

U3 Remarque:

$$\begin{aligned} p &= 1 - \left[\binom{0}{7} \binom{2-0}{10-7} \binom{0}{9} \binom{2-0}{11-9} \right] \left[\binom{2}{10} \binom{2}{11} \right]^{-1} = \\ &= 1 - \left[\binom{0}{7} \binom{2}{3} \binom{0}{9} \binom{2}{2} \right] \left[\binom{2}{10} \binom{2}{11} \right]^{-1} = \\ &= 1 - \frac{\binom{2}{3} \binom{2}{2}}{\binom{2}{10} \binom{2}{11}} = (1) \end{aligned}$$

$$\frac{\binom{2}{3} \binom{2}{2}}{\binom{2}{10} \binom{2}{11}} = \frac{\binom{2}{3}}{\binom{2}{10}} \cdot \frac{\binom{2}{2}}{\binom{2}{11}} =$$

$$= \frac{A_3^2}{2!} \left(\frac{A_{10}^2}{2!} \right)^{-1} \frac{A_2^2}{2!} \left(\frac{A_{11}^2}{2!} \right)^{-1} = \frac{A_3^2}{A_{10}^2} \frac{A_2^2}{A_{11}^2} =$$

$$= \frac{3 \cdot 2}{10 \cdot 9} \cdot \frac{2 \cdot 1}{11 \cdot 10} = \left(\frac{3}{10} \cdot \frac{2}{9} \right) \cdot \left(\frac{2}{11} \cdot \frac{1}{10} \right) =$$

$$= \frac{2 \cdot 2 \cdot \cancel{3}}{\cancel{3} \cdot 10 \cdot 10 \cdot 11} = \frac{1}{3 \cdot 5 \cdot 5} = \frac{1}{3 \cdot 25} = \frac{1}{75}$$

$$(1) = 1 - \frac{1}{75} = \frac{75-1}{75} = \frac{74}{75}$$

Donc:

$$p = 1 - \frac{\binom{2}{3} \binom{2}{2}}{\binom{2}{10} \binom{2}{11}} = \frac{74}{75}$$