# Designing an A\B Test

Udacity Data Analyst Nanodegree - Project 7

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# **Project Overview**

This is the seventh project on the Udacity Data Analyst NanoDegree. On this project, I will consider an actual experiment that was run by Udacity where I'll flesh the experiment idea out into a fully defined design, analyse the results, and propose a high-level follow-on experiment.

This project is connected to the A/B Testing course and built based on the submission template found <a href="here">here</a>. The submission consist on a series of questions (that you will see in the beginning of each section in blue) that I'll be answering though this document. It is not this project's objective to create a step-by-step documentation or explanation of an A\B test. If something seems "out of context" please refer to the template for further instructions.

This project doesn't require any explicit coding so all the calculations were done using google spreadsheets. I tried to present\document most of the intermediate steps.

This document is divided on the following section:

## Contents

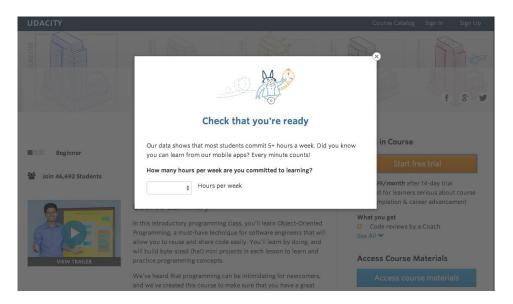
Project Overview	2
Experiment Overview: Free Trial Screener	3
Experiment Design	4
Metric Choice	4
Measuring Standard Deviation	6
Sizing	7
Number of Samples vs. Power	7
Duration vs. Exposure	8
Experiment Analysis	9
Sanity Checks	10
Result Analysis	10
Recommendation	13
Follow-Up Experiment	14

# **Experiment Overview: Free Trial Screener**

At the time of this experiment, Udacity courses currently have two options on the home page: "start free trial", and "access course materials". If the student clicks "start free trial", they will be asked to enter their credit card information, and then they will be enrolled in a free trial for the paid version of the course. After 14 days, they will automatically be charged unless they cancel first. If the student clicks "access course materials", they will be able to view the videos and take the quizzes for free, but they will not receive coaching support or a verified certificate, and they will not submit their final project for feedback.

In the experiment, Udacity tested a change where if the student clicked "start free trial", they were asked how much time they had available to devote to the course. If the student indicated 5 or more hours per week, they would be taken through the checkout process as usual. If they indicated fewer than 5 hours per week, a message would appear indicating that Udacity courses usually require a greater time commitment for successful completion, and suggesting that the student might like to access the course materials for free. At this point, the student would have the option to continue enrolling in the free trial, or access the course materials for free instead.

This screenshot shows what the experiment looks like.



The hypothesis was that this might set clearer expectations for students upfront, thus reducing the number of frustrated students who left the free trial because they didn't have enough time—without significantly reducing the number of students to continue past the free trial and eventually complete the course. If this hypothesis held true, Udacity could improve the overall student experience and improve coaches' capacity to support students who are likely to complete the course.

The unit of diversion is a cookie, although if the student enrols in the free trial, they are tracked by user-id from that point forward. The same user-id cannot enroll in the free trial twice. For users that do not enroll, their user-id is not tracked in the experiment, even if they were signed in when they visited the course overview page.

# **Experiment Design**

## **Metric Choice**

List which metrics you will use as invariant metrics and evaluation metrics here.

The metrics chosen for this experiment are:

Invariant Metrics: Number of Cookies, Number of Clicks

Evaluation Metrics: Gross Conversion, Retention, Net Conversion

Metrics Explanation:

#### Number of cookies:

Represents the number of unique cookies to view the course overview page.

Chosen as invariant metric because the number of cookies are independent from the experiments since the visits happen before the user sees the experiment.

#### Number of clicks:

Represents the number of unique cookies to click the "Start free trial" button (which happens before the free trial screener is trigger).

Chosen as an invariant metric for the same reason as the number of cookies. It happens before the experiment, so it will be the same for control and experiment group (equal probability of clicking the Start Free Trial button by both groups)

## Click-through-probability:

Represents the number of unique cookies to click the "Start free trial" button divided by number of unique cookies to view the course overview page.

Chosen as an invariant metric for the same reason as both metrics above (happens before the free trial screen).

#### Gross conversion:

Represents the number of user-ids to complete checkout and enroll in the free trial divided by number of unique cookies to click the "Start free trial" button.

Chosen as an evaluation metric because it directly depends on the effect of the experiment

#### Retention:

Represents the number of user-ids to remain enrolled past the 14-day boundary (and thus make at least one payment) divided by number of user-ids to complete checkout.

Chosen as an evaluation metric because it directly depends on the effect of the experiment and indicates financial gain resulted from the change

## Net conversion:

Represents the number of user-ids to remain enrolled past the 14-day boundary (and thus make at least one payment) divided by the number of unique cookies to click the "Start free trial" button.

Chosen as an evaluation metric because it directly depends on the effect of the experiment and indicates financial gain resulted from the change

## Number of user-ids:

Represents the number of users who enrol in the free trial. Not chosen as an invariant metric because the number of users who enroll in the free trial is dependent on the experiment. Neither chosen as an ideal evaluation metric because the number of visitor might reasonably be different between the control and experiment groups,

# **Measuring Standard Deviation**

## List the standard deviation of each of your evaluation metrics.

Bellow I'll list the standard deviation of each of the evaluation metrics. For each of them, I indicate whether the analytic estimate would be comparable to the empirical variability, or whether you expect them to be different. The standard deviation will be calculated using the formula:

$$\sigma = (p (1 - p)/n)^{1/2}$$

That's the standard deviation of a binomial distribution and refer to 40000 unique cookies view the page per day. From those, 3200 will click on the "Start free trial" button (0.08% of them). That's the click-through-probability on "Start free trial" button;

On the current course format, from all the 3200 clicks, 660 will enrol on the course, which gives a probability of enrolling of 0.20625 %.

Again, on the current course format, the probability of payment is 0.53%, which results on the probability of payment of 0.1093125%

Unique cookies to view page per day:	40000
Unique cookies to click "Start free trial" per day:	3200
Click-through-probability on "Start free trial":	0.08
Enrolments per day:	660

Gross Conversion	Probability of enrolling, given click:	0.20625
Retention	Probability of payment, given enroll:	0.53
Net Conversion	Probability of payment, given click	0.1093125

## Given a Sample size of 500:

	Numerator	Denominator	Ratio	Square Root
	P(1-p)	n		(Standard Deviation)
Gross Conversion	0.163710938	400	0.000409	0.02023
Retention	0.2491	82.5	0.003019	0.05495
Net Conversion	0.097363277	400	0.000243	0.01560

# Sizing

# **Number of Samples vs. Power**

Indicate whether you will use the Bonferroni correction during your analysis phase, and give the number of page views you will need to power you experiment appropriately.

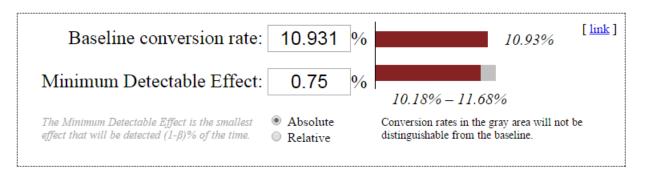
	Baseline	dmin	Samples	Page Views	times 2
	conversion rate		Needed		(Experiment and
					Control groups)
Gross Conversion	20.625%	1.00%	25,835	322,938	645,875
Retention	53.000%	1.00%	39,115	2,370,606	4,741,212
Net Conversion	10.931%	0.75%	27,413	342,663	685,325

#### Considerations:

- I did not use the "Bonferroni correction";
- Base Line Conversion rate: click-through-probability before making the change;
- dmin: Minimal detectable Effect: practical significance level;
- The evaluation metrics I selected to proceed with are Gross conversion and Net conversion.
- Since to evaluate retention would need over 8M page views, I've decide to use Gross Conversion and Net Conversion so 685 324 page views will be necessary;

The "samples needed" where calculated using this online calculator:

Question: How many subjects are needed for an A/B test?



Sample size:

27,413

per variation

Statistical power 1–β:	80%	Percent of the time the minimum effect size will be detected, assuming it	exists
Significance level α:	5%	Percent of the time a difference will be detected, assuming one does NO.	T exis

# **Duration vs. Exposure**

Indicate what fraction of traffic you would divert to this experiment and, given this, how many days you would need to run the experiment.

I would divert 100% of the traffic to the experiment, which will result on the experiment taking 18 days, which is a reasonable time. I chose that because I don't consider the experiment to be risky given that:

- It does not affect existing customers (either paying or non-paying);
- Is very simple, affecting only one step of the workflow;

# **Experiment Analysis**

The data for the analysis can see below. (Original spreadsheet <a href="here">here</a>). Note that on the spreadsheet there are two sheets - one for the experiment group, and one for the control group. I merged them on the same table for easy of use. The meaning of each column is:

- Page views: Number of unique cookies to view the course overview page that day.
- Clicks: Number of unique cookies to click the course overview page that day.
- Enrolments: Number of user-ids to enroll in the free trial that day.
- Payments: Number of user-ids who enrolled on that day to remain enrolled for 14 days and thus make a payment. (Note that the date for this column is the start date, that is, the date of enrolment, rather than the date of the payment. The payment happened 14 days later. Because of this, the enrolments and payments are tracked for 14 fewer days than the other columns.)

Control					Experiment				
Date	Pageviews	Clicks	Enrollments	Payments	Date	Pageviews	Clicks	Enrollments	Payments
Sat, Oct 11	7723	687	134	70	Sat, Oct 11	7716	686	105	34
Sun, Oct 12	9102	779	147	70	Sun, Oct 12	9288	785	116	91
Mon, Oct 13	10511	909	167	95	Mon, Oct 13	10480	884	145	79
Tue, Oct 14	9871	836	156	105	Tue, Oct 14	9867	827	138	92
Wed, Oct 15	10014	837	163	64	Wed, Oct 15	9793	832	140	94
Thu, Oct 16	9670	823	138	82	Thu, Oct 16	9500	788	129	61
Fri, Oct 17	9008	748	146	76	Fri, Oct 17	9088	780	127	44
Sat, Oct 18	7434	632	110	70	Sat, Oct 18	7664	652	94	62
Sun, Oct 19	8459	691	131	60	Sun, Oct 19	8434	697	120	77
Mon, Oct 20	10667	861	165	97	Mon, Oct 20	10496	860	153	98
Tue, Oct 21	10660	867	196	105	Tue, Oct 21	10551	864	143	71
Wed, Oct 22	9947	838	162	92	Wed, Oct 22	9737	801	128	70
Thu, Oct 23	8324	665	127	56	Thu, Oct 23	8176	642	122	68
Fri, Oct 24	9434	673	220	122	Fri, Oct 24	9402	697	194	94
Sat, Oct 25	8687	691	176	128	Sat, Oct 25	8669	669	127	81
Sun, Oct 26	8896	708	161	104	Sun, Oct 26	8881	693	153	101
Mon, Oct 27	9535	759	233	124	Mon, Oct 27	9655	771	213	119
Tue, Oct 28	9363	736	154	91	Tue, Oct 28	9396	736	162	120
Wed, Oct 29	9327	739	196	86	Wed, Oct 29	9262	727	201	96
Thu, Oct 30	9345	734	167	75	Thu, Oct 30	9308	728	207	67
Fri, Oct 31	8890	706	174	101	Fri, Oct 31	8715	722	182	123
Sat, Nov 1	8460	681	156	93	Sat, Nov 1	8448	695	142	100
Sun, Nov 2	8836	693	206	67	Sun, Nov 2	8836	724	182	103
Mon, Nov 3	9437	788			Mon, Nov 3	9359	789		
Tue, Nov 4	9420	781			Tue, Nov 4	9427	743		
Wed, Nov 5	9570	805			Wed, Nov 5	9633	808		
Thu, Nov 6	9921	830			Thu, Nov 6	9842	831		
Fri, Nov 7	9424	781			Fri, Nov 7	9272	767		
Sat, Nov 8	9010	756			Sat, Nov 8	8969	760		
Sun, Nov 9	9656	825			Sun, Nov 9	9697	850		
Mon, Nov 10	10419	874			Mon, Nov 10	10445	851		
Tue, Nov 11	9880	830			Tue, Nov 11	9931	831		
Wed, Nov 12	10134				Wed, Nov 12	10042			
Thu, Nov 13	9717	814			Thu, Nov 13	9721	829		
Fri, Nov 14	9192	735			Fri, Nov 14	9304	770		
Sat, Nov 15	8630	743			Sat, Nov 15	8668	724		
Sun, Nov 16	8970	722			Sun, Nov 16	8988	710		
Total	345,543	28,378	3,785	2,033		344,660	28,325	3,423	1,945

# **Sanity Checks**

For each of your invariant metrics, give the 95% confidence interval for the value you expect to observe, the actual observed value, and whether the metric passes your sanity check. For any sanity check that did not pass, explain your best guess as to what went wrong based on the day-by-day data.

First, I started by checking if the numbers of assignments on the control group is the same as the numbers on the experiment group:

Page views: Control: 345543 Experiment: 344660

The Control\Experiment allocation can be thought of a random event with exactly two outcomes (probability of assignment = 0.5) – binomial distribution. So we'll need to calculate the binomial confidence interval. The Total sample size is 690203, which is enough to assume a normal distribution. (The binomial distribution assumes a normal distribution when n is large). I will go step by step for the "Page View" calculation only:

1. Compute the standard deviation of a binomial distribution with probability of 0.5 of success:

$$SD = 0.0006$$

2. Calculate the margin of error with a 95% confidence interval:

3. Calculate the confidence Interval (5% of the time the observed values should fall into this range):

4. Check if the observed values is within the interval:

Values on the control group: 1 – (344,660 / 690,203) = 0.5006

Here's the summary:

						Margin of	Lower	Upper	Value on the
	Total	р	1-p	/ n	SD	Error @95	Bound	Bound	Control Group
Pageviews	690,203	0.5	0.5	0.00000036221	0.0006	0.001180	0.4988	0.5012	0.5006
Clicks	56,703	0.5	0.5	0.00000440894	0.0021	0.004116	0.4959	0.5041	0.5005

# **Result Analysis**

Effect Size Tests

For each of your evaluation metrics, give a 95% confidence interval around the difference between the experiment and control groups. Indicate whether each metric is statistically and practically significant.

We can only understand whether or not a user have gone through the full enrolment process until the 2nd of November, that's why the total clicks on the formulas will only include that interval

	Clicks	Enrollments	Payments
CONTROL	17293	3785	2033
<b>EXPERIMENT</b>	17260	3423	1945
Total	34553	7208	3978

For Gross Conversion, we calculate the "p – experiment" by dividing number of enrolments by number of clicks on the experiment totals and the "p – control" by doing the same calculation on the control Group. The Net Conversion follows the same logic but it uses the number of payments on the numerator:

	p - experiment	p - control	d
<b>Gross Convertion</b>	0.19832	0.21887	-0.02055
Net Convertion	0.11269	0.11756	-0.00487

Then we calculate the pooled probability by using the same formula on the total values and the standard error is calculated by the formula:

$$\sigma = (p (1 - p)/n)^{\frac{1}{2}}$$

n in this case being:

because the sample size on the control is different than the sample size on the experiment.

Next we calculate the margin of error by multiplying the SE by the z-score for 95% confidence (1.96) and apply the margin of error to the "d" to get the Lower and Upper CI boundaries:

Pooled Probability	SE	Margin of Error	Lower CI	Upper CI
0.2086	0.0044	0.0086	-0.0291	-0.0120
0.1151	0.0034	0.0067	-0.0116	0.0019

Considering that the practical significance (d\_min) for gross conversion is +/- 0.01 and for Net Conversion is 0.0075:

Gross conversion: Is statistically significant because the CI range doesn't contain zero and practically significant because the CI doesn't contain the d\_min value.

Net conversion: Is not statistically significant because the CI range contains zero and is not practically significant because the CI contains the d\_min value.

#### Sign Tests

For each of your evaluation metrics, do a sign test using the day-by-day data, and report the p-value of the sign test and whether the result is statistically significant

To do a sign test using the day-by-day data, we need to know how many successes we've for each measure and the total number of trials. Success can be considered when the metric was bigger on the experiment than on the control. Looking at the table above we can see that there were 4 successes for Gross Conversion and 10 successes for Net conversion. The number of trials is 23 in both cases.

Using an online calculator like this, we can plug in the values and get the two-tailed p value, which represents the chance of observing either X or fewer successes, or Y-X or more successes, in Y trials by chance.

	Sucesses	Trials	Probability	two-tailed p-value
<b>Gross Conversion</b>	4	23	0.5	0.0026
Net Conversion	10	23	0.5	0.6776

Since the p-value is smaller than the alpha of 0.5, the sign test agrees with the hypotheses test, that this result is unlikely to have unlikely to have come about by chance.

# Recommendation

#### Make a recommendation and briefly describe your reasoning.

Based on the test executed, I advise launching the change. Two hypothesis tests were performed to support that decision, one on "Gross Conversion" and the other on Net Conversion".

The hypothesis that the introduction of the new the pop-up page will improve the "Gross Conversion" of the site (number of users who complete the checkout divided by the number of users who start the free trial) proved to be statistically and practically significant.

This is a good thing because we are discouraging trial signups that are unlikely to complete the checkout (probably due to lack of available time to dedicate to the course)

The hypothesis that the introduction of the new the pop-up page will improve the "Net Conversion" of the site (number of users who make at least one payment divided by the number of users who start the free trial) was both statistically and practically insignificant.

# **Follow-Up Experiment**

Give a high-level description of the follow up experiment you would run, what your hypothesis would be, what metrics you would want to measure, what your unit of diversion would be, and your reasoning for these choices.

In order to increase the number of "paying students", I believe Udacity could follow a different approach when it comes to the "start free trial" process. Currently, when you select "start free trial", you are prompted to input your credit card (CC) information, even though the course is free for the first 14 days.

I believe that many students decide not to do it simply because they don't want to inform their CC information on such an early stage, especially if they are not sure they'll purchase the product (and there are many reason for that, they may think they'll get improper billing or that they even may forget to cancel and be charged for a service they are not using).

The way I see it should work is: the user should be able to take the 14-day trial without informing their CC information and only after the trial ended, be asked if he\she wants to continue, then being prompted for the CC information.

So my null hypothesis would be:

• Not requesting user's credit card information when starting the free trial will not increase the Net Conversion of the course.

The "Invariant Metric" would be "number of cookies" because we want to capture how many "cookies" will start the free trial and become paying users.

The Evaluation metric would be "Retention", the ratio between users that make one payment and the number of users who started the free trial.

#### References:

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https://en.wikipedia.org/wiki/Bernoulli distribution

http://www.evanmiller.org/ab-testing/sample-size.html

http://graphpad.com/quickcalcs/binomial1.cfm