

4.1) Привести к пределу по последовательности;

$$\lim_{h \rightarrow \infty} \frac{(23 - 2h^2)(3h^2 + 17)^2}{4h^6 + h - 1} = (1)$$

$$\begin{aligned} (23 - 2h^2)(3h^2 + 17)^2 &= h^2 \left(\frac{23}{h^2} - 2 \right) \left(h^2 \left(3 + \frac{17}{h^2} \right) \right)^2 = \\ &= h^2 \left(-2 + \frac{23}{h^2} \right) h^4 \left(3 + \frac{17}{h^2} \right)^2 = h^6 \left(-2 + \frac{23}{h^2} \right) \left(3 + \frac{17}{h^2} \right)^2 \\ 4h^6 + h - 1 &= h^6 \left(4 + \frac{h}{h^6} - \frac{1}{h^6} \right) = h^6 \left(4 + \frac{1}{h} - \frac{1}{h^6} \right) \end{aligned}$$

$$\begin{aligned} \frac{(23 - 2h^2)(3h^2 + 17)^2}{4h^6 + h - 1} &= \frac{h^6 \left(-2 + \frac{23}{h^2} \right) \left(3 + \frac{17}{h^2} \right)^2}{h^6 \left(4 + \frac{1}{h} - \frac{1}{h^6} \right)} = \\ &= \frac{\left(-2 + \frac{23}{h^2} \right) \left(3 + \frac{17}{h^2} \right)^2}{4 + \frac{1}{h} - \frac{1}{h^6}} \end{aligned}$$

$$(1) = \lim_{h \rightarrow \infty} \frac{\left(-2 + \frac{23}{h^2} \right) \left(3 + \frac{17}{h^2} \right)^2}{4 + \frac{1}{h} - \frac{1}{h^6}} =$$

$$\begin{aligned} &= \frac{\left(-2 + 23 \lim_{h \rightarrow \infty} \frac{1}{h^2} \right) \left(3 + 17 \lim_{h \rightarrow \infty} \frac{1}{h^2} \right)^2}{4 + \lim_{h \rightarrow \infty} \frac{1}{h} - \lim_{h \rightarrow \infty} \frac{1}{h^6}} = \\ &= \frac{(-2 + 23 \cdot 0)(3 + 17 \cdot 0)^2}{4 + 0 - 0} = \frac{(-2)(3)^2}{4} = -\frac{9}{2} \end{aligned}$$

Ответ: $\lim_{h \rightarrow \infty} \frac{(23 - 2h^2)(3h^2 + 17)^2}{4h^6 + h - 1} = -\frac{9}{2}$