PFNET Python Documentation

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CONTENTS

1	Getti		3
	1.1		3
	1.2		3
	1.3		3
	1.4	Example	4
2	Powe	er Networks	5
	2.1		5
	2.2		5
	2.3		5
	2.4		8
	2.5	1	9
	2.6	Projections	
	2.0		-
3	Data	Parsers 13	3
	3.1	MATPOWER case files	_
	3.2	ARTERE case files	
	3.3	RAW case files	3
4	Visua	alization 15	5
	4.1	Overview	
_	O-4:	mization Problems	_
5	_	mization Problems 17 Objective Function 17	
	5.1 5.2	Constraints	
	5.3		
	3.3	Problems	3
6	API	Reference 22	7
	6.1	Vector	7
	6.2	Matrix	7
	6.3	Bus	7
	6.4	Branch	2
	6.5	Generator	4
	6.6	Shunt	6
	6.7	Load	8
	6.8	Variable Generator	8
	6.9	Network	9
	6.10	Graph	7
	6.11	Function	7
	(10	Character int	റ
	6.12	Constraint	7
	6.12	Optimization Problem	

	6.14 References	53
7	Indices and tables	55
Bi	bliography	57
Ру	thon Module Index	59
Ру	thon Module Index	61
In	dex	63

Welcome! This is the documentation for the Python wrapper of PFNET, last updated March 06, 2016.

What is PFNET?

PFNET is a library for modeling and analyzing electric power networks. It provides data parsers, network visualization routines, and fast and customizable constraint and objective function evaluators for modeling network optimization problems.

License

PFNET is released under the BSD 2-clause license.

Citing

If you use PFNET in your work, please cite the software as follows:

```
@misc{pfnet,
   author={Tinoco De Rubira, Tomas},
   title={{PFNET}: A library for modeling and analyzing electric power networks},
   howpublished={\url{https://github.com/ttinoco/PFNET}},
   month={July},
   year={2015}
}
```

Contact

If you have any questions about PFNET or if you are interested in collaborating, send me an email:

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Documentation Contents

CONTENTS 1

2 CONTENTS

ONE

GETTING STARTED

This section describes how to get started with PFNET in Python. In particular, it covers required packages, installation, and provides a quick example showing how to use this package.

1.1 Dependencies

PFNET for Python has the following dependencies:

- Numpy (>=1.8.2): the fundamental package for scientific computing in Python.
- Scipy (>=0.13.3): a collection of mathematical algorithms and functions built on top of Numpy.
- PFNET: underlying C routines wrapped by this package (libpfnet).
- Graphviz (>= 2.38): graph visualization library (libgvc) (Optional).
- Raw parser (>=1.0): library for parsing power flow files in PSSE raw format version 32 (libraw_parser) (Optional).

1.2 Download

The latest version of PFNET can be downloaded from https://github.com/ttinoco/PFNET.

1.3 Installation

After building the C library libpfnet, the PFNET Python module can be installed using:

```
> sudo python setup.py install
```

from the python directory of the PFNET package.

If libpfnet was built without visualization capabilities, the argument --no_graphviz should be passed to setup.py. Similarly, if libpfnet was build without raw parsing capabilities, the argument --no_raw_parser should be passed to setup.py.

The installation can be tested using nose as follows:

> nosetests -v

1.4 Example

As a quick example of how to use the PFNET Python module, consider the task of constructing a power network from a MATPOWER-converted power flow file and computing the average bus degree. This can be done as follows:

```
>>> import numpy as np
>>> from pfnet import Network

>>> net = Network()
>>> net.load('ieee14.mat')

>>> print np.average([b.degree for b in net.buses])
2.86
```

TWO

POWER NETWORKS

This section describes how to load and analyze power networks using PFNET.

2.1 Overview

Power networks in PFNET are represented by objects of type *Network*. These objects are initially empty and need to be loaded with data contained in specific types of files. Once the data is loaded, the network and its components can be analyzed, visualized, and used to construct network optimization problems. After a network optimization problem is solved, the network object can be updated with the solution to perform further analysis.

An important attribute of the *Network* class is *base_power*. This quantity, which has units of MVA, is useful for converting power quantities in per unit system base power to MW or MVAr.

2.2 Loading Data

Power networks can be loaded with data using the <code>load()</code> class method. This method takes as input the filename of a supported power flow file. Information about the data parsers available in PFNET and the supported file formats can be found in Section <code>Data Parsers</code>. The following simple example shows how to load data from a power flow <code>mat file</code>:

```
>>> from pfnet import Network
>>> net = Network()
>>> print net.num_buses
0
>>> net.load('ieee14.mat')
>>> print net.num_buses
14
```

2.3 Components

Power networks have several components. These are *buses*, *branches*, *generators*, *shunt devices*, *loads*, and *variable generators* (*i.e.*, non-dispatchable). For obtaining an overview of the components that form a network, the class method <code>show_components()</code> can be used:

```
>>> net.show_components()

Network Components
------
```

```
buses
               : 14
 slack
               : 1
               : 5
 reg by gen
 reg by tran
               : 0
 reg by shunt
               : 0
shunts
 fixed
 switched v
              : 0
branches
              : 20
              : 17
 lines
 fixed trans : 3
 phase shifters : 0
 tap changers v : 0
 tap changers Q: 0
generators : 5
               : 1
 slack
               : 5
 req
loads
               : 11
vargens
```

2.3.1 Buses

Buses in a power network are objects of type <code>Bus</code>. Each bus has an <code>index</code>, a <code>number</code>, and a <code>name</code> attribute that can be used to identify this bus in a network. The <code>index</code> is associated with the location of the bus in the underlying C array of bus structures, while the <code>number</code> and <code>name</code> attributes are specified in the input data. An <code>index</code>, a <code>number</code>, or a <code>name</code> can be used to extract a specific bus from a network using the <code>Network</code> class methods <code>get_bus()</code>, <code>get_bus_by_number()</code>, and <code>get_bus_by_name()</code>, respectively:

```
>>> bus = net.get_bus(10)
>>> print bus.index == 10
True
>>> other_bus = net.get_bus_by_number(bus.number)
>>> print bus == other_bus
True
```

For convenience, a list of all the buses in the network is contained in the buses attribute of the Network class.

Buses in a network can have different properties. For example, some buses can be slack buses and others can have their voltage magnitudes regulated by generators, tap-changing transformers, or switched shunt devices. The Bus class provides methods for checking whether a bus has specific properties. The following example shows how to get a list of all the buses whose voltage magnitudes are regulated by generators:

```
>>> reg_buses = [b for b in net.buses if b.is_regulated_by_gen()]
>>> print len(reg_buses), net.get_num_buses_reg_by_gen()
5 5
```

A bus also has information about the devices that are connected to it or that are regulating its voltage magnitude. For example, the attributes *gens* and *reg_trans* contain a list of generators connected to the bus and a list of tap-changing transformers regulating its voltage magnitude, respectively.

2.3.2 Branches

Branches in a power network are objects of type *Branch* and are represented mathematically by the model described in Section 2.1.2 of [TTR2015]. Each branch has an *index* attribute that can be used to identify this branch in a network. The Network class method get_branch() can be used to extract a branch of a given index:

```
>>> branch = net.get_branch(5)

>>> print branch.index == 5
True
```

For convenience, a list of all the branches in the network is contained in the branches attribute of the Network class.

Branches in a power network can have different properties. Fore example, some branches can be transmission lines, fixed transformers, tap-changing transformers, or phase-shifting transformers. Tap-changing transformers in turn can control the reactive power flowing through the branch or the voltage magnitude of a bus. The *Branch* class provides methods for checking whether a branch has specific properties. The following example shows how to get a list of all the branches that are transmission lines:

```
>>> lines = [br for br in net.branches if br.is_line()]
>>> print len(lines), net.get_num_lines()
17 17
```

For branches that are transformers, the Branch class attributes ratio and phase correspond to the transformer's tap ratio and phase shift, respectively. These attributes correspond to the quantities a_{km} and ϕ_{km} of the branch model described in Section 2.1.2 of [TTR2015]. The quantity a_{mk} in this model is always one.

2.3.3 Generators

Generators in a power network are objects of type <code>Generator</code>. Each generator has an <code>index</code> attribute that can be used to identify this generator in a network. The <code>Network</code> class method <code>get_gen()</code> can be used to extract a generator of a given <code>index</code>:

```
>>> gen = net.get_gen(2)
>>> print gen.index == 2
True
```

For convenience, a list of all the generators in the network is contained in the *generators* attribute of the *Network* class.

Generators in a power network can have different properties. Fore example, some generators can be slack generators and others can provide bus voltage magnitude regulation. The *Generator* class provides methods for checking whether a generator has specific properties. The following example shows how to get a list of all the slack generators:

```
>>> slack_gens = [g for g in net.generators if g.is_slack()]
>>> print len(slack_gens), net.get_num_slack_gens()
1 1
```

The active and reactive powers that a generator injects into the bus to which it is connected are obtained from the *P* and *Q* attributes of the *Generator* class. These quantities are given in units of per unit *system base power*. The following example computes the total active power injected into the network by generators in units of MW:

```
>>> print sum([g.P for g in net.generators])*net.base_power 272.4
```

2.3. Components 7

2.3.4 Shunt Devices

Shunt devices in a power network are objects of type Shunt. Each shunt has an index attribute that can be used to identify this shunt in a network. The Network class method get_shunt() can be used to extract a shunt of a given index:

```
>>> shunt = net.get_shunt(0)
>>> print shunt.index == 0
True
```

For convenience, a list of all the shunt devices in the network is contained in the *shunts* attribute of the *Network* class

As other network components, shunt devices can have different properties. Some shunt devices can be fixed while others can be switchable and configured to regulate a bus voltage magnitude.

2.3.5 Loads

Loads in a power network are objects of type Load. As other components, the index attribute is used to identify a load in the network. A list of all the loads in the network is contained in the loads attribute of the Network class.

Similar to generators, the active and reactive powers that a load consumes from the bus to which it is connected are obtained from the *P* and *Q* attributes of the *Load* class. They are also given in units of per unit *system* base power.

2.3.6 Variable Generators

Variable generators in a power network are objects of type <code>VarGenerator</code>. They represent non-dispatchable energy sources such as wind generators or farms and photovoltaic power plants. As with other components, the <code>index</code> attribute is used to identify a variable generator in the network. In addition to the <code>index</code> attribute, a <code>name</code> attribute is also available, which can be used to extract a specific variable generator from the network using the <code>Network</code> class method <code>get_vargen_by_name()</code>. A list of all the variable generators in the network is also contained in the <code>var_generators</code> attribute of the <code>Network</code> class.

Similar to generators, the active and reactive powers produced by a variable generator are obtained from the P and Q attributes of the VarGenerator class in units of per unit $system\ base\ power$. This is the output of the device in the absence of uncertainty. When there is uncertainty, the output of the device is subject to variations about P that have a standard deviation given by the attribute P_std . Output limits of a variable generator are given by the P_min , P_max , Q_min , and Q_max attributes.

The output of variable generators in a network are subject to random variations that can be correlated, especially for devices that are "nearby". The method <code>create_vargen_P_sigma()</code> of the <code>Network</code> class allows constructing a covariance matrix for these variations based on a "correlation distance" N and a given correlation coefficient. The cross-covariance between the variation of two devices that are connected to buses that are less than N branches away from each other are set such that they have the given correlation coefficient.

Lastly, since many power network input files do not have variable generator information, these devices can be added to the network by using the <code>add_vargens()</code> method of the <code>Network</code> class.

2.4 Properties

A *Network* object has several quantities or properties that provide important information about the state of the network. The following table provides a description of each of these properties.

Names	Description	Units
bus_v_max		
bus_v_min		
bus_v_vio	Maximum bus voltage magnitude limit violation	per unit
bus_P_mis	Maximum absolute bus active power mismatch	MW
bus_Q_mis	Maximum absolute bus reactive power mismatch	MVAr
gen_P_cost	Total active power generation cost	
gen_v_dev	Maximum set point deviation of generator-regulated voltage	per unit
gen_Q_vio	Maximum generator reactive power limit violation	MVAr
gen_P_vio	Maximum band violation of transformer-regulated voltage Maximum tap ratio limit violation of tap-changing transformer Maximum phase shift limit violation of phase-shifting transformer Maximum band violation of shunt-regulated voltage Shunt_b_vio Maximum susceptance limit violation of switched shunt device	
tran_v_vio		
tran_r_vio		
tran_p_vio		
shunt_v_vio		
shunt_b_vio		
num_actions		

All of these properties are attributes of the *Network* class. If there is a change in the network, the class method *update_properties()* needs to be called in order for the network properties to reflect the change. The following example shows how to update and extract properties:

```
>>> print net.bus_v_max
1.09
>>> for bus in net.buses:
... bus.v_mag = bus.v_mag + 0.1
...
>>> print net.bus_v_max
1.09
>>> net.update_properties()
>>> print net.bus_v_max
1.19
```

For convenience, all the network properties can be extracted at once in a dictionary using the <code>get_properties()</code> class method:

```
>>> properties = net.get_properties()
>>> print properties['bus_v_max']
1.19
```

2.5 Variables

Network quantities can be specified to be variables. This is useful to represent network quantities with vectors and turn the network properties described above as functions of these vectors.

To set network quantities as variables, the <code>Network</code> class method <code>set_flags()</code> is used. This method takes as arguments a <code>component type</code>, a <code>flag mask</code> for specifying which flags types to set, a <code>property mask</code> for targeting components with specific properties, and a <code>variable mask</code> for specifying which component quantities should be affected.

Property masks are component-specific. They can be combined using logical OR to make properties more complex. More information can be found in the following sections:

2.5. Variables 9

- Bus Property Masks
- Branch Property Masks
- Generator Property Masks
- Shunt Property Masks
- Variable Generator Property Masks

Variable masks are also component-specific. They can be combined using logical OR to target more than one component quantity. More information can be found in the following sections:

- Bus Variable Masks
- Branch Variable Masks
- Generator Variable Masks
- Shunt Variable Masks
- Variable Generator Variable Masks

The following example shows how to set as variables all the voltage magnitudes and angles of buses regulated by generators:

Network components have a has_flags() method that allows checking whether flags of a certain type associated with specific quantities are set.

Once variables have been set, the *vector* containing all the current variable values can be extracted using <code>get_var_values()</code>:

```
>>> values = net.get_var_values()
>>> print type(values)
<type 'numpy.ndarray'>
>>> print values.shape
(10,)
```

The components that have quantities set as variables have indices that can be used to locate these quantities in the vector of all variable values:

```
>>> bus = [b for b in net.buses if b.is_reg_by_gen()][0]
>>> print bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VMAG)
True
```

```
>>> bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VANG)
True
>>> print bus.v_mag, net.get_var_values()[bus.index_v_mag]
1.09 1.09
>>> print bus.v_ang, net.get_var_values()[bus.index_v_ang]
-0.23 -0.23
```

A vector of variable values can be used to update the corresponding network quantities. This is done with the <code>Network</code> class method <code>set_var_values()</code>:

```
>>> bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VANG)
True
>>> values = net.get_var_values()
>>> print bus.v_mag
1.09
>>> values[bus.index_v_mag] = 1.20
>>> net.set_var_values(values)
>>> print bus.v_mag
1.20
```

As we will see in later, variables are also useful for constructing network optimization problems.

The class method get_var_values() can also be used to get upper or lower limits of the variables. To do this, a valid *variable value code* must be passed to this method.

In addition to the class method <code>set_flags()</code>, which allows specifying variables of components having certain properties, one can also use the <code>Network</code> class method <code>set_flags_of_component()</code> to specify variables of individual components. This is useful when the desired components cannot be targeted using a <code>property mask</code>. For example, the following code illustrates how to set as variables the voltage magnitudes of buses whose indices are multiples of three:

```
>>> net.clear_flags()
>>> for bus in net.buses:
...     if bus.index % 3 == 0:
...         net.set_flags_of_component(bus,pf.FLAG_VARS,pf.BUS_VAR_VMAG)
>>> print net.num_vars, len([b for b in net.buses if b.index % 3 == 0]), net.num_buses
5 5 14
```

2.6 Projections

As explained above, once the network variables have been set, a vector with the current values of the selected variables is obtained with the class method <code>get_var_values()</code>. To extract subvectors that contain values of specific variables, projection matrices can be used. These <code>matrices</code> can be obtained using the class method <code>get_var_projection()</code>, which take as arguments a <code>component type</code> and a <code>variable mask</code>, <code>e.g.</code>, <code>bus variable masks</code>. The next example sets the variables of the network to be the bus voltage magnitudes and angles of all the buses, extracts the vector of values of all variables, and then extracts two subvectors having only voltage magnitudes and only voltage angles, respectively:

2.6. Projections 11

```
>>> import numpy as np
>>> import pfnet as pf
>>> net = pf.Network()
>>> net.load('ieee14.mat')
>>> net.set_flags(pf.OBJ_BUS,
                 pf.FLAG_VARS,
                  pf.BUS_PROP_ANY,
                  pf.BUS_VAR_VMAG|pf.BUS_VAR_VANG)
. . .
>>> print net.num_vars, 2*net.num_buses
28 28
>>> P1 = net.get_var_projection(pf.OBJ_BUS,pf.BUS_VAR_VMAG)
>>> P2 = net.get_var_projection(pf.OBJ_BUS,pf.BUS_VAR_VANG)
>>> print type(P1)
<class 'scipy.sparse.coo.coo_matrix'>
>>> x = net.get_var_values()
\rightarrow > v_mags = P1*x
>>> v_angs = P2*x
>>> print v_mags
[ 1.036    1.05    1.055    1.057    1.051    1.056    1.09    1.062    1.07    1.02
 1.019 1.01 1.045 1.06]
>>> print v_angs
 [-0.27995081 \ -0.26459191 \ -0.26302112 \ -0.2581342 \ -0.26354472 \ -0.26075219 ] 
-0.23317599 \ -0.23335052 \ -0.24818582 \ -0.15323991 \ -0.18029251 \ -0.22200588
-0.0869174 0.]
>>> print np.linalg.norm(x - (P1.T*v_mags+P2.T*v_angs))
0.0
```

THREE

DATA PARSERS

This section describes the different data parsers available in PFNET and the supported file types.

3.1 MATPOWER case files

MATPOWER is a MATLAB package for solving power flow and optimal power flow problems. It contains several power flow and optimal power flow cases defined in MATLAB files. These "M" files can be converted to CSV files using the script mpc2mat.m. These MATPOWER-converted CSV files have extension.mat and can be used to load power networks in PFNET.

3.2 ARTERE case files

PFNET can load networks from case files used by ARTERE, which is a software for performing power flow computations using the Newton-Raphson method. These files should have extension .art. Details about these data files can be found in the document "ARTERE: description of data files".

Currently, PFNET has limited support of these files. More specifically:

- Components with open breakers are ignored.
- For LTC-V devices, tap positions are treated as continuous and the optional fields are ignored.
- The SWITCH, TRFO, PSHIFT-P, TURLIM, SVC, LFRESV, BUSPART and BRAPART records are not supported.
- Computation control parameters are ignored.

3.3 RAW case files

If built with raw parsing capabilities, which requires linking PFNET with <code>libraw_parser</code>, PFNET can load power networks from files with extension <code>.raw</code>. These files are used by the software PSS ® E and are widely used by North American power system operators.

FOUR

VISUALIZATION

This section describes how to visualize power networks using PFNET. To have this capability, PFNET needs the Graphviz library libgue.

4.1 Overview

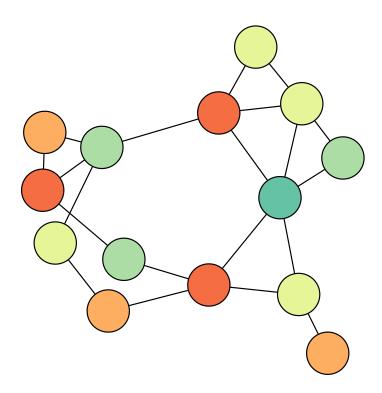
To visualize a power network, a *Graph* objects needs to be created. To do this, one needs to specify the power *Network* that is to be associated with the graph:

```
>>> import pfnet as pf
>>> net = pf.Network()
>>> net.load('ieee14.mat')
>>> g = pf.Graph(net)
```

Then, a layout must be created for graph. This can be done using the *Graph* class method *set_layout*. This method uses the sfdp algorithm of Graphviz.

The *Graph* class provides routines for coloring nodes (network buses) according to different criteria. For example, buses can be colored according to reactive power mismatches:

```
>>> g.set_layout()
>>> g.color_nodes_by_mismatch(pf.BUS_MIS_REACTIVE)
>>> g.view()
```



FIVE

OPTIMIZATION PROBLEMS

This section describes how to formulate power network optimization problems using PFNET.

5.1 Objective Function

The objective function ϕ for a network optimization problem created using PFNET is of the form

$$\varphi(x) = \sum_{i} w_i \varphi_i(x),$$

where w_i are weights, φ_i are general linear or nonlinear functions, and x is a vector of values of network quantities that have been set as variables. Each weight-function pair in the summation is represented by an object of type Function. To instantiate an object of this type, the function type and weight need to be specified as well as the Network object that is to be associated with the function. The following example sets all bus voltage magnitudes as variables and constructs a function that penalizes voltage magnitude deviations from ideal values:

After a Function object is created, its value, gradient and Hessian are zero, an empty vector, and an empty matrix, respectively. Before evaluating the function at a specific vector of values, it must be analyzed using the Function class method analyze. This routine analyzes the function and allocated the required vectors and matrices for storing its gradient and Hessian. After this, the function can be evaluated using the method eval:

```
>>> x = net.get_var_values()
>>> func.analyze()
```

```
>>> func.eval(x + 0.01)
>>> func.eval(x)
```

The value $\varphi_i(x)$, gradient $\nabla \varphi_i(x)$ and Hessian $\nabla^2 \varphi_i(x)$ of a function can then be extracted from the *phi*, *gphi* and *Hphi* attributes, respectively:

```
>>> print x.shape
14
>>> print func.phi
0.255
>>> print type(func.gphi), func.gphi.shape
<type 'numpy.ndarray'> (14,)
>>> print type(func.Hphi), func.Hphi.shape
<class 'scipy.sparse.coo.coo_matrix'> (14, 14)
```

For the Hessian matrix, only the lower triangular part is stored.

Details about each of the different function types available in PFNET are provided below.

5.1.1 Voltage magnitude regularization

This function is of type FUNC_TYPE_REG_VMAG. It penalizes deviations of bus voltage magnitudes from ideal values. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_k \left(\frac{v_k - v_k^t}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left(\frac{v_k^y}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left(\frac{v_k^z}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left(\frac{v_k^h}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left(\frac{v_k^h}{\Delta v} \right)^2,$$

where v are bus voltage magnitudes, v^t are voltage magnitude set points (one for buses not regulated by generators), v^y and v^z are positive and negative deviations of v from v^t , v^h and v^l are voltage band upper and lower limit violations, and Δv is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.2 Voltage magnitude soft limit penalty

This function is of type FUNC_TYPE_SLIM_VMAG. It reduces voltage (soft) limit violations by penalizing deviations of bus voltage magnitudes from the mid point of their ranges. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left(\frac{v_k - \bar{v}_k}{\Delta v} \right)^2,$$

where v are bus voltage magnitudes, \bar{v} are the mid points of their ranges, and Δv is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.3 Voltage angle regularization

This function is of type FUNC_TYPE_REG_VANG. It penalizes large bus voltage angles and voltage angle differences across branches. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left(\frac{\theta_k}{\Delta \theta} \right)^2 + \frac{1}{2} \sum_{(k,m)} \left(\frac{\theta_k - \theta_m - \phi_{km}}{\Delta \theta} \right)^2,$$

where θ are bus voltage angles, ϕ are branch phase shifts, and $\Delta\theta$ is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.4 Generator powers regularization

This function is of type FUNC_TYPE_REG_PQ. It penalizes deviations of generator powers from the midpoint of their ranges. It is defined by the expression

$$varphi(x) := \frac{1}{2} \sum_{k} \left(\frac{P_k^g - \bar{P}_k}{\Delta P} \right)^2 + \frac{1}{2} \sum_{k} \left(\frac{Q_k^g - \bar{Q}_k}{\Delta Q} \right)^2,$$

where P^g and Q^g are generator active and reactive powers, \bar{P} and \bar{Q} are midpoints of generator active and reactive power ranges, and $\Delta P = \Delta Q$ are normalization factors. Only terms that include optimization variables are included in the summation.

5.1.5 Active power generation cost

This function is of type FUNC_TYPE_GEN_COST. It measures active power generation cost by the expression

$$\varphi(x) := \sum_{k} q_{k0} + q_{k1} P_k^g + q_{k2} (P_k^g)^2,$$

where P^g are generator active powers in per unit base system power, and q^0 , q^1 , and q^2 are constant coefficients. These coefficients are attributes of each Generator object.

5.1.6 Transformer tap ratio regularization

This function is of type FUNC_TYPE_REG_RATIO. It penalizes deviations of tap ratios of tap-changing transformers from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left(\frac{t_k - t_k^0}{\Delta t} \right)^2 + \frac{1}{2} \sum_{k} \left(\frac{t_k^y}{\Delta t} \right)^2 + \frac{1}{2} \sum_{k} \left(\frac{t_k^z}{\Delta t} \right)^2,$$

where t are tap ratios of tap-changing transformers, t^0 are their initial values, t^y and t^z are positive and negative deviations of t from t^0 , and Δt is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.7 Transformer phase shift regularization

This function is of type FUNC_TYPE_REG_PHASE. It penalizes deviations of phase shifts of phase shifting transformers from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left(\frac{\phi_k - \phi_k^0}{\Delta \phi} \right)^2$$

where ϕ are phase shifts of phase-shifting transformers, ϕ^0 are their initial values, and $\Delta\phi$ is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.8 Switched shunt susceptance regularization

This function is of type FUNC_TYPE_REG_SUSC. It penalizes deviations of susceptances of switched shunt devices from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_k \left(\frac{b_k - b_k^0}{\Delta b} \right)^2 + \frac{1}{2} \sum_k \left(\frac{b_k^y}{\Delta b} \right)^2 + \frac{1}{2} \sum_k \left(\frac{b_k^z}{\Delta b} \right)^2,$$

where b are susceptances of switched shunt devices, b^0 are their initial values, b^y and b^z are positive and negative deviations of b from b^0 , and Δb is a normalization factor. Only terms that include optimization variables are included in the summation.

5.1.9 Sparsity inducing penalty for controls

This function is of type FUNC_TYPE_SP_CONTROLS. It encourages sparse control adjustments with the expression

$$\varphi(x) := \sum_{k} \sqrt{\left(\frac{u_k - u_k^0}{\Delta u_k}\right)^2 + \epsilon},$$

where u are control quantities, u^0 are their current values, and ϵ is a small positive scalar. The normalization factors Δu_k are given by

$$\Delta u_k := \max\{u_k^{\max} - u_k^{\min}, \delta\},\$$

where u^{\max} and u^{\min} are control limits, and δ is a small positive scalar. The control quantities that are considered by this function are specified using the Network class methods $set_flags()$ or $set_flags_of_component()$ using the flag type $FLAG_SPARSE$.

5.2 Constraints

Constraints in PFNET are of the form

$$Ax = b$$

$$f(x) = 0$$

$$l \le Gx \le u,$$

where A and G are matrices, b, l and u are vectors, f is a vector-valued nonlinear function, and x is a vector of values of network quantities that have been set as variables. They are represented by objects of type Constraint. To create an object of this type, the constraint type and the network to be associated with the constraint need to be specified. The following example sets all bus voltage magnitudes and angles as variables and constructs the power flow constraints:

Before a *Constraint* object can be used, it must be initialized using the *Constraint* class method *analyze*. This routine analyzes the constraint and allocates the required vectors and matrices. After this, the constraint can be evaluated using the method *eval*:

```
>>> x = net.get_var_values()
>>> constr.analyze()
>>> constr.eval(x + 0.01)
>>> constr.eval(x)
```

The matrices and vectors associated with the linear constraints can be extracted from the A, G, b, d and d attributes of the Constraint object. The vector of violations and Jacobian matrix of the nonlinear constraints can be extracted from the attributes d and d, respectively. Also, the Hessian matrix of any individual nonlinear constraint d can be extracted using the class method d and d are d are d and d are d and d are d and d are d are d and d are d are d and d are d

```
>>> import numpy as np
>>> f = constr.f

>>> print type(f), f.shape
<type 'numpy.ndarray'> (28,)

>>> print np.linalg.norm(f,np.inf)
0.042

>>> bus = net.get_bus(5)
>>> Hi = constr.get_H_single(bus.index_P)

>>> print type(Hi), Hi.shape, Hi.nnz
<class 'scipy.sparse.coo.coo_matrix'> (28, 28) 27
```

As before, all Hessian matrices have stored only the lower triangular part. In addition to being possible to extract Hessian matrices of individual nonlinear constraints, it is also possible to construct any linear combination of these individual Hessian matrices. This can be done using the *Constraint* class method *combine_H*. After this, the resulting matrix can be extracted from the *H* combined attribute:

```
>>> coefficients = np.random.randn(f.size)
>>> constr.combine_H(coefficients)
>>> H = constr.H_combined
>>> print type(H), H.shape, H.nnz
<class 'scipy.sparse.coo.coo_matrix'> (28, 28) 564
```

Lastly, Lagrange multiplier estimates of the linear and constraints can be used to store sensitivity information in the network components associated with the constraints. This is done using the class method <code>store_sensitivities</code>. Component-specific attributes that store sensitivity information are described in the *API Reference* section.

Details about each of the different constraint types available in PFNET are provided below.

5.2.1 Power balance

This constraint is of type CONSTR_TYPE_PF. It enforces active and reactive power balance at every bus of the network. It is given by

$$(P_k^g + jQ_k^g) - (P_k^l + jQ_k^l) - S_k^{sh} - \sum_{m \in [n]} S_{km} = 0, \ \forall \ k \in [n],$$

5.2. Constraints 21

where P^g and Q^g are generator active and reactive powers, P^l and Q^l are load active and reactive powers, S^{sh} are apparent powers flowing out of buses through branches, P^l are apparent powers flowing out of buses through branches, P^l is the number of buses, and P^l is the number of buses.

5.2.2 Variable fixing

This constraint is of type <code>CONSTR_TYPE_FIX</code>. It constrains specific variables to be fixed at their current value. The variables to be fixed are specified using the <code>Network</code> class methods <code>set_flags()</code> or <code>set_flags_of_component()</code> with the flag type <code>FLAG_FIXED</code>.

5.2.3 Variable bounding

This constraint is of type <code>CONSTR_TYPE_BOUND</code>. It constrains specific variables to be inside their bounds. The variables to be bounded are specified using the <code>Network</code> class methods <code>set_flags()</code> or <code>set_flags_of_component()</code> with the flag type <code>FLAG_BOUNDED</code>. These constraints are expressed as nonlinear equality constraints using the techniques described in Section 4.3.3 of <code>[TTR2015]</code>.

For conventional linear bounds, the constraint type CONSTR_TYPE_LBOUND can be used.

5.2.4 Generator participation

This constraint is of type CONSTR_TYPE_PAR_GEN. It enforces specific active power participations among slack generators, and reactive power participations among generators regulating the same bus voltage magnitude. For slack generators, all participate with equal active powers. For voltage regulating generators, each one participates with the same fraction of its total resources. More specifically, this constraint enforces

$$P_k^g = P_m^g,$$

for all slack generators k and m connected to the same bus, and

$$\frac{Q_k^g - Q_k^{\min}}{Q_k^{\max} - Q_k^{\min}} = \frac{Q_m^g - Q_m^{\min}}{Q_m^{\max} - Q_m^{\min}},$$

for all generators k and m regulating the same bus voltage magnitude, where Q^{\min} and Q^{\max} are generator reactive power limits.

5.2.5 Voltage set-point regulation by generators

This constraint is of type CONSTR_TYPE_REG_GEN. It enforces voltage set-point regulation by generators. It approximates the constraints

$$\begin{aligned} v_k &= v_k^t + v_k^y - v_k^z \\ 0 &\leq (Q_k - Q_k^{\min}) \perp v_k^y \geq 0 \\ 0 &\leq (Q_k^{\max} - Q_k) \perp v_k^z \geq 0, \end{aligned}$$

for each bus k whose voltage is regulated by generators, where v are bus voltage magnitudes, v^t are their set points, v^y and v^z are positive and negative deviations of v from v^t , and Q, Q^{\max} and Q^{\min} are aggregate reactive powers and limits of the generators regulating the same bus voltage magnitude.

5.2.6 Voltage band regulation by transformers

This constraint is of type CONSTR_TYPE_REG_TRAN. It enforces voltage band regulation by tap-changing transformers. It approximates the constraints

$$\begin{split} t_k &= t_k^0 + t_k^y - t_k^z \\ 0 &\leq (v_k + v_k^l - v_k^{\min}) \perp t_k^y \geq 0 \\ 0 &\leq (v_k^{\max} - v_k + v_k^h) \perp t_k^z \geq 0 \\ 0 &\leq (t_k^{\max} - t_k) \perp v_k^l \geq 0 \\ 0 &\leq (t_k - t_k^{\min}) \perp v_k^h \geq 0, \end{split}$$

for each bus k whose voltage is regulated by tap-changing transformers, where v are bus voltage magnitudes, v^{\max} and v^{\min} are their band limits, v^l and v^h are voltage violations of band lower and upper limits, t are transformer tap ratios, t^0 , t^{\max} and t^{\min} are their current values and limits, and t^y and t^z are positive and negative deviations of t from t^0 . The above equations assume that the sensitivity between voltage magnitude and transformer tap ratio is positive. If it is negative, t^y and t^z are interchanged in the first two complementarity constraints, and v^l are interchanged in the bottom two complementarity constraints.

5.2.7 Voltage band regulation by switched shunts

This constraint is of type CONSTR_TYPE_REG_SHUNT. It enforces voltage band regulation by switched shunt devices. It approximates the constraints

$$\begin{aligned} b_k &= b_k^0 + b_k^y - b_k^z \\ 0 &\leq (v_k + v_k^l - v_k^{\min}) \perp b_k^y \geq 0 \\ 0 &\leq (v_k^{\max} - v_k + v_k^h) \perp b_k^z \geq 0 \\ 0 &\leq (b_k^{\max} - b_k) \perp v_k^l \geq 0 \\ 0 &\leq (b_k - b_k^{\min}) \perp v_k^h \geq 0, \end{aligned}$$

for each bus k whose voltage is regulated by switched shunt devices, where v are bus voltage magnitudes, v^{\max} and v^{\min} are their band limits, v^l and v^h are voltage violations of band lower and upper limits, b are switched shunt susceptances, b^0 , b^{\max} and b^{\min} are their current values and limits, and b^y and b^z are positive and negative deviations of b from b^0 .

5.3 Problems

Optimization problems constructed with PFNET are of the form

$$\begin{array}{ll} \text{minimize} & \varphi(x) \\ \text{subject to} & Ax = b \\ & f(x) = 0 \\ & l \leq Gx \leq u, \end{array}$$

As already noted, the objective function φ is a weighted sum of functions φ_i . The linear and nonlinear constraints $Ax = b, l \leq Gx \leq u$, and f(x) = 0 correspond to one or more of the constraints described above. An optimization problem in PFNET is represented by an object of type Problem.

After instantiation, a *Problem* is empty and one needs to specify the *Network* that is to be associated with the problem, the *Constraints* to include, and the *Functions* that form the objective function. This can be done using the *Problem* class methods <code>set_network</code>, <code>add_constraint</code>, and <code>add_function</code>. The following example shows how to construct a simple power flow problem and solve it using the Newton-Raphson method:

5.3. Problems 23

```
import pfnet as pf
from numpy import hstack
from numpy.linalg import norm
from scipy.sparse import bmat
from scipy.sparse.linalg import spsolve
def NRsolve(net):
   net.clear_flags()
    # bus voltage angles
    net.set_flags(pf.OBJ_BUS,
                  pf.FLAG_VARS,
                  pf.BUS_PROP_NOT_SLACK,
                  pf.BUS_VAR_VANG)
    # bus voltage magnitudes
    net.set_flags(pf.OBJ_BUS,
                  pf.FLAG_VARS,
                  pf.BUS_PROP_NOT_REG_BY_GEN,
                  pf.BUS_VAR_VMAG)
    # slack gens active powers
   net.set_flags(pf.OBJ_GEN,
                  pf.FLAG_VARS,
                  pf.GEN_PROP_SLACK,
                  pf.GEN_VAR_P)
    # regulator gens reactive powers
    net.set_flags(pf.OBJ_GEN,
                  pf.FLAG_VARS,
                  pf.GEN_PROP_REG,
                  pf.GEN_VAR_Q)
   p = pf.Problem()
   p.set_network(net)
   p.add_constraint(pf.CONSTR_TYPE_PF)
                                               # power flow
   p.add_constraint(pf.CONSTR_TYPE_PAR_GEN_P) # generator participation
   p.add_constraint(pf.CONSTR_TYPE_PAR_GEN_Q) # generator participation
   p.analyze()
   x = p.get_init_point()
   p.eval(x)
   residual = lambda x: hstack((p.A*x-p.b,p.f))
   while norm(residual(x)) > 1e-4:
        x = x + spsolve(bmat([[p.A], [p.J]], format='csr'), -residual(x))
        p.eval(x)
    net.set_var_values(x)
    net.update_properties()
```

The above routine can then be used as follows:

```
>>> net = Network()
>>> net.load('case3012wp.mat')
```

```
>>> print net.bus_P_mis, net.bus_Q_mis
2.79e+0 1.56e+1
>>> NRsolve(net)
>>> print net.bus_P_mis, net.bus_Q_mis
2.37e-6 3.58e-6
```

As shown in the example, the <code>Problem</code> class method <code>analyze</code> needs to be called before the vectors and matrices associated with the problem constraints and functions can be used. The method <code>eval</code> can then be used for evaluating the problem objective and constraint functions at different points. As is the case for <code>Constraints</code>, a <code>Problem</code> has a method <code>combine_H</code> for forming linear combinations of individual constraint Hessians, and a method <code>store_sensitivities</code> for storing sensitivity information in the network components associated with the constraints.

5.3. Problems 25

SIX

API REFERENCE

6.1 Vector

class numpy.ndarray
See numpy documentation.

6.2 Matrix

class scipy.sparse.coo_matrix
 See scipy documentation.

6.3 Bus

6.3.1 Bus Property Masks

pfnet.BUS_PROP_ANY Any bus.

pfnet.BUS_PROP_SLACK
Slack bus.

 ${\tt pfnet.BUS_PROP_REG_BY_GEN}$

Bus voltage magnitude is regulated by generators.

pfnet.BUS_PROP_REG_BY_TRAN

Bus voltage magnitude is regulated by tap-changing transformers.

pfnet.BUS_PROP_REG_BY_SHUNT

Bus voltage magnitude is regulated by switched shunt devices.

pfnet.BUS_PROP_NOT_REG_BY_GEN

Bus voltage magnitude is not regulated by generators.

pfnet.BUS_PROP_NOT_SLACK

Bus is not slack.

6.3.2 Bus Variable Masks

pfnet.BUS_VAR_VMAG

Voltage magnitude.

pfnet.BUS_VAR_VANG

Voltage angle.

pfnet.BUS_VAR_VDEV

Voltage magnitude positive and negative set point deviations.

pfnet.BUS_VAR_VVIO

Voltage magnitude upper and lower bound violations.

6.3.3 Bus Sensitivities

pfnet.BUS_SENS_LARGEST

Largest objective function sensitivity with respect to constraints involving this bus.

pfnet.BUS_SENS_P_BALANCE

Objective function sensitivity with respect to active power balance.

pfnet.BUS_SENS_Q_BALANCE

Objective function sensitivity with respect to reactive power balance.

pfnet.BUS_SENS_V_MAG_U_BOUND

Objective function sensitivity with respect to voltage magnitude upper bound.

pfnet.BUS_SENS_V_MAG_L_BOUND

Objective function sensitivity with respect to voltage magnitude lower bound.

pfnet.BUS SENS V ANG U BOUND

Objective function sensitivity with respect to voltage angle upper bound.

pfnet.BUS_SENS_V_ANG_L_BOUND

Objective function sensitivity with respect to voltage angle lower bound.

pfnet.BUS_SENS_V_REG_BY_GEN

Objective function sensitivity with respect to voltage magnitude regulation by generators.

pfnet.BUS_SENS_V_REG_BY_TRAN

Objective function sensitivity with respect to voltage magnitude regulation by tap-changing transformers.

pfnet.BUS SENS V REG BY SHUNT

Objective function sensitivity with respect to voltage magnitude regulation by switched shunt devices.

6.3.4 Bus Power Mismatches

pfnet.BUS_MIS_LARGEST

Largest bus power mismatch.

pfnet.BUS_MIS_ACTIVE

Bus active power mismatch.

pfnet.BUS_MIS_REACTIVE

Bus reactive power mismatch.

6.3.5 Bus Class

class pfnet .Bus (alloc=True)

Bus class.

Parameters alloc: {True, False}

P mis Bus active power mismatch (p.u. system base MVA) (float). Q mis Bus reactive power mismatch (p.u. system base MVA) (float). branches List of branches incident on this bus (list). branches from List of branches that have this bus on the "from" side (list). branches to List of branches that have this bus on the "to" side (list). degree Bus degree (number of incident branches) (float). gens List of generators connected to this bus (list). get_largest_mis(self) Gets the bus power mismatch of largest absolute value. Returns mis: float get_largest_mis_type (self) Gets the type of bus power mismatch of largest absolute value. **Returns type**: int get_largest_sens(self) Gets the bus sensitivity of largest absolute value. Returns sens: float get_largest_sens_type (self) Gets the type of bus sensitivity of largest absolute value. Returns type: int get_quantity (self, type) Gets the bus quantity of the given type. **Parameters type**: int (Bus Sensitivities:, Bus Power Mismatches) Returns value: float get_total_gen_P (self) Gets the total active power injected by generators connected to this bus. Returns P: float get_total_gen_Q(self) Gets the total reactive power injected by generators connected to this bus.

 $\begin{tabular}{ll} \bf gen_Q_min~(\it self) \\ \bf Gets~the~smallest~total~reactive~power~that~can~be~injected~by~generators~connected~to~this~bus. \\ \end{tabular}$

Gets the largest total reactive power that can be injected by generators connected to this bus.

Returns Q: float

get_total_gen_Q max(self)

Returns Q_max: float

6.3. Bus 29

```
Returns Q_min: float
get_total_load_P (self)
     Gets the total active power consumed by loads connected to this bus.
         Returns P: float
get total load Q(self)
     Gets the total reactive power consumed by loads connected to this bus.
         Returns Q: float
get_total_shunt_b (self)
     Gets the combined susceptance of shunt devices connected to this bus.
         Returns b: float
get_total_shunt_g(self)
     Gets the combined conductance of shunt devices connected to this bus.
         Returns g: float
has flags (self, fmask, vmask)
     Determines whether the bus has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Bus Variable Masks)
         Returns flag: {True, False}
index
     Bus index (int).
index P
     Index of bus active power mismatch (int).
index 0
     Index for bus reactive power mismatch (int).
index_v_ang
     Index of voltage angle variable (int).
index v mag
     Index of voltage magnitude variable (int).
index vh
     Index of voltage high limit violation variable (int).
index vl
     Index of voltage low limit violation variable (int).
index y
     Index of voltage magnitude positive deviation variable (int).
index_z
     Index of voltage magnitude negative deviation variable (int).
is_regulated_by_gen(self)
     Determines whether the bus is regulated by a generator.
         Returns flag: {True, False}
```

is regulated by shunt (self)

Determines whether the bus is regulated by a shunt device.

```
Returns flag: {True, False}
```

is_regulated_by_tran(self)

Determines whether the bus is regulated by a transformer.

```
Returns flag: {True, False}
```

is slack (self)

Determines whether the bus is a slack bus.

```
Returns flag: {True, False}
```

loads

List of loads connected to this bus (list).

name

Bus name (sting).

number

Bus number (int).

obj_type

Object type (int).

reg_gens

List of generators regulating the voltage magnitude of this bus (list).

reg_shunts

List of switched shunt devices regulating the voltage magnitude of this bus (list).

reg_trans

List of tap-changing transformers regulating the voltage magnitude of this bus (list).

sens_P_balance

Objective function sensitivity with respect to bus active power balance (float).

sens_Q_balance

Objective function sensitivity with respect to bus reactive power balance (float).

sens_v_ang_l_bound

Objective function sensitivity with respect to voltage angle lower bound (float).

sens_v_ang_u_bound

Objective function sensitivity with respect to voltage angle upper bound (float).

${\tt sens_v_mag_l_bound}$

Objective function sensitivity with respect to voltage magnitude lower bound (float).

sens v mag u bound

Objective function sensitivity with respect to voltage magnitude upper bound (float).

sens_v_reg_by_gen

Objective function sensitivity with respect to bus voltage regulation by generators (float).

sens_v_reg_by_shunt

Objective function sensitivity with respect to bus voltage regulation by shunts (float).

sens_v_reg_by_tran

Objective function sensitivity with respect to bus voltage regulation by transformers (float).

show(self)

Shows bus properties.

v ang

Bus voltage angle (radians) (float).

6.3. Bus 31

v_mag

Bus volatge magnitude (p.u. bus base kv) (float).

v max

Bus volatge upper bound (p.u. bus base kv) (float).

v_min

Bus voltage lower bound (p.u. bus base kv) (float).

v set

Bus voltage set point (p.u. bus base kv) (float). Equals one if bus is not regulated by a generator.

vargens

List of variable generators connected to this bus (list).

6.4 Branch

6.4.1 Branch Property Masks

```
pfnet.BRANCH_PROP_ANY
```

Any branch.

pfnet.BRANCH_PROP_TAP_CHANGER

Branch is tap-changing transformer.

pfnet.BRANCH_PROP_TAP_CHANGER_V

Branch is tap-changing transformer regulating bus voltage magnitude.

pfnet.BRANCH_PROP_TAP_CHANGER_Q

Branch is tap-changing transformer regulating reactive power flow.

pfnet.BRANCH PROP PHASE SHIFTER

Branch is phase-shifting transformer regulating active power flow.

6.4.2 Branch Variable Masks

pfnet.BRANCH_VAR_RATIO

Transformer tap ratio.

pfnet.BRANCH_VAR_RATIO_DEV

Transformer tap ratio deviations from current value.

pfnet.BRANCH_VAR_PHASE

Transformer phase shift.

6.4.3 Branch Class

```
class pfnet .Branch (alloc=True)
```

Branch class.

```
Parameters alloc: {True, False}
```

P_flow_DC

Active power flow (DC approx.) from bus "from" to bus "to" (float).

b

Branch series susceptance (p.u.) (float).

b from b to

Branch shunt susceptance at the "from" side (p.u.) (float).

Branch shunt susceptance at the "to" side (p.u.) (float).

bus from

Bus connected to the "from" side.

bus to

Bus connected to the "to" side.

Branch series conductance (p.u.) (float).

Branch shunt conductance at the "from" side (p.u.) (float).

g_to

Branch shunt conductance at the "to" side (p.u.) (float).

has_flags (self, fmask, vmask)

Determines whether the branch has the flags associated with specific quantities set.

```
Parameters fmask: int (Flag Masks)
   vmask: int (Branch Variable Masks)
Returns flag: {True, False}
```

has_pos_ratio_v_sens(self)

Determines whether tap-changing transformer has positive sensitivity between tap ratio and controlled bus voltage magnitude.

```
Returns flag: {True, False}
```

index

Branch index (int).

index_phase

Index of transformer phase shift variable (int).

index ratio

Index of transformer tap ratio variable (int).

index_ratio_y

Index of transformer tap ratio positive deviation variable (int).

index ratio z

Index of transformer tap ratio negative deviation variable (int).

is fixed tran(self)

Determines whether branch is fixed transformer.

```
Returns flag: {True, False}
```

is line (self)

Determines whether branch is transmission line.

```
Returns flag: {True, False}
```

is_phase_shifter(self)

Determines whether branch is phase shifter.

```
Returns flag: {True, False}
```

6.4. Branch 33

is_tap_changer(self)

Determines whether branch is tap-changing transformer.

Returns flag: {True, False}

is_tap_changer_Q(self)

Determines whether branch is tap-changing transformer that regulates reactive power flow.

Returns flag: {True, False}

is_tap_changer_v(self)

Determines whether branch is tap-changing transformer that regulates bus voltage magnitude.

Returns flag: {True, False}

obj_type

Object type (int).

phase

Transformer phase shift (radians) (float).

phase_max

Transformer phase shift upper limit (radians) (float).

phase_min

Transformer phase shift lower limit (radians) (float).

ratingA

Branch thermal rating A (p.u. system base power) (float).

ratingE

Branch thermal rating B (p.u. system base power) (float).

ratingC

Branch thermal rating C (p.u. system base power) (float).

ratio

Transformer tap ratio (float).

ratio_max

Transformer tap ratio upper limit (float).

ratio_min

Transformer tap ratio lower limit (float).

reg bus

Bus whose voltage is regulated by this tap-changing transformer.

sens P 1 bound

Objective function sensitivity with respect to active power flow lower bound (float).

sens_P_u_bound

Objective function sensitivity with respect to active power flow upper bound (float).

6.5 Generator

6.5.1 Generator Property Masks

pfnet.GEN_PROP_ANY

Any generator.

```
pfnet.GEN_PROP_SLACK
     Slack generator.
pfnet.GEN_PROP_REG
     Generator that regulates bus voltage magnitude.
pfnet.GEN PROP NOT REG
     Generator that does not regulate bus voltage magnitude.
pfnet.GEN PROP NOT SLACK
     Generator that is not slack.
pfnet.GEN_PROP_P_ADJUST
     Generator that can adjust its active power (P_min < P_max).
6.5.2 Generator Variable Masks
pfnet.GEN_VAR_P
     Generator active power.
pfnet.GEN VAR Q
     Generator reactive power.
6.5.3 Generator Class
class pfnet .Generator (alloc=True)
     Generator class.
          Parameters alloc: {True, False}
     P
          Generator active power (p.u. system base MVA) (float).
     P_cost
          Active power generation cost ($/hr).
     P max
          Generator active power upper limit (p.u. system base MVA) (float).
     P min
          Generator active power lower limit (p.u. system base MVA) (float).
     Q
          Generator reactive power (p.u. system base MVA) (float).
     Q_max
          Generator reactive power upper limit (p.u. system base MVA) (float).
     O min
          Generator reactive power lower limit (p.u. system base MVA) (float).
     bus
          Bus to which generator is connected.
     cost_coeff_Q0
          Coefficient for quadratic generation cost (constant term, units of $/hr).
     cost_coeff_Q1
          Coefficient for quadratic generation cost (linear term. units of $/(hr p.u.)).
```

6.5. Generator 35

```
cost coeff Q2
     Coefficient for quadratic generation cost (quadratic term, units of $/(hr p.u.^2)).
has_flags (self, fmask, vmask)
     Determines whether the generator has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Generator Variable Masks)
         Returns flag: {True, False}
index
     Generator index (int).
index P
     Index of generator active power variable (int).
index_Q
     Index of generator reactive power variable (int).
is P adjustable (self)
     Determines whether generator has adjustable active power.
         Returns flag: {True, False}
is regulator (self)
     Determines whether generator provides voltage regulation.
         Returns flag: {True, False}
is slack (self)
     Determines whether generator is slack.
         Returns flag: {True, False}
obj_type
     Object type (int).
reg_bus
     Bus whose voltage is regulated by this generator.
sens P 1 bound
     Objective function sensitivity with respect to active power lower bound (float).
sens P u bound
     Objective function sensitivity with respect to active power upper bound (float).
```

6.6 Shunt

6.6.1 Shunt Property Masks

```
pfnet.SHUNT_PROP_ANY
Any shunt.

pfnet.SHUNT_PROP_SWITCHED_V
Switched shunt devices that regulates bus voltage magnitude.
```

6.6.2 Shunt Variable Masks

pfnet.SHUNT_VAR_SUSC

```
Switched shunt susceptance.
pfnet.SHUNT_VAR_SUSC_DEV
     Switched shunt susceptance deviations from current point.
6.6.3 Shunt Class
class pfnet . Shunt (alloc=True)
     Shunt class.
           Parameters alloc: {True, False}
     b
           Shunt susceptance (p.u.) (float).
     b_{max}
           Shunt susceptance upper limit (p.u.) (float).
     b min
           Shunt susceptance lower limit (p.u.) (float).
     bus
           Bus to which the shunt devices is connected.
     g
           Shunt conductance (p.u.) (float).
     has_flags (self, fmask, vmask)
          Determines whether the shunt devices has flags associated with certain quantities set.
               Parameters fmask: int (Flag Masks)
                   vmask: int (Bus Variable Masks)
               Returns flag: {True, False}
     index
           Shunt index (int).
     index b
          Index of shunt susceptance variable (int).
     index_y
           Index of shunt susceptance positive deviation variable (int).
     index_z
          Index of shunt susceptance negative deviation variable (int).
     is fixed (self)
           Determines whether the shunt device is fixed (as opposed to switched).
               Returns flag: {True, False}
     is switched v(self)
           Determines whether the shunt is switchable and regulates bus voltage magnitude.
               Returns flag: {True, False}
     obj_type
           Object type (int).
```

6.6. Shunt 37

reg_bus

Bus whose voltage magnitude is regulated by this shunt device.

6.7 Load

6.7.1 Load Class

```
class pfnet . Load (alloc=True)
    Load class.
    Parameters alloc : {True, False}

P
    Load active power (p.u. system base MVA) (float).

Q
    Load reactive power (p.u. system base MVA) (float).

bus
    Bus to which load is connected.

index
    Load index (int).

obj_type
    Object type (int).
```

6.8 Variable Generator

6.8.1 Variable Generator Property Masks

```
pfnet . VARGEN_PROP_ANY
Any variable generator.
```

6.8.2 Variable Generator Variable Masks

```
pfnet.VARGEN_VAR_P
Variable generator active power.

pfnet.VARGEN_VAR_Q
Variable generator reactive power.
```

6.8.3 Variable Generator Class

```
class pfnet . VarGenerator (alloc=True)
    Variable generator class.
    Parameters alloc : {True, False}

P
    Variable generator active power (p.u. system base MVA) (float).
```

```
P max
     Variable generator active power upper limit (p.u. system base MVA) (float).
P min
     Variable generator active power lower limit (p.u. system base MVA) (float).
P std
     Variable generator active power standard deviation (p.u. system base MVA) (float).
     Variable generator reactive power (p.u. system base MVA) (float).
Q_max
     Variable generator maximum reactive power (p.u. system base MVA) (float).
Q_min
     Variable generator minimum reactive power (p.u. system base MVA) (float).
bus
     Bus to which variable generator is connected.
has_flags (self, fmask, vmask)
     Determines whether the variable generator has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Variable Generator Variable Masks)
         Returns flag: {True, False}
index
     Variable generator index (int).
index P
     Index of variable generator active power variable (int).
index_Q
     Index of variable generator reactive power variable (int).
name
     Variable generator name (string).
```

6.9 Network

obj_type

6.9.1 Component Types

Object type (int).

```
pfnet.OBJ_BUS
Bus.

pfnet.OBJ_GEN
Generator.

pfnet.OBJ_BRANCH
Branch.

pfnet.OBJ_SHUNT
Shunt device.
```

6.9. Network 39

```
pfnet.OBJ_LOAD
Load.
pfnet.OBJ_VARGEN
Variable generator.
```

6.9.2 Flag Masks

```
pfnet.FLAG_VARS
For specifying quantities as variable.

pfnet.FLAG_FIXED
For specifying variables that should be fixed.

pfnet.FLAG_BOUNDED
For specifying variables that should be bounded.

pfnet.FLAG_SPARSE
For specifying control adjustments that should be sparse.
```

6.9.3 Variable Value Codes

```
pfnet.CURRENT
Current variable value.

pfnet.UPPER_LIMIT
Upper limit of variable.

pfnet.LOWER_LIMIT
Lower limit of variable.
```

6.9.4 Network Class

```
class pfnet .Network (alloc=True)
   Network class.
   Parameters alloc : {True, False}

add_vargens (self, buses, penetration, uncertainty, corr_radius, corr_value)
   Adds variable generators to the network.

Parameters buses : list of Buses

penetration : float
   percentage
   uncertainty : float
   percentage
   corr_radius : int
   number of branches
   corr_value : float
   correlation coefficient
```

adjust_generators(self)

Adjusts powers of slack and regulator generators connected to or regulating the same bus to correct generator participations without modifying the total power injected.

base_power

System base power (MVA) (float).

branches

List of network branches (list).

bus P mis

Largest bus active power mismatch in the network (MW) (float).

bus_Q_mis

Largest bus reactive power mismatch in the network (MVAr) (float).

bus_v_max

Maximum bus voltage magnitude (p.u.) (float).

bus_v_min

Minimum bus voltage magnitude (p.u.) (float).

bus_v_vio

Maximum bus voltage magnitude limit violation (p.u.) (float).

buses

List of network buses (list).

clear_error(self)

Clear error flag and message string.

clear_flags(self)

Clears all the flags of all the network components.

clear_properties (self)

Clears all the network properties.

clear_sensitivities (self)

Clears all sensitivity information.

create_sorted_bus_list (self, sort_by)

Creates list of buses sorted in descending order according to a specific quantity.

Parameters sort_by: int (Bus Sensitivities, Bus Power Mismatches).

Returns buses: list of Buses

create_vargen_P_sigma (self, spread, corr)

Creates covariance matrix (lower triangular part) for variable vargen active powers.

Parameters spead : int

Determines correlation neighborhood in terms of number of edges.

corr: float

Desired correlation coefficient for neighboring vargens.

Returns sigma: coo_matrix

gen_P_cost

Total active power generation cost (\$/hr) (float).

gen P vio

Largest generator active power limit violation (MW) (float).

6.9. Network 41

```
gen_Q_vio
    Largest generator reactive power limit violation (MVAr) (float).
gen_v_dev
    Largest voltage magnitude deviation from set point of bus regulated by generator (p.u.) (float).
generators
    List of network generators (list).
get_branch (self, index)
    Gets branch with the given index.
         Parameters index: int
         Returns branch: Branch
get_bus (self, index)
     Gets bus with the given index.
         Parameters index: int
         Returns bus: Bus
get_bus_by_name (self, name)
     Gets bus with the given name.
         Parameters name: string
         Returns bus: Bus
get_bus_by_number (self, number)
     Gets bus with the given number.
         Parameters number: int
         Returns bus: Bus
get_gen (self, index)
     Gets generator with the given index.
         Parameters index: int
         Returns gen: Generator
get_gen_buses (self)
    Gets list of buses where generators are connected.
         Returns buses: list
get_load (self, index)
     Gets load with the given index.
         Parameters index: int
         Returns gen: Load
get_load_buses (self)
     Gets list of buses where loads are connected.
         Returns buses: list
get_num_P_adjust_gens (self)
     Gets number of generators in the network that have adjustable active powers.
```

Returns num: int

```
get_num_branches (self)
     Gets number of branches in the network.
         Returns num: int
get num buses(self)
     Gets number of buses in the network.
         Returns num: int
get_num_buses_reg_by_gen(self)
     Gets number of buses whose voltage magnitudes are regulated by generators.
         Returns num: int
get_num_buses_reg_by_shunt (self, only=False)
     Gets number of buses whose voltage magnitudes are regulated by switched shunt devices.
         Returns num: int
get_num_buses_reg_by_tran (self, only=False)
     Gets number of buses whose voltage magnitudes are regulated by tap-changing transformers.
         Returns num: int
get_num_fixed_shunts(self)
     Gets number of fixed shunts in the network.
         Returns num: int
get_num_fixed_trans(self)
     Gets number of fixed transformers in the network.
         Returns num: int
get_num_gens (self)
     Gets number of generators in the network.
         Returns num: int
get_num_lines(self)
     Gets number of transmission lines in the network.
         Returns num: int
get num loads (self)
     Gets number of loads in the network.
         Returns num: int
get_num_phase_shifters(self)
     Gets number of phase-shifting transformers in the network.
         Returns num: int
get_num_reg_gens (self)
     Gets number generators in the network that provide voltage regulation.
         Returns num: int
get_num_shunts(self)
     Gets number of shunts in the network.
```

6.9. Network 43

Returns num: int

Gets number of slack buses in the network.

get_num_slack_buses(self)

```
Returns num: int
get_num_slack_gens(self)
     Gets number of slack generators in the network.
         Returns num: int
get num switched shunts (self)
     Gets number of switched shunts in the network.
         Returns num: int
get_num_tap_changers (self)
     Gets number of tap-changing transformers in the network.
         Returns num: int
get_num_tap_changers_Q(self)
     Gets number of tap-changing transformers in the network that regulate reactive flows.
         Returns num: int
get_num_tap_changers_v (self)
     Gets number of tap-changing transformers in the network that regulate voltage magnitudes.
         Returns num: int
get_num_vargens (self)
     Gets number of variable generators in the network.
         Returns num: int
get_properties (self)
     Gets network properties.
         Returns properties: dict
get_shunt (self, index)
     Gets shunt with the given index.
         Parameters index: int
         Returns gen: Shunt
get_var_projection (self, obj_type, var)
     Gets projection matrix for specific object variables.
         Parameters obj_type : int (Component Types)
             var: int (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks, Shunt
             Variable Masks)
get_var_values (self, code=CURRENT)
     Gets network variable values.
         Parameters code: int (See var values)
         Returns values: ndarray
get_vargen (self, index)
     Gets variable generator with the given index.
         Parameters index: int
```

Returns vargen: VarGenerator

get_vargen_by_name (self, name)

Gets vargen with the given name.

Parameters name: string

Returns vargen: VarGenerator

has_error(self)

Indicates whether the network has the error flag set due to an invalid operation.

load (self, filename)

Loads a network data contained in a specific file.

Parameters filename: string

loads

List of network loads (list).

num_actions

Number of control adjustments (int).

num bounded

Number of network quantities that have been set to bounded (int).

num branches

Number of branches in the network (int).

num_buses

Number of buses in the network (int).

num fixed

Number of network quantities that have been set to fixed (int).

num_gens

Number of generators in the network (int).

num loads

Number of loads in the network (int).

num shunts

Number of shunt devices in the network (int).

num_sparse

Number of network control quantities that have been set to sparse (int).

num_vargens

Number of variable generators in the network (int).

num vars

Number of network quantities that have been set to variable (int).

set_flags (self, obj_type, flags, props, vals)

Sets flags of network components with specific properties.

Parameters obj_type : int (Component Types)

flags: int or list (Flag Masks)

props: int or list (Bus Property Masks, Branch Property Masks, Generator Property Masks, Shunt Property Masks)

vals: int or list (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks, Shunt Variable Masks)

6.9. Network 45

set_flags_of_component (self, obj, flags, vals)

Sets flags of network components with specific properties.

Parameters obj: Bus, Branch, Generator, Load, Shunt, VarGenerator

flags: int or list (Flag Masks)

vals: int or list (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks,

Shunt Variable Masks)

set_var_values (self, values)

Sets network variable values.

Parameters values: ndarray

show_buses (self, number, sort_by)

Shows information about the most relevant network buses sorted by a specific quantity.

Parameters number: int

sort_by : int (Bus Sensitivities, Bus Power Mismatches)

show components (self)

Shows information about the number of network components of each type.

show_properties(self)

Shows information about the state of the network component quantities.

shunt b vio

Largest switched shunt susceptance limit violation (p.u.) (float).

shunt v vio

Largest voltage magnitude band violation of voltage regulated by switched shunt device (p.u.) (float).

shunts

List of network shunts (list).

tran_p_vio

Largest transformer phase shift limit violation (float).

tran_r_vio

Largest transformer tap ratio limit violation (float).

tran_v_vio

Largest voltage magnitude band violation of voltage regulated by transformer (p.u.) (float).

update_properties (self, values=None)

Re-computes the network properties using the given values of the network variables. If no values are given, then the current values of the network variables are used.

Parameters values: ndarray

update_set_points(self)

Updates voltage magnitude set points of gen-regulated buses to be equal to the bus voltage magnitudes.

var_generators

List of network variable generators (list).

vargen_corr_radius

Correlation radius of variable generators (number of edges).

vargen_corr_value

Correlation value (coefficient) of variable generators.

6.10 Graph

```
class pfnet .Graph (net, alloc=True)
     Graph class.
          Parameters net: Network
               alloc: {True, False}
     color_nodes_by_mismatch (self, mis_type)
          Colors the graphs nodes according to their power mismatch.
               Parameters mis_type : int (Bus Power Mismatches)
     color_nodes_by_sensitivity (self, sens_type)
          Colors the graphs nodes according to their sensitivity.
               Parameters sens_type : int (Bus Sensitivities)
     set_edges_property (self, prop, value)
          Sets property of edges. See Graphviz documentation.
               Parameters prop: string
                   value: string
     set_layout (self)
          Determines and saves a layout for the graph nodes.
     set_nodes_property (self, prop, value)
          Sets property of nodes. See Graphviz documentation.
               Parameters prop: string
                   value: string
     view(self)
          Displays the graph.
     write (self, format, filename)
          Writes the graph to a file.
               Parameters format: string (Graphviz output formats)
                   filename: string
```

6.11 Function

6.11.1 Function Types

```
pfnet.FUNC_TYPE_UNKNOWN
Unknown function.

pfnet.FUNC_TYPE_REG_VMAG
Bus voltage magnitude regularization.

pfnet.FUNC_TYPE_SLIM_VMAG
Bus voltage magnitude soft limits penalty.

pfnet.FUNC_TYPE_REG_VANG
Bus voltage angle regularization.
```

6.10. Graph 47

```
pfnet.FUNC_TYPE_REG_PQ
     Generator active and reactive power regularization.
pfnet.FUNC_TYPE_GEN_COST
     Active power generation cost.
pfnet.FUNC TYPE REG RATIO
     Transformer tap ratio regularization.
pfnet.FUNC TYPE REG PHASE
     Transformer phase shift regularization.
pfnet.FUNC_TYPE_REG_SUSC
     Switched shunt susceptance regularization.
pfnet.FUNC_TYPE_SP_CONTROLS
     Sparsity-inducing penalty for control adjustments.
6.11.2 Function Class
class pfnet . Function (int type, float weight, Network net, alloc=True)
     Function class.
          Parameters type: int (Function Types)
              weight: float
              net: Network
              alloc: {True, False}
     Hcounter
          Number of nonzero entries in Hessian matrix (int).
     Hphi
          Function Hessian matrix (only the lower triangular part) (coo_matrix).
     analyze(self)
          Analyzes function and allocates required vectors and matrices.
     clear_error (self)
          Clears internal error flag.
     eval (self, var values)
          Evaluates function value, gradient, and Hessian using the given variable values.
              Parameters var_values: ndarray
     qphi
          Function gradient vector (ndarray).
     phi
          Function value (float).
     type
          Function type (int).
     update_network (self)
          Updates internal arrays to be compatible with any network changes.
     weight
          Function weight (float).
```

6.12 Constraint

6.12.1 Constraint Types

```
pfnet.CONSTR_TYPE_PF
```

Constraint for enforcing power balance at every bus of the network.

```
pfnet.CONSTR_TYPE_DCPF
```

Constraint for enforcing DC power balance at every bus of the network.

```
pfnet.CONSTR_TYPE_FIX
```

Constraint for fixing a subset of variables to their current value.

```
pfnet.CONSTR TYPE BOUND
```

Constraint for forcing a subset of variables to be within their bounds (nonlinear).

```
pfnet.CONSTR_TYPE_LBOUND
```

Constraint for forcing a subset of variables to be within their bounds (linear).

```
pfnet.CONSTR_TYPE_PAR_GEN_P
```

Constraint for enforcing generator active power participations.

```
pfnet.CONSTR TYPE PAR GEN Q
```

Constraint for enforcing generator reactive power participations.

```
pfnet.CONSTR_TYPE_REG_GEN
```

Constraint for enforcing voltage set point regulation by generators.

```
pfnet.CONSTR_TYPE_REG_TRAN
```

Constraint for enforcing voltage band regulation by tap-changing transformers.

```
pfnet.CONSTR_TYPE_REG_SHUNT
```

Constraint for enforcing voltage band regulation by switched shunt devices.

```
pfnet.CONSTR_TYPE_DC_FLOW_LIM
```

Constraint for enforcing DC power flow limits on every branch

6.12.2 Constraint Class

```
class pfnet.Constraint (int type, Network net, alloc=True)
    Contraint class.
```

Parameters type: int (*Constraint Types*)

```
net : Network
alloc : {True, False}
```

Matrix for linear equality constraints (coo_matrix).

Aconstr_index

Index of linear equality constraint (int).

Acounter

Number of nonzero entries in the matrix of linear equality constraints (int).

G

Α

Matrix for linear inequality constraints (coo_matrix).

6.12. Constraint 49

```
Gconstr index
     Index of linear inequality constraint (int).
Gcounter
     Number of nonzero entries in the matrix of linear inequality constraints (int).
H combined
     Linear combination of Hessian matrices of individual nonlinear equality constraints (only the lower trian-
     gular part) (coo_matrix).
J
     Jacobian matrix of nonlinear equality constraints (coo_matrix).
Jconstr_index
     Index of nonlinear equality constraint (int).
Jcounter
     Number of nonzero entries in the Jacobian matrix of the nonlinear equality constraints (int).
analyze (self)
     Analyzes constraint and allocates required vectors and matrices.
b
     Right-hand side vector of linear equality constraints (ndarray).
clear error(self)
     Clears internal error flag.
combine_H (self, coeff, ensure_psd=False)
     Forms and saves a linear combination of the individual constraint Hessians.
         Parameters coeff: ndarray
             ensure_psd : {True, False}
eval (self, var_values)
     Evaluates constraint violations, Jacobian, and individual Hessian matrices.
         Parameters var_values: ndarray
f
     Vector of nonlinear equality constraint violations (ndarray).
get_H_single (self, i)
     Gets the Hessian matrix (only lower triangular part) of an individual constraint.
         Parameters i: int
         Returns H: coo_matrix
1
     Lower bound vector of linear inequality constraints (ndarray).
store_sensitivities (self, sA, sf, sGu, sGl)
     Stores Lagrange multiplier estimates of the constraints in the power network components.
         Parameters sA: ndarray
                sensitivities for linear equality constraints (Ax = b)
             sf: ndarray
                sensitivities for nonlinear equality constraints (f(x) = 0)
             sGu: ndarray
```

```
\mathbf{sGl}: ndarray \mathbf{sGl}: ndarray sensitivities for linear inequality constraints (l \leq Gx) \mathbf{type} Constraint type (Constraint Types) (int). \mathbf{u} Upper bound vector of linear inequality constraints (ndarray). \mathbf{update\_network} \ (self) Updates internal arrays to be compatible with any network changes.
```

6.13 Optimization Problem

6.13.1 Problem Class

```
class pfnet.Problem
     Optimization problem class.
           Constraint matrix of linear equality constraints (coo_matrix).
     G
           Constraint matrix of linear inequality constraints (coo_matrix).
     H combined
           Linear combination of Hessian matrices of individual nonlinear equality constraints (only the lower trian-
           gular part) (coo_matrix).
     Hphi
           Objective function Hessian matrix (only the lower triangular part) (coo_matrix).
     J
           Jacobian matrix of the nonlinear equality constraints (coo_matrix).
     add_constraint (self, ctype)
           Adds constraint to optimization problem.
               Parameters ctype: int (Constraint Types)
     add_function (self, ftype, weight)
           Adds function to optimization problem objective.
               Parameters ftype: int (Function Types)
                   weight: float
     analyze(self)
           Analyzes function and constraint structures and allocates required vectors and matrices.
     b
           Right hand side vectors of the linear equality constraints (ndarray).
     clear(self)
           Resets optimization problem data.
     combine_H (self, coeff, ensure_psd)
           Forms and saves a linear combination of the individual constraint Hessians.
```

```
Parameters coeff: ndarray
             ensure_psd : {True, False}
constraints
     List of constraints of this optimization problem (list).
eval (self, var values)
     Evaluates objective function and constraints as well as their first and second derivatives using the given
     variable values.
         Parameters var_values: ndarray
f
     Vector of nonlinear equality constraints violations (ndarray).
find_constraint (self, type)
     Finds constraint of give type among the constraints of this optimization problem.
         Parameters type: int (Constraint Types)
functions
    List of functions that form the objective function of this optimization problem (list).
get_init_point (self)
     Gets initial solution estimate from the current value of the network variables.
         Returns point: ndarray
get_lower_limits(self)
     Gets vector of lower limits for the network variables.
         Returns limits: ndarray
get_network (self)
     Gets the power network associated with this optimization problem.
get_upper_limits (self)
     Gets vector of upper limits for the network variables.
         Returns limits: ndarray
aphi
     Objective function gradient vector (ndarray).
1
     Lower bound for linear inequality constraints (ndarray).
lam
     Initial dual point (ndarray).
network
     Power network associated with this optimization problem (Network).
nu
     Initial dual point (ndarray).
phi
     Objective function value (float).
set_network (self, net)
     Sets the power network associated with this optimization problem.
show (self)
     Shows information about this optimization problem.
```

```
store_sensitivities (self, sA, sf, sGu, sGl)
     Stores Lagrange multiplier estimates of the constraints in the power network components.
         Parameters sA: ndarray
                sensitivities for linear equality constraints (Ax = b)
             sf: ndarray
                sensitivities for nonlinear equality constraints (f(x) = 0)
             sGu: ndarray
                sensitivities for linear inequality constraints (Gx \le u)
             sGl: ndarray
                sensitivities for linear inequality constraints (l \leq Gx)
u
     Upper bound for linear inequality constraints (ndarray).
update_lin(self)
     Updates linear equality constraints.
x
     Initial primal point (ndarray).
```

6.14 References

6.14. References 53

CHAPTER

SEVEN

INDICES AND TABLES

- genindex
- modindex
- search

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58 Bibliography

PYTHON MODULE INDEX

 $\begin{array}{c} \textbf{p} \\ \text{pfnet}, 1 \end{array}$

60 Python Module Index

PYTHON MODULE INDEX

$\begin{array}{c} \textbf{p} \\ \text{pfnet}, 1 \end{array}$

62 Python Module Index

A	С
A (pfnet.Constraint attribute), 49	clear() (pfnet.Problem method), 51
A (pfnet.Problem attribute), 51	clear_error() (pfnet.Constraint method), 50
Aconstr_index (pfnet.Constraint attribute), 49	clear_error() (pfnet.Function method), 48
Acounter (pfnet.Constraint attribute), 49	clear_error() (pfnet.Network method), 41
add_constraint() (pfnet.Problem method), 51	clear_flags() (pfnet.Network method), 41
add_function() (pfnet.Problem method), 51	clear_properties() (pfnet.Network method), 41
add_vargens() (pfnet.Network method), 40	clear_sensitivities() (pfnet.Network method), 41
adjust_generators() (pfnet.Network method), 40	color_nodes_by_mismatch() (pfnet.Graph method), 47
analyze() (pfnet.Constraint method), 50	color_nodes_by_sensitivity() (pfnet.Graph method), 47
analyze() (pfnet.Function method), 48	combine_H() (pfnet.Constraint method), 50
analyze() (pfnet.Problem method), 51	combine_H() (pfnet.Problem method), 51
D	Constraint (class in pfnet), 49
В	constraints (pfnet.Problem attribute), 52
b (pfnet.Branch attribute), 32	cost_coeff_Q0 (pfnet.Generator attribute), 35
b (pfnet.Constraint attribute), 50	cost_coeff_Q1 (pfnet.Generator attribute), 35
b (pfnet.Problem attribute), 51	cost_coeff_Q2 (pfnet.Generator attribute), 35
b (pfnet.Shunt attribute), 37	<pre>create_sorted_bus_list() (pfnet.Network method), 41</pre>
b_from (pfnet.Branch attribute), 32	create_vargen_P_sigma() (pfnet.Network method), 41
b_max (pfnet.Shunt attribute), 37	D
b_min (pfnet.Shunt attribute), 37	D
b_to (pfnet.Branch attribute), 33	degree (pfnet.Bus attribute), 29
base_power (pfnet.Network attribute), 41	F
Branch (class in pfnet), 32	E
branches (pfnet.Bus attribute), 29	eval() (pfnet.Constraint method), 50
branches (pfnet.Network attribute), 41	eval() (pfnet.Function method), 48
branches_from (pfnet.Bus attribute), 29	eval() (pfnet.Problem method), 52
branches_to (pfnet.Bus attribute), 29	_
Bus (class in pfnet), 28	F
bus (pfnet.Generator attribute), 35	f (pfnet.Constraint attribute), 50
bus (pfnet.Load attribute), 38	f (pfnet.Problem attribute), 52
bus (pfnet.Shunt attribute), 37	find_constraint() (pfnet.Problem method), 52
bus (pfnet. VarGenerator attribute), 39	Function (class in pfnet), 48
bus_from (pfnet.Branch attribute), 33	functions (pfnet.Problem attribute), 52
bus_P_mis (pfnet.Network attribute), 41	
bus_Q_mis (pfnet.Network attribute), 41	G
bus_to (pfnet.Branch attribute), 33	g (pfnet.Branch attribute), 33
bus_v_max (pfnet.Network attribute), 41	G (pfnet.Constraint attribute), 49
bus_v_min (pfnet.Network attribute), 41	G (pfnet.Problem attribute), 51
bus_v_vio (pfnet.Network attribute), 41	g (pfnet.Shunt attribute), 37
buses (pfnet.Network attribute), 41	g_from (pfnet.Branch attribute), 33
	g_to (pfnet.Branch attribute), 33
	<i>C</i> = <i>u</i>

Gconstr_index (pfnet.Constraint attribute), 49	get_total_gen_Q_max() (pfnet.Bus method), 29
Gcounter (pfnet.Constraint attribute), 50	get_total_gen_Q_min() (pfnet.Bus method), 29
gen_P_cost (pfnet.Network attribute), 41	get_total_load_P() (pfnet.Bus method), 30
gen_P_vio (pfnet.Network attribute), 41	get_total_load_Q() (pfnet.Bus method), 30
gen_Q_vio (pfnet.Network attribute), 41	get_total_shunt_b() (pfnet.Bus method), 30
gen_v_dev (pfnet.Network attribute), 42	get_total_shunt_g() (pfnet.Bus method), 30
Generator (class in pfnet), 35	get_upper_limits() (pfnet.Problem method), 52
generators (pfnet.Network attribute), 42	get_var_projection() (pfnet.Network method), 44
gens (pfnet.Bus attribute), 29	get_var_values() (pfnet.Network method), 44
get_branch() (pfnet.Network method), 42	get_vargen() (pfnet.Network method), 44
get_bus() (pfnet.Network method), 42	get_vargen_by_name() (pfnet.Network method), 44
get_bus_by_name() (pfnet.Network method), 42	gphi (pfnet.Function attribute), 48
get_bus_by_number() (pfnet.Network method), 42	gphi (pfnet.Problem attribute), 52
get_gen() (pfnet.Network method), 42	Graph (class in pfnet), 47
get_gen_buses() (pfnet.Network method), 42	1 //
get_H_single() (pfnet.Constraint method), 50	Н
get_init_point() (pfnet.Problem method), 52	H_combined (pfnet.Constraint attribute), 50
get_largest_mis() (pfnet.Bus method), 29	H_combined (pfnet.Problem attribute), 51
get_largest_mis_type() (pfnet.Bus method), 29	has_error() (pfnet.Network method), 45
get_largest_sens() (pfnet.Bus method), 29	has_flags() (pfnet.Branch method), 33
get_largest_sens_type() (pfnet.Bus method), 29	has_flags() (pfnet.Bus method), 30
get_load() (pfnet.Network method), 42	has_flags() (pfnet.Generator method), 36
get_load_buses() (pfnet.Network method), 42	has_flags() (pfnet.Shunt method), 37
get_lower_limits() (pfnet.Problem method), 52	has_flags() (pfnet.VarGenerator method), 39
get_network() (pfnet.Problem method), 52	has_pos_ratio_v_sens() (pfnet.Branch method), 33
get_num_branches() (pfnet.Network method), 42	Hounter (pfnet.Function attribute), 48
get_num_buses() (pfnet.Network method), 43	Hphi (pfnet.Function attribute), 48
get_num_buses_reg_by_gen() (pfnet.Network method),	Hphi (pfnet.Problem attribute), 51
43	Tipin (pinet.) Toolem attribute), 31
get_num_buses_reg_by_shunt() (pfnet.Network method),	
43	in the Coffee Down the ACT AND 22
get_num_buses_reg_by_tran() (pfnet.Network method),	index (pfnet.Branch attribute), 33
43	index (pfnet.Bus attribute), 30
get_num_fixed_shunts() (pfnet.Network method), 43	index (pfnet Lead attribute), 36
get_num_fixed_trans() (pfnet.Network method), 43	index (pfnet.Load attribute), 38
get_num_gens() (pfnet.Network method), 43	index (pfnet.Shunt attribute), 37
get_num_lines() (pfnet.Network method), 43	index (pfnet.VarGenerator attribute), 39
get_num_loads() (pfnet.Network method), 43	index_b (pfnet.Shunt attribute), 37
get_num_P_adjust_gens() (pfnet.Network method), 42	index_P (pfnet.Bus attribute), 30
get_num_phase_shifters() (pfnet.Network method), 43	index_P (pfnet.Generator attribute), 36
get_num_reg_gens() (pfnet.Network method), 43	index_P (pfnet.VarGenerator attribute), 39
get_num_shunts() (pfnet.Network method), 43	index_phase (pfnet.Branch attribute), 33
get_num_slack_buses() (pfnet.Network method), 43	index_Q (pfnet.Bus attribute), 30
get_num_slack_gens() (pfnet.Network method), 44	index_Q (pfnet.Generator attribute), 36
get_num_switched_shunts() (pfnet.Network method), 44	index_Q (pfnet.VarGenerator attribute), 39
get_num_tap_changers() (pfnet.Network method), 44	index_ratio (pfnet.Branch attribute), 33
get_num_tap_changers_Q() (pfnet.Network method), 44	index_ratio_y (pfnet.Branch attribute), 33
get_num_tap_changers_v() (pfnet.Network method), 44	index_ratio_z (pfnet.Branch attribute), 33
get_num_vargens() (pfnet.Network method), 44	index_v_ang (pfnet.Bus attribute), 30
get_properties() (pfnet.Network method), 44	index_v_mag (pfnet.Bus attribute), 30
get_quantity() (pfnet.Bus method), 29	index_vl (pfnet.Bus attribute), 30
get_shunt() (pfnet.Network method), 44	index_vl (pfnet.Bus attribute), 30
get_total_gen_P() (pfnet.Bus method), 29	index_y (pfnet.Bus attribute), 30
get_total_gen_Q() (pfnet.Bus method), 29	index_y (pfnet.Shunt attribute), 37
C = -C - C \ \(\)	index_z (pfnet.Bus attribute), 30

index_z (pfnet.Shunt attribute), 37 is_fixed() (pfnet.Shunt method), 37 is_fixed_tran() (pfnet.Branch method), 33 is_line() (pfnet.Branch method), 33 is_P_adjustable() (pfnet.Generator method), 36	obj_type (pfnet.Bus attribute), 31 obj_type (pfnet.Generator attribute), 36 obj_type (pfnet.Load attribute), 38 obj_type (pfnet.Shunt attribute), 37 obj_type (pfnet.VarGenerator attribute), 39
is_phase_shifter() (pfnet.Branch method), 33	P
is_regulated_by_gen() (pfnet.Bus method), 30 is_regulated_by_shunt() (pfnet.Bus method), 30	
is_regulated_by_tran() (pfnet.Bus method), 31	P (pfnet.Generator attribute), 35
is_regulator() (pfnet.Generator method), 36	P (pfnet.Load attribute), 38
is_slack() (pfnet.Bus method), 31	P (pfnet. VarGenerator attribute), 38
is_slack() (pfnet.Generator method), 36	P_cost (pfnet.Generator attribute), 35
is_switched_v() (pfnet.Shunt method), 37	P_flow_DC (pfnet.Branch attribute), 32
is_tap_changer() (pfnet.Branch method), 33	P_max (pfnet.Generator attribute), 35
is_tap_changer_Q() (pfnet.Branch method), 34	P_max (pfnet.VarGenerator attribute), 38
is_tap_changer_v() (pfnet.Branch method), 34	P_min (pfnet.Generator attribute), 35
is_tap_changer_v() (princt.Dranen method), 34	P_min (pfnet.VarGenerator attribute), 39
J	P_mis (pfnet.Bus attribute), 28
	P_std (pfnet.VarGenerator attribute), 39
J (pfnet.Constraint attribute), 50	pfnet (module), 1
J (pfnet.Problem attribute), 51	pfnet.BRANCH_PROP_ANY (built-in variable), 32
Jconstr_index (pfnet.Constraint attribute), 50	pfnet.BRANCH_PROP_PHASE_SHIFTER (built-in
Jcounter (pfnet.Constraint attribute), 50	variable), 32
I	pfnet.BRANCH_PROP_TAP_CHANGER (built-in vari-
1/ 6 - 6	able), 32
1 (pfnet.Constraint attribute), 50	pfnet.BRANCH_PROP_TAP_CHANGER_Q (built-in
1 (pfnet.Problem attribute), 52	variable), 32
lam (pfnet.Problem attribute), 52	pfnet.BRANCH_PROP_TAP_CHANGER_V (built-in
Load (class in pfnet), 38	variable), 32
load() (pfnet.Network method), 45	pfnet.BRANCH_VAR_PHASE (built-in variable), 32
loads (pfnet.Bus attribute), 31	pfnet.BRANCH_VAR_RATIO (built-in variable), 32
loads (pfnet.Network attribute), 45	pfnet.BRANCH_VAR_RATIO_DEV (built-in variable),
N	32
	pfnet.BUS_MIS_ACTIVE (built-in variable), 28
name (pfnet.Bus attribute), 31	pfnet.BUS_MIS_LARGEST (built-in variable), 28
name (pfnet.VarGenerator attribute), 39	pfnet.BUS_MIS_REACTIVE (built-in variable), 28
Network (class in pfnet), 40	pfnet.BUS_PROP_ANY (built-in variable), 27
network (pfnet.Problem attribute), 52	pfnet.BUS_PROP_NOT_REG_BY_GEN (built-in vari-
nu (pfnet.Problem attribute), 52	able), 27
num_actions (pfnet.Network attribute), 45	pfnet.BUS_PROP_NOT_SLACK (built-in variable), 27
num_bounded (pfnet.Network attribute), 45	pfnet.BUS_PROP_REG_BY_GEN (built-in variable), 27
num_branches (pfnet.Network attribute), 45	pfnet.BUS_PROP_REG_BY_SHUNT (built-in variable),
num_buses (pfnet.Network attribute), 45	27
num_fixed (pfnet.Network attribute), 45	pfnet.BUS_PROP_REG_BY_TRAN (built-in variable), 27
num_gens (pfnet.Network attribute), 45	pfnet.BUS_PROP_SLACK (built-in variable), 27
num_loads (pfnet.Network attribute), 45	pfnet.BUS_SENS_LARGEST (built-in variable), 28
num_shunts (pfnet.Network attribute), 45	
num_sparse (pfnet.Network attribute), 45	pfnet.BUS_SENS_P_BALANCE (built-in variable), 28 pfnet.BUS_SENS_Q_BALANCE (built-in variable), 28
num_vargens (pfnet.Network attribute), 45	
num_vars (pfnet.Network attribute), 45	pfnet.BUS_SENS_V_ANG_L_BOUND (built-in vari-
number (pfnet.Bus attribute), 31	able), 28
numpy.ndarray (built-in class), 27	pfnet.BUS_SENS_V_ANG_U_BOUND (built-in vari-
0	able), 28 pfnet.BUS_SENS_V_MAG_L_BOUND (built-in vari-
ohi type (nfnet Branch attribute) 34	able), 28
ODE TYPE CHIEF DIVICE AUTIDITE) 34	uoio), 20

pfnet.BUS_SENS_V_MAG_U_BOUND (built-in vari-	pfnet.OBJ_BRANCH (built-in variable), 39
able), 28	pfnet.OBJ_BUS (built-in variable), 39
pfnet.BUS_SENS_V_REG_BY_GEN (built-in variable),	pfnet.OBJ_GEN (built-in variable), 39
28	pfnet.OBJ_LOAD (built-in variable), 39
pfnet.BUS_SENS_V_REG_BY_SHUNT (built-in vari-	pfnet.OBJ_SHUNT (built-in variable), 39
able), 28	pfnet.OBJ_VARGEN (built-in variable), 40
pfnet.BUS_SENS_V_REG_BY_TRAN (built-in vari-	pfnet.SHUNT_PROP_ANY (built-in variable), 36
able), 28	pfnet.SHUNT_PROP_SWITCHED_V (built-in variable)
pfnet.BUS_VAR_VANG (built-in variable), 28	36
pfnet.BUS_VAR_VDEV (built-in variable), 28	pfnet.SHUNT_VAR_SUSC (built-in variable), 37
pfnet.BUS_VAR_VMAG (built-in variable), 27	pfnet.SHUNT_VAR_SUSC_DEV (built-in variable), 37
pfnet.BUS_VAR_VVIO (built-in variable), 28	pfnet.UPPER_LIMIT (built-in variable), 40
pfnet.CONSTR_TYPE_BOUND (built-in variable), 49	pfnet.VARGEN_PROP_ANY (built-in variable), 38
pfnet.CONSTR_TYPE_DC_FLOW_LIM (built-in vari-	pfnet.VARGEN_VAR_P (built-in variable), 38
able), 49	pfnet.VARGEN_VAR_Q (built-in variable), 38
pfnet.CONSTR_TYPE_DCPF (built-in variable), 49	phase (pfnet.Branch attribute), 34
pfnet.CONSTR_TYPE_FIX (built-in variable), 49	phase_max (pfnet.Branch attribute), 34
pfnet.CONSTR_TYPE_LBOUND (built-in variable), 49	phase_min (pfnet.Branch attribute), 34
pfnet.CONSTR_TYPE_PAR_GEN_P (built-in variable),	phi (pfnet.Function attribute), 48
princt. CONSTR_TTTE_FAR_OEN_F (built-iii variable),	
pfnet.CONSTR_TYPE_PAR_GEN_Q (built-in variable),	phi (pfnet.Problem attribute), 52
princt.CONSTR_TTPE_PAR_GEN_Q (built-iii variable),	Problem (class in pfnet), 51
	Q
pfnet.CONSTR_TYPE_PF (built-in variable), 49	·
pfnet.CONSTR_TYPE_REG_GEN (built-in variable), 49	Q (pfnet.Generator attribute), 35
pfnet.CONSTR_TYPE_REG_SHUNT (built-in vari-	Q (pfnet.Load attribute), 38
able), 49	Q (pfnet. VarGenerator attribute), 39
pfnet.CONSTR_TYPE_REG_TRAN (built-in variable),	Q_max (pfnet.Generator attribute), 35
49	Q_max (pfnet.VarGenerator attribute), 39
pfnet.CURRENT (built-in variable), 40	Q_min (pfnet.Generator attribute), 35
pfnet.FLAG_BOUNDED (built-in variable), 40	Q_min (pfnet.VarGenerator attribute), 39
pfnet.FLAG_FIXED (built-in variable), 40	Q_mis (pfnet.Bus attribute), 29
pfnet.FLAG_SPARSE (built-in variable), 40	_
pfnet.FLAG_VARS (built-in variable), 40	R
pfnet.FUNC_TYPE_GEN_COST (built-in variable), 48	ratingA (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_PHASE (built-in variable), 48	ratingB (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_PQ (built-in variable), 47	ratingC (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_RATIO (built-in variable), 48	ratio (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_SUSC (built-in variable), 48	ratio_max (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_VANG (built-in variable), 47	ratio_min (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_REG_VMAG (built-in variable), 47	reg_bus (pfnet.Branch attribute), 34
pfnet.FUNC_TYPE_SLIM_VMAG (built-in variable),	reg_bus (pfnet.Generator attribute), 36
47	reg_bus (pfnet.Shunt attribute), 37
pfnet.FUNC_TYPE_SP_CONTROLS (built-in variable),	reg_gens (pfnet.Bus attribute), 31
48	reg_shunts (pfnet.Bus attribute), 31
pfnet.FUNC_TYPE_UNKNOWN (built-in variable), 47	reg_trans (pfnet.Bus attribute), 31
pfnet.GEN_PROP_ANY (built-in variable), 34	reg_trans (prifet.bus attribute), 31
pfnet.GEN_PROP_NOT_REG (built-in variable), 35	S
pfnet.GEN_PROP_NOT_SLACK (built-in variable), 35	
pfnet.GEN_PROP_P_ADJUST (built-in variable), 35	scipy.sparse.coo_matrix (built-in class), 27
pfnet.GEN_PROP_REG (built-in variable), 35	sens_P_balance (pfnet.Bus attribute), 31
pfnet.GEN_PROP_SLACK (built-in variable), 34	sens_P_l_bound (pfnet.Branch attribute), 34
pfnet.GEN_VAR_P (built-in variable), 35	sens_P_l_bound (pfnet.Generator attribute), 36
pfnet.GEN_VAR_Q (built-in variable), 35	sens_P_u_bound (pfnet.Branch attribute), 34
pfnet.GOEV_VINC_Q (built in variable), 39 pfnet.LOWER_LIMIT (built-in variable), 40	sens_P_u_bound (pfnet.Generator attribute), 36
r	

```
sens O balance (pfnet.Bus attribute), 31
                                                          view() (pfnet.Graph method), 47
sens_v_ang_l_bound (pfnet.Bus attribute), 31
                                                           W
sens v ang u bound (pfnet.Bus attribute), 31
sens_v_mag_l_bound (pfnet.Bus attribute), 31
                                                          weight (pfnet.Function attribute), 48
sens_v_mag_u_bound (pfnet.Bus attribute), 31
                                                          write() (pfnet.Graph method), 47
sens v reg by gen (pfnet.Bus attribute), 31
                                                          X
sens v reg by shunt (pfnet.Bus attribute), 31
sens v reg by tran (pfnet.Bus attribute), 31
                                                          x (pfnet.Problem attribute), 53
set edges property() (pfnet.Graph method), 47
set_flags() (pfnet.Network method), 45
set_flags_of_component() (pfnet.Network method), 45
set_layout() (pfnet.Graph method), 47
set_network() (pfnet.Problem method), 52
set_nodes_property() (pfnet.Graph method), 47
set_var_values() (pfnet.Network method), 46
show() (pfnet.Bus method), 31
show() (pfnet.Problem method), 52
show buses() (pfnet.Network method), 46
show_components() (pfnet.Network method), 46
show properties() (pfnet.Network method), 46
Shunt (class in pfnet), 37
shunt b vio (pfnet.Network attribute), 46
shunt_v_vio (pfnet.Network attribute), 46
shunts (pfnet.Network attribute), 46
store sensitivities() (pfnet.Constraint method), 50
store sensitivities() (pfnet.Problem method), 52
Т
tran_p_vio (pfnet.Network attribute), 46
tran_r_vio (pfnet.Network attribute), 46
tran_v_vio (pfnet.Network attribute), 46
type (pfnet.Constraint attribute), 51
type (pfnet.Function attribute), 48
u (pfnet.Constraint attribute), 51
u (pfnet.Problem attribute), 53
update lin() (pfnet.Problem method), 53
update network() (pfnet.Constraint method), 51
update network() (pfnet.Function method), 48
update properties() (pfnet.Network method), 46
update_set_points() (pfnet.Network method), 46
V
v_ang (pfnet.Bus attribute), 31
v_mag (pfnet.Bus attribute), 31
v_max (pfnet.Bus attribute), 32
v_min (pfnet.Bus attribute), 32
v set (pfnet.Bus attribute), 32
var_generators (pfnet.Network attribute), 46
vargen corr radius (pfnet.Network attribute), 46
vargen_corr_value (pfnet.Network attribute), 46
VarGenerator (class in pfnet), 38
```

vargens (pfnet.Bus attribute), 32