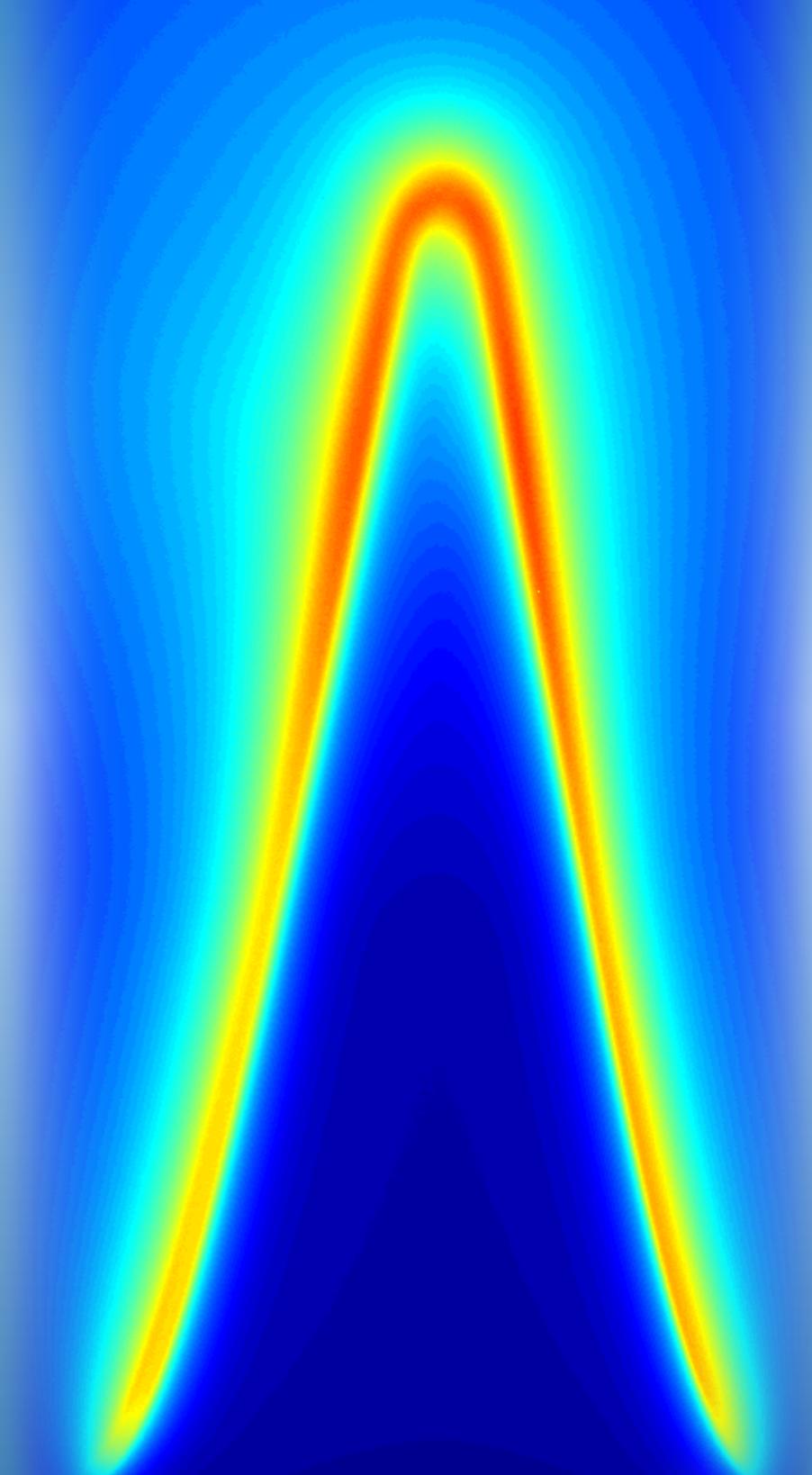
Difference	\mathcal{G}_r
T50h-T120h	11 %
Flame root FTF	11 %
Actual FTF	14 %

So, how is the flame stabilized?



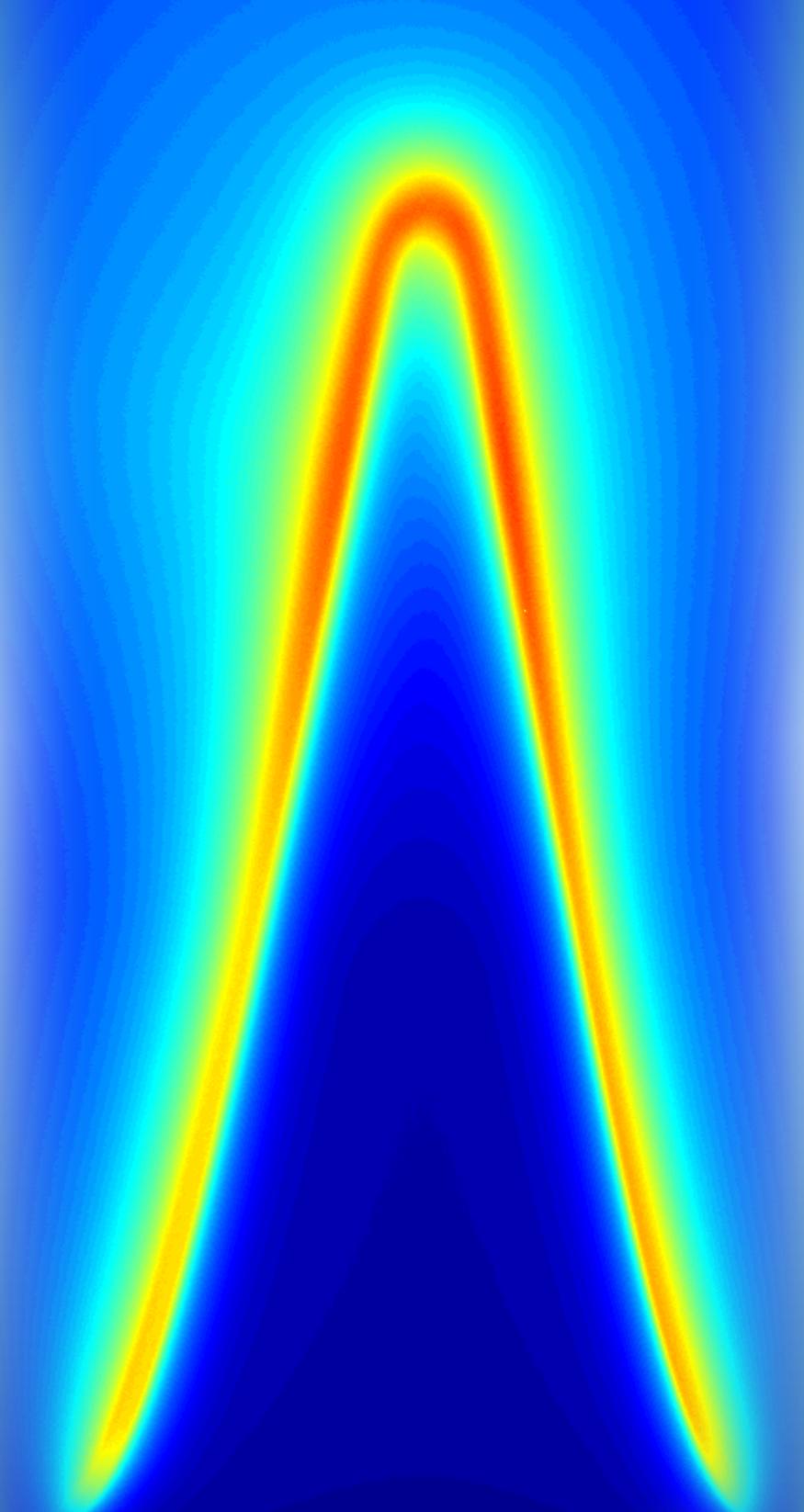
Objectives

1. Derive a stability model able to predict the experimental observations.
2. Determine which mechanism(s) is/are responsible for stabilizing the flame.
3. Understand how this mechanism(s) work(s).



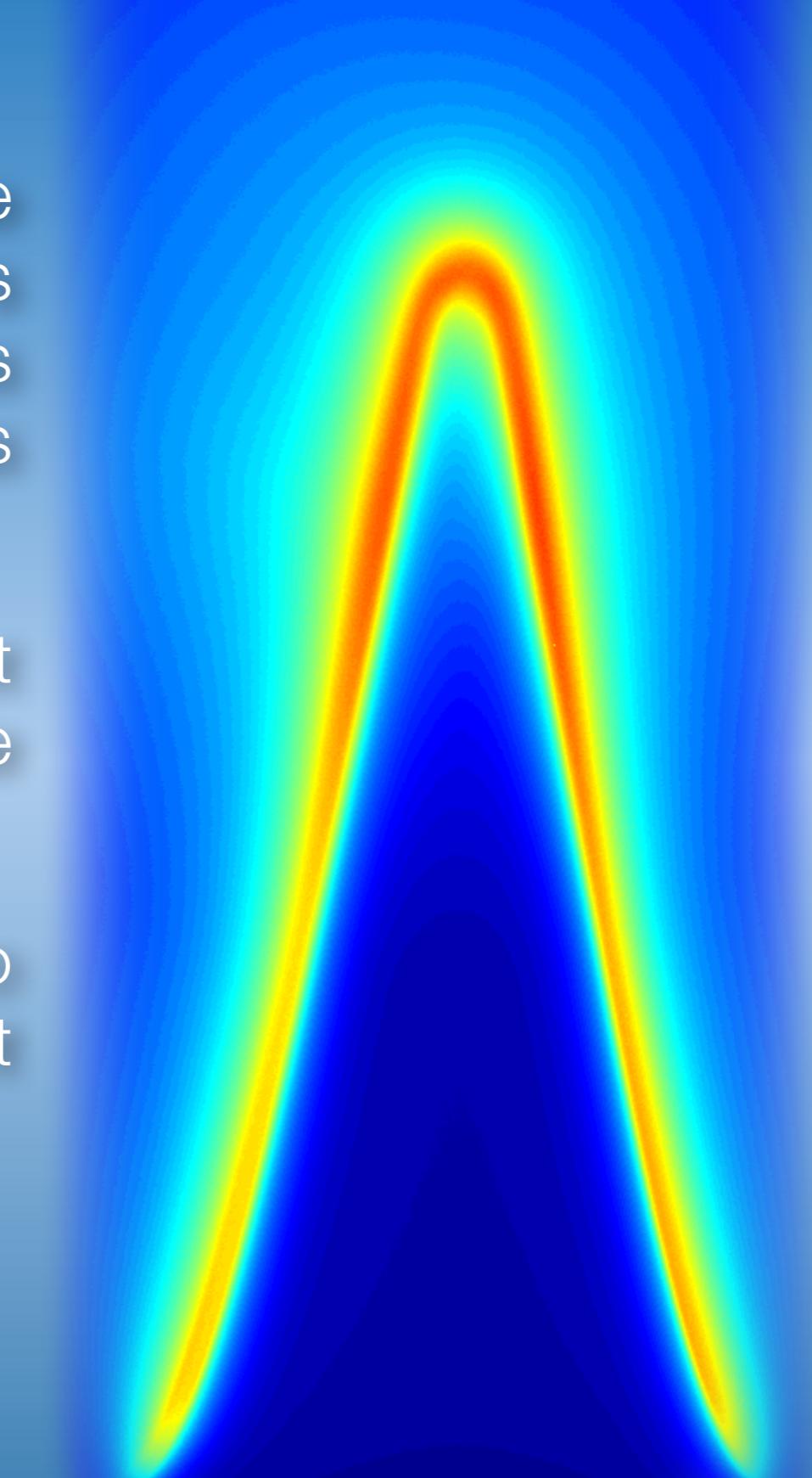
Conclusions

1. We show an experiment where the wall temperature T_s can be controlled.
2. We have shown an experiment where the stability of the flame can be controlled by changing only the wall temperature T_s .
3. A stability model was proposed and we show that the wall temperature modifies the stability limits of the system by small modifications on the flame response to acoustic oscillations.
4. We use existing results to propose a model and we show that the flame root dynamics must be taken into account in order to predict the stability limit of the system.



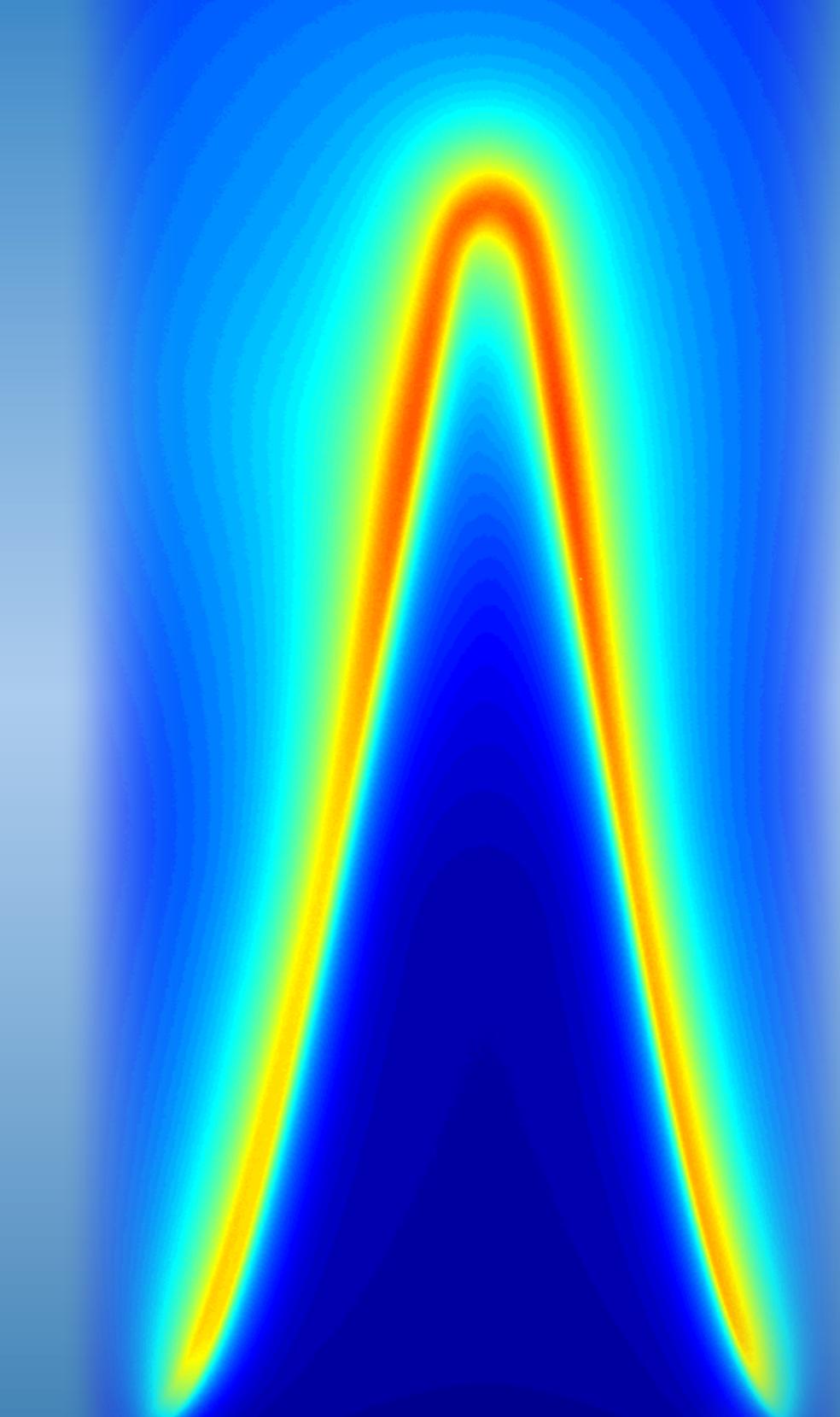
Perspectives

1. Perform DNS simulations and evaluate the ability of CFD solvers to account for parameters such as the slot temperature in the predictions of the combustion instabilities (Work in progress at the IMFT).
2. Improve the analytical model of the flame root response and expand to the scenario of the non-linear response of the flame.
3. It will be interesting to expand this study to more realistic configurations such as turbulent flames and more complicated geometries.

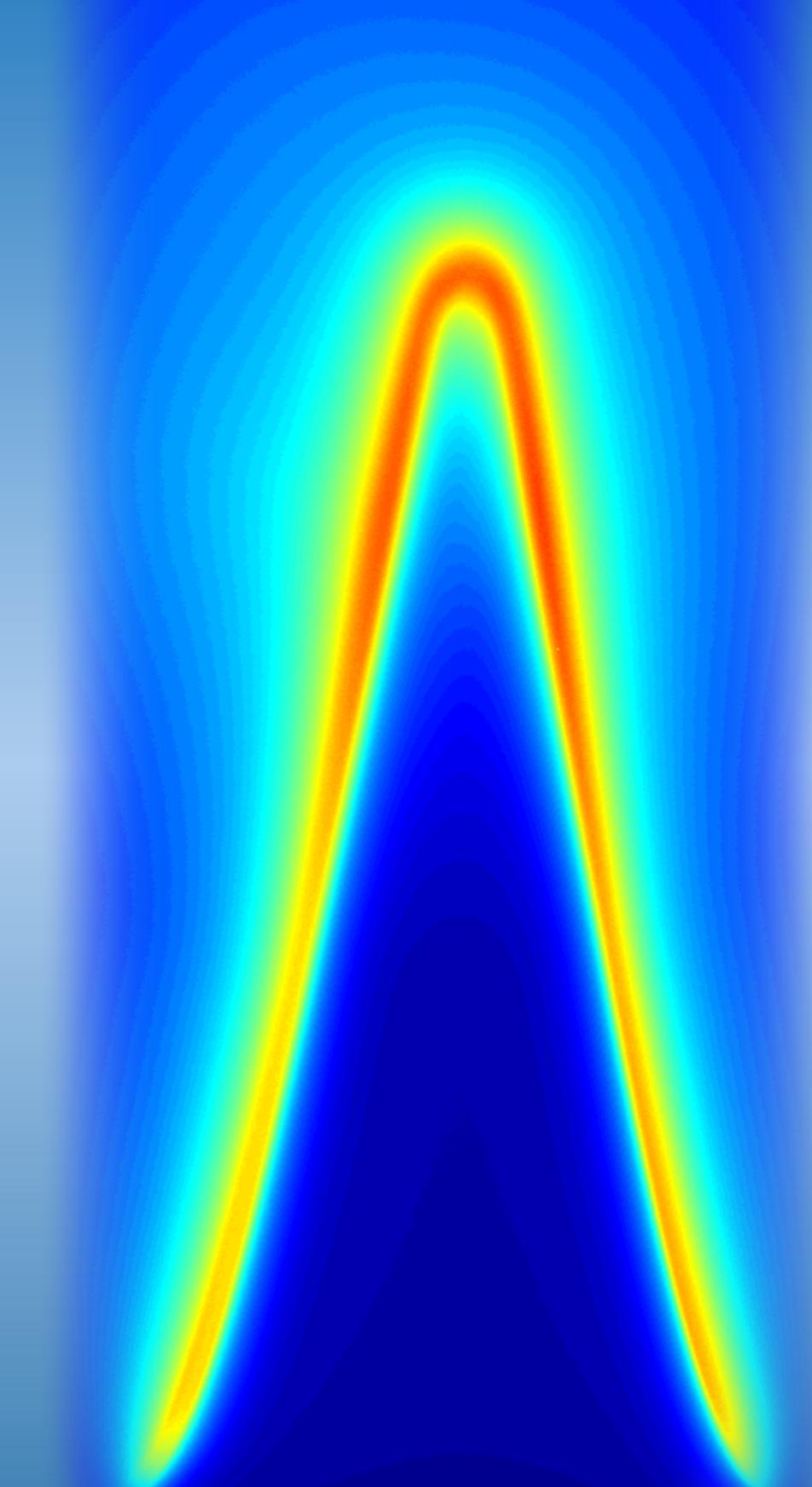


Thanks for your attention !

Premixed laminar flame
 $\Phi = 0.95$
 $U_b = 1.7 \text{ m/s}$

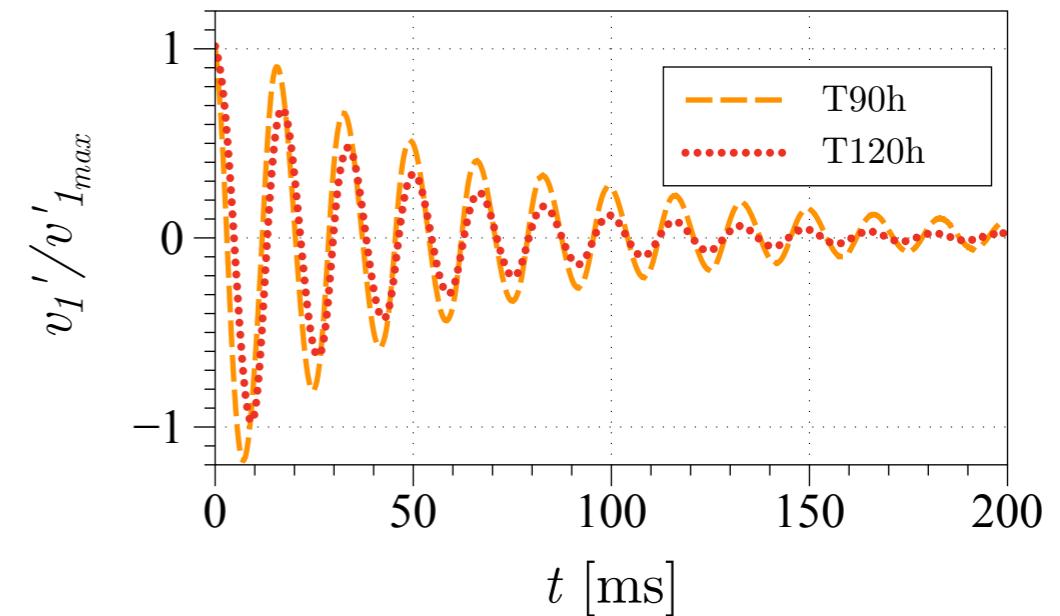
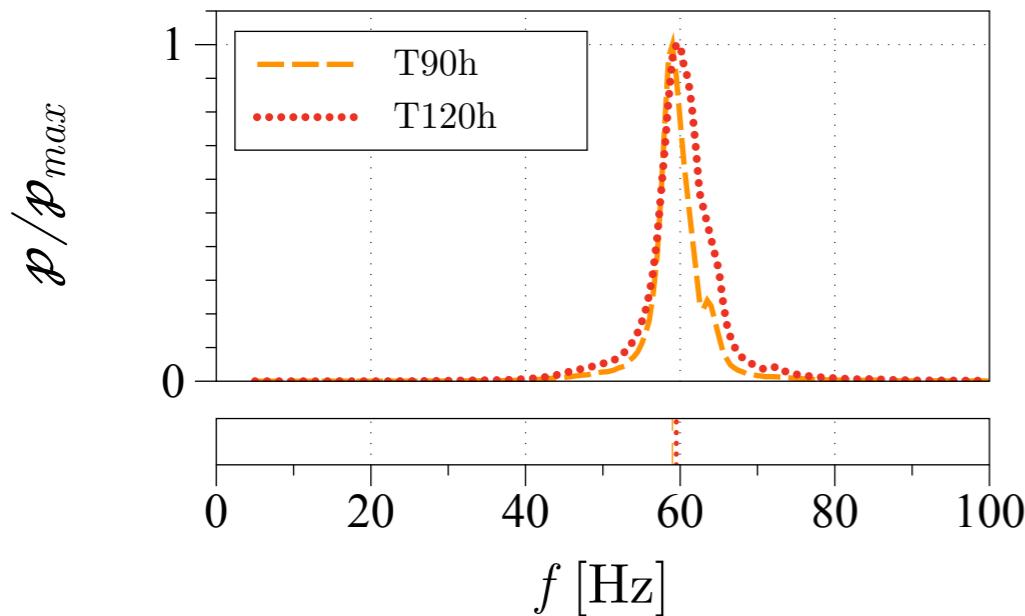


Backup

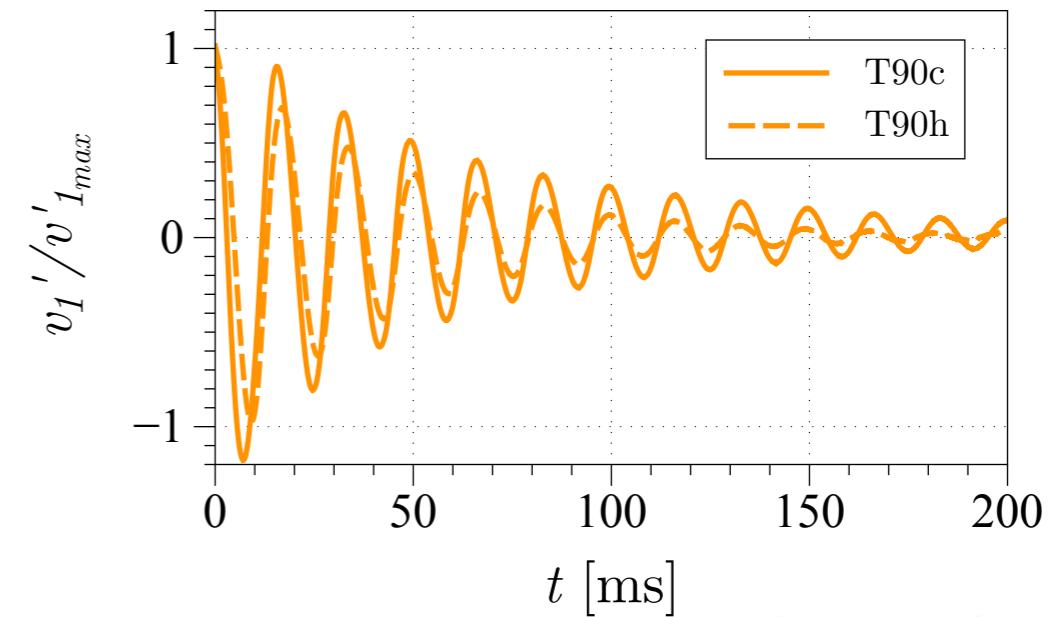
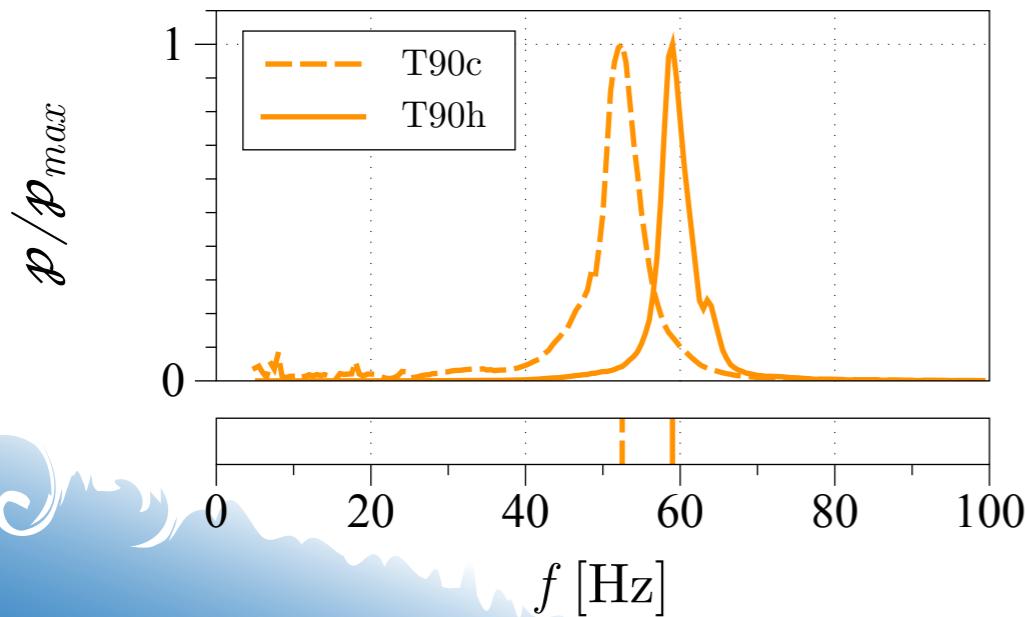


Reacting acoustics

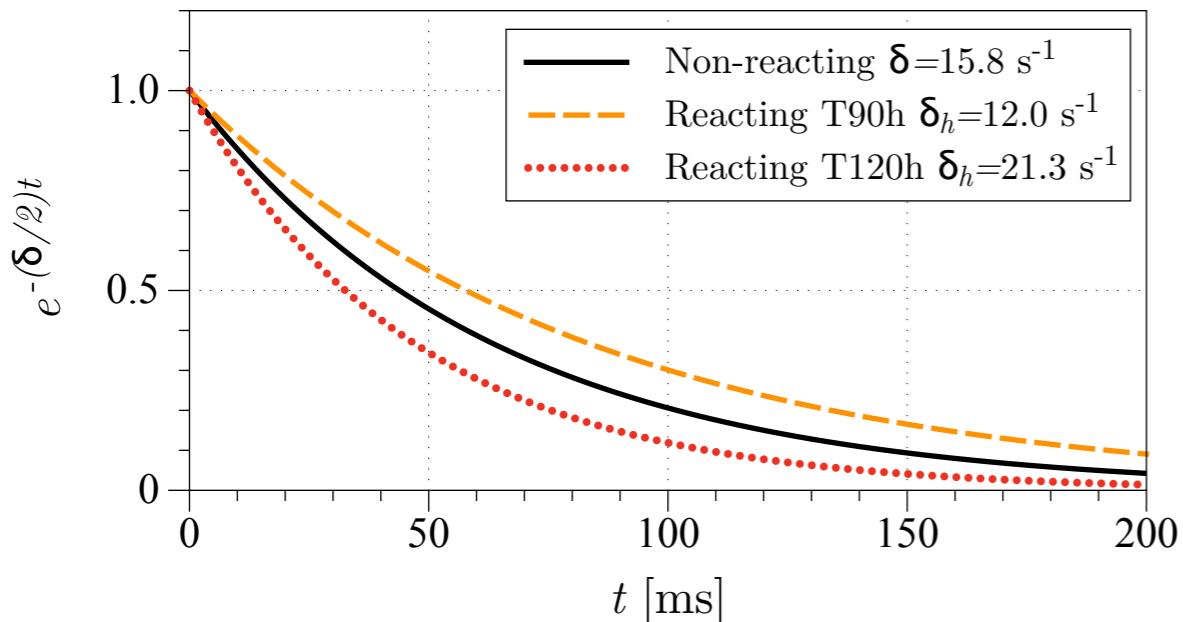
1. Comparison between two reacting cases



2. Comparison between two equivalent reacting and non-reacting cases



3. Flame effect on the system stability

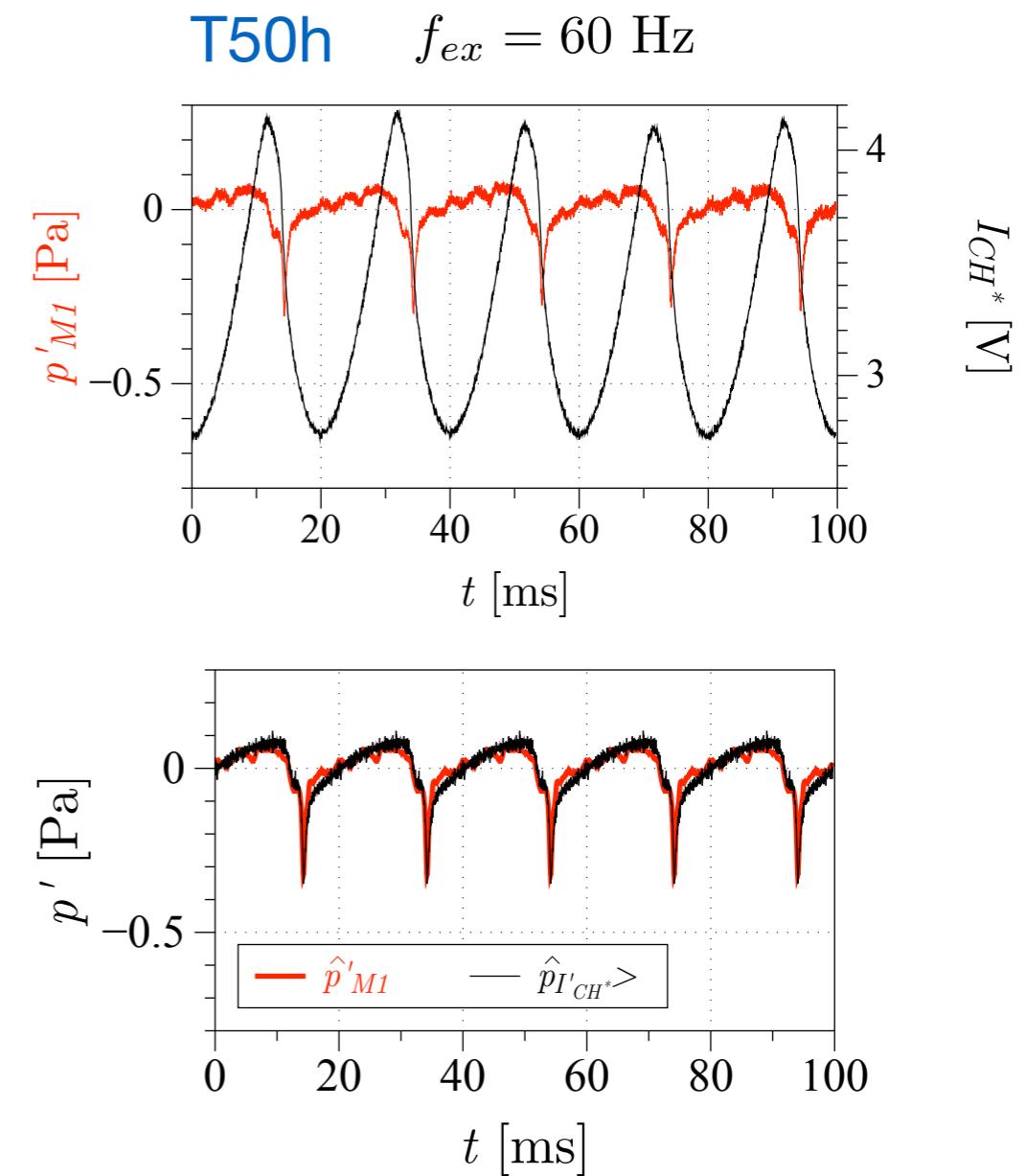
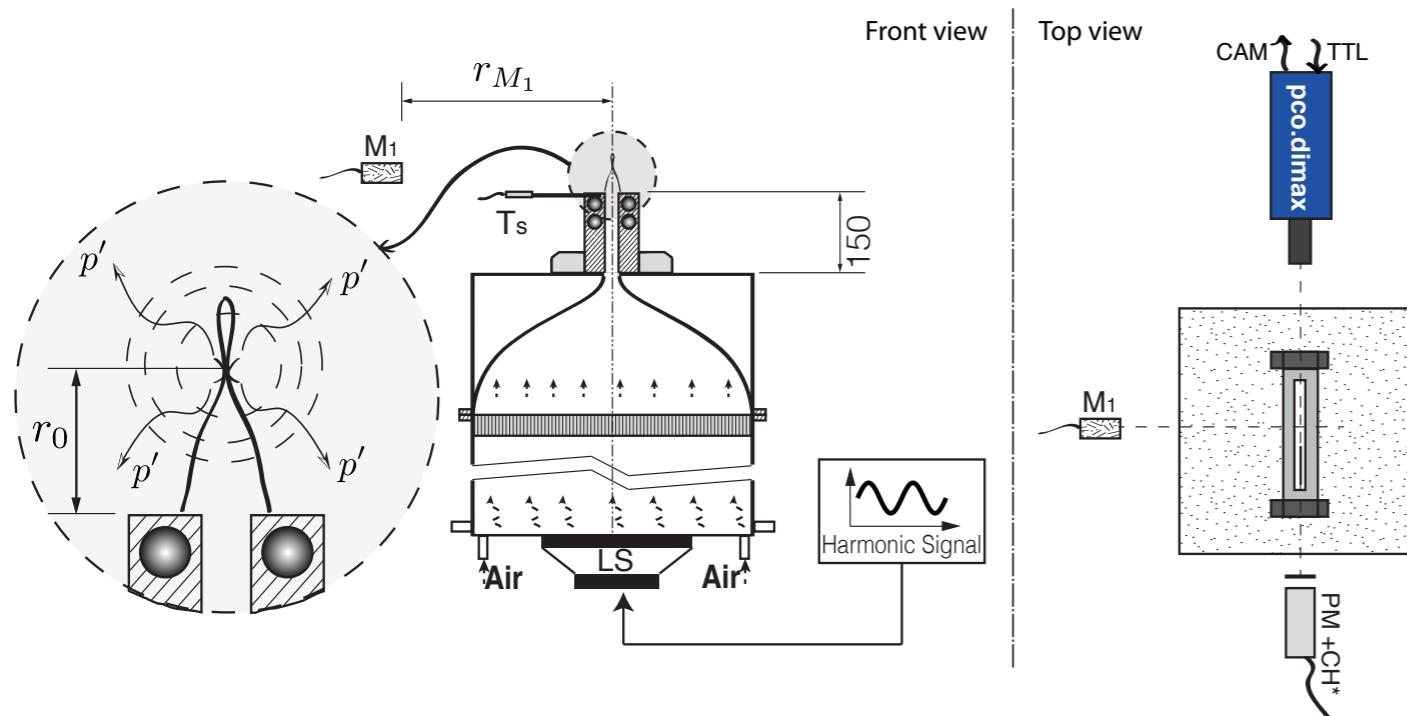


	$\delta \text{ [s}^{-1}\text{]}$
T50c	15.8
T90h	12.0
T120h	21.3

Combustion noise

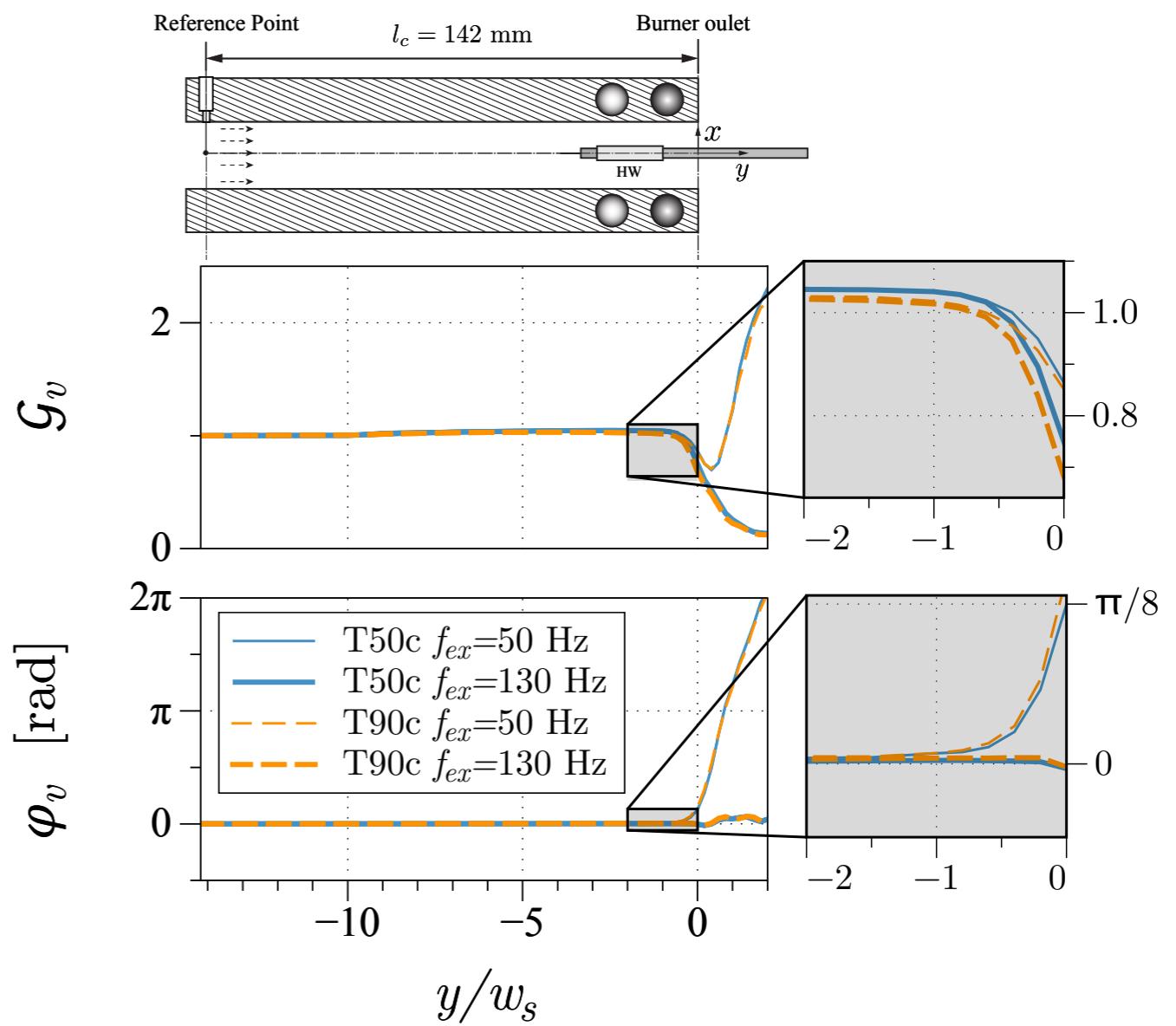
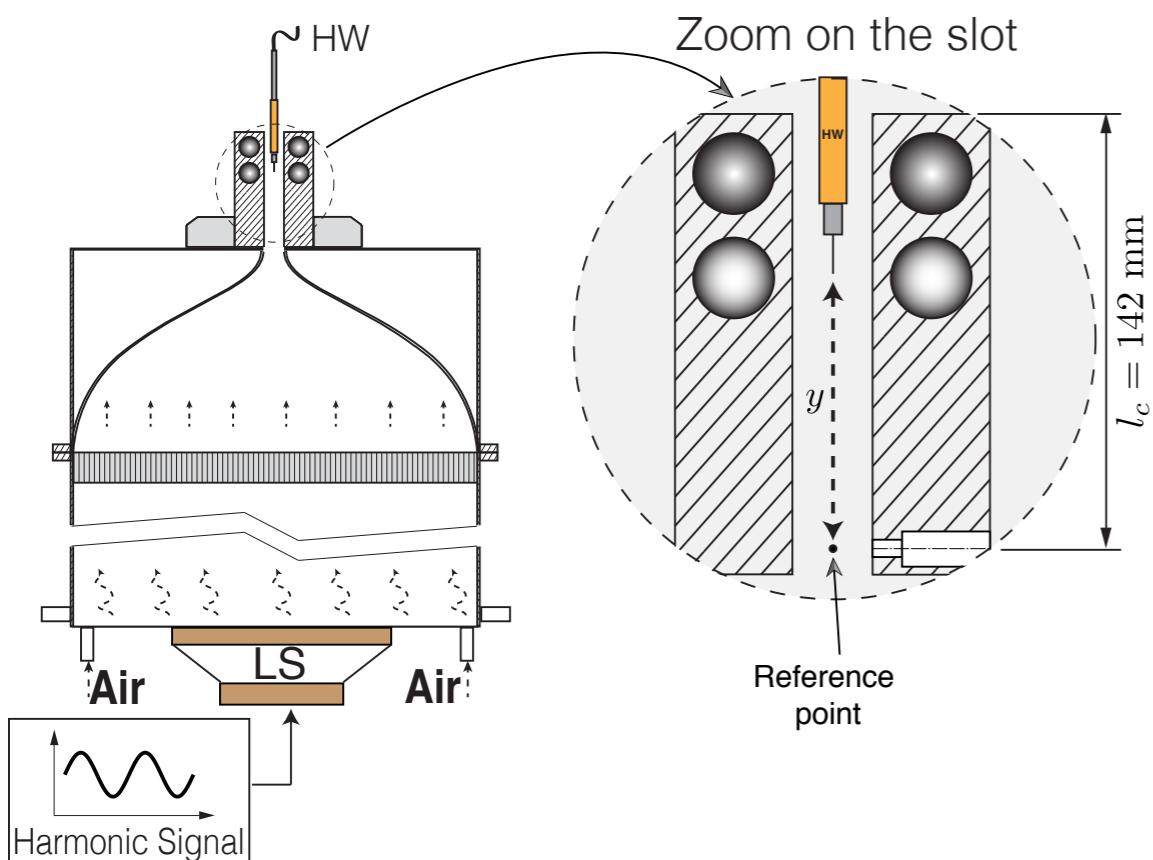
1. Is classical combustion noise theory suitable for a slot burner?

$$p'_{M1}(r_{M1}, t) = \frac{\rho_u(E - 1)}{4\pi r_{M1}} \kappa \left[\frac{d I_{CH^*}}{dt} \right]_{t-\tau_{M1}}$$

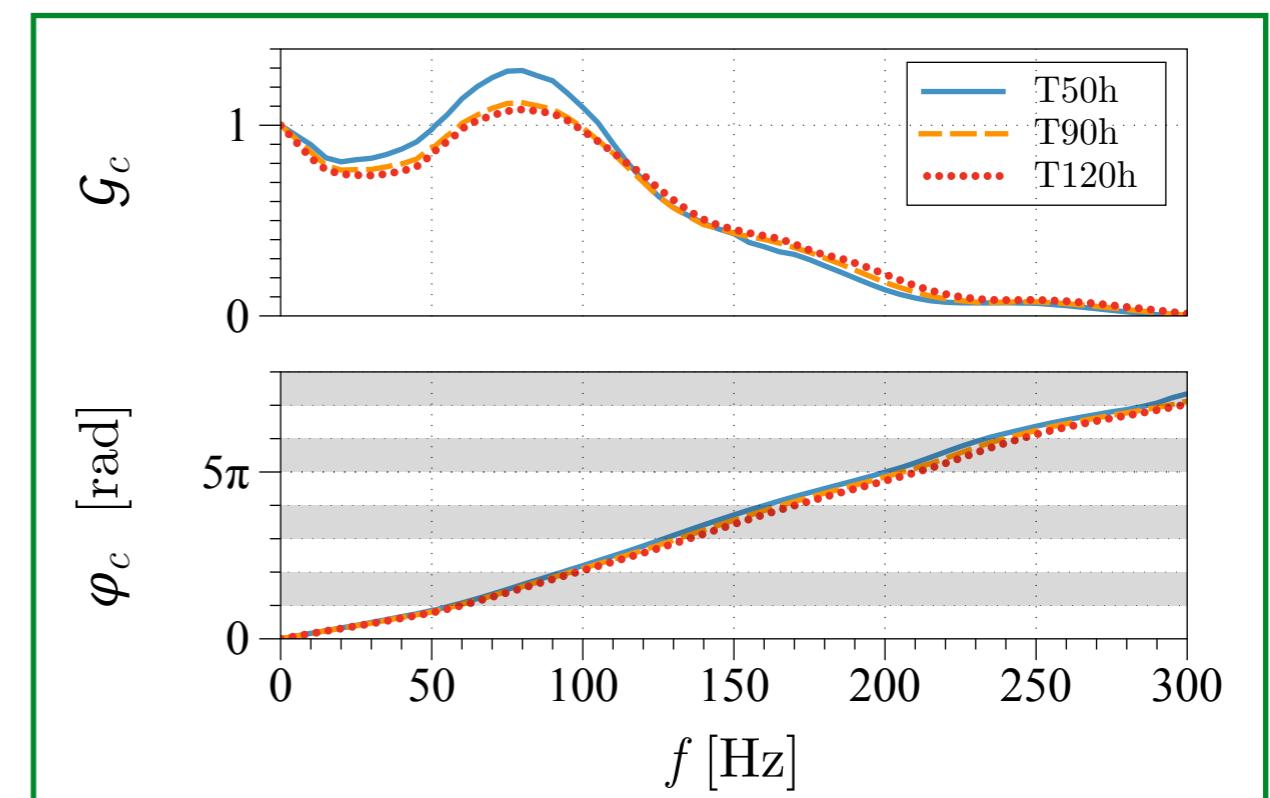
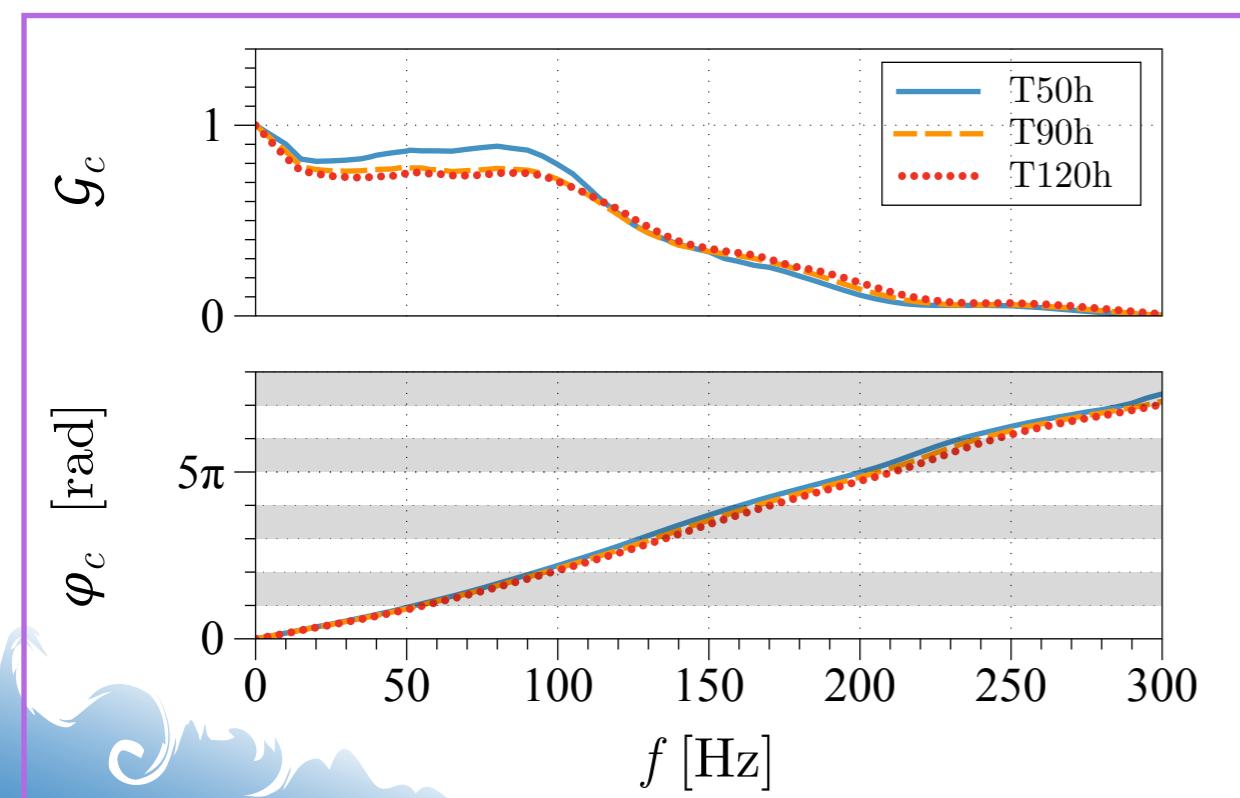
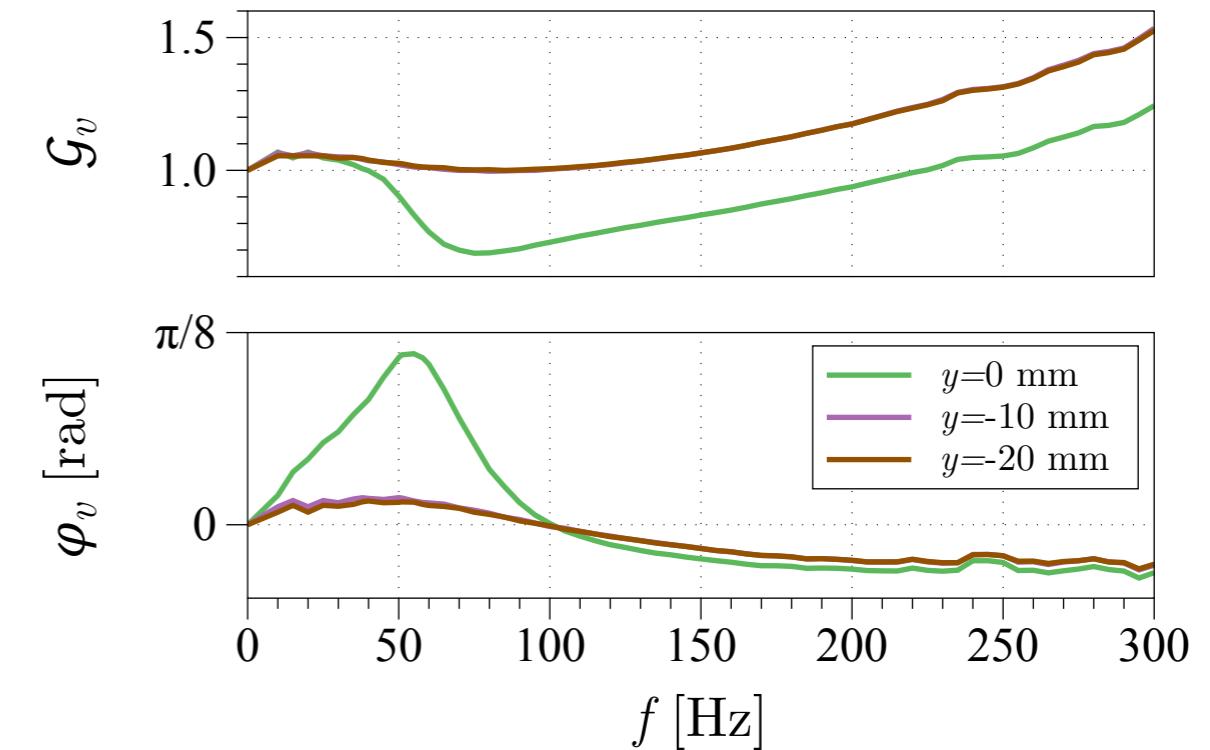
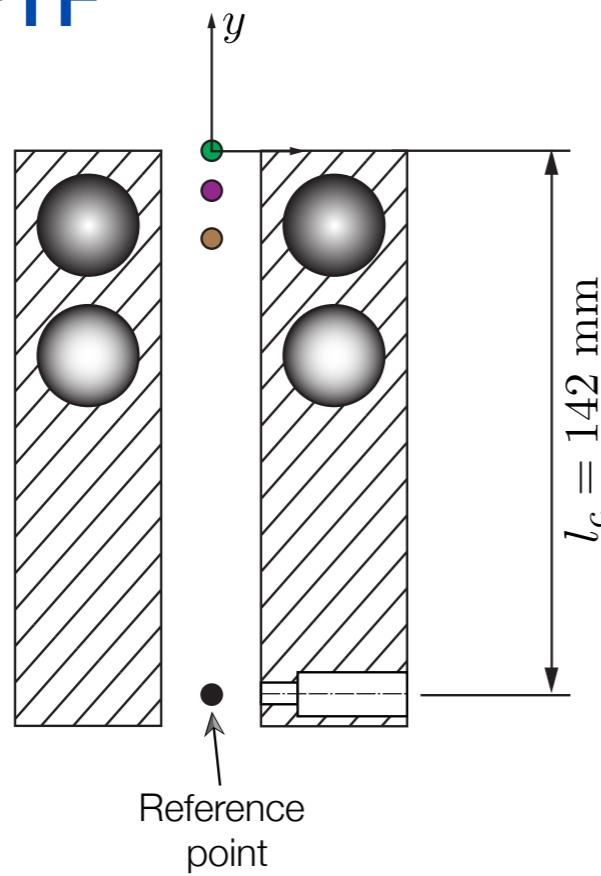


Velocity transfer function

Does the FTF depends on the reference point ?

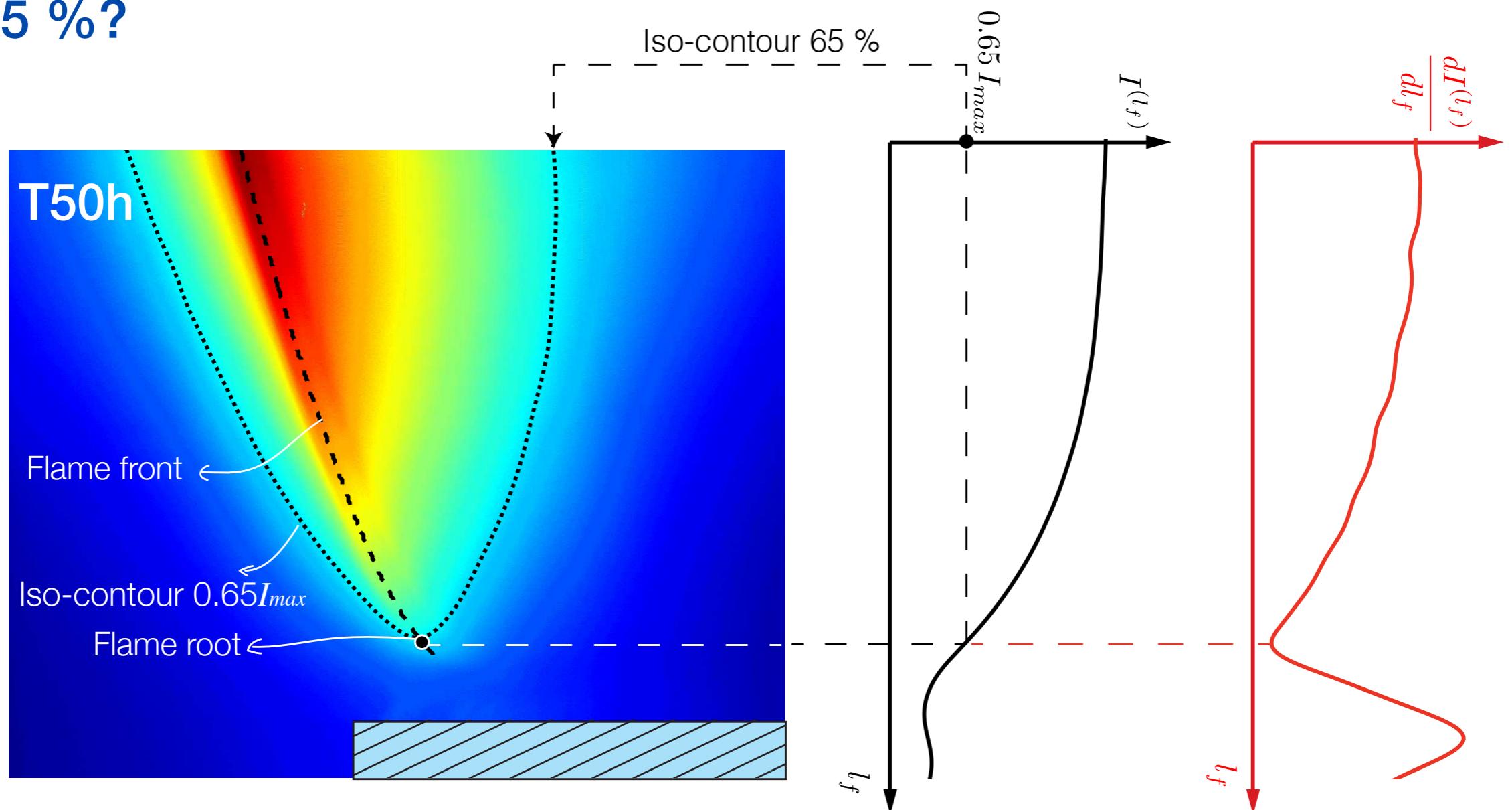


Corrected FTF

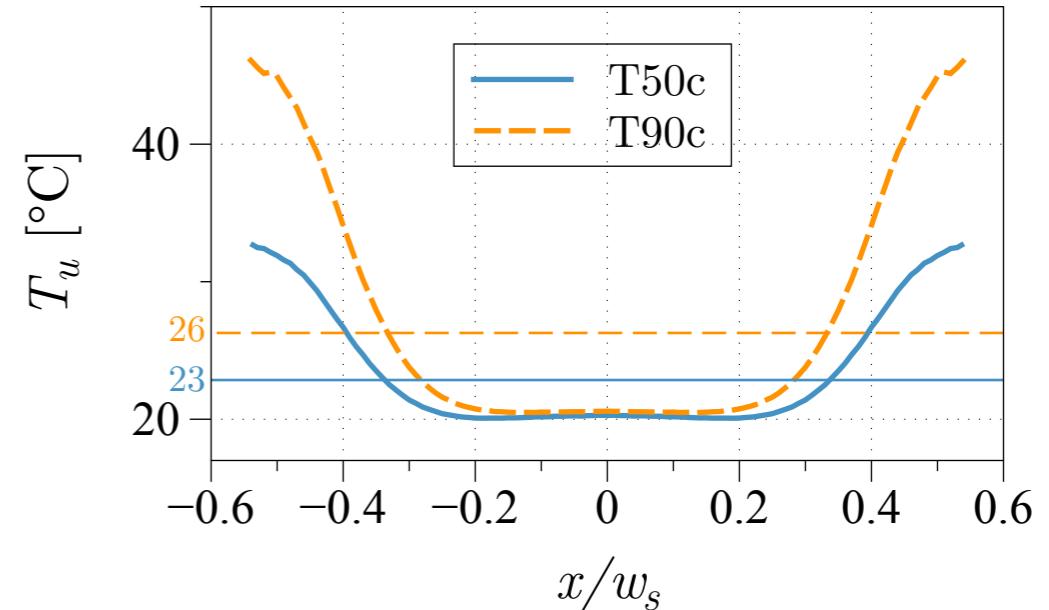
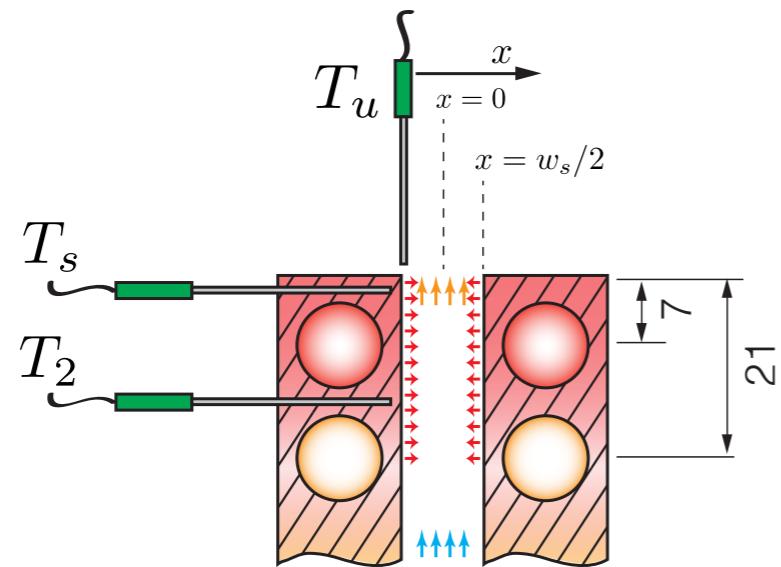


Flame Root Definition

Why 65 %?



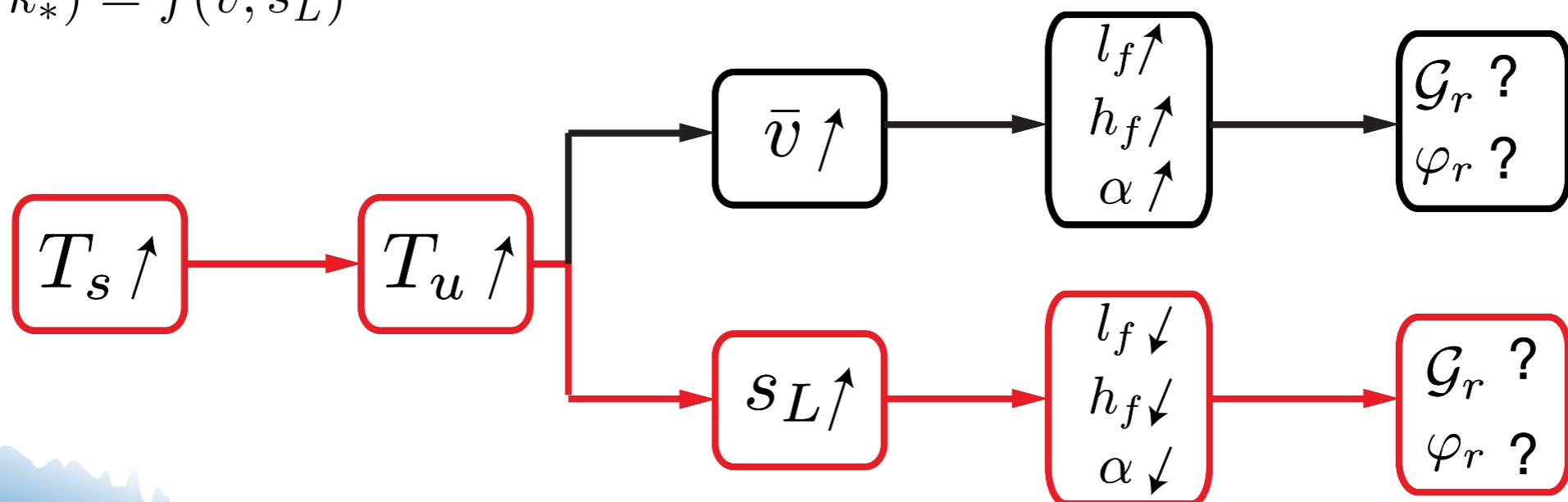
3. Does wall temperature modify the reactants temperature profile ?



The pre-heating of the fresh gases cause:

- ★ Acceleration of the reactants $\bar{v} \uparrow$
- ★ Increase of the flame speed $s_L \uparrow$

$$\mathcal{F}_A = f(\omega_*, k_*) = f(\bar{v}, s_L)$$



4. Does the increase in s_L explain the changes on the FTF ?

$$s_L \propto \left(\frac{T_{fg}}{T_{fg}^0} \right)^{\alpha_T}$$

$\alpha_T \approx 1.9$

T50h-T90h		s_L Impact on the FTF	
ΔT_u [°]	Δs_L [cm s ⁻¹]	\mathcal{G}_r	φ_r
3	1	3.4 %	2.2 %
		11.5 %	3.6 %
Actual FTF difference T50h-T90h			

[1] Gu et al. 2000 cf.

$$T_s = 90^\circ\text{C} \quad f = 58 \text{ Hz} \quad \Phi = 0.9 \text{ to } 1.02$$

