

## Problem J: Malaysia Airlines

We all remember Malaysia Airlines flight 370, that mysteriously disappeared somewhere in the Indian ocean, on March 8, 2014. The flight had left Kuala Lumpur and was bound to Beijing. Normally, it should fly in the north-east direction, towards the Chinese capital.

However, less than an hour after takeoff, it turned westward, for no apparent reason, and eventually vanished from the radar screens.

If some kind of an alarm had been triggered at the air traffic control when the plane made that inexplicable turn, perhaps we would have a better idea of what happened afterwards.

In general, commercial planes fly on a straight line, from one airport to another airport. For example, when I fly from Lisbon to New York, I expect that the plane always goes towards the West, even if the pilots sometimes deviate a little to avoid a storm on the route.

Obviously, we need a system that automatically controls the amount of deviation of a plane during a flight.

### Task

Write a program that, given a *flight path*, computes the *flight angle*.

The flight path is the sequence of the *flight points* of a plane during a flight, each represented by its x-y coordinates.

In a *normal* flight, the flight angle is represented by a pair of vectors: the *counterclockwisemost* flight vector and the *clockwisemost* flight vector.

A *flight vector* is a vector defined by two consecutive flight points.

We say that a vector  $u$  is more counterclockwise than a vector  $v$  if changing from the direction of  $v$  to the direction of  $u$  corresponds to turning to the left; likewise, we say that a vector  $u$  is more clockwise than a vector  $v$  if changing from the direction of  $v$  to the direction of  $u$  corresponds to turning to the right.

Note that, given a set of vectors all in the same half-plane, a counterclockwisemost vector  $u$  is a vector in the set for which no other vector in the set is more counterclockwise than  $u$ , and likewise for the clockwisemost vector.

A normal flight is one where the plane never turns back more than 180 degrees, on any part of the flight path. In other words, a flight is normal if all the flight vectors are in the same half-plane.

### Input

The first line of the input contains one integer,  $N$ , representing the number of flight points.

$N$  lines follow; each line contains two integer numbers,  $X_i$  and  $Y_i$ , for  $i$  from 1 to  $N$ , separated by one space, representing the x-y coordinates of the  $i$ -th flight point.

### Output

For a normal flight, your program shall print four space separated integers: the first two



represent the *earliest* counterclockwisemost flight vector; the remaining two represent *earliest* clockwise-most flight vector.

For the purpose of the above specification, we say that a vector  $v$  is *earlier* than another vector  $u$  if the first occurrence of  $v$  occurs before the first occurrence of  $u$  in the flight path.

If the flight is not normal, your program shall print the coordinates of the last flight points that belongs to the initial normal part of the flight.

## Constraints

$2 \leq N \leq 10,000$  Number of points in the flight path  
 $-10^9 \leq X_i, Y_i \leq 10^9$  Coordinates of points

The following constraints also apply to all the input test cases:

- Consecutive points are not equal.
- The angle of two consecutive flight vector is less than 180 degrees.
- The magnitude of all vectors is less than 10,000.

## Input Example 1

```
8
-350 -200
-100 -100
0 -100
100 200
200 200
300 100
300 -100
350 -150
```

## Output Example 1

```
100 300 0 -200
```

## Explanation of Example 1

The image below represents the flight path.

The third vector, with components  $\langle 100, 300 \rangle$ , is the counterclockwisemost; the sixth vector, with components  $\langle 0, -200 \rangle$ , is the clockwisemost.

### Input Example 2

```
10
-150 250
-200 150
-300 50
-200 -50
-100 -50
0 50
100 100
200 100
200 200
300 100
```

### Output Example 2

```
200 100
```

### Explanation of Example 2

The image below represents the flight path.

The angle of the eight vector and the second vector is greater than 180 degrees. Actually, this is also true for the angle of the eight vector and the first vector. But note that the angle of the second vector and the fifth vector is exactly 180 degrees.

The normal part of the flight ends at point  $\langle 200, 100 \rangle$ .

---

*This document was translated from  $L^A T_E X$  by [H<sup>E</sup>V<sup>E</sup>A](#).*