

1.2) Найти предел функции:

$$\lim_{x \rightarrow 7} \frac{x^2 - 49}{x^2 - 13x + 42} = (1)$$

$$\lim_{x \rightarrow 7} x^2 - 49 = (x^2 - 49)_{x=7} = 7^2 - 49 = 49 - 49 = 0$$

$$\lim_{x \rightarrow 7} x^2 - 13x + 42 = (x^2 - 13x + 42)_{x=7} =$$

$$= 7^2 - 13 \cdot 7 + 42 = 49 - 91 + 42 = 91 - 91 = 0$$

$$(1) = \left(\frac{0}{0} \right)$$

$$x^2 - 49 = x^2 - 7^2 = (x - 7)(x + 7)$$

$$x^2 - 13x + 42 = x^2 - 7x - 6x + 42 = x(x - 7) - 6(x - 7) = \\ = (x - 6)(x - 7)$$

$$\frac{x^2 - 49}{x^2 - 13x + 42} = \frac{(x - 7)(x + 7)}{(x - 6)(x - 7)} = \left\{ x - 7 \neq 0; x \neq 7 \right\} = \frac{x + 7}{x - 6}$$

$$(1) = \lim_{x \rightarrow 7} \frac{x + 7}{x - 6} = \left(\frac{x + 7}{x - 6} \right)_{x=7} = \frac{7 + 7}{7 - 6} = \frac{14}{1} = 14$$

Ответ:

$$\lim_{x \rightarrow 7} \frac{x^2 - 49}{x^2 - 13x + 42} = 14$$