CS 434: Implementation Assignment 1

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Linear Regression

1. The learned weight vector of the test data is:

```
\begin{bmatrix} 3.95843212e + 01 \\ -1.01137046e - 01 \\ 4.58935299e - 02 \\ -2.73038670e - 03 \\ 3.07201340e + 00 \\ -1.72254072e + 01 \\ 3.71125235e + 00 \\ 7.15862492e - 03 \\ -1.59900210e + 00 \\ 3.73623375e - 01 \\ -1.57564197e - 02 \\ -1.02417703e + 00 \\ 9.69321451e - 03 \\ -5.85969273e - 01 \end{bmatrix}
```

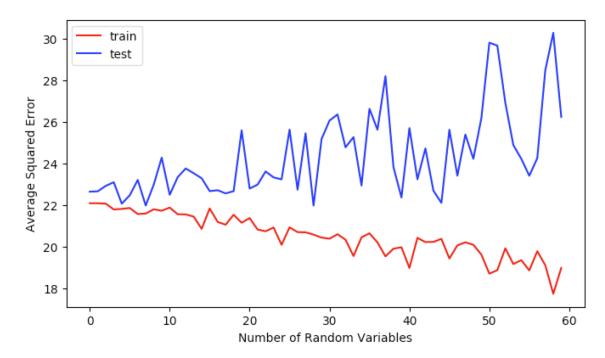
Here is the learned weight vector next to the features that each weight describes:

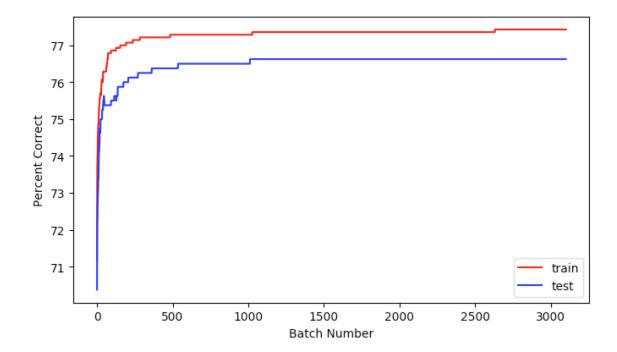
| Weight | Feature |
|--------------------|---|
| 3.95843212e+01 | Dummy |
| -1.01137046e-01 | per capita crime rate by town |
| 4.58935299 e-02 | proportion of residential land zoned for lots over 25,000sq.ft. |
| -2.73038670e-03 | proportion of non-retail business acres per town |
| 3.07201340e+00 | Charles River dummy variable |
| -1.72254072e+01 | nitric oxides concentration (parts per 10 million) |
| 3.71125235e+00 | average number of rooms per dwelling |
| 7.15862492e-03 | proportion of owner-occupied units built prior to 1940 |
| -1.59900210e+00 | weighted distances to five Boston employment centres |
| 3.73623375e-01 | index of accessibility to radial highways |
| -1.57564197e-02 | full-value property-tax rate per \$10,000 |
| -1.02417703e+00 | pupil-teacher ratio by town |
| 9.69321451e-03 | 1000(Bk - 0.63) ² where Bk is the proportion of blacks by town |
| -5.85969273e -01 | % lower status of the population |

- 2. Training Dataset ASE: 22.081273187 Test Dataset ASE: 22.6382562966
- 3. Training Dataset ASE (Without Dummy): 24.4758827846 Test Dataset ASE (Without Dummy): 24.2922381757

The reason the dummy variable improves the accuracy of the optimal weight vector is because it provides the y intercept (or b) for the regression.

4. The addition of random features increases the accuracy of the regression when applying it to the training data, but also decreases the accuracy of the regression when applied to other data. Adding more features leads to worse performance when it comes to applying the learned weight vector to other datasets. This is because the addition of features allows the weight vector to be trained more precisely, but it comes at the expense of overfitting the regression to the specific case of the training data.





Logistic Regression

1.

2. Adding regularization will allow the algorithm to train with more sensitivity to the size of the weights. By adding a function of the weights, the regression will be less likely to overfit using extreme weights. This will prevent a misled learning of data, and help make the final weights more accurate. Our L2 algorithm is similar to the regression algorithm, but with the added weight calculation:

$$\sum_{i=1}^{n} l(g(w^{T}x^{i}), y^{i}) + \frac{1}{2}\lambda |w|^{2}$$

This algorithm translates into code very similar to our initial code for the logistic regression. Below is how this algorithm would function, with the batch_train function being called iteratively until the delta norm is lower than a set bound.

```
batch_train(input_matrix, output_matrix, w):
lambda, eta = 10^-3, 10^-7
delta = [weight matrix initialized with zeros]
for each element x,y in input_matrix,output_matrix:
   y_hat = 1 / (1 + exponential(-transposed w * x))
   loss = ((y_hat - y) * x)
   regularization = (|w|^2) / 2
   current_delta = loss + lambda * regularization
   batch_delta + current_delta
w = w - (eta * batch_delta)
```

3: 999 78.4286 77.5000 399.96065 102: 1061 78.2857 77.5000 399.91662 $10^{**}1$: 1211 78.1429 77.5000 399.93002