# **PFNET Python Documentation**

Release 1.2

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Welcome! This is the documentation for the Python wrapper of PFNET, last updated March 29, 2016.

#### What is PFNET?

PFNET is a library for modeling and analyzing electric power networks. It provides data parsers, network visualization routines, and fast and customizable constraint and objective function evaluators for modeling network optimization problems.

#### License

PFNET is released under the BSD 2-clause license.

#### Citing

If you use PFNET in your work, please cite the software as follows:

```
@misc{pfnet,
   author={Tinoco De Rubira, Tomas},
   title={{PFNET}: A library for modeling and analyzing electric power networks},
   howpublished={\url{https://github.com/ttinoco/PFNET}},
   month={July},
   year={2015}
}
```

#### Contact

If you have any questions about PFNET or if you are interested in collaborating, send me an email:

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#### **Documentation Contents**

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**CHAPTER** 

ONE

# **GETTING STARTED**

This section describes how to get started with PFNET in Python. In particular, it covers required packages, installation, and provides a quick example showing how to use this package.

# 1.1 Dependencies

PFNET for Python has the following dependencies:

- Numpy (>=1.8.2): the fundamental package for scientific computing in Python.
- Scipy (>=0.13.3): a collection of mathematical algorithms and functions built on top of Numpy.
- PFNET: underlying C routines wrapped by this package (libpfnet).
- Graphviz (>= 2.38): graph visualization library (libgvc) (Optional).
- Raw parser (>=1.0): library for parsing power flow files in PSSE raw format version 32 (libraw\_parser) (Optional).

# 1.2 Download

The latest version of PFNET can be downloaded from https://github.com/ttinoco/PFNET.

# 1.3 Installation

After building the C library libpfnet, the PFNET Python module can be installed using:

```
> sudo python setup.py install
```

from the python directory of the PFNET package.

If libpfnet was built without visualization capabilities, the argument --no\_graphviz should be passed to setup.py. Similarly, if libpfnet was build without raw parsing capabilities, the argument --no\_raw\_parser should be passed to setup.py.

The installation can be tested using nose as follows:

```
> nosetests -v
```

# 1.4 Example

As a quick example of how to use the PFNET Python module, consider the task of constructing a power network from a MATPOWER-converted power flow file and computing the average bus degree. This can be done as follows:

```
>>> import numpy as np
>>> from pfnet import Network

>>> net = Network()
>>> net.load('ieee14.mat')

>>> print np.average([b.degree for b in net.buses])
2.86
```

**CHAPTER** 

**TWO** 

# **POWER NETWORKS**

This section describes how to load and analyze power networks using PFNET.

# 2.1 Overview

Power networks in PFNET are represented by objects of type Network. These objects are initially empty and need to be loaded with data contained in specific types of files. Once the data is loaded, the network and its components can be analyzed, visualized, and used to construct network optimization problems. After a network optimization problem is solved, the network object can be updated with the solution to perform further analysis.

An important attribute of the Network class is base\_power. This quantity, which has units of MVA, is useful for converting power quantities in per unit system base power to MW or MVAr.

# 2.2 Loading Data

Power networks can be loaded with data using the load() class method. This method takes as input the filename of a supported power flow file. Information about the data parsers available in PFNET and the supported file formats can be found in Section *Data Parsers*. The following simple example shows how to load data from a power flow mat file:

```
>>> from pfnet import Network
>>> net = Network()
>>> print net.num_buses
0
>>> net.load('ieee14.mat')
>>> print net.num_buses
14
```

# 2.3 Components

Power networks have several components. These are *buses*, *branches*, *generators*, *shunt devices*, *loads*, and *variable generators* (*i.e.*, non-dispatchable). For obtaining an overview of the components that form a network, the class method show\_components () can be used:

```
>>> net.show_components()

Network Components
-----
```

```
buses
               : 14
 slack
               : 1
               : 5
 reg by gen
 reg by tran
 reg by shunt
shunts
 fixed
 switched v
             : 0
branches
              : 17
 lines
 fixed trans : 3
 phase shifters : 0
 tap changers v : 0
 tap changers Q : 0
generators : 5
 slack
               : 1
 reg
loads
               : 11
vargens
```

#### 2.3.1 **Buses**

Buses in a power network are objects of type Bus. Each bus has an index, a number, and a name attribute that can be used to identify this bus in a network. The index is associated with the location of the bus in the underlying C array of bus structures, while the number and name attributes are specified in the input data. An index, a number, or a name can be used to extract a specific bus from a network using the Network class methods get\_bus(), get\_bus\_by\_number(), and get\_bus\_by\_name(), respectively:

```
>>> bus = net.get_bus(10)
>>> print bus.index == 10
True
>>> other_bus = net.get_bus_by_number(bus.number)
>>> print bus == other_bus
True
```

For convenience, a list of all the buses in the network is contained in the buses attribute of the Network class.

Buses in a network can have different properties. For example, some buses can be slack buses and others can have their voltage magnitudes regulated by generators, tap-changing transformers, or switched shunt devices. The Bus class provides methods for checking whether a bus has specific properties. The following example shows how to get a list of all the buses whose voltage magnitudes are regulated by generators:

```
>>> reg_buses = [b for b in net.buses if b.is_regulated_by_gen()]
>>> print len(reg_buses), net.get_num_buses_reg_by_gen()
5 5
```

A bus also has information about the devices that are connected to it or that are regulating its voltage magnitude. For example, the attributes gens and reg\_trans contain a list of generators connected to the bus and a list of tap-changing transformers regulating its voltage magnitude, respectively.

#### 2.3.2 Branches

Branches in a power network are objects of type Branch and are represented mathematically by the model described in Section 2.1.2 of [TTR2015]. Each branch has an index attribute that can be used to identify this branch in a network. The Network class method get\_branch() can be used to extract a branch of a given index:

```
>>> branch = net.get_branch(5)
>>> print branch.index == 5
True
```

For convenience, a list of all the branches in the network is contained in the branches attribute of the Network class.

Branches in a power network can have different properties. Fore example, some branches can be transmission lines, fixed transformers, tap-changing transformers, or phase-shifting transformers. Tap-changing transformers in turn can control the reactive power flowing through the branch or the voltage magnitude of a bus. The Branch class provides methods for checking whether a branch has specific properties. The following example shows how to get a list of all the branches that are transmission lines:

```
>>> lines = [br for br in net.branches if br.is_line()]
>>> print len(lines), net.get_num_lines()
17 17
```

For branches that are transformers, the Branch class attributes ratio and phase correspond to the transformer's tap ratio and phase shift, respectively. These attributes correspond to the quantities  $a_{km}$  and  $\phi_{km}$  of the branch model described in Section 2.1.2 of [TTR2015]. The quantity  $a_{mk}$  in this model is always one.

#### 2.3.3 Generators

Generators in a power network are objects of type Generator. Each generator has an index attribute that can be used to identify this generator in a network. The Network class method get\_gen() can be used to extract a generator of a given index:

```
>>> gen = net.get_gen(2)
>>> print gen.index == 2
True
```

For convenience, a list of all the generators in the network is contained in the generators attribute of the Network class

Generators in a power network can have different properties. Fore example, some generators can be slack generators and others can provide bus voltage magnitude regulation. The Generator class provides methods for checking whether a generator has specific properties. The following example shows how to get a list of all the slack generators:

```
>>> slack_gens = [g for g in net.generators if g.is_slack()]
>>> print len(slack_gens), net.get_num_slack_gens()
1 1
```

The active and reactive powers that a generator injects into the bus to which it is connected are obtained from the P and Q attributes of the Generator class. These quantities are given in units of per unit system base power. The following example computes the total active power injected into the network by generators in units of MW:

```
>>> print sum([g.P for g in net.generators])*net.base_power 272.4
```

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#### 2.3.4 Shunt Devices

Shunt devices in a power network are objects of type Shunt. Each shunt has an index attribute that can be used to identify this shunt in a network. The Network class method get\_shunt() can be used to extract a shunt of a given index:

```
>>> shunt = net.get_shunt(0)
>>> print shunt.index == 0
True
```

For convenience, a list of all the shunt devices in the network is contained in the shunts attribute of the Network class.

As other network components, shunt devices can have different properties. Some shunt devices can be fixed while others can be switchable and configured to regulate a bus voltage magnitude.

### 2.3.5 Loads

Loads in a power network are objects of type Load. As other components, the index attribute is used to identify a load in the network. A list of all the loads in the network is contained in the loads attribute of the Network class.

Similar to generators, the active and reactive powers that a load consumes from the bus to which it is connected are obtained from the P and Q attributes of the Load class. They are also given in units of per unit system base power.

#### 2.3.6 Variable Generators

Variable generators in a power network are objects of type VarGenerator. They represent non-dispatchable energy sources such as wind generators or farms and photovoltaic power plants. As with other components, the index attribute is used to identify a variable generator in the network. In addition to the index attribute, a name attribute is also available, which can be used to extract a specific variable generator from the network using the Network class method get\_vargen\_by\_name(). A list of all the variable generators in the network is also contained in the var\_generators attribute of the Network class.

Similar to generators, the active and reactive powers produced by a variable generator are obtained from the P and Q attributes of the VarGenerator class in units of per unit system base power. This is the output of the device in the absence of uncertainty. When there is uncertainty, the output of the device is subject to variations about P that have a standard deviation given by the attribute  $P_std$ . Output limits of a variable generator are given by the  $P_min$ ,  $P_max$ ,  $Q_min$ , and  $Q_max$  attributes.

The output of variable generators in a network are subject to random variations that can be correlated, especially for devices that are "nearby". The method <code>create\_vargen\_P\_sigma()</code> of the <code>Network</code> class allows constructing a covariance matrix for these variations based on a "correlation distance" N and a given correlation coefficient. The cross-covariance between the variation of two devices that are connected to buses that are less than N branches away from each other are set such that they have the given correlation coefficient.

Lastly, since many power network input files do not have variable generator information, these devices can be added to the network by using the add\_vargens() method of the Network class.

# 2.4 Properties

A Network object has several quantities or properties that provide important information about the state of the network. The following table provides a description of each of these properties.

Names	Description	Units
bus_v_max	Maximum bus voltage magnitude  Minimum bus voltage magnitude	
bus_v_min		
bus_v_vio	Maximum bus voltage magnitude limit violation	per unit
bus_P_mis	Maximum absolute bus reactive power mismatch gen_P_cost Total active power generation cost gen_v_dev Maximum set point deviation of generator-regulated voltage gen_Q_vio Maximum generator reactive power limit violation gen_P_vio Maximum generator active power limit violation tran_v_vio Maximum band violation of transformer-regulated voltage tran_r_vio Maximum tap ratio limit violation of tap-changing transformer tran_p_vio Maximum phase shift limit violation of phase-shifting transformer shunt_v_vio Maximum band violation of shunt-regulated voltage shunt_b_vio Maximum susceptance limit violation of switched shunt device	
bus_Q_mis		
gen_P_cost		
gen_v_dev		
gen_Q_vio		
gen_P_vio		
tran_v_vio		
tran_r_vio		
tran_p_vio		
shunt_v_vio		
shunt_b_vio		
num_actions		

All of these properties are attributes of the Network class. If there is a change in the network, the class method update\_properties() needs to be called in order for the network properties to reflect the change. The following example shows how to update and extract properties:

```
>>> print net.bus_v_max
1.09
>>> for bus in net.buses:
...     bus.v_mag = bus.v_mag + 0.1
...
>>> print net.bus_v_max
1.09
>>> net.update_properties()
>>> print net.bus_v_max
1.19
```

For convenience, all the network properties can be extracted at once in a dictionary using the get\_properties() class method:

```
>>> properties = net.get_properties()
>>> print properties['bus_v_max']
1.19
```

# 2.5 Variables

Network quantities can be specified to be variables. This is useful to represent network quantities with vectors and turn the network properties described above as functions of these vectors.

To set network quantities as variables, the Network class method set\_flags() is used. This method takes as arguments a *component type*, a *flag mask* for specifying which flags types to set, a property mask for targeting components with specific properties, and a variable mask for specifying which component quantities should be affected.

**Property masks** are component-specific. They can be combined using logical OR to make properties more complex. More information can be found in the following sections:

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- Bus Property Masks
- Branch Property Masks
- Generator Property Masks
- Shunt Property Masks
- Variable Generator Property Masks

**Variable masks** are also component-specific. They can be combined using logical OR to target more than one component quantity. More information can be found in the following sections:

- Bus Variable Masks
- Branch Variable Masks
- Generator Variable Masks
- Shunt Variable Masks
- Variable Generator Variable Masks

The following example shows how to set as variables all the voltage magnitudes and angles of buses regulated by generators:

Network components have a has\_flags() method that allows checking whether flags of a certain type associated with specific quantities are set.

Once variables have been set, the *vector* containing all the current variable values can be extracted using get\_var\_values():

```
>>> values = net.get_var_values()
>>> print type(values)
<type 'numpy.ndarray'>
>>> print values.shape
(10,)
```

The components that have quantities set as variables have indices that can be used to locate these quantities in the vector of all variable values:

```
>>> bus = [b for b in net.buses if b.is_reg_by_gen()][0]
>>> print bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VMAG)
True
```

```
>>> bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VANG)
True
>>> print bus.v_mag, net.get_var_values()[bus.index_v_mag]
1.09 1.09
>>> print bus.v_ang, net.get_var_values()[bus.index_v_ang]
-0.23 -0.23
```

A vector of variable values can be used to update the corresponding network quantities. This is done with the Network class method set\_var\_values():

```
>>> bus.has_flags(pf.FLAG_VARS,pf.BUS_VAR_VANG)
True
>>> values = net.get_var_values()
>>> print bus.v_mag
1.09
>>> values[bus.index_v_mag] = 1.20
>>> net.set_var_values(values)
>>> print bus.v_mag
1.20
```

As we will see in later, variables are also useful for constructing network optimization problems.

The class method get\_var\_values() can also be used to get upper or lower limits of the variables. To do this, a valid *variable value code* must be passed to this method.

In addition to the class method <code>set\_flags()</code>, which allows specifying variables of components having certain properties, one can also use the <code>Network</code> class method <code>set\_flags\_of\_component()</code> to specify variables of individual components. This is useful when the desired components cannot be targeted using a <code>property mask</code>. For example, the following code illustrates how to set as variables the voltage magnitudes of buses whose indices are multiples of three:

```
>>> net.clear_flags()
>>> for bus in net.buses:
... if bus.index % 3 == 0:
... net.set_flags_of_component(bus,pf.FLAG_VARS,pf.BUS_VAR_VMAG)
>>> print net.num_vars, len([b for b in net.buses if b.index % 3 == 0]), net.num_buses
5 5 14
```

# 2.6 Projections

As explained above, once the network variables have been set, a vector with the current values of the selected variables is obtained with the class method <code>get\_var\_values()</code>. To extract subvectors that contain values of specific variables, projection matrices can be used. These *matrices* can be obtained using the class method <code>get\_var\_projection()</code>, which take as arguments a *component type* and a <code>variable mask</code>, <code>e.g.</code>, <code>bus variable masks</code>. The next example sets the variables of the network to be the bus voltage magnitudes and angles of all the buses, extracts the vector of values of all variables, and then extracts two subvectors having only voltage magnitudes and only voltage angles, respectively:

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```
>>> import numpy as np
>>> import pfnet as pf
>>> net = pf.Network()
>>> net.load('ieee14.mat')
>>> net.set_flags(pf.OBJ_BUS,
                 pf.FLAG_VARS,
                  pf.BUS_PROP_ANY,
. . .
                  pf.BUS_VAR_VMAG|pf.BUS_VAR_VANG)
. . .
>>> print net.num_vars, 2*net.num_buses
28 28
>>> P1 = net.get_var_projection(pf.OBJ_BUS,pf.BUS_VAR_VMAG)
>>> P2 = net.get_var_projection(pf.OBJ_BUS,pf.BUS_VAR_VANG)
>>> print type(P1)
<class 'scipy.sparse.coo.coo_matrix'>
>>> x = net.get_var_values()
>>> v_mags = P1*x
>>> v_angs = P2*x
>>> print v_mags
[ 1.036    1.05    1.055    1.057    1.051    1.056    1.09    1.062    1.07    1.02
 1.019 1.01 1.045 1.06]
>>> print v_angs
 [-0.27995081 \ -0.26459191 \ -0.26302112 \ -0.2581342 \ -0.26354472 \ -0.26075219 ] 
 -0.23317599 \ -0.23335052 \ -0.24818582 \ -0.15323991 \ -0.18029251 \ -0.22200588
-0.0869174 0.]
>>> print np.linalg.norm(x - (P1.T*v_mags+P2.T*v_angs))
0.0
```

**CHAPTER** 

THREE

# **DATA PARSERS**

This section describes the different data parsers available in PFNET and the supported file types.

# 3.1 MATPOWER case files

MATPOWER is a MATLAB package for solving power flow and optimal power flow problems. It contains several power flow and optimal power flow cases defined in MATLAB files. These "M" files can be converted to CSV files using the script mpc2mat.m. These MATPOWER-converted CSV files have extension.mat and can be used to load power networks in PFNET.

# 3.2 ARTERE case files

PFNET can load networks from case files used by ARTERE, which is a software for performing power flow computations using the Newton-Raphson method. These files should have extension .art. Details about these data files can be found in the document "ARTERE: description of data files".

Currently, PFNET has limited support of these files. More specifically:

- Components with open breakers are ignored.
- For LTC-V devices, tap positions are treated as continuous and the optional fields are ignored.
- The SWITCH, TRFO, PSHIFT-P, TURLIM, SVC, LFRESV, BUSPART and BRAPART records are not supported.
- Computation control parameters are ignored.

# 3.3 RAW case files

If built with raw parsing capabilities, which requires linking PFNET with <code>libraw\_parser</code>, PFNET can load power networks from files with extension <code>.raw</code>. These files are used by the software PSS ® E and are widely used by North American power system operators.

**CHAPTER** 

# **FOUR**

# **VISUALIZATION**

This section describes how to visualize power networks using PFNET. To have this capability, PFNET needs the Graphviz library libgue.

# 4.1 Overview

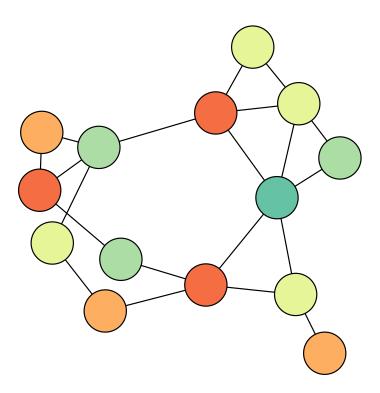
To visualize a power network, a Graph objects needs to be created. To do this, one needs to specify the power Network that is to be associated with the graph:

```
>>> import pfnet as pf
>>> net = pf.Network()
>>> net.load('ieee14.mat')
>>> g = pf.Graph(net)
```

Then, a layout must be created for graph. This can be done using the Graph class method set\_layout. This method uses the sfdp algorithm of Graphviz.

The Graph class provides routines for coloring nodes (network buses) according to different criteria. For example, buses can be colored according to reactive power mismatches:

```
>>> g.set_layout()
>>> g.color_nodes_by_mismatch(pf.BUS_MIS_REACTIVE)
>>> g.view()
```



# **OPTIMIZATION PROBLEMS**

This section describes how to formulate power network optimization problems using PFNET.

# 5.1 Objective Function

The objective function  $\phi$  for a network optimization problem created using PFNET is of the form

$$\varphi(x) = \sum_{i} w_i \varphi_i(x),$$

where  $w_i$  are weights,  $\varphi_i$  are general linear or nonlinear functions, and x is a vector of values of network quantities that have been set as variables. Each weight-function pair in the summation is represented by an object of type Function. To instantiate an object of this type, the function type and weight need to be specified as well as the Network object that is to be associated with the function. The following example sets all bus voltage magnitudes as variables and constructs a function that penalizes voltage magnitude deviations from ideal values:

After a Function object is created, its value, gradient and Hessian are zero, an empty vector, and an empty matrix, respectively. Before evaluating the function at a specific vector of values, it must be analyzed using the Function class method analyze. This routine analyzes the function and allocated the required vectors and matrices for storing its gradient and Hessian. After this, the function can be evaluated using the method eval:

```
>>> x = net.get_var_values()
>>> func.analyze()
```

```
>>> func.eval(x + 0.01)
>>> func.eval(x)
```

The value  $\varphi_i(x)$ , gradient  $\nabla \varphi_i(x)$  and Hessian  $\nabla^2 \varphi_i(x)$  of a function can then be extracted from the phi, gphi and Hphi attributes, respectively:

```
>>> print x.shape
14
>>> print func.phi
0.255
>>> print type(func.gphi), func.gphi.shape
<type 'numpy.ndarray'> (14,)
>>> print type(func.Hphi), func.Hphi.shape
<class 'scipy.sparse.coo.coo_matrix'> (14, 14)
```

For the Hessian matrix, only the lower triangular part is stored.

Details about each of the different function types available in PFNET are provided below.

# 5.1.1 Voltage magnitude regularization

This function is of type FUNC\_TYPE\_REG\_VMAG. It penalizes deviations of bus voltage magnitudes from ideal values. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_k \left( \frac{v_k - v_k^t}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left( \frac{v_k^y}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left( \frac{v_k^z}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left( \frac{v_k^h}{\Delta v} \right)^2 + \frac{1}{2} \sum_k \left( \frac{v_k^h}{\Delta v} \right)^2,$$

where v are bus voltage magnitudes,  $v^t$  are voltage magnitude set points (one for buses not regulated by generators),  $v^y$  and  $v^z$  are positive and negative deviations of v from  $v^t$ ,  $v^h$  and  $v^l$  are voltage band upper and lower limit violations, and  $\Delta v$  is a normalization factor. Only terms that include optimization variables are included in the summation.

# 5.1.2 Voltage magnitude soft limit penalty

This function is of type FUNC\_TYPE\_SLIM\_VMAG. It reduces voltage (soft) limit violations by penalizing deviations of bus voltage magnitudes from the mid point of their ranges. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left( \frac{v_k - \bar{v}_k}{\Delta v} \right)^2,$$

where v are bus voltage magnitudes,  $\bar{v}$  are the mid points of their ranges, and  $\Delta v$  is a normalization factor. Only terms that include optimization variables are included in the summation.

# 5.1.3 Voltage angle regularization

This function is of type FUNC\_TYPE\_REG\_VANG. It penalizes large bus voltage angles and voltage angle differences across branches. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left( \frac{\theta_k}{\Delta \theta} \right)^2 + \frac{1}{2} \sum_{(k,m)} \left( \frac{\theta_k - \theta_m - \phi_{km}}{\Delta \theta} \right)^2,$$

where  $\theta$  are bus voltage angles,  $\phi$  are branch phase shifts, and  $\Delta\theta$  is a normalization factor. Only terms that include optimization variables are included in the summation.

# 5.1.4 Generator powers regularization

This function is of type FUNC\_TYPE\_REG\_PQ. It penalizes deviations of generator powers from the midpoint of their ranges. It is defined by the expression

$$varphi(x) := \frac{1}{2} \sum_{k} \left( \frac{P_k^g - \bar{P}_k}{\Delta P} \right)^2 + \frac{1}{2} \sum_{k} \left( \frac{Q_k^g - \bar{Q}_k}{\Delta Q} \right)^2,$$

where  $P^g$  and  $Q^g$  are generator active and reactive powers,  $\bar{P}$  and  $\bar{Q}$  are midpoints of generator active and reactive power ranges, and  $\Delta P = \Delta Q$  are normalization factors. Only terms that include optimization variables are included in the summation.

# 5.1.5 Active power generation cost

This function is of type FUNC\_TYPE\_GEN\_COST. It measures active power generation cost by the expression

$$\varphi(x) := \sum_{k} q_{k0} + q_{k1} P_k^g + q_{k2} (P_k^g)^2,$$

where  $P^g$  are generator active powers in per unit base system power, and  $q^0$ ,  $q^1$ , and  $q^2$  are constant coefficients. These coefficients are attributes of each Generator object.

# 5.1.6 Transformer tap ratio regularization

This function is of type FUNC\_TYPE\_REG\_RATIO. It penalizes deviations of tap ratios of tap-changing transformers from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left( \frac{t_k - t_k^0}{\Delta t} \right)^2 + \frac{1}{2} \sum_{k} \left( \frac{t_k^y}{\Delta t} \right)^2 + \frac{1}{2} \sum_{k} \left( \frac{t_k^z}{\Delta t} \right)^2,$$

where t are tap ratios of tap-changing transformers,  $t^0$  are their initial values,  $t^y$  and  $t^z$  are positive and negative deviations of t from  $t^0$ , and  $\Delta t$  is a normalization factor. Only terms that include optimization variables are included in the summation.

# 5.1.7 Transformer phase shift regularization

This function is of type FUNC\_TYPE\_REG\_PHASE. It penalizes deviations of phase shifts of phase shifting transformers from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_{k} \left( \frac{\phi_k - \phi_k^0}{\Delta \phi} \right)^2$$

where  $\phi$  are phase shifts of phase-shifting transformers,  $\phi^0$  are their initial values, and  $\Delta\phi$  is a normalization factor. Only terms that include optimization variables are included in the summation.

## 5.1.8 Switched shunt susceptance regularization

This function is of type FUNC\_TYPE\_REG\_SUSC. It penalizes deviations of susceptances of switched shunt devices from their initial value. It is defined by the expression

$$\varphi(x) := \frac{1}{2} \sum_k \left( \frac{b_k - b_k^0}{\Delta b} \right)^2 + \frac{1}{2} \sum_k \left( \frac{b_k^y}{\Delta b} \right)^2 + \frac{1}{2} \sum_k \left( \frac{b_k^z}{\Delta b} \right)^2,$$

where b are susceptances of switched shunt devices,  $b^0$  are their initial values,  $b^y$  and  $b^z$  are positive and negative deviations of b from  $b^0$ , and  $\Delta b$  is a normalization factor. Only terms that include optimization variables are included in the summation.

# 5.1.9 Sparsity inducing penalty for controls

This function is of type FUNC\_TYPE\_SP\_CONTROLS. It encourages sparse control adjustments with the expression

$$\varphi(x) := \sum_{k} \sqrt{\left(\frac{u_k - u_k^0}{\Delta u_k}\right)^2 + \epsilon},$$

where u are control quantities,  $u^0$  are their current values, and  $\epsilon$  is a small positive scalar. The normalization factors  $\Delta u_k$  are given by

$$\Delta u_k := \max\{u_k^{\max} - u_k^{\min}, \delta\},\$$

where  $u^{\max}$  and  $u^{\min}$  are control limits, and  $\delta$  is a small positive scalar. The control quantities that are considered by this function are specified using the <code>Network</code> class methods <code>set\_flags()</code> or <code>set\_flags\_of\_component()</code> using the flag type <code>FLAG\_SPARSE</code>.

## 5.2 Constraints

Constraints in PFNET are of the form

$$Ax = b$$

$$f(x) = 0$$

$$l \le Gx \le u,$$

where A and G are matrices, b, l and u are vectors, f is a vector-valued nonlinear function, and x is a vector of values of network quantities that have been set as variables. They are represented by objects of type Constraint. To create an object of this type, the constraint type and the network to be associated with the constraint need to be specified. The following example sets all bus voltage magnitudes and angles as variables and constructs the power flow constraints:

Before a Constraint object can be used, it must be initialized using the Constraint class method analyze. This routine analyzes the constraint and allocates the required vectors and matrices. After this, the constraint can be evaluated using the method eval:

```
>>> x = net.get_var_values()
>>> constr.analyze()
>>> constr.eval(x + 0.01)
>>> constr.eval(x)
```

The matrices and vectors associated with the linear constraints can be extracted from the A, G, b, 1 and u attributes of the Constraint object. The vector of violations and Jacobian matrix of the nonlinear constraints can be extracted from the attributes f and J, respectively. Also, the Hessian matrix of any individual nonlinear constraint  $f_i(x) = 0$  can be extracted using the class method get\_H\_single. The following example shows how to extract the largest power flow mismatch in per unit system base power and the Hessian matrix corresponding to the active power balance constraint of a bus:

```
>>> import numpy as np
>>> f = constr.f

>>> print type(f), f.shape
<type 'numpy.ndarray'> (28,)

>>> print np.linalg.norm(f,np.inf)
0.042

>>> bus = net.get_bus(5)
>>> Hi = constr.get_H_single(bus.index_P)

>>> print type(Hi), Hi.shape, Hi.nnz
<class 'scipy.sparse.coo.coo_matrix'> (28, 28) 27
```

As before, all Hessian matrices have stored only the lower triangular part. In addition to being possible to extract Hessian matrices of individual nonlinear constraints, it is also possible to construct any linear combination of these individual Hessian matrices. This can be done using the Constraint class method combine\_H. After this, the resulting matrix can be extracted from the H combined attribute:

```
>>> coefficients = np.random.randn(f.size)
>>> constr.combine_H(coefficients)
>>> H = constr.H_combined
>>> print type(H), H.shape, H.nnz
<class 'scipy.sparse.coo.coo_matrix'> (28, 28) 564
```

Lastly, Lagrange multiplier estimates of the linear and constraints can be used to store sensitivity information in the network components associated with the constraints. This is done using the class method store\_sensitivities. Component-specific attributes that store sensitivity information are described in the *API Reference* section.

Details about each of the different constraint types available in PFNET are provided below.

### 5.2.1 AC Power balance

This constraint is of type CONSTR\_TYPE\_PF. It enforces active and reactive power balance at every bus of the network. It is given by

$$(P_k^g + jQ_k^g) - (P_k^l + jQ_k^l) - S_k^{sh} - \sum_{m \in [n]} S_{km} = 0, \ \forall \ k \in [n],$$

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where  $P^g$  and  $Q^g$  are generator active and reactive powers,  $P^l$  and  $Q^l$  are load active and reactive powers,  $S^{sh}$  are apparent powers flowing out of buses through branches,  $P^l$  are apparent powers flowing out of buses through branches,  $P^l$  is the number of buses, and  $P^l$  is the number of buses.

#### 5.2.2 DC Power balance

This constraint is of type CONSTR\_TYPE\_DCPF. It enforces "DC" active power balance at every bus of the network. It is given by

$$P_k^g - P_k^l + \sum_{m \in [n]} b_{km} (\theta_k - \theta_m - \phi_{km}) = 0, \ \forall \ k \in [n],$$

where  $P^g$  are generator active powers,  $P^l$  are load active powers,  $b_{km}$  are branch susceptances,  $\theta_k$  are bus voltage angles,  $\phi_{km}$  are phase shifts of phase-shifting transformers, n is the number of buses, and  $[n] := \{1, \ldots, n\}$ .

# 5.2.3 Branch DC power flow limits

This constraint is of type CONSTR\_TYPE\_DC\_FLOW\_LIM. It enforces branch "DC" power flow limits due to thermal ratings. It is given by

$$-P_{km}^{\max} \le -b_{km} \left(\theta_k - \theta_m - \phi_{km}\right) \le P_{km}^{\max}$$

for each branch (k, m), where  $b_{km}$  are branch susceptances,  $\theta_k$  are bus voltage angles,  $\phi_{km}$  are phase shifts of phase-shifting transformers, and  $P_{km}^{\max}$  are branch power flow limits.

# 5.2.4 Variable fixing

This constraint is of type <code>CONSTR\_TYPE\_FIX</code>. It constrains specific variables to be fixed at their current value. The variables to be fixed are specified using the <code>Network</code> class methods <code>set\_flags()</code> or <code>set\_flags\_of\_component()</code> with the flag type <code>FLAG\_FIXED</code>.

## 5.2.5 Variable bounding

This constraint is of type CONSTR\_TYPE\_BOUND. It constrains specific variables to be inside their bounds. The variables to be bounded are specified using the Network class methods set\_flags() or set\_flags\_of\_component() with the flag type FLAG\_BOUNDED. These constraints are expressed as nonlinear equality constraints using the techniques described in Section 4.3.3 of [TTR2015].

For conventional linear bounds, the constraint type CONSTR\_TYPE\_LBOUND can be used.

### 5.2.6 Generator participation

This constraint is of type CONSTR\_TYPE\_PAR\_GEN. It enforces specific active power participations among slack generators, and reactive power participations among generators regulating the same bus voltage magnitude. For slack generators, all participate with equal active powers. For voltage regulating generators, each one participates with the same fraction of its total resources. More specifically, this constraint enforces

$$P_k^g = P_m^g$$

for all slack generators k and m connected to the same bus, and

$$\frac{Q_k^g - Q_k^{\min}}{Q_k^{\max} - Q_k^{\min}} = \frac{Q_m^g - Q_m^{\min}}{Q_m^{\max} - Q_m^{\min}},$$

for all generators k and m regulating the same bus voltage magnitude, where  $Q^{\min}$  and  $Q^{\max}$  are generator reactive power limits.

# 5.2.7 Voltage set-point regulation by generators

This constraint is of type CONSTR\_TYPE\_REG\_GEN. It enforces voltage set-point regulation by generators. It approximates the constraints

$$v_k = v_k^t + v_k^y - v_k^z$$

$$0 \le (Q_k - Q_k^{\min}) \perp v_k^y \ge 0$$

$$0 \le (Q_k^{\max} - Q_k) \perp v_k^z \ge 0,$$

for each bus k whose voltage is regulated by generators, where v are bus voltage magnitudes,  $v^t$  are their set points,  $v^y$  and  $v^z$  are positive and negative deviations of v from  $v^t$ , and Q,  $Q^{\max}$  and  $Q^{\min}$  are aggregate reactive powers and limits of the generators regulating the same bus voltage magnitude.

# 5.2.8 Voltage band regulation by transformers

This constraint is of type CONSTR\_TYPE\_REG\_TRAN. It enforces voltage band regulation by tap-changing transformers. It approximates the constraints

$$\begin{split} t_k &= t_k^0 + t_k^y - t_k^z \\ 0 &\leq (v_k + v_k^l - v_k^{\min}) \perp t_k^y \geq 0 \\ 0 &\leq (v_k^{\max} - v_k + v_k^h) \perp t_k^z \geq 0 \\ 0 &\leq (t_k^{\max} - t_k) \perp v_k^l \geq 0 \\ 0 &\leq (t_k - t_k^{\min}) \perp v_k^l \geq 0, \end{split}$$

for each bus k whose voltage is regulated by tap-changing transformers, where v are bus voltage magnitudes,  $v^{\max}$  and  $v^{\min}$  are their band limits,  $v^l$  and  $v^h$  are voltage violations of band lower and upper limits, t are transformer tap ratios,  $t^0$ ,  $t^{\max}$  and  $t^{\min}$  are their current values and limits, and  $t^y$  and  $t^z$  are positive and negative deviations of t from  $t^0$ . The above equations assume that the sensitivity between voltage magnitude and transformer tap ratio is positive. If it is negative,  $t^y$  and  $t^z$  are interchanged in the first two complementarity constraints, and  $v^l$  and  $v^h$  are interchanged in the bottom two complementarity constraints.

# 5.2.9 Voltage band regulation by switched shunts

This constraint is of type CONSTR\_TYPE\_REG\_SHUNT. It enforces voltage band regulation by switched shunt devices. It approximates the constraints

$$\begin{split} b_k &= b_k^0 + b_k^y - b_k^z \\ 0 &\leq (v_k + v_k^l - v_k^{\min}) \perp b_k^y \geq 0 \\ 0 &\leq (v_k^{\max} - v_k + v_k^h) \perp b_k^z \geq 0 \\ 0 &\leq (b_k^{\max} - b_k) \perp v_k^l \geq 0 \\ 0 &\leq (b_k - b_k^{\min}) \perp v_k^l \geq 0, \end{split}$$

for each bus k whose voltage is regulated by switched shunt devices, where v are bus voltage magnitudes,  $v^{\max}$  and  $v^{\min}$  are their band limits,  $v^l$  and  $v^h$  are voltage violations of band lower and upper limits, b are switched shunt susceptances,  $b^0$ ,  $b^{\max}$  and  $b^{\min}$  are their current values and limits, and  $b^y$  and  $b^z$  are positive and negative deviations of b from  $b^0$ .

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# 5.3 Problems

Optimization problems constructed with PFNET are of the form

```
\begin{array}{ll} \text{minimize} & \varphi(x) \\ \text{subject to} & Ax = b \\ & f(x) = 0 \\ & l \leq Gx \leq u, \end{array}
```

As already noted, the objective function  $\varphi$  is a weighted sum of functions  $\varphi_i$ . The linear and nonlinear constraints  $Ax = b, l \leq Gx \leq u$ , and f(x) = 0 correspond to one or more of the constraints described above. An optimization problem in PFNET is represented by an object of type Problem.

After instantiation, a Problem is empty and one needs to specify the Network that is to be associated with the problem, the Constraints to include, and the Functions that form the objective function. This can be done using the Problem class methods set\_network, add\_constraint, and add\_function. The following example shows how to construct a simple power flow problem and solve it using the Newton-Raphson method:

```
import pfnet as pf
from numpy import hstack
from numpy.linalg import norm
from scipy.sparse import bmat
from scipy.sparse.linalg import spsolve
def NRsolve(net):
    net.clear_flags()
    # bus voltage angles
    net.set_flags(pf.OBJ_BUS,
                  pf.FLAG_VARS,
                  pf.BUS_PROP_NOT_SLACK,
                  pf.BUS_VAR_VANG)
    # bus voltage magnitudes
    net.set_flags(pf.OBJ_BUS,
                  pf.FLAG_VARS,
                  pf.BUS_PROP_NOT_REG_BY_GEN,
                  pf.BUS_VAR_VMAG)
    # slack gens active powers
    net.set_flags(pf.OBJ_GEN,
                  pf.FLAG_VARS,
                  pf.GEN_PROP_SLACK,
                  pf.GEN_VAR_P)
    # regulator gens reactive powers
    net.set_flags(pf.OBJ_GEN,
                  pf.FLAG_VARS,
                  pf.GEN_PROP_REG,
                  pf.GEN_VAR_Q)
    p = pf.Problem()
    p.set_network(net)
    p.add_constraint(pf.CONSTR_TYPE_PF)
                                                 # power flow
    p.add_constraint(pf.CONSTR_TYPE_PAR_GEN_P) # generator participation
    p.add_constraint(pf.CONSTR_TYPE_PAR_GEN_Q) # generator participation
```

```
p.analyze()

x = p.get_init_point()
p.eval(x)

residual = lambda x: hstack((p.A*x-p.b,p.f))

while norm(residual(x)) > 1e-4:
    x = x + spsolve(bmat([[p.A],[p.J]],format='csr'),-residual(x))
    p.eval(x)

net.set_var_values(x)
net.update_properties()
```

The above routine can then be used as follows:

```
>>> net = Network()
>>> net.load('case3012wp.mat')
>>> print net.bus_P_mis, net.bus_Q_mis
2.79e+0 1.56e+1
>>> NRsolve(net)
>>> print net.bus_P_mis, net.bus_Q_mis
2.37e-6 3.58e-6
```

As shown in the example, the Problem class method analyze needs to be called before the vectors and matrices associated with the problem constraints and functions can be used. The method eval can then be used for evaluating the problem objective and constraint functions at different points. As is the case for Constraints, a Problem has a method combine\_H for forming linear combinations of individual constraint Hessians, and a method store\_sensitivities for storing sensitivity information in the network components associated with the constraints.

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**CHAPTER** 

SIX

# **API REFERENCE**

# 6.1 Vector

class numpy.ndarray
See numpy documentation.

# 6.2 Matrix

class scipy.sparse.coo\_matrix
 See scipy documentation.

# 6.3 Bus

# 6.3.1 Bus Property Masks

pfnet.BUS\_PROP\_ANY Any bus.

pfnet.BUS\_PROP\_SLACK
Slack bus.

 ${\tt pfnet.BUS\_PROP\_REG\_BY\_GEN}$ 

Bus voltage magnitude is regulated by generators.

pfnet.BUS\_PROP\_REG\_BY\_TRAN

Bus voltage magnitude is regulated by tap-changing transformers.

pfnet.BUS\_PROP\_REG\_BY\_SHUNT

Bus voltage magnitude is regulated by switched shunt devices.

pfnet.BUS\_PROP\_NOT\_REG\_BY\_GEN

Bus voltage magnitude is not regulated by generators.

pfnet.BUS\_PROP\_NOT\_SLACK

Bus is not slack.

# 6.3.2 Bus Variable Masks

pfnet.BUS\_VAR\_VMAG

Voltage magnitude.

#### pfnet.BUS\_VAR\_VANG

Voltage angle.

#### pfnet.BUS\_VAR\_VDEV

Voltage magnitude positive and negative set point deviations.

#### pfnet.BUS VAR VVIO

Voltage magnitude upper and lower bound violations.

#### 6.3.3 Bus Sensitivities

#### pfnet.BUS\_SENS\_LARGEST

Largest objective function sensitivity with respect to constraints involving this bus.

#### pfnet.BUS\_SENS\_P\_BALANCE

Objective function sensitivity with respect to active power balance.

#### pfnet.BUS\_SENS\_Q\_BALANCE

Objective function sensitivity with respect to reactive power balance.

#### pfnet.BUS SENS V MAG U BOUND

Objective function sensitivity with respect to voltage magnitude upper bound.

#### pfnet.BUS\_SENS\_V\_MAG\_L\_BOUND

Objective function sensitivity with respect to voltage magnitude lower bound.

#### pfnet.BUS\_SENS\_V\_ANG\_U\_BOUND

Objective function sensitivity with respect to voltage angle upper bound.

#### pfnet.BUS\_SENS\_V\_ANG\_L\_BOUND

Objective function sensitivity with respect to voltage angle lower bound.

#### pfnet.BUS\_SENS\_V\_REG\_BY\_GEN

Objective function sensitivity with respect to voltage magnitude regulation by generators.

#### pfnet.BUS\_SENS\_V\_REG\_BY\_TRAN

Objective function sensitivity with respect to voltage magnitude regulation by tap-changing transformers.

#### pfnet.BUS SENS V REG BY SHUNT

Objective function sensitivity with respect to voltage magnitude regulation by switched shunt devices.

#### 6.3.4 Bus Power Mismatches

#### pfnet.BUS\_MIS\_LARGEST

Largest bus power mismatch.

#### pfnet.BUS\_MIS\_ACTIVE

Bus active power mismatch.

### pfnet.BUS\_MIS\_REACTIVE

Bus reactive power mismatch.

#### 6.3.5 Bus Class

#### class pfnet .Bus (alloc=True)

Bus class.

Parameters alloc: {True, False}

# P mis Bus active power mismatch (p.u. system base MVA) (float). Q mis Bus reactive power mismatch (p.u. system base MVA) (float). branches List of branches incident on this bus (list). branches from List of branches that have this bus on the "from" side (list). branches to List of branches that have this bus on the "to" side (list). degree Bus degree (number of incident branches) (float). gens List of generators connected to this bus (list). get\_largest\_mis(self) Gets the bus power mismatch of largest absolute value. Returns mis: float get\_largest\_mis\_type (self) Gets the type of bus power mismatch of largest absolute value. **Returns type**: int get\_largest\_sens(self) Gets the bus sensitivity of largest absolute value. Returns sens: float get\_largest\_sens\_type (self) Gets the type of bus sensitivity of largest absolute value. Returns type: int get\_quantity (self, type) Gets the bus quantity of the given type. **Parameters type**: int (Bus Sensitivities:, Bus Power Mismatches) Returns value: float get\_total\_gen\_P (self) Gets the total active power injected by generators connected to this bus. Returns P: float get\_total\_gen\_Q(self) Gets the total reactive power injected by generators connected to this bus. **Returns Q**: float

 $\begin{tabular}{ll} \bf gen\_Q\_min~(self)\\ \hline Gets~the~smallest~total~reactive~power~that~can~be~injected~by~generators~connected~to~this~bus. \\ \end{tabular}$ 

Gets the largest total reactive power that can be injected by generators connected to this bus.

get\_total\_gen\_Q\_max(self)

Returns Q\_max: float

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```
Returns Q_min: float
get_total_load_P (self)
     Gets the total active power consumed by loads connected to this bus.
         Returns P: float
get total load Q(self)
     Gets the total reactive power consumed by loads connected to this bus.
         Returns Q: float
get_total_shunt_b (self)
     Gets the combined susceptance of shunt devices connected to this bus.
         Returns b: float
get_total_shunt_g(self)
     Gets the combined conductance of shunt devices connected to this bus.
         Returns g: float
has flags (self, fmask, vmask)
     Determines whether the bus has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Bus Variable Masks)
         Returns flag: {True, False}
index
     Bus index (int).
index P
     Index of bus active power mismatch (int).
index 0
     Index for bus reactive power mismatch (int).
index_v_ang
     Index of voltage angle variable (int).
index v mag
     Index of voltage magnitude variable (int).
index vh
     Index of voltage high limit violation variable (int).
index vl
     Index of voltage low limit violation variable (int).
index y
     Index of voltage magnitude positive deviation variable (int).
index_z
     Index of voltage magnitude negative deviation variable (int).
is_regulated_by_gen(self)
     Determines whether the bus is regulated by a generator.
         Returns flag: {True, False}
```

is regulated by shunt (self)

Determines whether the bus is regulated by a shunt device.

```
Returns flag: {True, False}
```

#### is\_regulated\_by\_tran(self)

Determines whether the bus is regulated by a transformer.

```
Returns flag: {True, False}
```

#### is slack (self)

Determines whether the bus is a slack bus.

```
Returns flag: {True, False}
```

#### loads

List of loads connected to this bus (list).

#### name

Bus name (sting).

#### number

Bus number (int).

#### obj\_type

Object type (int).

#### reg\_gens

List of generators regulating the voltage magnitude of this bus (list).

#### reg shunts

List of switched shunt devices regulating the voltage magnitude of this bus (list).

#### reg\_trans

List of tap-changing transformers regulating the voltage magnitude of this bus (list).

#### sens\_P\_balance

Objective function sensitivity with respect to bus active power balance (float).

### sens\_Q\_balance

Objective function sensitivity with respect to bus reactive power balance (float).

#### sens\_v\_ang\_l\_bound

Objective function sensitivity with respect to voltage angle lower bound (float).

#### sens\_v\_ang\_u\_bound

Objective function sensitivity with respect to voltage angle upper bound (float).

### ${\tt sens\_v\_mag\_l\_bound}$

Objective function sensitivity with respect to voltage magnitude lower bound (float).

#### sens v mag u bound

Objective function sensitivity with respect to voltage magnitude upper bound (float).

#### sens\_v\_reg\_by\_gen

Objective function sensitivity with respect to bus voltage regulation by generators (float).

### sens\_v\_reg\_by\_shunt

Objective function sensitivity with respect to bus voltage regulation by shunts (float).

#### sens\_v\_reg\_by\_tran

Objective function sensitivity with respect to bus voltage regulation by transformers (float).

#### show(self)

Shows bus properties.

#### v ang

Bus voltage angle (radians) (float).

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#### v\_mag

Bus volatge magnitude (p.u. bus base kv) (float).

#### v max

Bus volatge upper bound (p.u. bus base kv) (float).

#### v\_min

Bus voltage lower bound (p.u. bus base kv) (float).

#### v set

Bus voltage set point (p.u. bus base kv) (float). Equals one if bus is not regulated by a generator.

#### vargens

List of variable generators connected to this bus (list).

# 6.4 Branch

# 6.4.1 Branch Property Masks

```
pfnet.BRANCH_PROP_ANY
```

Any branch.

#### pfnet.BRANCH\_PROP\_TAP\_CHANGER

Branch is tap-changing transformer.

#### pfnet.BRANCH\_PROP\_TAP\_CHANGER\_V

Branch is tap-changing transformer regulating bus voltage magnitude.

#### pfnet.BRANCH\_PROP\_TAP\_CHANGER\_Q

Branch is tap-changing transformer regulating reactive power flow.

#### pfnet.BRANCH PROP PHASE SHIFTER

Branch is phase-shifting transformer regulating active power flow.

#### 6.4.2 Branch Variable Masks

#### pfnet.BRANCH\_VAR\_RATIO

Transformer tap ratio.

#### pfnet.BRANCH\_VAR\_RATIO\_DEV

Transformer tap ratio deviations from current value.

#### pfnet.BRANCH\_VAR\_PHASE

Transformer phase shift.

### 6.4.3 Branch Class

```
class pfnet .Branch (alloc=True)
```

Branch class.

```
Parameters alloc: {True, False}
```

#### P\_flow\_DC

Active power flow (DC approx.) from bus "from" to bus "to" (float).

b

Branch series susceptance (p.u.) (float).

### b from Branch shunt susceptance at the "from" side (p.u.) (float). b to Branch shunt susceptance at the "to" side (p.u.) (float). bus from Bus connected to the "from" side. bus to Bus connected to the "to" side. Branch series conductance (p.u.) (float). Branch shunt conductance at the "from" side (p.u.) (float). g\_to Branch shunt conductance at the "to" side (p.u.) (float). has\_flags (self, fmask, vmask) Determines whether the branch has the flags associated with specific quantities set. **Parameters fmask**: int (*Flag Masks*) vmask: int (Branch Variable Masks) Returns flag: {True, False} has\_pos\_ratio\_v\_sens(self) Determines whether tap-changing transformer has positive sensitivity between tap ratio and controlled bus voltage magnitude. Returns flag: {True, False} index Branch index (int). index\_phase Index of transformer phase shift variable (int). index ratio Index of transformer tap ratio variable (int). index\_ratio\_y Index of transformer tap ratio positive deviation variable (int). index ratio z Index of transformer tap ratio negative deviation variable (int). is fixed tran(self) Determines whether branch is fixed transformer.

Returns flag: {True, False}

Returns flag: {True, False}

Determines whether branch is phase shifter.

Returns flag: {True, False}

Determines whether branch is transmission line.

is line (self)

is\_phase\_shifter(self)

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#### is\_tap\_changer(self)

Determines whether branch is tap-changing transformer.

Returns flag: {True, False}

#### is\_tap\_changer\_Q(self)

Determines whether branch is tap-changing transformer that regulates reactive power flow.

Returns flag: {True, False}

#### is\_tap\_changer\_v(self)

Determines whether branch is tap-changing transformer that regulates bus voltage magnitude.

Returns flag: {True, False}

#### obj\_type

Object type (int).

#### phase

Transformer phase shift (radians) (float).

#### phase max

Transformer phase shift upper limit (radians) (float).

#### phase min

Transformer phase shift lower limit (radians) (float).

#### ratingA

Branch thermal rating A (p.u. system base power) (float).

#### ratingE

Branch thermal rating B (p.u. system base power) (float).

#### ratingC

Branch thermal rating C (p.u. system base power) (float).

#### ratio

Transformer tap ratio (float).

#### ratio\_max

Transformer tap ratio upper limit (float).

#### ratio\_min

Transformer tap ratio lower limit (float).

#### reg bus

Bus whose voltage is regulated by this tap-changing transformer.

#### sens P 1 bound

Objective function sensitivity with respect to active power flow lower bound (float).

#### sens\_P\_u\_bound

Objective function sensitivity with respect to active power flow upper bound (float).

#### 6.5 Generator

#### **6.5.1 Generator Property Masks**

#### pfnet.GEN\_PROP\_ANY

Any generator.

```
pfnet.GEN_PROP_SLACK
     Slack generator.
pfnet.GEN_PROP_REG
     Generator that regulates bus voltage magnitude.
pfnet.GEN PROP NOT REG
     Generator that does not regulate bus voltage magnitude.
pfnet.GEN PROP NOT SLACK
     Generator that is not slack.
pfnet.GEN_PROP_P_ADJUST
     Generator that can adjust its active power (P_min < P_max).
6.5.2 Generator Variable Masks
pfnet.GEN_VAR_P
     Generator active power.
pfnet.GEN VAR Q
     Generator reactive power.
6.5.3 Generator Class
class pfnet .Generator (alloc=True)
     Generator class.
          Parameters alloc: {True, False}
     P
          Generator active power (p.u. system base MVA) (float).
     P_cost
          Active power generation cost ($/hr).
     P max
          Generator active power upper limit (p.u. system base MVA) (float).
     P min
          Generator active power lower limit (p.u. system base MVA) (float).
     Q
          Generator reactive power (p.u. system base MVA) (float).
     Q_max
          Generator reactive power upper limit (p.u. system base MVA) (float).
     O min
          Generator reactive power lower limit (p.u. system base MVA) (float).
     bus
          Bus to which generator is connected.
     cost_coeff_Q0
          Coefficient for quadratic generation cost (constant term, units of $/hr).
     cost_coeff_Q1
          Coefficient for quadratic generation cost (linear term. units of $/(hr p.u.)).
```

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```
cost coeff Q2
     Coefficient for quadratic generation cost (quadratic term, units of $/(hr p.u.^2)).
has_flags (self, fmask, vmask)
     Determines whether the generator has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Generator Variable Masks)
         Returns flag: {True, False}
index
     Generator index (int).
index P
     Index of generator active power variable (int).
index_Q
     Index of generator reactive power variable (int).
is P adjustable (self)
     Determines whether generator has adjustable active power.
         Returns flag: {True, False}
is regulator (self)
     Determines whether generator provides voltage regulation.
         Returns flag: {True, False}
is slack (self)
     Determines whether generator is slack.
         Returns flag: {True, False}
obj_type
     Object type (int).
reg_bus
     Bus whose voltage is regulated by this generator.
sens P 1 bound
     Objective function sensitivity with respect to active power lower bound (float).
sens P u bound
     Objective function sensitivity with respect to active power upper bound (float).
```

#### 6.6 Shunt

#### 6.6.1 Shunt Property Masks

```
pfnet.SHUNT_PROP_ANY
Any shunt.

pfnet.SHUNT_PROP_SWITCHED_V
Switched shunt devices that regulates bus voltage magnitude.
```

#### 6.6.2 Shunt Variable Masks

pfnet.SHUNT\_VAR\_SUSC

```
Switched shunt susceptance.
pfnet.SHUNT_VAR_SUSC_DEV
     Switched shunt susceptance deviations from current point.
6.6.3 Shunt Class
class pfnet . Shunt (alloc=True)
     Shunt class.
           Parameters alloc: {True, False}
     b
           Shunt susceptance (p.u.) (float).
     b_{max}
           Shunt susceptance upper limit (p.u.) (float).
     b min
           Shunt susceptance lower limit (p.u.) (float).
     bus
           Bus to which the shunt devices is connected.
     g
           Shunt conductance (p.u.) (float).
     has_flags (self, fmask, vmask)
          Determines whether the shunt devices has flags associated with certain quantities set.
               Parameters fmask: int (Flag Masks)
                   vmask: int (Bus Variable Masks)
               Returns flag: {True, False}
     index
           Shunt index (int).
     index b
          Index of shunt susceptance variable (int).
     index_y
           Index of shunt susceptance positive deviation variable (int).
     index_z
          Index of shunt susceptance negative deviation variable (int).
     is fixed (self)
           Determines whether the shunt device is fixed (as opposed to switched).
               Returns flag: {True, False}
     is switched v(self)
           Determines whether the shunt is switchable and regulates bus voltage magnitude.
               Returns flag: {True, False}
     obj_type
           Object type (int).
```

6.6. Shunt 37

#### reg\_bus

Bus whose voltage magnitude is regulated by this shunt device.

#### 6.7 Load

#### 6.7.1 Load Class

```
class pfnet . Load (alloc=True)
    Load class.
    Parameters alloc : {True, False}

P
    Load active power (p.u. system base MVA) (float).

Q
    Load reactive power (p.u. system base MVA) (float).

bus
    Bus to which load is connected.

index
    Load index (int).

obj_type
    Object type (int).
```

#### 6.8 Variable Generator

#### 6.8.1 Variable Generator Property Masks

```
pfnet.VARGEN_PROP_ANY
Any variable generator.
```

#### 6.8.2 Variable Generator Variable Masks

```
pfnet.VARGEN_VAR_P
Variable generator active power.

pfnet.VARGEN_VAR_Q
Variable generator reactive power.
```

#### 6.8.3 Variable Generator Class

```
class pfnet . VarGenerator (alloc=True)
    Variable generator class.
    Parameters alloc : {True, False}

P
    Variable generator active power (p.u. system base MVA) (float).
```

```
P max
     Variable generator active power upper limit (p.u. system base MVA) (float).
P min
     Variable generator active power lower limit (p.u. system base MVA) (float).
P std
     Variable generator active power standard deviation (p.u. system base MVA) (float).
     Variable generator reactive power (p.u. system base MVA) (float).
Q_max
     Variable generator maximum reactive power (p.u. system base MVA) (float).
Q_min
     Variable generator minimum reactive power (p.u. system base MVA) (float).
bus
     Bus to which variable generator is connected.
has_flags (self, fmask, vmask)
     Determines whether the variable generator has the flags associated with certain quantities set.
         Parameters fmask: int (Flag Masks)
             vmask: int (Variable Generator Variable Masks)
         Returns flag: {True, False}
index
     Variable generator index (int).
index P
     Index of variable generator active power variable (int).
index_Q
     Index of variable generator reactive power variable (int).
name
     Variable generator name (string).
obj_type
```

#### 6.9 Network

#### 6.9.1 Component Types

Object type (int).

```
pfnet.OBJ_BUS
Bus.

pfnet.OBJ_GEN
Generator.

pfnet.OBJ_BRANCH
Branch.

pfnet.OBJ_SHUNT
Shunt device.
```

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```
pfnet.OBJ_LOAD
    Load.
pfnet.OBJ_VARGEN
    Variable generator.
6.9.2 Flag Masks
```

```
pfnet.FLAG_VARS
     For specifying quantities as variable.
pfnet.FLAG_FIXED
     For specifying variables that should be fixed.
pfnet.FLAG_BOUNDED
     For specifying variables that should be bounded.
pfnet.FLAG_SPARSE
     For specifying control adjustments that should be sparse.
```

#### 6.9.3 Variable Value Codes

```
pfnet.CURRENT
     Current variable value.
pfnet.UPPER_LIMIT
     Upper limit of variable.
pfnet.LOWER_LIMIT
     Lower limit of variable.
```

#### 6.9.4 Network Class

```
class pfnet . Network (alloc=True)
     Network class.
           Parameters alloc: {True, False}
     add_vargens (self, buses, penetration, uncertainty, corr_radius, corr_value)
           Adds variable generators to the network.
               Parameters buses: list of Buses
                   penetration: float
                     percentage
                   uncertainty: float
                     percentage
                   corr_radius: int
                     number of branches
                   corr_value: float
                     correlation coefficient
```

#### adjust\_generators (self)

Adjusts powers of slack and regulator generators connected to or regulating the same bus to correct generator participations without modifying the total power injected.

#### base\_power

System base power (MVA) (float).

#### branches

List of network branches (list).

#### bus P mis

Largest bus active power mismatch in the network (MW) (float).

#### bus\_Q\_mis

Largest bus reactive power mismatch in the network (MVAr) (float).

#### bus\_v\_max

Maximum bus voltage magnitude (p.u.) (float).

#### bus\_v\_min

Minimum bus voltage magnitude (p.u.) (float).

#### bus\_v\_vio

Maximum bus voltage magnitude limit violation (p.u.) (float).

#### buses

List of network buses (list).

#### clear\_error(self)

Clear error flag and message string.

#### clear\_flags (self)

Clears all the flags of all the network components.

#### clear\_properties (self)

Clears all the network properties.

#### clear\_sensitivities (self)

Clears all sensitivity information.

#### create\_sorted\_bus\_list(self, sort\_by)

Creates list of buses sorted in descending order according to a specific quantity.

**Parameters sort\_by**: int (Bus Sensitivities, Bus Power Mismatches).

Returns buses: list of Buses

#### create\_vargen\_P\_sigma (self, spread, corr)

Creates covariance matrix (lower triangular part) for variable vargen active powers.

#### **Parameters spead**: int

Determines correlation neighborhood in terms of number of edges.

corr: float

Desired correlation coefficient for neighboring vargens.

Returns sigma: coo\_matrix

#### gen\_P\_cost

Total active power generation cost (\$/hr) (float).

#### gen P vio

Largest generator active power limit violation (MW) (float).

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```
gen_Q_vio
    Largest generator reactive power limit violation (MVAr) (float).
gen_v_dev
    Largest voltage magnitude deviation from set point of bus regulated by generator (p.u.) (float).
generators
    List of network generators (list).
get_branch (self, index)
    Gets branch with the given index.
         Parameters index: int
         Returns branch: Branch
get_bus (self, index)
     Gets bus with the given index.
         Parameters index: int
         Returns bus: Bus
get_bus_by_name (self, name)
     Gets bus with the given name.
         Parameters name: string
         Returns bus: Bus
get_bus_by_number (self, number)
     Gets bus with the given number.
         Parameters number: int
         Returns bus: Bus
get_gen (self, index)
     Gets generator with the given index.
         Parameters index: int
         Returns gen: Generator
get_gen_buses (self)
    Gets list of buses where generators are connected.
         Returns buses: list
get_load (self, index)
     Gets load with the given index.
         Parameters index: int
         Returns gen: Load
get_load_buses (self)
     Gets list of buses where loads are connected.
         Returns buses: list
get_num_P_adjust_gens (self)
     Gets number of generators in the network that have adjustable active powers.
```

Returns num: int

### get\_num\_branches (self) Gets number of branches in the network. Returns num: int get num buses(self) Gets number of buses in the network. Returns num: int $get_num_buses_reg_by_gen(self)$ Gets number of buses whose voltage magnitudes are regulated by generators. Returns num: int get\_num\_buses\_reg\_by\_shunt (self, only=False) Gets number of buses whose voltage magnitudes are regulated by switched shunt devices. Returns num: int get\_num\_buses\_reg\_by\_tran (self, only=False) Gets number of buses whose voltage magnitudes are regulated by tap-changing transformers. **Returns num:** int get\_num\_fixed\_shunts(self) Gets number of fixed shunts in the network. Returns num: int get\_num\_fixed\_trans(self) Gets number of fixed transformers in the network. Returns num: int get\_num\_gens (self) Gets number of generators in the network. Returns num: int get\_num\_lines(self) Gets number of transmission lines in the network. Returns num: int get num loads (self) Gets number of loads in the network. Returns num: int get\_num\_phase\_shifters(self) Gets number of phase-shifting transformers in the network. Returns num: int get\_num\_reg\_gens (self) Gets number generators in the network that provide voltage regulation. Returns num: int get\_num\_shunts(self) Gets number of shunts in the network.

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Returns num: int

Gets number of slack buses in the network.

get\_num\_slack\_buses(self)

```
Returns num: int
get_num_slack_gens(self)
     Gets number of slack generators in the network.
         Returns num: int
get num switched shunts (self)
     Gets number of switched shunts in the network.
         Returns num: int
get_num_tap_changers (self)
     Gets number of tap-changing transformers in the network.
         Returns num: int
get_num_tap_changers_Q(self)
     Gets number of tap-changing transformers in the network that regulate reactive flows.
         Returns num: int
get_num_tap_changers_v (self)
     Gets number of tap-changing transformers in the network that regulate voltage magnitudes.
         Returns num: int
get_num_vargens (self)
     Gets number of variable generators in the network.
         Returns num: int
get_properties (self)
     Gets network properties.
         Returns properties: dict
get_shunt (self, index)
     Gets shunt with the given index.
         Parameters index: int
         Returns gen: Shunt
get_var_projection (self, obj_type, var)
     Gets projection matrix for specific object variables.
         Parameters obj_type : int (Component Types)
             var: int (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks, Shunt
             Variable Masks)
get_var_values (self, code=CURRENT)
     Gets network variable values.
         Parameters code: int (See var values)
         Returns values: ndarray
get_vargen (self, index)
     Gets variable generator with the given index.
         Parameters index: int
```

Returns vargen: VarGenerator

#### get\_vargen\_by\_name (self, name)

Gets vargen with the given name.

Parameters name: string

Returns vargen: VarGenerator

#### has\_error(self)

Indicates whether the network has the error flag set due to an invalid operation.

#### load (self, filename)

Loads a network data contained in a specific file.

Parameters filename: string

#### loads

List of network loads (list).

#### num\_actions

Number of control adjustments (int).

#### num bounded

Number of network quantities that have been set to bounded (int).

#### num branches

Number of branches in the network (int).

#### num\_buses

Number of buses in the network (int).

#### num fixed

Number of network quantities that have been set to fixed (int).

#### num\_gens

Number of generators in the network (int).

#### num\_loads

Number of loads in the network (int).

#### num shunts

Number of shunt devices in the network (int).

#### num\_sparse

Number of network control quantities that have been set to sparse (int).

#### num\_vargens

Number of variable generators in the network (int).

#### num vars

Number of network quantities that have been set to variable (int).

#### set\_flags (self, obj\_type, flags, props, vals)

Sets flags of network components with specific properties.

Parameters obj\_type : int (Component Types)

**flags**: int or list (*Flag Masks*)

**props**: int or list (Bus Property Masks, Branch Property Masks, Generator Property Masks, Shunt Property Masks)

**vals**: int or list (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks, Shunt Variable Masks)

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#### set\_flags\_of\_component (self, obj, flags, vals)

Sets flags of network components with specific properties.

#### Parameters obj: Bus, Branch, Generator, Load, Shunt, VarGenerator

```
flags: int or list (Flag Masks)
```

vals: int or list (Bus Variable Masks, Branch Variable Masks, Generator Variable Masks,

Shunt Variable Masks)

#### set\_var\_values (self, values)

Sets network variable values.

Parameters values: ndarray

#### show\_buses (self, number, sort\_by)

Shows information about the most relevant network buses sorted by a specific quantity.

#### Parameters number: int

```
sort_by : int (Bus Sensitivities, Bus Power Mismatches)
```

#### show components (self)

Shows information about the number of network components of each type.

#### show\_properties(self)

Shows information about the state of the network component quantities.

#### shunt b vio

Largest switched shunt susceptance limit violation (p.u.) (float).

#### shunt v vio

Largest voltage magnitude band violation of voltage regulated by switched shunt device (p.u.) (float).

#### shunts

List of network shunts (list).

#### tran\_p\_vio

Largest transformer phase shift limit violation (float).

#### tran\_r\_vio

Largest transformer tap ratio limit violation (float).

#### tran\_v\_vio

Largest voltage magnitude band violation of voltage regulated by transformer (p.u.) (float).

#### update\_properties (self, values=None)

Re-computes the network properties using the given values of the network variables. If no values are given, then the current values of the network variables are used.

Parameters values: ndarray

#### update\_set\_points(self)

Updates voltage magnitude set points of gen-regulated buses to be equal to the bus voltage magnitudes.

#### var\_generators

List of network variable generators (list).

#### vargen\_corr\_radius

Correlation radius of variable generators (number of edges).

#### vargen\_corr\_value

Correlation value (coefficient) of variable generators.

### 6.10 Graph

```
class pfnet .Graph (net, alloc=True)
     Graph class.
          Parameters net: Network
               alloc: {True, False}
     clear_error(self)
          Clear error flag and message string.
     color_nodes_by_mismatch (self, mis_type)
          Colors the graphs nodes according to their power mismatch.
               Parameters mis_type : int (Bus Power Mismatches)
     color_nodes_by_sensitivity (self, sens_type)
          Colors the graphs nodes according to their sensitivity.
               Parameters sens_type : int (Bus Sensitivities)
     has_error(self)
          Indicates whether the graph has the error flag set due to an invalid operation.
     has_viz(self)
          Determines whether graph has visualization capabilities.
               Returns flag: {True, False}
     set_edges_property (self, prop, value)
          Sets property of edges. See Graphviz documentation.
               Parameters prop: string
                   value: string
     set_layout (self)
          Determines and saves a layout for the graph nodes.
     set_nodes_property (self, prop, value)
          Sets property of nodes. See Graphviz documentation.
               Parameters prop: string
                   value: string
     view(self)
          Displays the graph.
     write (self, format, filename)
          Writes the graph to a file.
               Parameters format : string (Graphviz output formats)
                   filename: string
```

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#### 6.11 Function

### 6.11.1 Function Types

pfnet.FUNC\_TYPE\_UNKNOWN

```
Unknown function.
pfnet.FUNC_TYPE_REG_VMAG
     Bus voltage magnitude regularization.
pfnet.FUNC_TYPE_SLIM_VMAG
     Bus voltage magnitude soft limits penalty.
pfnet.FUNC_TYPE_REG_VANG
     Bus voltage angle regularization.
pfnet.FUNC_TYPE_REG_PQ
     Generator active and reactive power regularization.
pfnet.FUNC TYPE GEN COST
     Active power generation cost.
pfnet.FUNC TYPE REG RATIO
     Transformer tap ratio regularization.
pfnet.FUNC_TYPE_REG_PHASE
     Transformer phase shift regularization.
pfnet.FUNC_TYPE_REG_SUSC
     Switched shunt susceptance regularization.
pfnet.FUNC_TYPE_SP_CONTROLS
     Sparsity-inducing penalty for control adjustments.
6.11.2 Function Class
class pfnet . Function (int type, float weight, Network net, alloc=True)
     Function class.
          Parameters type: int (Function Types)
              weight : float
              net: Network
              alloc: {True, False}
     Hcounter
          Number of nonzero entries in Hessian matrix (int).
     Hphi
          Function Hessian matrix (only the lower triangular part) (coo_matrix).
     analyze(self)
          Analyzes function and allocates required vectors and matrices.
     clear error(self)
          Clears internal error flag.
     eval (self, var_values)
          Evaluates function value, gradient, and Hessian using the given variable values.
```

```
Parameters var_values: ndarray
     gphi
          Function gradient vector (ndarray).
     phi
          Function value (float).
     type
          Function type (int).
     update_network (self)
          Updates internal arrays to be compatible with any network changes.
     weight
          Function weight (float).
6.12 Constraint
6.12.1 Constraint Types
pfnet.CONSTR_TYPE_PF
     Constraint for enforcing power balance at every bus of the network.
pfnet.CONSTR TYPE DCPF
     Constraint for enforcing DC power balance at every bus of the network.
pfnet.CONSTR_TYPE_FIX
     Constraint for fixing a subset of variables to their current value.
pfnet.CONSTR_TYPE_BOUND
     Constraint for forcing a subset of variables to be within their bounds (nonlinear).
pfnet.CONSTR TYPE LBOUND
     Constraint for forcing a subset of variables to be within their bounds (linear).
pfnet.CONSTR_TYPE_PAR_GEN_P
     Constraint for enforcing generator active power participations.
pfnet.CONSTR_TYPE_PAR_GEN_Q
     Constraint for enforcing generator reactive power participations.
pfnet.CONSTR_TYPE_REG_GEN
     Constraint for enforcing voltage set point regulation by generators.
pfnet.CONSTR_TYPE_REG_TRAN
     Constraint for enforcing voltage band regulation by tap-changing transformers.
pfnet.CONSTR_TYPE_REG_SHUNT
```

Constraint for enforcing voltage band regulation by switched shunt devices.

Constraint for enforcing DC power flow limits on every branch

#### 6.12.2 Constraint Class

pfnet.CONSTR\_TYPE\_DC\_FLOW\_LIM

6.12. Constraint 49

```
Parameters type: int (Constraint Types)
         net: Network
         alloc: {True, False}
Α
     Matrix for linear equality constraints (coo matrix).
Aconstr index
     Index of linear equality constraint (int).
Acounter
     Number of nonzero entries in the matrix of linear equality constraints (int).
G
     Matrix for linear inequality constraints (coo_matrix).
Gconstr_index
     Index of linear inequality constraint (int).
Gcounter
     Number of nonzero entries in the matrix of linear inequality constraints (int).
H combined
     Linear combination of Hessian matrices of individual nonlinear equality constraints (only the lower trian-
     gular part) (coo_matrix).
     Jacobian matrix of nonlinear equality constraints (coo_matrix).
Jconstr_index
     Index of nonlinear equality constraint (int).
Jcounter
     Number of nonzero entries in the Jacobian matrix of the nonlinear equality constraints (int).
analyze (self)
     Analyzes constraint and allocates required vectors and matrices.
b
     Right-hand side vector of linear equality constraints (ndarray).
clear error(self)
     Clears internal error flag.
combine_H (self, coeff, ensure_psd=False)
     Forms and saves a linear combination of the individual constraint Hessians.
         Parameters coeff: ndarray
             ensure_psd : {True, False}
eval (self, var_values)
     Evaluates constraint violations, Jacobian, and individual Hessian matrices.
         Parameters var_values: ndarray
f
     Vector of nonlinear equality constraint violations (ndarray).
get_H_single (self, i)
     Gets the Hessian matrix (only lower triangular part) of an individual constraint.
         Parameters i: int
```

```
Returns H: coo matrix
     1
           Lower bound vector of linear inequality constraints (ndarray).
     store_sensitivities (self, sA, sf, sGu, sGl)
           Stores Lagrange multiplier estimates of the constraints in the power network components.
               Parameters sA: ndarray
                     sensitivities for linear equality constraints (Ax = b)
                   sf: ndarray
                     sensitivities for nonlinear equality constraints (f(x) = 0)
                   sGu: ndarray
                     sensitivities for linear inequality constraints (Gx \le u)
                   sGl: ndarray
                     sensitivities for linear inequality constraints (l \leq Gx)
     type
           Constraint type (Constraint Types) (int).
           Upper bound vector of linear inequality constraints (ndarray).
     update_network (self)
           Updates internal arrays to be compatible with any network changes.
6.13 Optimization Problem
6.13.1 Problem Class
class pfnet.Problem
     Optimization problem class.
     Α
           Constraint matrix of linear equality constraints (coo_matrix).
     G
           Constraint matrix of linear inequality constraints (coo_matrix).
     H_combined
           Linear combination of Hessian matrices of individual nonlinear equality constraints (only the lower trian-
           gular part) (coo_matrix).
     Hphi
           Objective function Hessian matrix (only the lower triangular part) (coo_matrix).
           Jacobian matrix of the nonlinear equality constraints (coo_matrix).
     add_constraint (self, ctype)
           Adds constraint to optimization problem.
```

**Parameters ctype**: int (*Constraint Types*)

```
add_function (self, ftype, weight)
     Adds function to optimization problem objective.
         Parameters ftype: int (Function Types)
             weight: float
analyze (self)
     Analyzes function and constraint structures and allocates required vectors and matrices.
b
     Right hand side vectors of the linear equality constraints (ndarray).
clear (self)
     Resets optimization problem data.
combine_H (self, coeff, ensure_psd)
     Forms and saves a linear combination of the individual constraint Hessians.
         Parameters coeff: ndarray
             ensure_psd : {True, False}
constraints
     List of constraints of this optimization problem (list).
eval (self, var values)
     Evaluates objective function and constraints as well as their first and second derivatives using the given
     variable values.
         Parameters var values: ndarray
f
     Vector of nonlinear equality constraints violations (ndarray).
find_constraint (self, type)
     Finds constraint of give type among the constraints of this optimization problem.
         Parameters type: int (Constraint Types)
functions
     List of functions that form the objective function of this optimization problem (list).
get_init_point(self)
     Gets initial solution estimate from the current value of the network variables.
         Returns point: ndarray
get_lower_limits(self)
     Gets vector of lower limits for the network variables.
         Returns limits: ndarray
get_network (self)
     Gets the power network associated with this optimization problem.
get_upper_limits(self)
     Gets vector of upper limits for the network variables.
         Returns limits: ndarray
gphi
     Objective function gradient vector (ndarray).
1
     Lower bound for linear inequality constraints (ndarray).
```

```
lam
     Initial dual point (ndarray).
network
     Power network associated with this optimization problem (Network).
nu
     Initial dual point (ndarray).
phi
     Objective function value (float).
set_network (self, net)
     Sets the power network associated with this optimization problem.
show (self)
     Shows information about this optimization problem.
store_sensitivities (self, sA, sf, sGu, sGl)
     Stores Lagrange multiplier estimates of the constraints in the power network components.
         Parameters sA: ndarray
                sensitivities for linear equality constraints (Ax = b)
             sf: ndarray
                sensitivities for nonlinear equality constraints (f(x) = 0)
             sGu: ndarray
                sensitivities for linear inequality constraints (Gx \leq u)
             sGl: ndarray
                sensitivities for linear inequality constraints (l \leq Gx)
u
     Upper bound for linear inequality constraints (ndarray).
update_lin(self)
     Updates linear equality constraints.
x
     Initial primal point (ndarray).
```

### 6.14 References

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## **SEVEN**

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