



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$r_L = \sqrt{r(t)^2 + d^2 - 2r(t)d \cos(\phi - \omega t)}$$

$$T = \frac{1}{2} m (\dot{r}^2 + r^2 \dot{\phi}^2) \quad V = -\frac{GmM_T}{r} - \frac{GmM_L}{r_L(r, \phi, t)}$$

$$H = T + V \quad p_r = \frac{\partial L}{\partial \dot{r}} = m\dot{r}, \quad p_\phi = \frac{\partial L}{\partial \dot{\phi}} = mr^2 \dot{\phi}$$

$$H = \frac{p_r^2}{2m} + \frac{p_\phi^2}{2mr^2} - \frac{GmM_T}{r} - \frac{GmM_L}{r_L(r, \phi, t)}$$

$$\dot{r} = \frac{\partial H}{\partial p_r} = \frac{p_r}{m} \quad \dot{p}_r = -\frac{\partial H}{\partial r} = \frac{p_\phi^2}{mr^3} - \frac{GmM_T}{r^2} - \frac{GmM_L}{r_L^3} \times (r - d_{TL} \cos(\phi - \omega t))$$

$$\dot{\phi} = \frac{\partial H}{\partial p_\phi} = \frac{p_\phi}{mr^2} \quad \dot{p}_\phi = -\frac{\partial H}{\partial \phi} = -\frac{GmM_L}{r_L^3} r d_{TL} \sin(\phi - \omega t)$$

$$\tilde{r} = \frac{r}{d}$$

$$\tilde{\phi} = \phi$$

$$\dot{\tilde{r}} = \frac{1}{d} \dot{r} = \frac{1}{d} \frac{\partial H}{\partial \tilde{p}_r} = \frac{\tilde{p}_r}{m}$$

$$\tilde{p}_r = \frac{p_r}{md}$$

$$\ddot{\tilde{\phi}} = \frac{1}{d^2} \ddot{\phi} = \frac{1}{d^2} \frac{\partial H}{\partial \tilde{p}_\phi} = \frac{p_\phi}{m \tilde{r}^2}$$

$$\tilde{p}_\phi = \frac{p_\phi}{md^2}$$

$$\tilde{\dot{p}}_r = \frac{1}{d} \dot{p}_r = \frac{1}{d} \left(-\frac{\partial H}{\partial \tilde{r}} \right)$$

$$= \tilde{p}_\phi^2 \frac{1}{\tilde{r}^3} - \Delta \left(\frac{1}{\tilde{r}^2} + \mu \frac{1}{\tilde{r}^3} (\tilde{r} - \cos(\phi - \omega t)) \right)$$

$$\tilde{\dot{p}}_\phi = \frac{1}{d^2} \dot{p}_\phi = \frac{1}{d^2} \left(-\frac{\partial H}{\partial \tilde{\phi}} \right) = -\Delta \mu \frac{\tilde{r}}{\tilde{r}^3} \sin(\phi - \omega t)$$