## Pseudocode for a recursive solution to the Knight's Tour problem.

The players:

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o Let N be the size of the board ( N \times N ).
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- o Let  $\mathbf{M} = \mathbf{N}^2 1$ . This is the number of valid moves the knight must make to complete a tour.
- o Let **visited** be a two dimensional,  $\mathbf{N} \times \mathbf{N}$ , array of Boolean values. This array is initialized to false, and a location,  $(\mathbf{x}, \mathbf{y})$ , in the array is set to true when the knight visits that spot.
- o Let  $\mathbf{m}$  be an integer between 0 and  $\mathbf{M}$ . It represents a move number. The initial location of the knight is  $\mathbf{m}=0$  and, when the knight has completed a tour,  $\mathbf{m}=\mathbf{M}$ .

```
Boolean Algorithm Move(x, y, m)
// (x, y) is a location of the board and m is a move number
  if (x < 0) OR (x \ge N) OR (y < 0) OR (y \ge N)
     return false //A coordinate is off the board
  if( visited[x, y] = true )
     return false //Can't move here; it has already been visited
  if(m = M)
     //This is a valid move and the knight has now made M moves; so,
     //we have a solution!!!
     print "A solution has been found"
     print "x, y " //This starts printing the solution
     set visited[x, y] = true
     return true
  else
     //This is a valid move, but a tour has not been completed.
     //So, try all the moves that can be made from this location
     //recursively.
     let result be a Boolean variable //MUST be local
     set result = false
     set result = result OR Move(x+2, y+1, m+1)
     set result = result OR Move(x+2, y-1, m+1)
     set result = result OR Move(x-2, y+1, m+1)
     set result = result OR Move(x-2, y-1, m+1)
     set result = result OR Move(x+1, y+2, m+1)
     set result = result OR Move(x+1, y-2, m+1)
     set result = result OR Move(x-1, y+2, m+1)
     set result = result OR Move(x-1, y-2, m+1)
```

```
if( result = true )
   //One of the 8 moves above led to a completed tour. So, this
   //position is part of a successful tour.
   print " x, y "
   return true
else
   //None of the moves from this position led to a successful
   //tour. Now we must backtrack and try a different path
   set visited[x, y] = false //Unvisit this location
   return false
```

To find a tour, for example, starting from (3, 3) on a  $5 \times 5$  board, the initial call would be

```
Move( 3, 3, 0 )
```

If this call returns true, a tour is found and the solution is printed in reverse order. If the call returns false, no solution was found.