

$$\textcircled{3} \quad n=144, \quad p=\frac{1}{2}$$

$$k=70$$

Решение 1 (симметричное рассуждение):

$$n \in \mathbb{Z} \quad n \geq 0 \quad \Omega = \{(x_1, x_2, \dots, x_n) \mid \forall i=1, n \quad x_i \in \{1, 0\}\}$$

$$p \in \mathbb{R} \quad 0 \leq p \leq 1 \quad \forall i=1, n \quad p(x_i=1) = p$$

$$\Xi_n = \sum_{i=1}^n x_i$$

$$\Xi_n \sim \text{Bin}(n, p)$$

$$q=1-p$$

$$k \in \mathbb{Z} \quad 0 \leq k \leq n \quad p(\Xi_n=k) = f(k; n, p) = C_n^k p^k q^{n-k}$$

$$q=1-p=1-\frac{1}{2}=\frac{1}{2}=p$$

$$p(\Xi_n=k) = f(k; n, \frac{1}{2}) = C_n^k p^k p^{n-k} = C_n^k p^{k+(n-k)} = C_n^k p^n =$$

$$= C_n^k \left(\frac{1}{2}\right)^n = \frac{C_n^k}{2^n}$$

$$p(\Xi_n=70) = f(70; 144, \frac{1}{2}) = \frac{C_{144}^{70}}{2^{144}}$$

Решение 2:

$$p(\Xi_n=k) = \frac{C_n^k}{A_2^n} = \frac{C_n^k}{2^n}$$

$$p(\Xi_n=70) = \frac{C_{144}^{70}}{2^{144}}$$

Ответ:

$$\Xi_n \sim \text{Bin}(n, p) \quad p(\Xi_n=70) = \frac{C_{144}^{70}}{2^{144}}$$