Computational Neurobiology

Lecture 7: Neural Encoding

Dmitriy Bozhko

RESEARCH

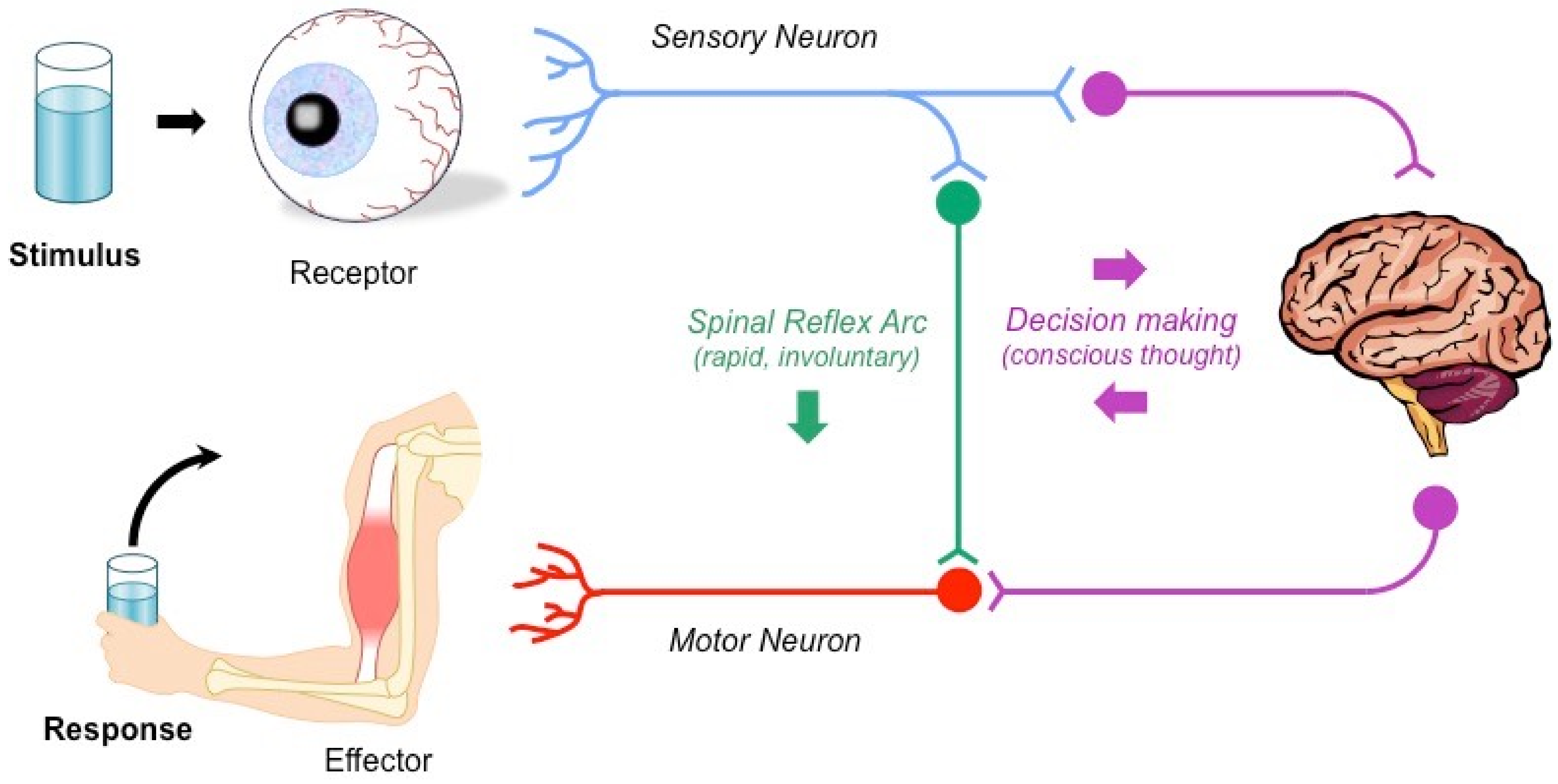
Syllabus

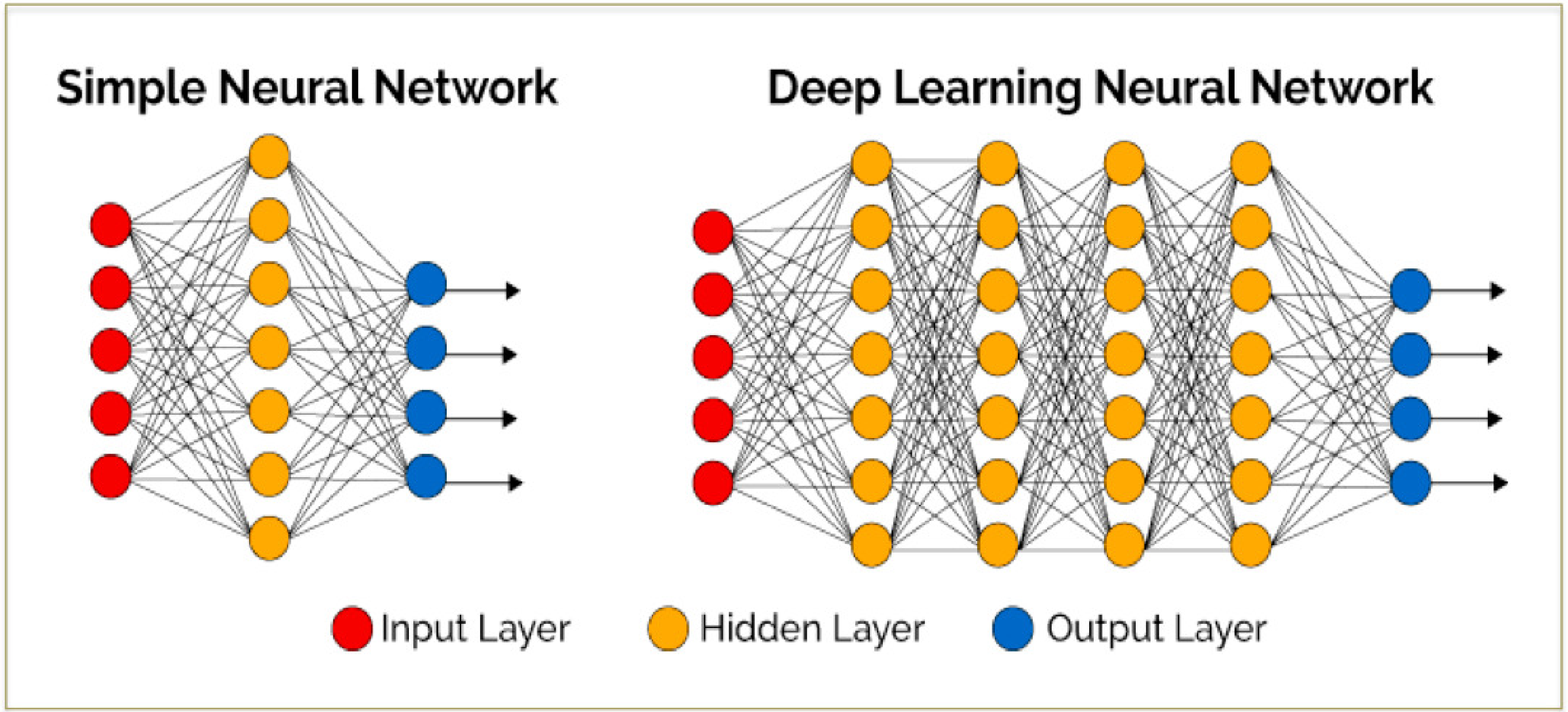
- Stimulus, response, spike train
- Spike train statistics
- The neural code

Stimulus, response, spike train

- From stimulus to response
- Spike trains and firing rates
- Variability of spike trains and its source

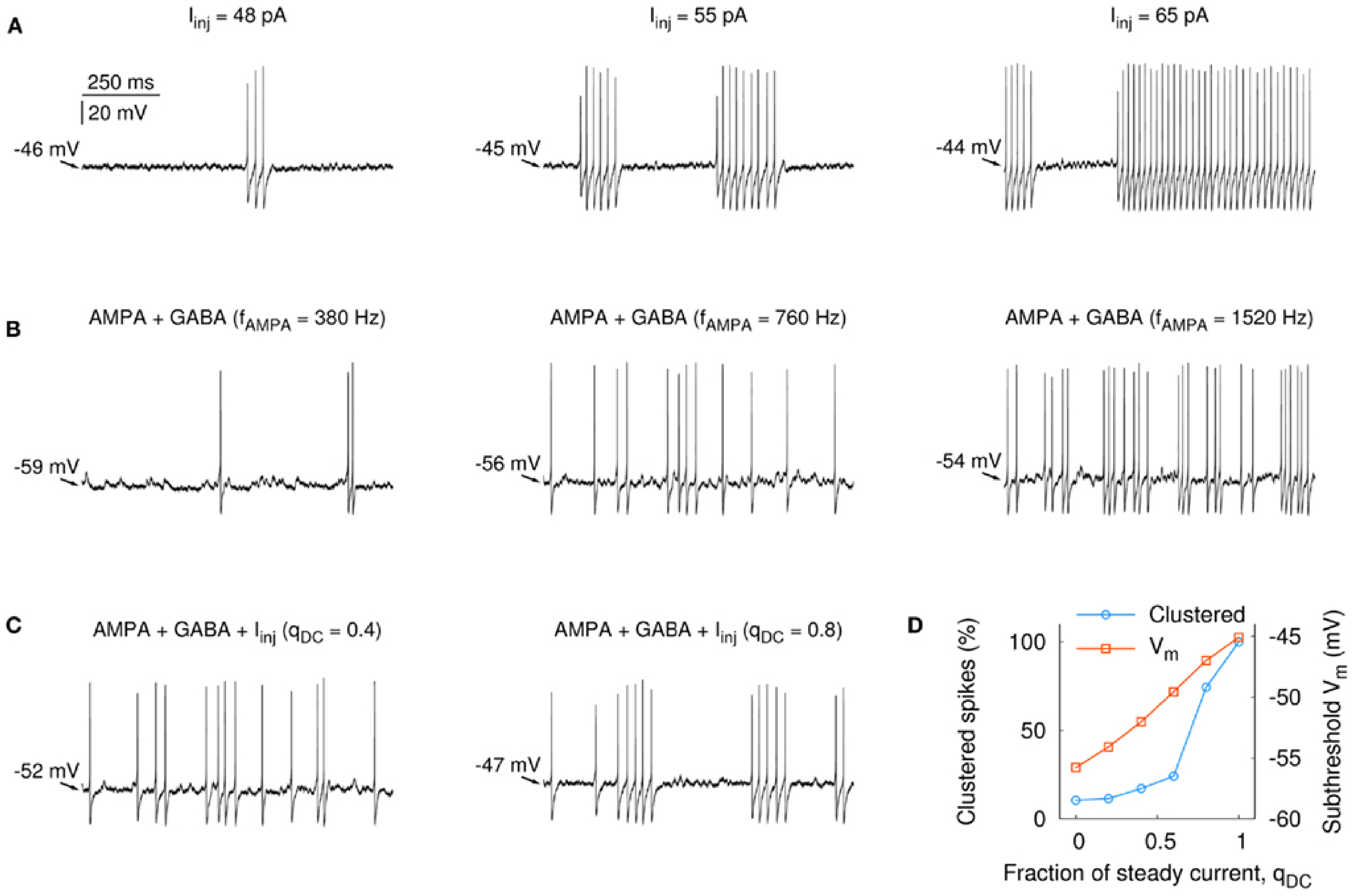
From stimulus to response



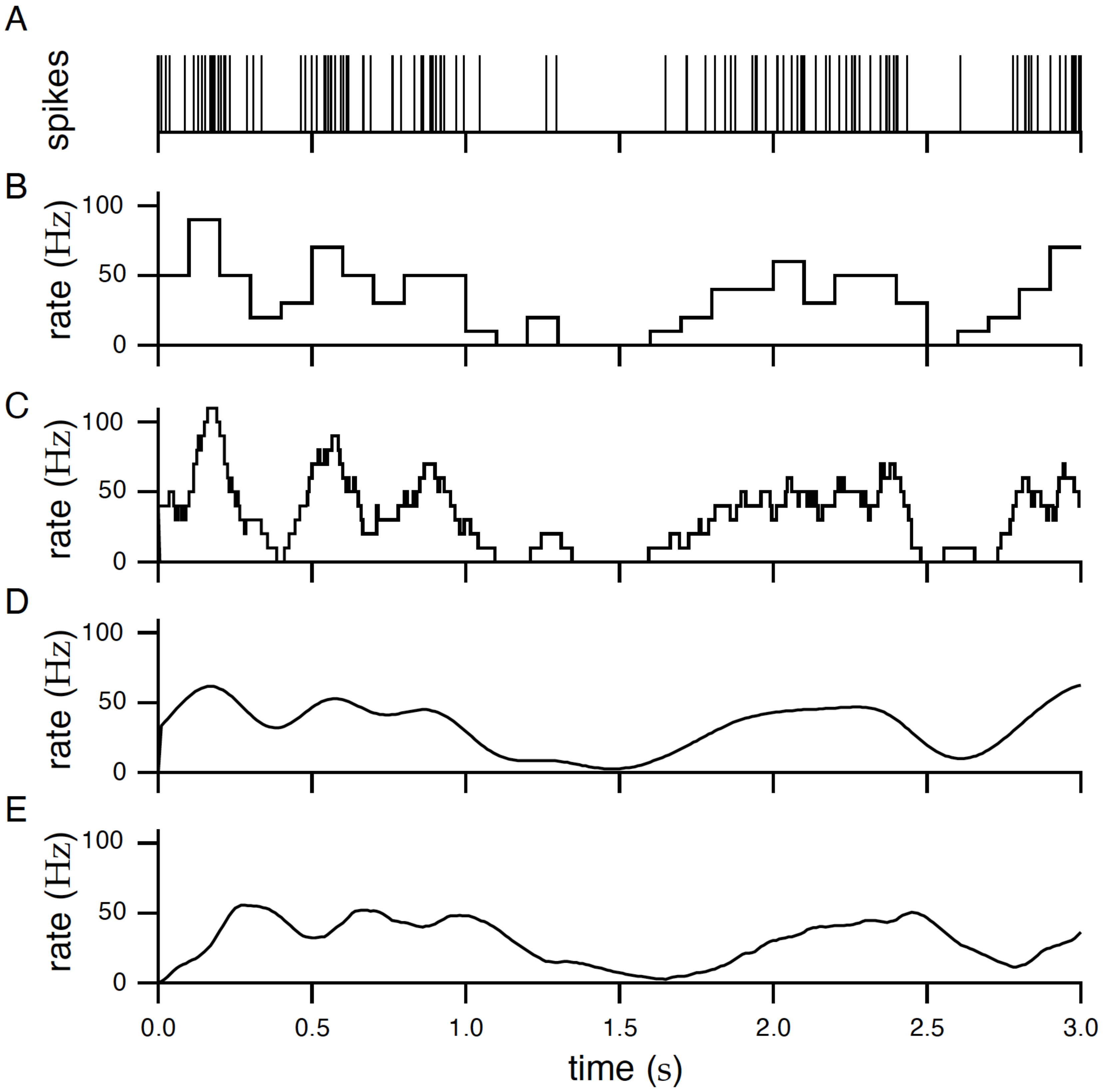


ANN principle architecture

Spike trains and firing rates

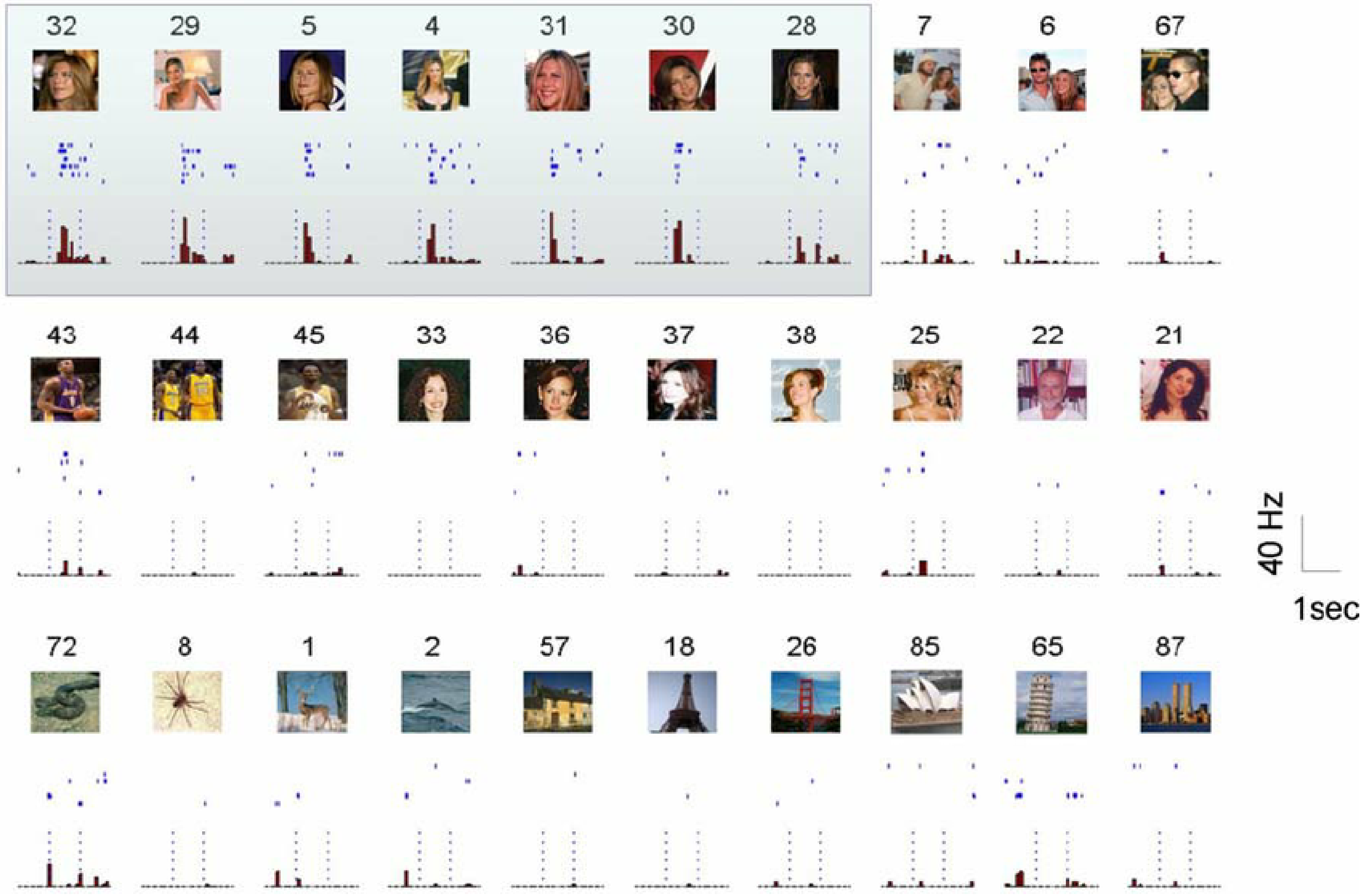


Fast-spiking firing discharge and subthreshold membrane potential in the model neuron



A spike train from a neuron in the inferotemporal cortex of a monkey recorded while that animal watched a video on a monitor under free viewing conditions

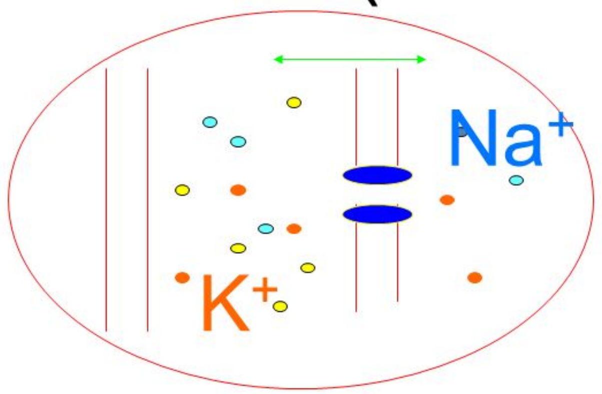
Variability of spike trains



Long-term coding of personal and universal associations

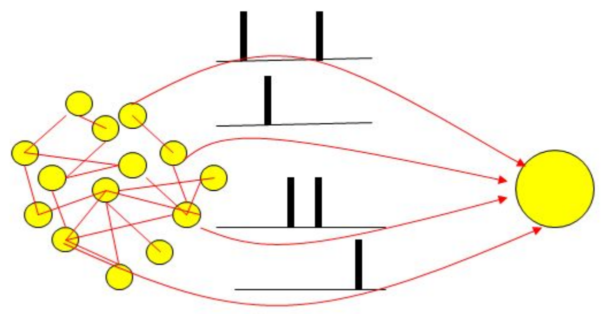
Source of variability

- Intrinsic noise (ion channels)



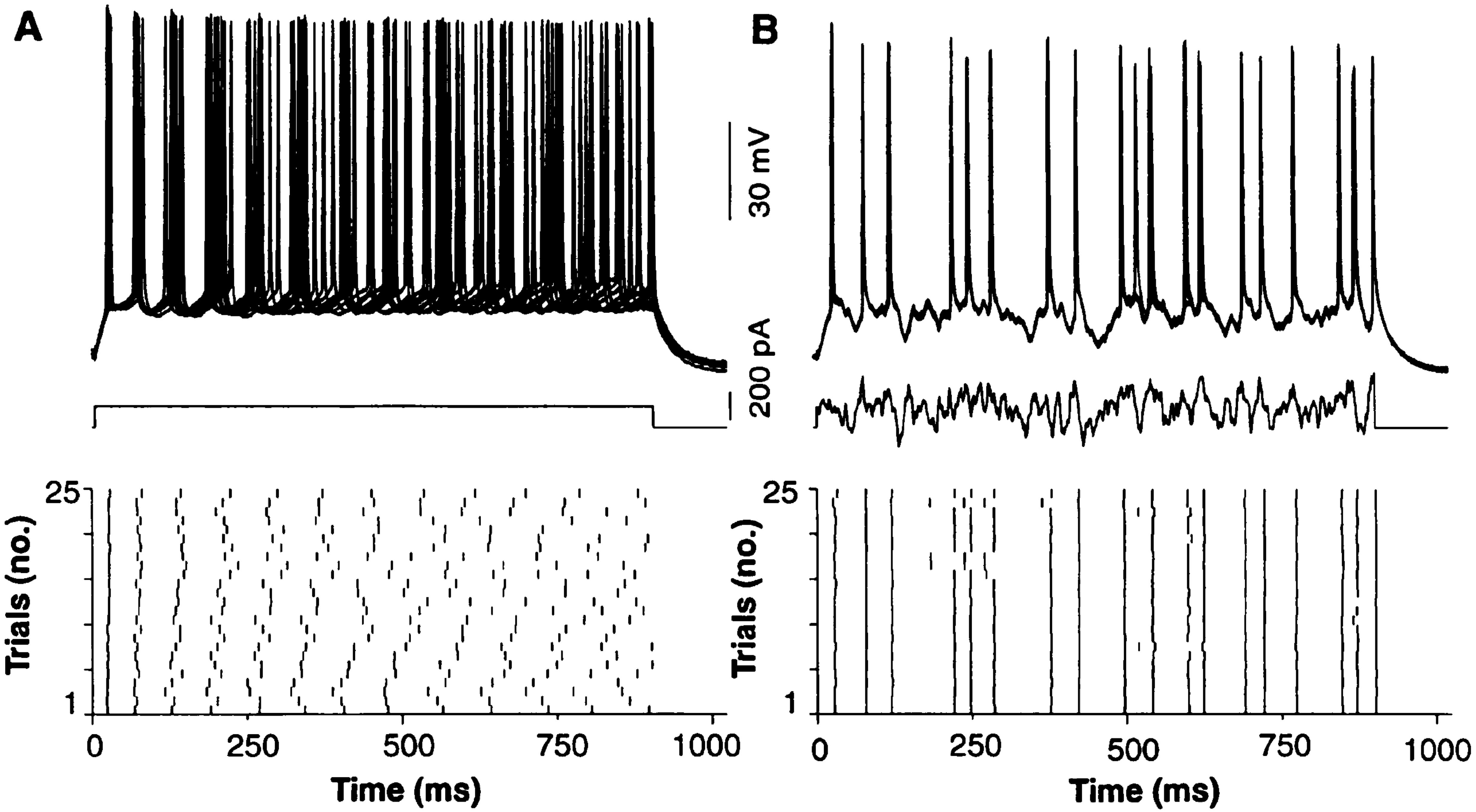
-Finite number of channels
-Finite temperature

-Network noise (background activity)



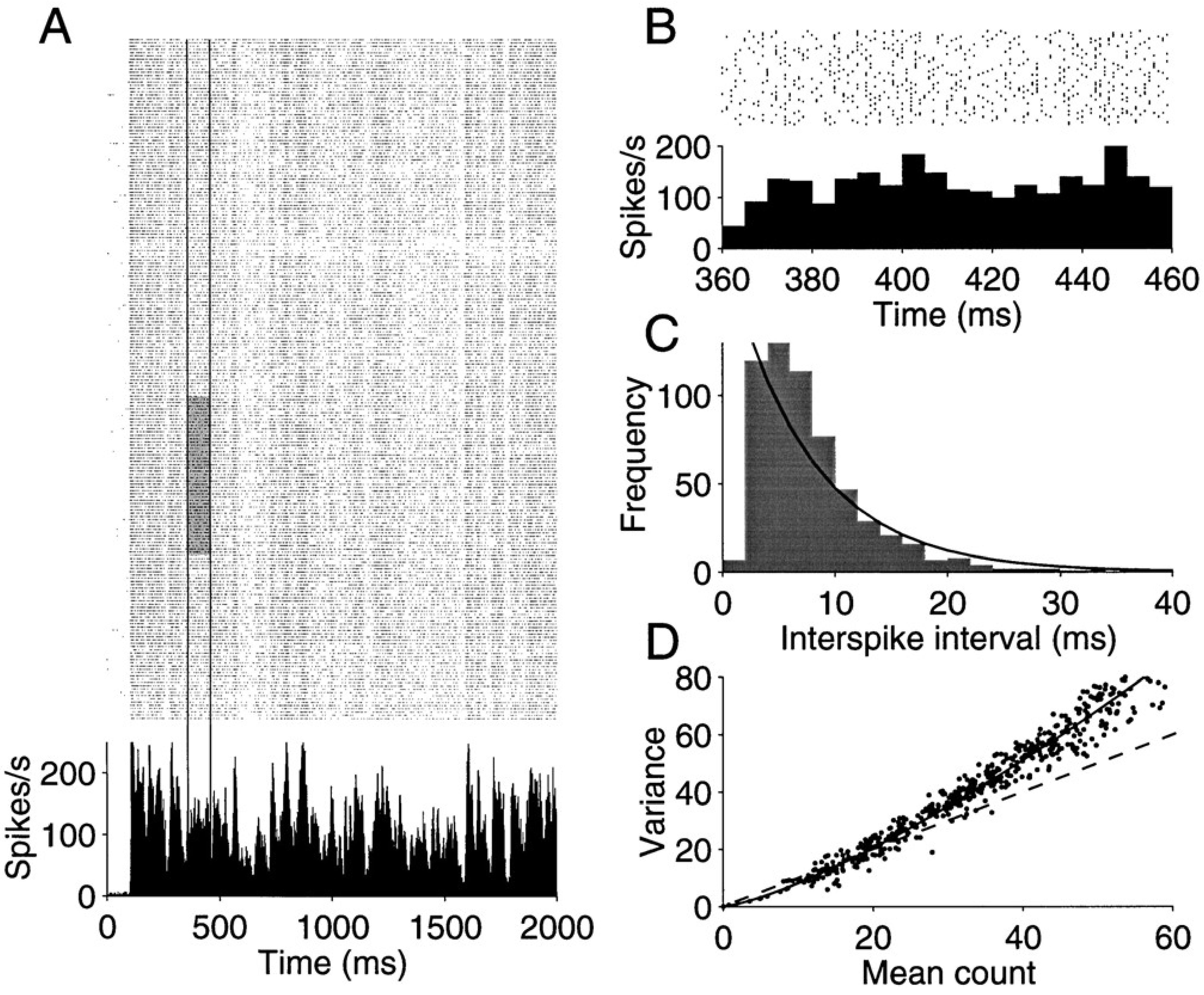
-Spike arrival from other neurons
-Beyond control of experimentalist

Variability in vitro



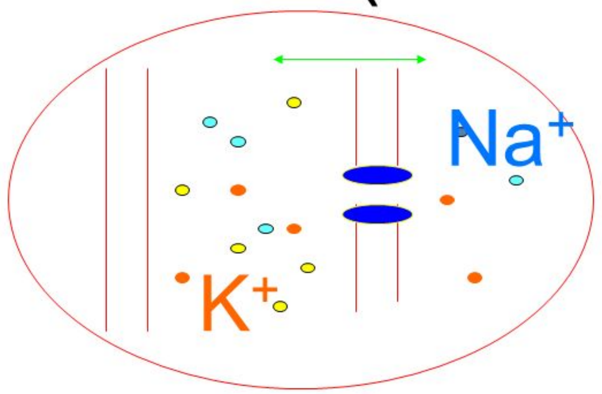
Mainen, Z., & Sejnowski, T. (1995). Reliability of spike timing in neocortical neurons. Science, 268(5216), 1503–1506. doi:10.1126/science.7770778

Variability in vivo



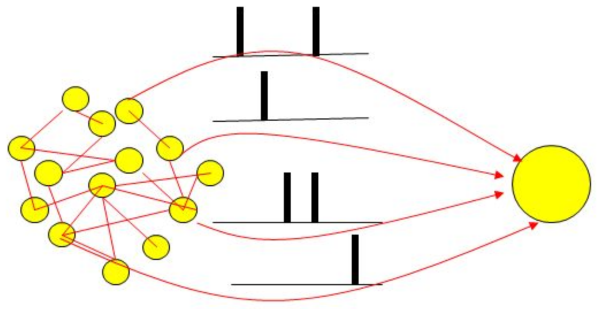
Source of variability

- Intrinsic noise (ion channels)



-Finite number of channels
-Finite temperature

-Network noise (background activity)



-Spike arrival from other neurons
-Beyond control of experimentalist

Spike train statistics

- Poisson model
- Membrane potential fluctuations
- Stochastic spikes

Poisson model

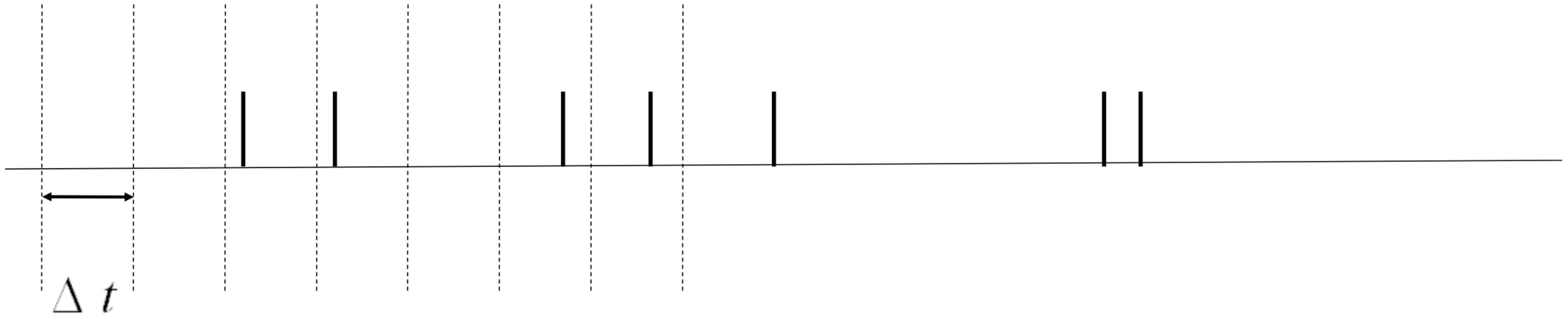
The Poisson process provides an extremely useful approximation of stochastic neuronal firing.

If the number of events per unit time:

- ρ is constant, then it's homogenous Poisson process (HPP)
- ρ changes over time, then it's non-homogenous Poisson process (NHPP)

Homogenous Poisson process (HPP)

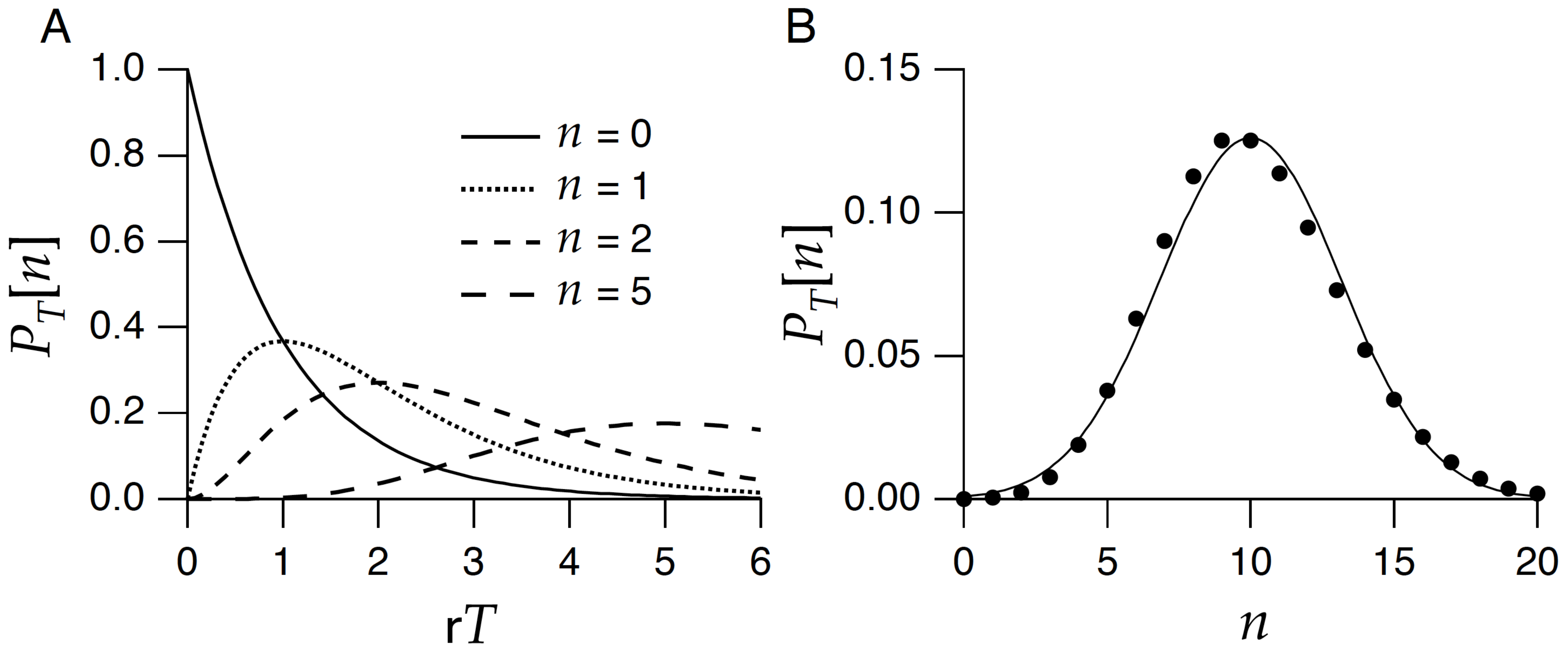
Rate is constant



Probability of firing: $P_F = \rho_0 \Delta t$

Survivor function: $\frac{d}{dt} S(t_1 | t_0) = -\rho_0 S(t_1 | t_0)$

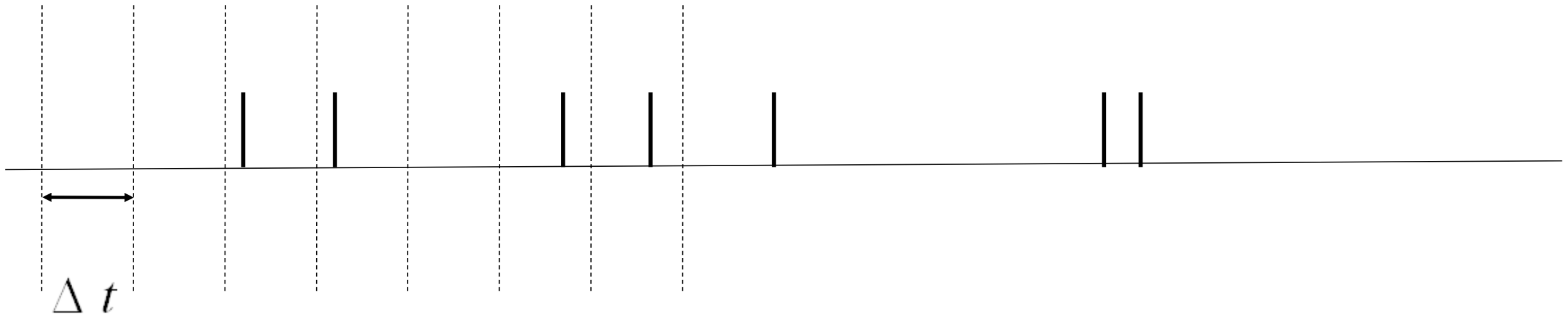
Homogenous Poisson process (HPP)



(A) The probability that a homogeneous Poisson process generates n spikes in a time period of duration T plotted for $n = 0, 1, 2,$ and 5. The probability is plotted as function of the rate times the duration of the interval, rT, to make the plot applicable for any rate. (B) The probability of finding n spikes during a time period for which r$T = 10$ (dots) compared with a Gaussian distribution with mean and variance equal to 10 (line).

Non-homogenous Poisson process (NHPP)

Rate changes

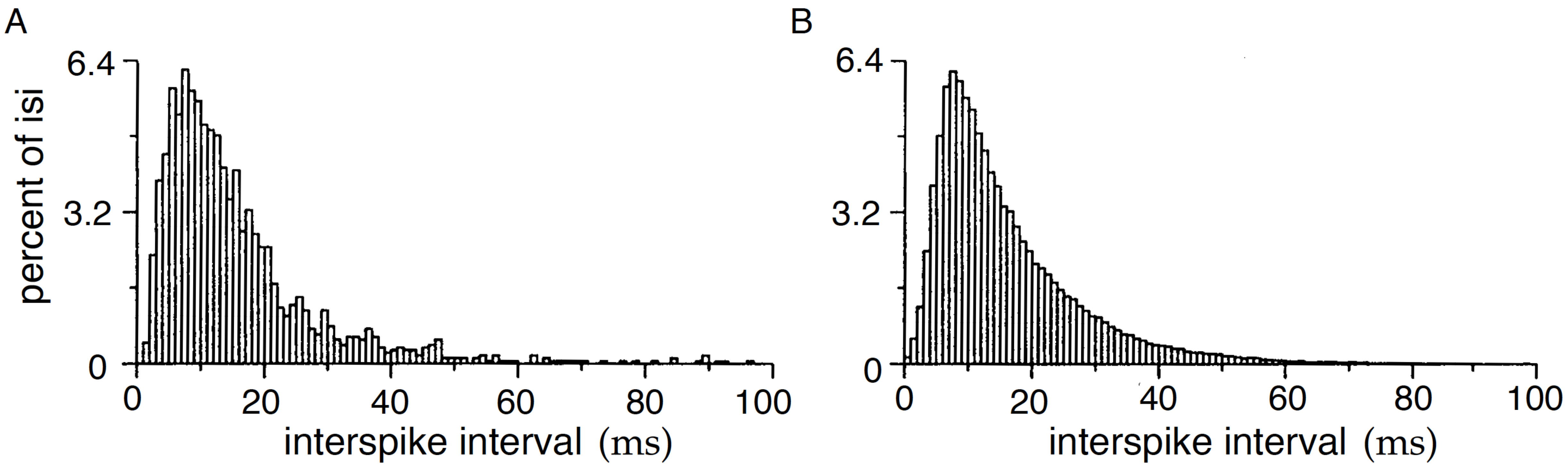


Probability of firing: $P_F = \rho(t)\Delta t$

Survivor function: $S(t|\hat{t}) = exp(-\int_{\hat{t}}^{t} \rho(t')dt')$

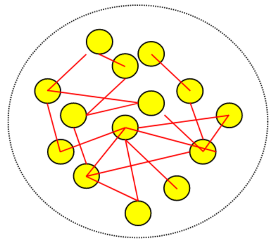
Interval distribution: $P(t|\hat{t}) = \rho(t)S(t|\hat{t})$

Comparison with data

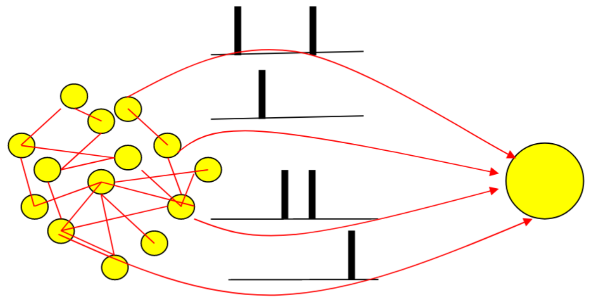


(A) Interspike interval distribution from an MT neuron responding to a moving, random-dot image. The probability of interspike intervals falling into the different bins, expressed as a percentage, is plotted against interspike interval. (B) Interspike interval histogram generated from a Poisson model with a stochastic refractory period. (Adapted from Bair et al., 1994.)

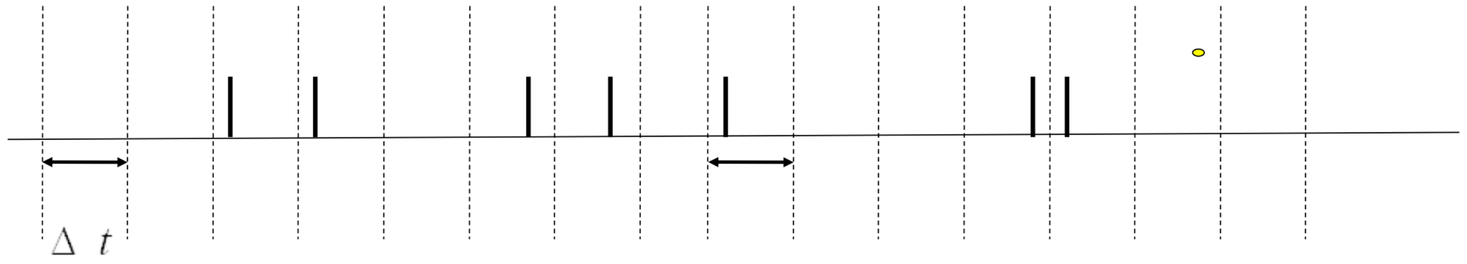
Stochastic spike arrival



Pull out one neuron



Total spike train of K presynaptic neurons



spike train

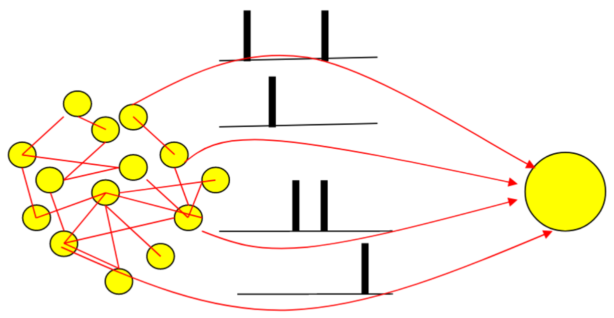
Probability of spike arrival:

$$P_F = K\rho_0 \,\Delta t$$

Take $\Delta t \to 0$ *expectation*

$$S(t) = \sum_{k=1}^{K} \sum_{f} \delta(t - t_k^f)$$

Membrane potential fluctuations



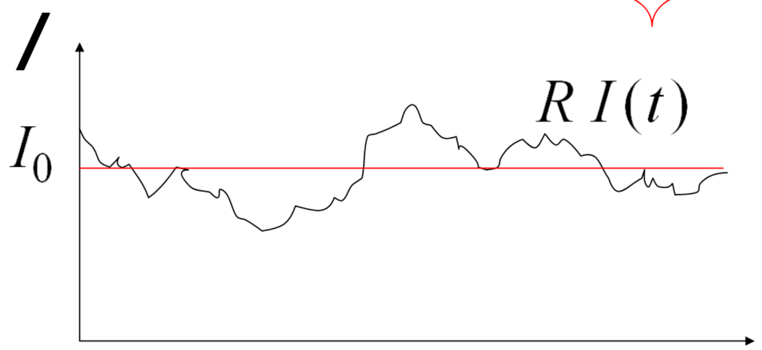
Synaptic current pulses of shape α

$$RI^{syn}(t) = \sum_k w_k \sum_f \alpha(t - t_k^f)$$

EPSC

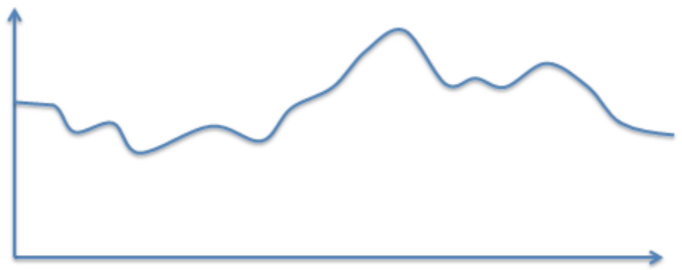
Passive membrane

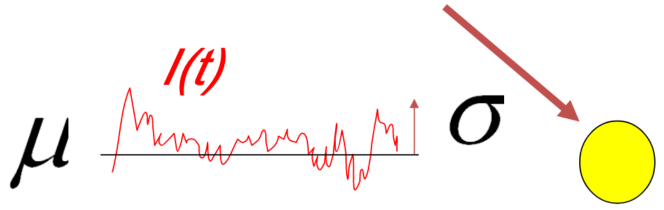
$$\tau \frac{d}{dt}u = -(u - u_{rest}) \quad + RI^{syn}(t)$$



$$I^{syn}(t) = I_0 + I^{fluct}(t)$$

→ Fluctuating potential

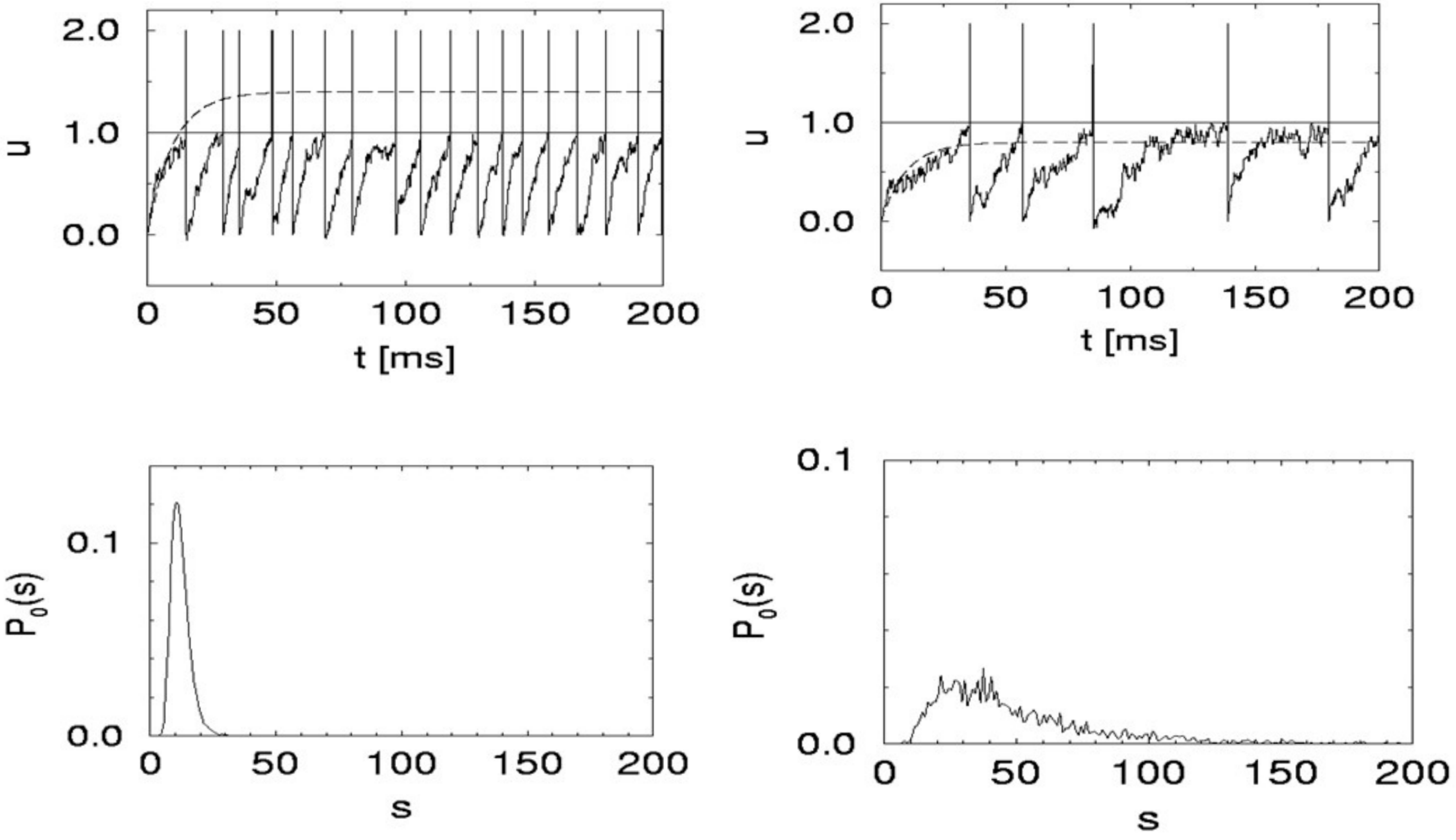




Fluctuating input current

Stochastic spikes in IF models

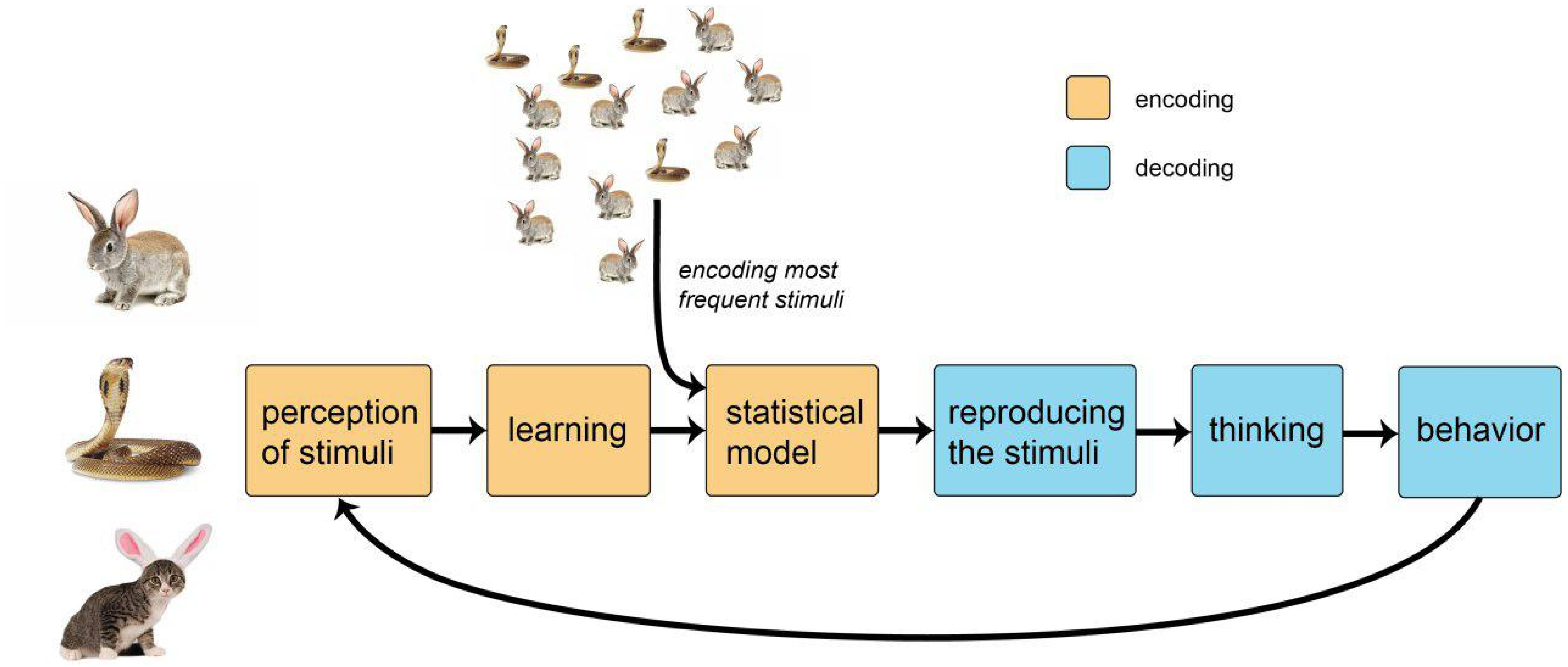
Superthreshold vs. Subthreshold regime



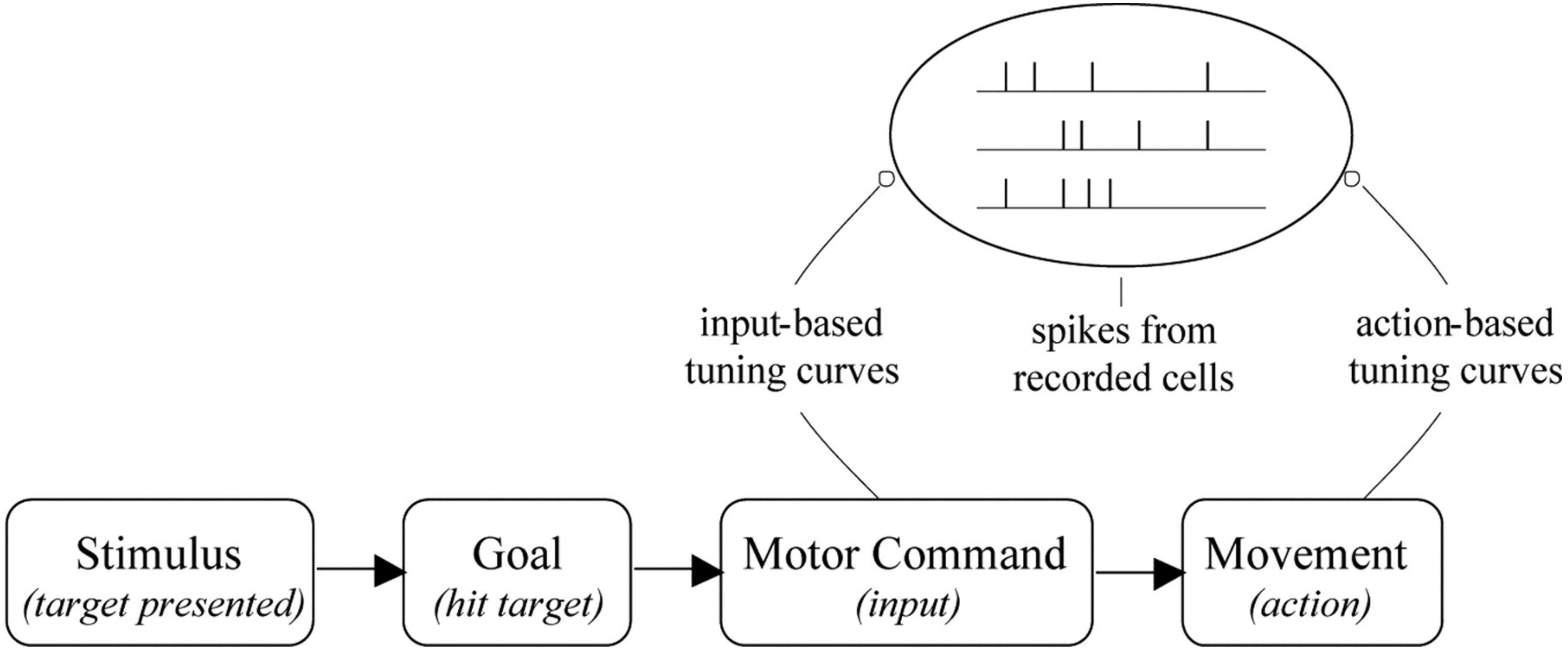
The neural code

- What is neural code?
- Encoding/decoding
- Types of neural code

Neural code


encoding
decoding
encoding most
frequent stimuli
perception
of stimuli
learning
statistical
model
reproducing
the stimuli
thinking
behavior

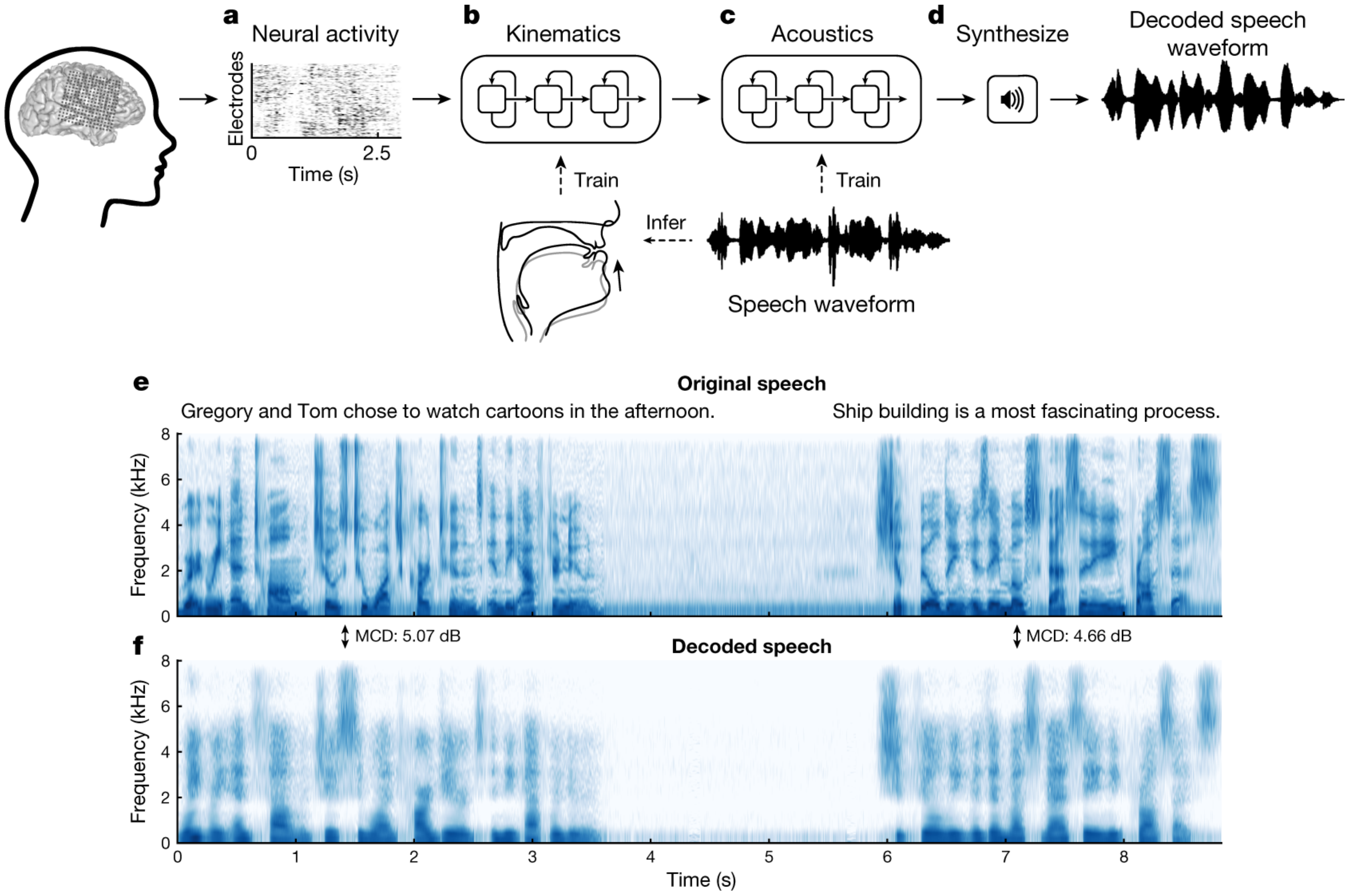
Encoding



input-based tuning curves
spikes from recorded cells
action-based tuning curves
Stimulus
(target presented)
Goal
(hit target)
Motor Command
(input)
Movement
(action)

Decoding

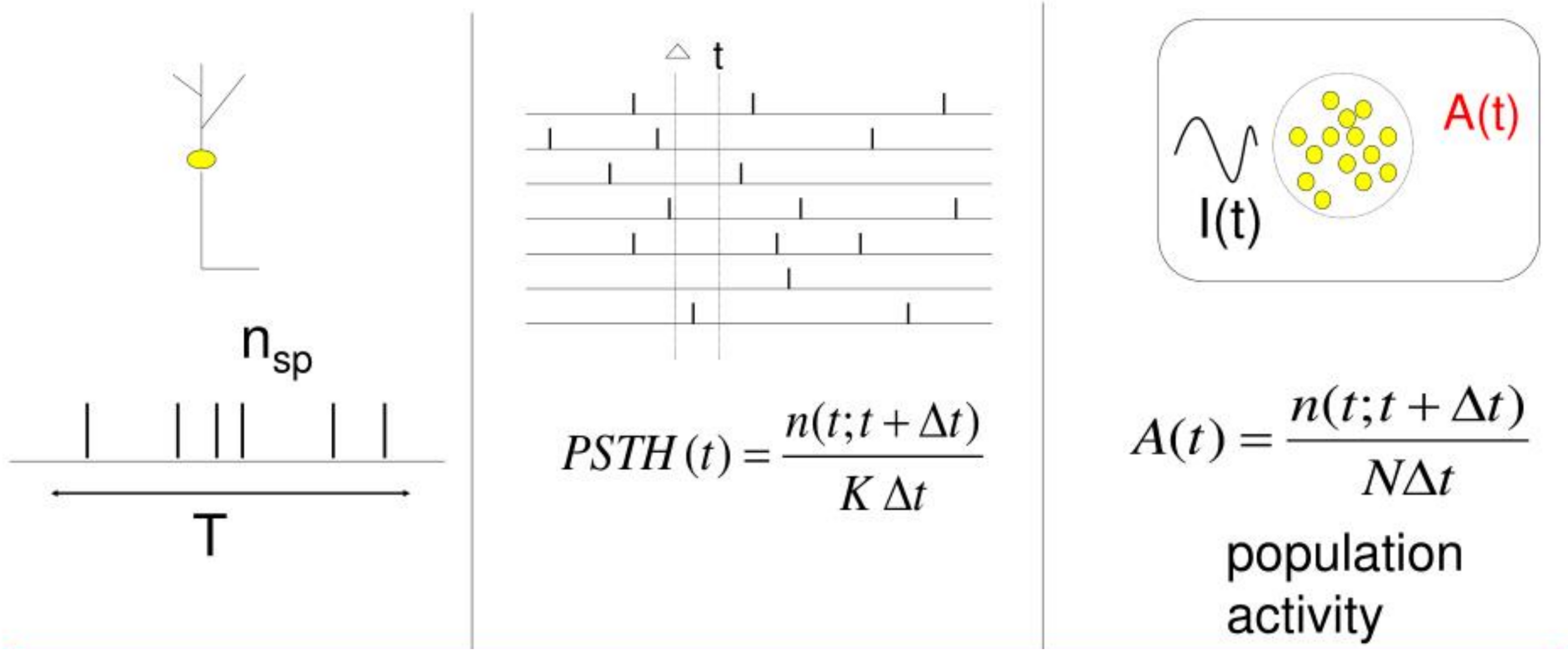
- Neural decoding is the process of taking statistical consistencies, a statistical model of the world, and reproducing the stimuli
- Maps to the process of thinking and acting, which in turn guide what stimuli we receive
- Completes the "*stimuli* $\longrightarrow$ *response* $\longrightarrow$ *behavior* $\longrightarrow$ *stimuli* $\longrightarrow$ *...*" loop


a
Neural activity
Electrodes
0
2.5
Time (s)
b
Kinematics
Train
c
Acoustics
Train
d
Synthesize
Decoded speech waveform
Infer
Speech waveform
e
Original speech
Gregory and Tom chose to watch cartoons in the afternoon.
Ship building is a most fascinating process.
Frequency (kHz)
MCD: 5.07 dB
MCD: 4.66 dB
f
Decoded speech
Frequency (kHz)
Time (s)

Neural coding scheme (hypothesized)

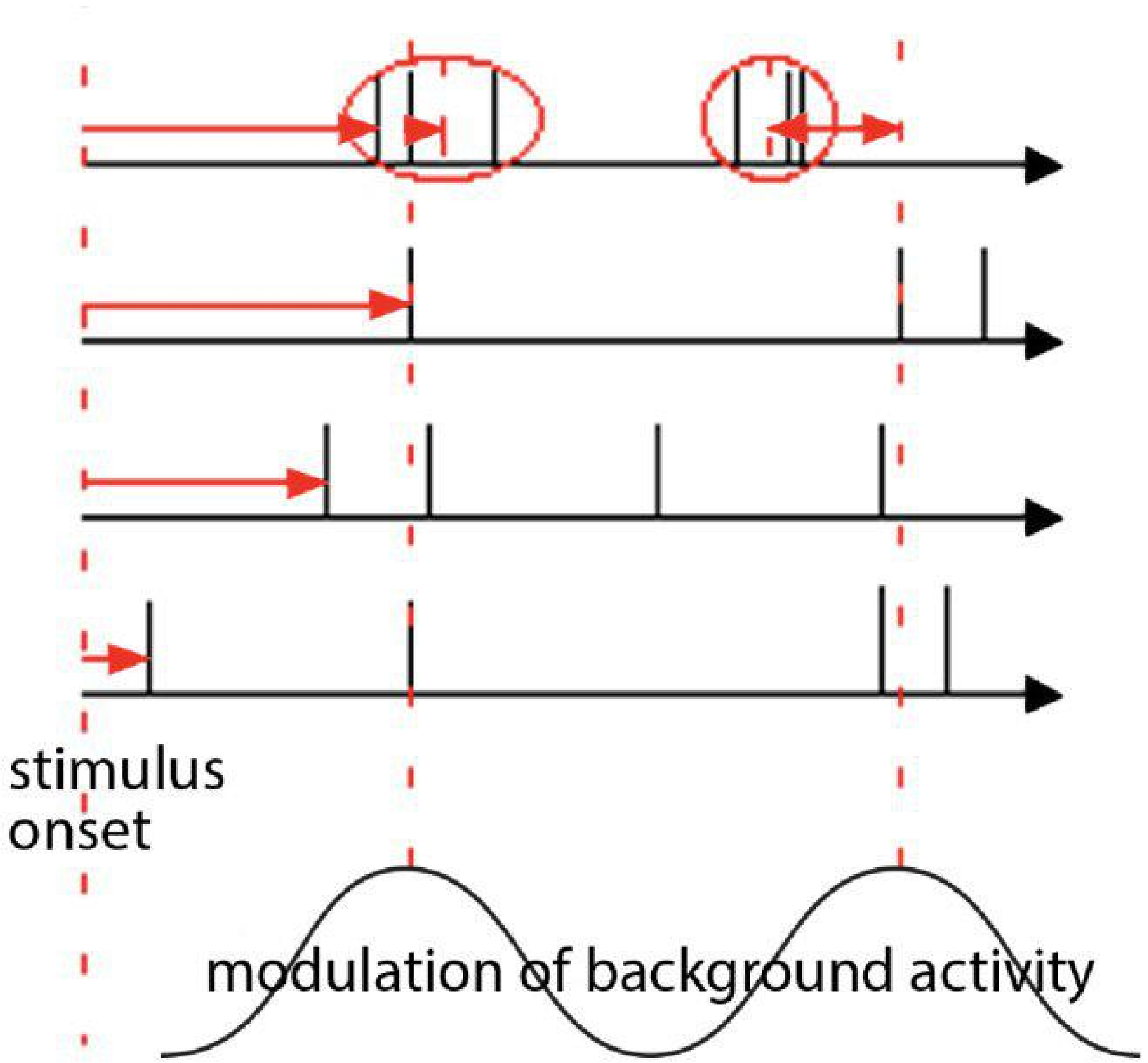
- **Rate** coding
- **Temporal** code
- **Population** code
- **Sparse** code

Rate coding



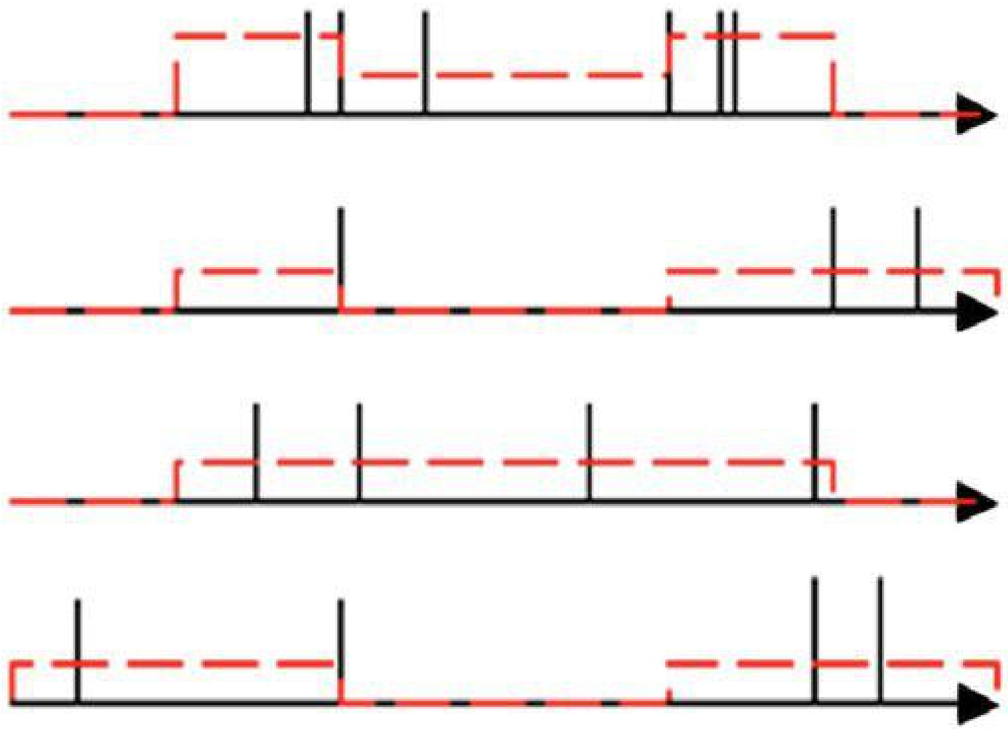
n_{sp}
T
Δ t
$PSTH(t) = \frac{n(t; t+\Delta t)}{K \, \Delta t}$
I(t)
A(t)
$A(t) = \frac{n(t; t+\Delta t)}{N \Delta t}$
population activity

Temporal coding



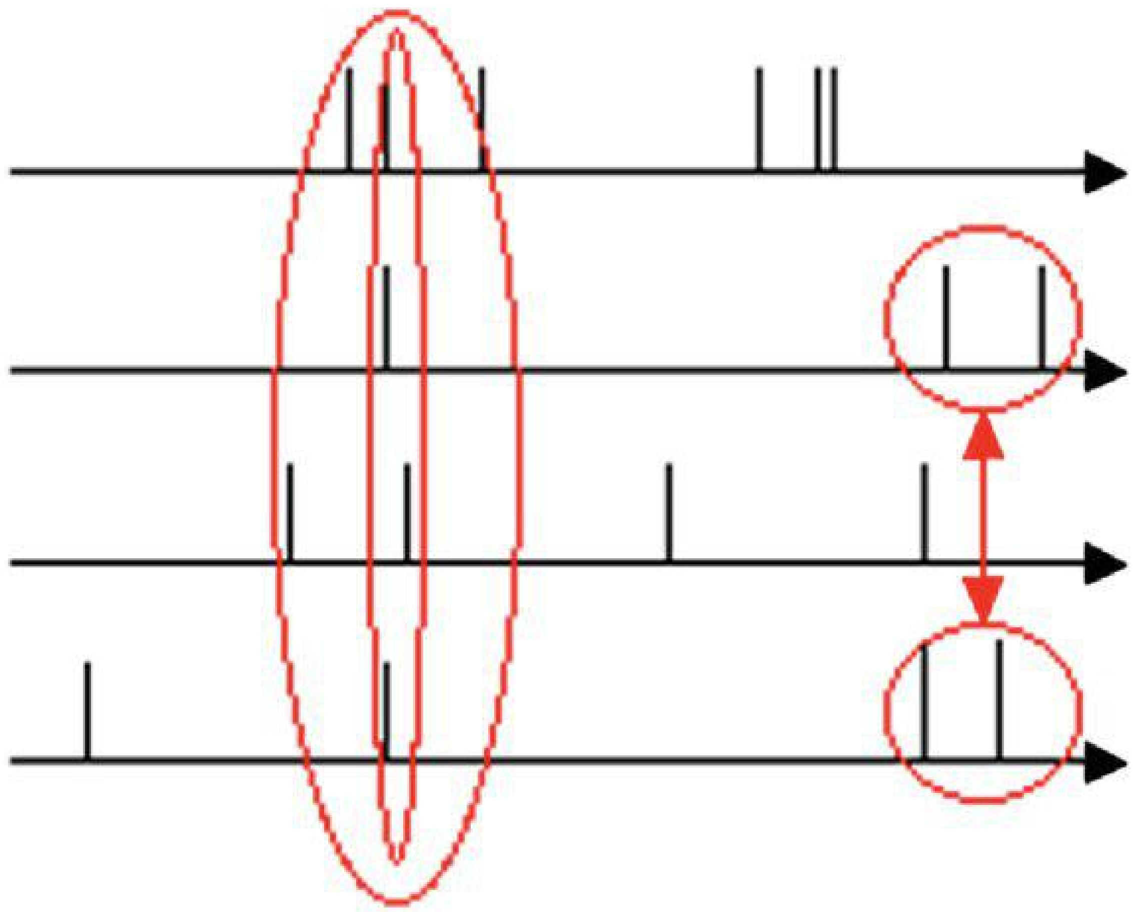
Patterns across time and space

Temporal coding



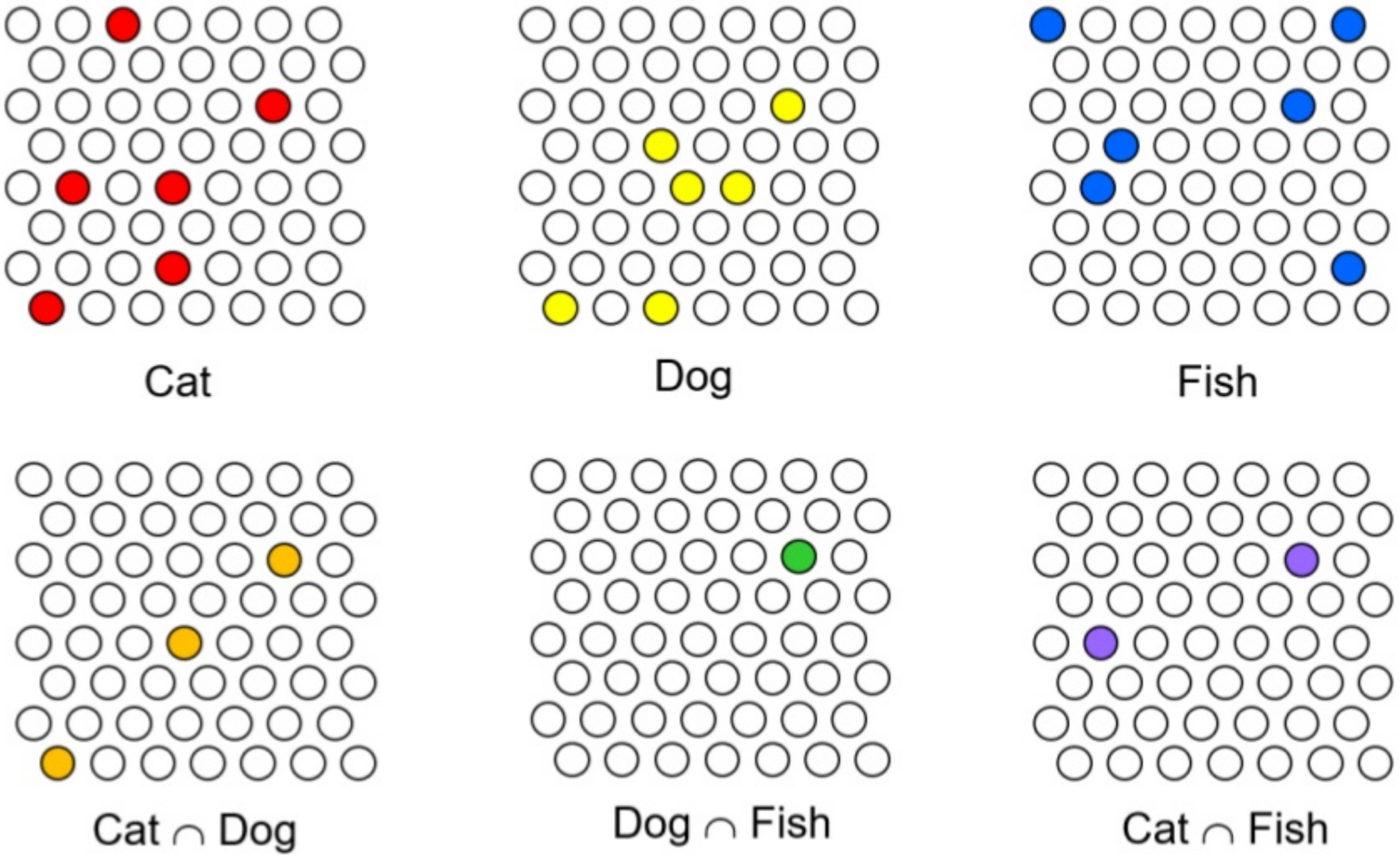
Temporal: no averaging over time
Rate: averaging over time (e.g. a few 100 ms)

Population coding



Population: averaging over space
Synchrony: patterns across space

Sparse coding



Hierarchical sparse distributed representations in VC