FEUP/MIEIC THEORY OF COMPUTING

EXERCISES ABOUT PUSHDOWN AUTOMATA (PDAS)

- 1 Consider the context-free language over the alphabet $\Sigma = \{a,b\}$ defined by: $L = \{a^nb^k \mid n \le k \le 2n\}$.
 - a) Write a context-free grammar (CFG) for L.
 - b) Obtain a PDA for recognizing that language.
 - c) Show the sequences of instantaneous descriptions of the automaton for the input string *aabbb*.
 - d) What does happen when the input string is *aaabb*? Justify using the instantaneous descriptions.
- 2 Consider the CFG $G = (\{S, A\}, \{0, 1\}, P, S)$ with productions:

$$S \rightarrow A 1 A$$

$$A \rightarrow 1A \mid 0 \mid A \mid \epsilon$$

Obtain a PDA, accepting by empty stack, which recognizes the language of the grammar G.

3 Consider the CFG $G = (\{S\}, \{i, e\}, P, S)$ sith the following productions:

$$S \rightarrow SS \mid iS \mid iS eS \mid \varepsilon$$

Obtain a PDA, accepting by empty stack, which recognizes the language of the grammar G.

4 Consider the following PDA wich accepts by empty stack

$$P = (\{p, s\}, \{0, 1\}, \{Z, 0, 1\}, \delta, p, Z).$$

Function δ is defined as follows:

$$\begin{array}{lll} \delta(p,0,Z) \,=\, \{\,(p,0Z)\,\} & \delta(p,1,Z) \,=\, \{\,(p,1Z)\,\} \\ \delta(p,0,1) \,=\, \{\,(p,\epsilon)\,\} & \delta(p,1,0) \,=\, \{\,(p,\epsilon)\,\} \\ \delta(p,0,0) \,=\, \{\,(p,00)\,\} & \delta(p,1,1) \,=\, \{\,(p,11)\,\} \\ \delta(p,\epsilon,Z) \,=\, \{\,(s,\epsilon)\,\} & \end{array}$$

- a) Show the sequence of reacheable configurations when starting from configuration (p, 1100, Z).
- b) Is the string 1100 recognized by the automaton? Why?
- c) What does happen with the sequence of reacheable configurations when starting from configuration (p, 101, Z)?
- 5 "A context-free grammar is ambiguous if there exist a leftmost and a rightmost derivation of at least a string recognized by the grammar". Is this statement true? Justify.