101B_final_project_June_4

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Appendix

Figure A.1

Section B: Fractional Factorial Design:

Figure B.1

```
set.seed(1000)
frac.design <- FrF2(nruns = 32, nfactors = 7, randomize = T)
print(desnum(frac.design))</pre>
```

```
##
       Α
         в с
              D
                 Ε
## 1
       1
          1
            1
               1 -1
       1
          1 -1 -1 -1
     -1
          1 -1
             1 -1
## 5
## 6
             1 -1
       1 -1 -1 -1
      -1 -1
             1
               1
## 10
       1 -1
            1 -1 -1 -1 -1
## 11 -1 -1
            1 1 -1
## 12 -1
            1 -1
          1
## 13 -1 -1 -1 -1 -1
## 14 -1 -1 -1
## 15 -1 -1 -1
               1 1 -1
## 16 -1 -1
            1 -1 -1
## 17
                  1
                     1
       1
          1
            1
               1
## 18
       1 -1
            1
               1 -1 -1
       1 -1 -1
               1
## 20
       1 -1 -1
                1 -1
## 21 -1
          1 -1
               1
## 22
          1 -1
               1 -1 -1 -1
## 23
       1
          1 -1
## 24 -1
          1
             1 -1 -1 -1
## 25
       1
         1
            1 -1 -1
                    1
## 26 -1 1 1 1 1 -1 -1
```

```
## 27 1 1 -1 -1 1 -1 -1
## 28 1 -1 1 1 1 -1 -1
## 29 -1 1 1 1 -1 -1 1
## 30 -1 -1 -1 -1 1 -1 -1
## 31 -1 -1 1 -1 1 -1
## 32 1 -1 -1 -1 1 -1
design.info(frac.design)$aliased
## $legend
## [1] "A=A" "B=B" "C=C" "D=D" "E=E" "F=F" "G=G"
## $main
## character(0)
##
## $fi2
## [1] "AB=CF" "AC=BF" "AF=BC"
D <- desnum(frac.design) # Extract the design.
# Create the model matrix including main effects and two-factor interactions.
```

Figure B.2

 $X \leftarrow model.matrix(\sim(A + B + C + D + E + F + G)^2-1, data.frame(D))$

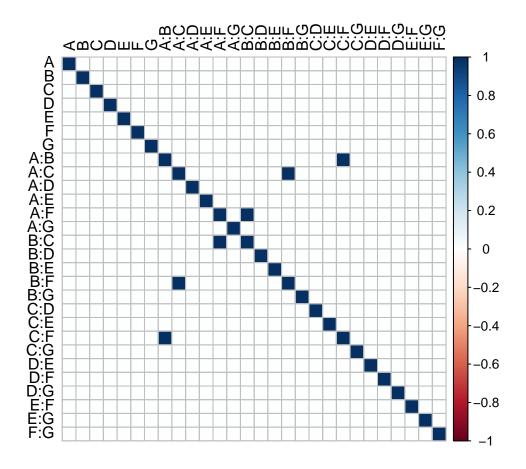


Figure B.3

source("CrossValidation_RF.R")

```
## randomForest 4.7-1.1
## Type rfNews() to see new features/changes/bug fixes.
D.frac <- data.frame(D)</pre>
new_frac.data <- D.frac</pre>
new_frac.data[,1][new_frac.data[,1]==1] <- 1000</pre>
new_frac.data[,1][new_frac.data[,1]==-1] <- 100</pre>
new_frac.data[,2][new_frac.data[,2]==1] <- 6</pre>
new_frac.data[,2][new_frac.data[,2]==-1] <- 2</pre>
new_frac.data[,3][new_frac.data[,3]==1] <- 1</pre>
new_frac.data[,3][new_frac.data[,3]==-1] <- 0
new_frac.data[,4][new_frac.data[,4]==1] <- 11</pre>
new_frac.data[,4][new_frac.data[,4]==-1] <- 1</pre>
new_frac.data[,5][new_frac.data[,5]==1] <- 0.9
new_frac.data[,5][new_frac.data[,5]==-1] \leftarrow 0.5
new_frac.data[,6][new_frac.data[,6]==1] <- 0.8</pre>
new_frac.data[,6][new_frac.data[,6]==-1] \leftarrow 0.2
new frac.data[,7][new frac.data[,7]==1] <- 1000</pre>
```

```
new_frac.data[,7][new_frac.data[,7]==-1] <- 10</pre>
colnames(new_frac.data) <- c("ntree", "mtry", "replace", "nodesize", "classwt", "cutoff", "maxnodes")</pre>
new_data <- new_frac.data</pre>
load("diabetes.RData")
new.frac.design_rf <- cv.rf(new_data, y, X) # With the data actual values, we get a CV as a response va
## Collecting response on test combination 1
## Collecting response on test combination 2
## Collecting response on test combination 3
## Collecting response on test combination 4
## Collecting response on test combination 5
## Collecting response on test combination 6
## Collecting response on test combination
## Collecting response on test combination 8
## Collecting response on test combination 9
## Collecting response on test combination 10
## Collecting response on test combination 11
## Collecting response on test combination 12
## Collecting response on test combination 13
## Collecting response on test combination 14
## Collecting response on test combination 15
## Collecting response on test combination 16
## Collecting response on test combination 17
## Collecting response on test combination 18
## Collecting response on test combination
## Collecting response on test combination 20
## Collecting response on test combination 21
## Collecting response on test combination
## Collecting response on test combination
## Collecting response on test combination
## Collecting response on test combination 25
## Collecting response on test combination 26
## Collecting response on test combination 27
## Collecting response on test combination 28
## Collecting response on test combination 29
## Collecting response on test combination 30
## Collecting response on test combination 31
## Collecting response on test combination
new.frac.design <- new.frac.design_rf # matrix with actual values and CV.
new.frac.design
##
      ntree mtry replace nodesize classwt cutoff maxnodes
                                                                  CV
## 1
       1000
               6
                               11
                                      0.5
                                             0.8
                                                       10 0.6936670
                                                     1000 0.6256757
## 2
      1000
               6
                                      0.5
                                             0.2
                       0
                                1
## 3
       100
               6
                       0
                               11
                                      0.5
                                             0.8
                                                     1000 0.6824084
## 4
      1000
               2
                       1
                                1
                                      0.9
                                             0.2
                                                     1000 0.5011689
## 5
       100
               6
                       0
                                      0.9
                                                     1000 0.6508802
                                1
                                             0.8
## 6
      1000
               6
                                      0.9
                       1
                                1
                                             0.8
                                                       10 0.5208853
```

0.8

0.8

10 0.6955822

1000 0.6962893

0.5

0.9

1

1

7

8

100

1000

6

0

##	9	100	2	1	11	0.9	0.8	1000	0.6858889
##	10	1000	2	1	1	0.5	0.2	10	0.6818311
##	11	100	2	1	11	0.5	0.8	10	0.6637956
##	12	100	6	1	1	0.9	0.2	1000	0.6301023
##	13	100	2	0	1	0.5	0.2	1000	0.6574491
##	14	100	2	0	11	0.5	0.2	10	0.6846669
##	15	100	2	0	11	0.9	0.2	1000	0.5001023
##	16	100	2	1	1	0.5	0.8	1000	0.6683292
##	17	1000	6	1	11	0.9	0.8	1000	0.7157822
##	18	1000	2	1	11	0.5	0.2	1000	0.6614709
##	19	1000	2	0	11	0.9	0.8	10	0.5000578
##	20	1000	2	0	11	0.5	0.8	1000	0.6851604
##	21	100	6	0	11	0.9	0.8	10	0.5166346
##	22	1000	6	0	11	0.9	0.2	1000	0.5202358
##	23	1000	6	0	11	0.5	0.2	10	0.7096264
##	24	100	6	1	1	0.5	0.2	10	0.7075201
##	25	1000	6	1	1	0.5	0.8	1000	0.6521690
##	26	100	6	1	11	0.9	0.2	10	0.5000000
##	27	1000	6	0	1	0.9	0.2	10	0.5000001
##	28	1000	2	1	11	0.9	0.2	10	0.5000000
##	29	100	6	1	11	0.5	0.2	1000	0.6383911
##	30	100	2	0	1	0.9	0.2	10	0.5000001
##	31	100	2	1	1	0.9	0.8	10	0.5010490
##	32	1000	2	0	1	0.5	0.8	10	0.6655513

Figure B.4

```
coded.frac.design <- cbind(D.frac,new.frac.design$CV)
colnames(coded.frac.design) <- c("ntree", "mtry", "replace", "nodesize", "classwt", "cutoff", "maxnodes
coded.frac.design # matrix with coded values and CV.</pre>
```

##		ntree	mtry	replace	nodesize	classwt	cutoff	maxnodes	CV
##	1	1	1	1	1	-1	1	-1	0.6936670
##	2	1	1	-1	-1	-1	-1	1	0.6256757
##	3	-1	1	-1	1	-1	1	1	0.6824084
##	4	1	-1	1	-1	1	-1	1	0.5011689
##	5	-1	1	-1	-1	1	1	1	0.6508802
##	6	1	1	1	-1	1	1	-1	0.5208853
##	7	-1	1	-1	-1	-1	1	-1	0.6955822
##	8	1	-1	-1	-1	1	1	1	0.6962893
##	9	-1	-1	1	1	1	1	1	0.6858889
##	10	1	-1	1	-1	-1	-1	-1	0.6818311
##	11	-1	-1	1	1	-1	1	-1	0.6637956
##	12	-1	1	1	-1	1	-1	1	0.6301023
##	13	-1	-1	-1	-1	-1	-1	1	0.6574491
##	14	-1	-1	-1	1	-1	-1	-1	0.6846669
##	15	-1	-1	-1	1	1	-1	1	0.5001023
##	16	-1	-1	1	-1	-1	1	1	0.6683292
##	17	1	1	1	1	1	1	1	0.7157822
##	18	1	-1	1	1	-1	-1	1	0.6614709
##	19	1	-1	-1	1	1	1	-1	0.5000578
##	20	1	-1	-1	1	-1	1	1	0.6851604

```
## 21
         -1
                                  1
                                          1
                                                           -1 0.5166346
                1
                                                  1
## 22
          1
                1
                       -1
                                  1
                                          1
                                                 -1
                                                            1 0.5202358
                                                           -1 0.7096264
## 23
                       -1
                                  1
                                                 -1
                                                 -1
## 24
                                                           -1 0.7075201
         -1
                1
                        1
                                 -1
                                         -1
## 25
          1
               1
                        1
                                 -1
                                          -1
                                                  1
                                                            1 0.6521690
## 26
         -1
               1
                        1
                                  1
                                          1
                                                 -1
                                                           -1 0.5000000
## 27
                                                           -1 0.5000001
          1
               1
                       -1
                                 -1
                                          1
                                                 -1
                                                 -1
## 28
          1
              -1
                        1
                                 1
                                          1
                                                           -1 0.5000000
##
  29
         -1
               1
                        1
                                  1
                                          -1
                                                 -1
                                                            1 0.6383911
## 30
         -1
                                                 -1
              -1
                       -1
                                 -1
                                          1
                                                           -1 0.5000001
## 31
         -1
              -1
                        1
                                 -1
                                          1
                                                 1
                                                           -1 0.5010490
## 32
              -1
                                 -1
                                                           -1 0.6655513
          1
                       -1
                                          -1
                                                  1
```

Figure B.5

```
### use summary() to see significant effects
model <- lm(CV~.^2, data = coded.frac.design)
summary(model)</pre>
```

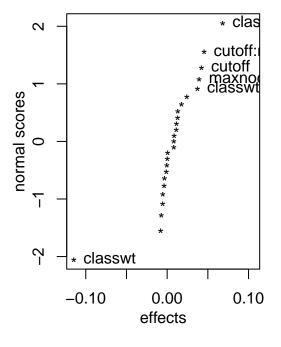
```
##
## Call:
## lm.default(formula = CV ~ .^2, data = coded.frac.design)
## Residuals:
##
        Min
                   1Q
                        Median
                                      30
                                              Max
## -0.035267 -0.003779 0.000000 0.003779
##
## Coefficients: (3 not defined because of singularities)
##
                     Estimate Std. Error t value Pr(>|t|)
                     ## (Intercept)
## ntree
                   -0.0016634
                               0.0059075 -0.282 0.78773
                    0.0064609
                               0.0059075
                                          1.094
## mtry
                                                 0.31605
## replace
                               0.0059075
                    0.0041166
                                          0.697
                                                 0.51198
## nodesize
                    0.0001064
                               0.0059075
                                          0.018 0.98621
## classwt
                   ## cutoff
                    0.0211215 0.0059075
                                          3.575
                                                0.01171 *
## maxnodes
                                          3.336
                    0.0197074
                              0.0059075
                                                0.01569
## ntree:mtry
                   -0.0035539
                              0.0059075 -0.602
                                                0.56946
## ntree:replace
                   -0.0025930 0.0059075
                                        -0.439
                                                 0.67608
## ntree:nodesize
                    0.0087954
                              0.0059075
                                         1.489
                                                 0.18710
                                         -0.038
## ntree:classwt
                   -0.0002265
                               0.0059075
                                                 0.97066
## ntree:cutoff
                    0.0057255
                               0.0059075
                                          0.969
                                                 0.36988
## ntree:maxnodes
                   -0.0018116
                               0.0059075
                                         -0.307
                                                 0.76947
## mtry:replace
                           NA
                                     NA
                                             NA
                                                      NA
## mtry:nodesize
                    -0.0004858
                               0.0059075
                                         -0.082
                                                 0.93714
## mtry:classwt
                    0.0041618
                               0.0059075
                                          0.705
                                                 0.50753
## mtry:cutoff
                           NA
                                     NA
                                             NA
                                                      NA
                    -0.0027243
## mtry:maxnodes
                               0.0059075
                                         -0.461
                                                 0.66093
## replace:nodesize
                    0.0121399
                               0.0059075
                                          2.055
                                                 0.08565 .
                    0.0065507
## replace:classwt
                               0.0059075
                                          1.109
                                                 0.30994
## replace:cutoff
                           NA
                                     NA
                                             NA
                                                      NA
## replace:maxnodes
                    0.0043273 0.0059075
                                          0.733
                                                0.49147
```

```
## nodesize:classwt -0.0039610 0.0059075
                                            -0.671
                                                   0.52749
## nodesize:cutoff
                      0.0056848
                                0.0059075
                                             0.962
                                                   0.37306
                                             0.060
                                                    0.95409
## nodesize:maxnodes
                     0.0003546
                                0.0059075
## classwt:cutoff
                      0.0186196
                                0.0059075
                                             3.152
                                                    0.01977 *
## classwt:maxnodes
                      0.0341566
                                0.0059075
                                             5.782
                                                    0.00117 **
  cutoff:maxnodes
                      0.0227729
                                0.0059075
                                             3.855
                                                    0.00841 **
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.03342 on 6 degrees of freedom
## Multiple R-squared: 0.9694, Adjusted R-squared: 0.8418
## F-statistic: 7.597 on 25 and 6 DF, p-value: 0.008985
```

Figure B.6

```
### we could also use DanielPlot() to check significant effects
par(mfrow = c(1,2))
DanielPlot(model, half =F, cex.fac = 1, cex.lab = 1, cex.pch = 1, cex.legend = 1)
DanielPlot(model, half =T, cex.fac = 1, cex.lab = 1, cex.pch = 1, cex.legend = 1)
```

Normal Plot for CV, alpha=0.05 Half Normal Plot for CV, alpha=0.0



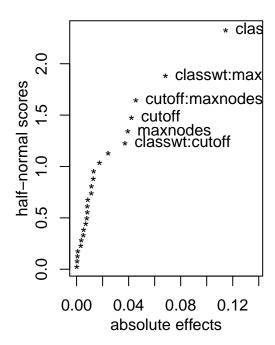


Figure B.7

```
### based on the result above (summary() and DanielPlot), we make a model.reduced.
model.reduced <- lm(CV ~ classwt + cutoff + maxnodes + classwt:maxnodes + cutoff:maxnodes +
     classwt:cutoff, data = coded.frac.design
 )
summary(model.reduced)
##
## Call:
## lm.default(formula = CV ~ classwt + cutoff + maxnodes + classwt:maxnodes +
##
      cutoff:maxnodes + classwt:cutoff, data = coded.frac.design)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                  3Q
                                         Max
## -0.049940 -0.020995 -0.000721 0.012140 0.080060
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 ## classwt
                 ## cutoff
                 0.019707 0.005238
## maxnodes
                                    3.763 0.000909 ***
## classwt:maxnodes 0.034157 0.005238 6.521 7.86e-07 ***
## cutoff:maxnodes
                           0.005238 4.348 0.000202 ***
                 0.022773
## classwt:cutoff
                 ## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.02963 on 25 degrees of freedom
## Multiple R-squared: 0.8997, Adjusted R-squared: 0.8756
## F-statistic: 37.38 on 6 and 25 DF, p-value: 2.643e-11
```

Figure B.8

Normal Q-Q Plot

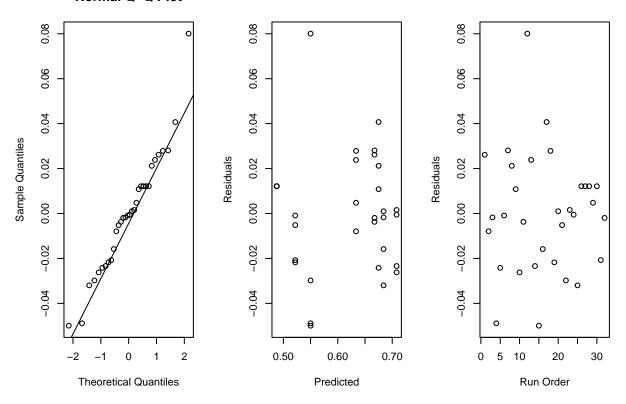


Figure B.9

```
##
                            Var.32run VIF.32run
## classwt
                              0.03125
## cutoff
                              0.03125
                              0.03125
## maxnodes
                                               1
## classwt:cutoff
                              0.03125
## classwt:maxnodes
                              0.03125
                                               1
## cutoff:maxnodes
                              0.03125
## classwt:cutoff:maxnodes
                              0.03125
```

Section C: D-Optimal Design

Figure C.1

```
# Create color map on pairwise correlations.
contrast.vectors.correlations.opt <- cor(X.opt)
corrplot(
   contrast.vectors.correlations.opt,
   type = "full",
   addgrid.col = "gray",
   tl.col = "black",
   tl.srt = 90,
   method = "color",
   tl.cex = 0.8
)</pre>
```

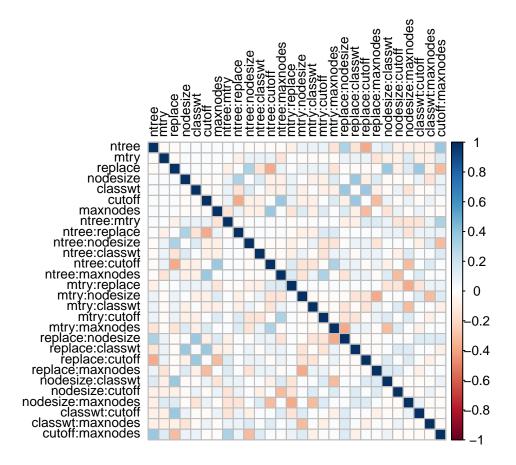


Figure C.3

```
var.eff.one1 <- diag(solve(t(X.opt)%*%X.opt))
results.opt <- data.frame('Var.35run' = var.eff.one1, 'VIF.35run' = nrow(X.opt)*var.eff.one1)
print.data.frame(results.opt)</pre>
```

```
##
                      Var.35run VIF.35run
## ntree
                     0.08922772 3.122970
## mtry
                     0.04061037 1.421363
## replace
                     0.36330573 12.715701
## nodesize
                     0.07035283 2.462349
## classwt
                                 2.803345
                     0.08009557
## cutoff
                     0.15530419
                                 5.435647
## maxnodes
                     0.16493098
                                 5.772584
                     0.08742056
                                 3.059720
## ntree:mtry
## ntree:replace
                     0.10260262
                                 3.591092
## ntree:nodesize
                     0.10456142
                                 3.659650
## ntree:classwt
                     0.03787607 1.325662
## ntree:cutoff
                     0.33133136 11.596597
## ntree:maxnodes
                     0.06801427
                                 2.380499
## mtry:replace
                     0.19896379
                                 6.963733
## mtry:nodesize
                     0.13366595
                                 4.678308
## mtry:classwt
                     0.05537739 1.938209
```

```
## mtry:cutoff
                    0.05071482 1.775019
                    0.18397234
                                6.439032
## mtry:maxnodes
                                2.689722
## replace:nodesize 0.07684919
## replace:classwt
                    0.07131243
                                2.495935
## replace:cutoff
                    0.08083831
                                2.829341
## replace:maxnodes 0.11435907
                                4.002568
## nodesize:classwt
                    0.25098104
                                8.784336
## nodesize:cutoff
                                2.153269
                    0.06152198
## nodesize:maxnodes 0.09795519
                                3.428432
## classwt:cutoff
                    0.19642274
                                6.874796
## classwt:maxnodes
                    0.05655215
                                1.979325
## cutoff:maxnodes
                    0.10004042
                                3.501415
```

Use cv.rf function to have a response variable

```
new_data1 <- D.opt</pre>
new_data1[,1][new_data1[,1]==1] <- 1000
new_data1[,1][new_data1[,1]==-1] <- 100
new data1[,2][new data1[,2]==1] \leftarrow 6
new_data1[,2][new_data1[,2]==-1] <- 2
new_data1[,3][new_data1[,3]==1] <- 1
new_data1[,3][new_data1[,3]==-1] <- 0
new_data1[,4][new_data1[,4]==1] <- 11
new_data1[,4][new_data1[,4]==-1] <- 1
new_data1[,5][new_data1[,5]==1] <- 0.9
new_data1[,5][new_data1[,5]==-1] <- 0.5
new_data1[,6][new_data1[,6]==1] <- 0.8
new_data1[,6][new_data1[,6]==-1] <- 0.2
new_data1[,7][new_data1[,7]==1] <- 1000</pre>
new_data1[,7][new_data1[,7]==-1] <- 10
print(new_data1) # data with actual values
```

```
##
        ntree mtry replace nodesize classwt cutoff maxnodes
## 3
                                                    0.2
          100
                  6
                           0
                                     1
                                            0.5
## 6
         1000
                                     1
                                            0.5
                                                    0.2
                                                                10
                  2
                           1
## 9
          100
                  2
                           0
                                    11
                                            0.5
                                                    0.2
                                                                10
## 16
         1000
                           1
                                    11
                                            0.5
                                                    0.2
                                                                10
## 18
         1000
                  2
                           0
                                     1
                                            0.9
                                                    0.2
                                                                10
## 20
                                            0.9
                                                    0.2
         1000
                  6
                           0
                                     1
                                                                10
## 25
          100
                  2
                           0
                                    11
                                            0.9
                                                    0.2
                                                                10
## 28
         1000
                           0
                                    11
                                            0.9
                                                    0.2
                                                                10
## 32
         1000
                                            0.9
                                                    0.2
                                                                10
                  6
                           1
                                    11
## 36
         1000
                  6
                           0
                                     1
                                            0.5
                                                    0.8
                                                                10
## 37
          100
                  2
                                     1
                                            0.5
                                                    0.8
                                                                10
                           1
## 39
          100
                                            0.5
                                                    0.8
                                                                10
                  6
                           1
                                     1
## 41
                                            0.5
                                                    0.8
          100
                  2
                           0
                                    11
                                                                10
## 42
         1000
                  2
                           0
                                    11
                                            0.5
                                                    0.8
                                                                10
## 53
          100
                  2
                           1
                                     1
                                            0.9
                                                    0.8
                                                                10
## 55
          100
                           1
                                     1
                                            0.9
                                                    0.8
                                                                10
                  6
                                            0.9
## 62
         1000
                  2
                           1
                                    11
                                                    0.8
                                                                10
```

```
## 63
          100
                                     11
                                            0.9
                                                     0.8
                                                                10
                           1
## 69
          100
                  2
                                            0.5
                                                     0.2
                                                              1000
                           1
                                      1
## 70
         1000
                                             0.5
                                                     0.2
                                                              1000
                                                              1000
## 75
          100
                           0
                                            0.5
                                                     0.2
                  6
                                    11
##
  78
         1000
                  2
                           1
                                     11
                                             0.5
                                                     0.2
                                                              1000
## 79
          100
                                            0.5
                                                     0.2
                                                              1000
                  6
                           1
                                    11
## 81
                                            0.9
                                                     0.2
                                                              1000
          100
                  2
                           0
                                      1
                                            0.9
                                                     0.2
                                                              1000
## 83
          100
                  6
                           0
                                      1
## 87
          100
                  6
                           1
                                      1
                                            0.9
                                                     0.2
                                                              1000
## 94
                                                     0.2
                                                              1000
         1000
                  2
                           1
                                     11
                                            0.9
## 98
         1000
                  2
                           0
                                     1
                                             0.5
                                                     0.8
                                                              1000
         1000
                                            0.5
                                                     0.8
                                                              1000
## 104
                  6
                           1
                                      1
## 107
          100
                  6
                           0
                                    11
                                            0.5
                                                     0.8
                                                              1000
## 108
                                                     0.8
         1000
                           0
                                            0.5
                                                              1000
## 114
         1000
                  2
                           0
                                            0.9
                                                     0.8
                                                              1000
                                     1
## 116
         1000
                  6
                           0
                                     1
                                            0.9
                                                     0.8
                                                              1000
## 125
                  2
                                                     0.8
                                                              1000
          100
                                    11
                                            0.9
                           1
## 128
         1000
                                             0.9
                                                     0.8
                                                              1000
```

Figure C.5

```
load("diabetes.RData")
```

```
new.opt.design.rf <- cv.rf(new_data1, y, X) # With the data actual values, we get a CV as a response va
```

```
## Collecting response on test combination
## Collecting response on test combination 11
## Collecting response on test combination
                                           17
## Collecting response on test combination
```

```
## Collecting response on test combination 24
## Collecting response on test combination 26
## Collecting response on test combination 26
## Collecting response on test combination 27
## Collecting response on test combination 28
## Collecting response on test combination 29
## Collecting response on test combination 30
## Collecting response on test combination 31
## Collecting response on test combination 32
## Collecting response on test combination 33
## Collecting response on test combination 34
## Collecting response on test combination 34
## Collecting response on test combination 35
```

new.opt.design <- new.opt.design.rf # matrix with actual values and CV.
new.opt.design</pre>

##		ntree	mtry	replace	nodesize	classwt	cutoff	maxnodes	CV
##	3	100	6	0	1	0.5	0.2	10	0.7096932
##	6	1000	2	1	1	0.5	0.2	10	0.6815332
##	9	100	2	0	11	0.5	0.2	10	0.6818357
##	16	1000	6	1	11	0.5	0.2	10	0.7100314
##	18	1000	2	0	1	0.9	0.2	10	0.5000000
##	20	1000	6	0	1	0.9	0.2	10	0.5000000
##	25	100	2	0	11	0.9	0.2	10	0.5000001
##	28	1000	6	0	11	0.9	0.2	10	0.5000000
##	32	1000	6	1	11	0.9	0.2	10	0.5000001
##	36	1000	6	0	1	0.5	0.8	10	0.6944846
##	37	100	2	1	1	0.5	0.8	10	0.6618889
##	39	100	6	1	1	0.5	0.8	10	0.6965686
##	41	100	2	0	11	0.5	0.8	10	0.6656089
##	42	1000	2	0	11	0.5	0.8	10	0.6676577
##	53	100	2	1	1	0.9	0.8	10	0.5002356
##	55	100	6	1	1	0.9	0.8	10	0.5161497
##	62	1000	2	1	11	0.9	0.8	10	0.5001244
##	63	100	6	1	11	0.9	0.8	10	0.5204936
##	69	100	2	1	1	0.5	0.2	1000	0.6571467
##	70	1000	2	1	1	0.5	0.2	1000	0.6567867
##	75	100	6	0	11	0.5	0.2	1000	0.6515474
##	78	1000	2	1	11	0.5	0.2	1000	0.6657825
##	79	100	6	1	11	0.5	0.2	1000	0.6387148
##	81	100	2	0	1	0.9	0.2	1000	0.5022576
##	83	100	6	0	1	0.9	0.2	1000	0.6339957
##	87	100	6	1	1	0.9	0.2	1000	0.6296801
##	94	1000	2	1	11	0.9	0.2	1000	0.5000089
##	98	1000	2	0	1	0.5	0.8	1000	0.6750711
##	104	1000	6	1	1	0.5	0.8	1000	0.6519865
##	107	100	6	0	11	0.5	0.8	1000	0.6762086
##	108	1000	6	0	11	0.5	0.8	1000	0.6810003
##	114	1000	2	0	1	0.9	0.8	1000	0.6975021
##	116	1000	6	0	1	0.9	0.8	1000	0.6539375
##	125	100	2	1	11	0.9	0.8	1000	0.6861553
##	128	1000	6	1	11	0.9	0.8	1000	0.7175336

```
extraction.data.coded <- cbind(D.opt,new.opt.design$CV)
colnames(extraction.data.coded)[8] <- "CV"
extraction.data.coded # data with coded values</pre>
```

```
##
                                                                            CV
        ntree mtry replace nodesize classwt cutoff maxnodes
                                                                -1 0.7096932
## 3
           -1
                  1
                          -1
                                     -1
                                              -1
                                                      -1
## 6
            1
                 -1
                           1
                                     -1
                                              -1
                                                      -1
                                                                -1 0.6815332
## 9
           -1
                 -1
                                              -1
                                                      -1
                                                                -1 0.6818357
                          -1
                                      1
                                                                -1 0.7100314
## 16
            1
                  1
                           1
                                      1
                                              -1
                                                      -1
## 18
            1
                 -1
                          -1
                                     -1
                                               1
                                                      -1
                                                                -1 0.5000000
## 20
            1
                  1
                          -1
                                     -1
                                                      -1
                                                                -1 0.5000000
## 25
                                                                -1 0.5000001
           -1
                 -1
                          -1
                                      1
                                               1
                                                      -1
## 28
            1
                  1
                          -1
                                      1
                                               1
                                                      -1
                                                                -1 0.5000000
## 32
            1
                                               1
                                                                -1 0.5000001
                  1
                           1
                                      1
                                                      -1
## 36
            1
                          -1
                                     -1
                                              -1
                                                                -1 0.6944846
## 37
                                                                -1 0.6618889
           -1
                 -1
                           1
                                     -1
                                              -1
                                                       1
## 39
           -1
                  1
                                     -1
                                              -1
                                                                -1 0.6965686
                           1
## 41
           -1
                 -1
                          -1
                                      1
                                              -1
                                                       1
                                                                -1 0.6656089
## 42
                 -1
                                              -1
                                                       1
                                                                -1 0.6676577
            1
                          -1
                                      1
                 -1
## 53
                                                       1
                                                                -1 0.5002356
           -1
                           1
                                     -1
                                               1
                                                                -1 0.5161497
## 55
           -1
                  1
                           1
                                     -1
                                               1
                                                       1
## 62
                                                                -1 0.5001244
            1
                 -1
                           1
                                      1
                                               1
                                                       1
## 63
                                                                -1 0.5204936
           -1
                  1
                           1
                                      1
                                               1
                                                       1
## 69
           -1
                 -1
                                     -1
                                              -1
                                                                 1 0.6571467
                           1
                                                      -1
## 70
            1
                 -1
                           1
                                     -1
                                              -1
                                                      -1
                                                                 1 0.6567867
## 75
                                              -1
           -1
                  1
                          -1
                                      1
                                                      -1
                                                                 1 0.6515474
                 -1
## 78
                                              -1
                                                      -1
                                                                 1 0.6657825
            1
                           1
                                      1
## 79
           -1
                  1
                           1
                                      1
                                              -1
                                                      -1
                                                                  1 0.6387148
## 81
           -1
                 -1
                          -1
                                     -1
                                               1
                                                      -1
                                                                  1 0.5022576
## 83
                  1
                                     -1
                                               1
                                                                  1 0.6339957
## 87
                                                      -1
                                                                  1 0.6296801
           -1
                  1
                                     -1
                                               1
                           1
## 94
            1
                 -1
                           1
                                     1
                                               1
                                                      -1
                                                                  1 0.5000089
## 98
                                                                 1 0.6750711
            1
                 -1
                          -1
                                     -1
                                              -1
                                                       1
## 104
            1
                           1
                                              -1
                                                       1
                                                                 1 0.6519865
## 107
                                              -1
                                                                 1 0.6762086
           -1
                          -1
                                                       1
                  1
                                      1
## 108
                                                       1
                                                                 1 0.6810003
            1
                  1
                          -1
                                      1
                                              -1
                                                                 1 0.6975021
## 114
            1
                 -1
                                     -1
                                               1
                                                       1
                          -1
## 116
            1
                  1
                          -1
                                     -1
                                               1
                                                       1
                                                                 1 0.6539375
## 125
           -1
                 -1
                           1
                                      1
                                               1
                                                       1
                                                                  1 0.6861553
## 128
            1
                  1
                           1
                                               1
                                                       1
                                                                  1 0.7175336
```

```
# Here, we've got 2 types of data.set (1: with actual values 2: with coded.values)
# new.opt.design # with actual values
# extraction.data.coded # with coded values
```

Figure C.7

```
coded.model <- lm(CV~., data = extraction.data.coded)
summary(coded.model) # Here, we now want to find significant effects</pre>
```

##

```
## Call:
## lm.default(formula = CV ~ ., data = extraction.data.coded)
## Residuals:
                1Q
                   Median
                                 3Q
## -0.07394 -0.04064 -0.01566 0.04080 0.11002
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.6187998 0.0096143 64.363 < 2e-16 ***
## ntree
             0.0008358 0.0096143
                                   0.087
                                           0.9314
## mtry
              0.0079794 0.0096143
                                          0.4138
                                   0.830
## replace
             -0.0026431 0.0096143 -0.275
                                          0.7855
## nodesize
             -0.0044734 0.0096143 -0.465
                                           0.6455
## classwt
             ## cutoff
              0.0177435 0.0096143
                                   1.846
                                           0.0760 .
                                           0.0189 *
## maxnodes
             0.0240051 0.0096143
                                   2.497
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.05668 on 27 degrees of freedom
## Multiple R-squared: 0.6218, Adjusted R-squared: 0.5238
## F-statistic: 6.342 on 7 and 27 DF, p-value: 0.0001839
```

```
coded.model.int <- lm(CV~.^2, data = extraction.data.coded)
summary(coded.model.int) # what about two-interaction terms!</pre>
```

```
##
## lm.default(formula = CV ~ .^2, data = extraction.data.coded)
##
## Residuals:
##
        Min
                       Median
                  1Q
                                    30
                                             Max
## -0.041591 -0.020273 0.002848 0.015621 0.028378
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -0.0052847 0.0145850 -0.362 0.72952
## ntree
                   0.0115837 0.0097774
                                        1.185 0.28092
## mtry
## replace
                   -0.0090624
                             0.0311111
                                       -0.291 0.78064
                   -0.0006818
                             0.0129063 -0.053 0.95959
## nodesize
## classwt
                   -0.0510300 0.0137362 -3.715 0.00991 **
                   0.0234086 0.0192612
## cutoff
                                        1.215 0.26989
## maxnodes
                   0.0248004 0.0205536
                                        1.207 0.27299
                   -0.0050591 0.0149293 -0.339 0.74625
## ntree:mtry
## ntree:replace
                   0.0005055 0.0155612
                                         0.032 0.97514
## ntree:nodesize
                   0.0056171 0.0159766
                                       0.352 0.73717
## ntree:classwt
                  -0.0055235 0.0094612 -0.584 0.58062
## ntree:cutoff
                   -0.0006514 0.0288473 -0.023 0.98272
```

```
## ntree:maxnodes
                   -0.0027048 0.0127550 -0.212 0.83908
## mtry:replace 0.0049627 0.0232095 0.214 0.83777
## mtry:nodesize
                  -0.0002519 0.0186627 -0.013 0.98967
                   0.0077227 0.0114717
## mtry:classwt
                                        0.673 0.52589
## mtry:cutoff
                  -0.0086406 0.0111727 -0.773 0.46867
## mtry:maxnodes
                  0.0025891 0.0211858 0.122 0.90672
## replace:nodesize -0.0015711 0.0135589 -0.116 0.91153
                   -0.0091661 0.0130129 -0.704 0.50760
## replace:classwt
## replace:cutoff
                  -0.0059641 0.0141653 -0.421 0.68840
## replace:maxnodes 0.0085898 0.0168493 0.510 0.62839
## nodesize:classwt 0.0074111 0.0259237 0.286 0.78458
                    0.0021030 0.0121429 0.173 0.86820
## nodesize:cutoff
## nodesize:maxnodes 0.0061127 0.0156883 0.390 0.71026
## classwt:cutoff 0.0230303 0.0228151 1.009 0.35173
## classwt:maxnodes 0.0341955 0.0117437
                                         2.912 0.02692 *
## cutoff:maxnodes
                   0.0195318 0.0157752
                                         1.238 0.26191
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.04849 on 6 degrees of freedom
## Multiple R-squared: 0.9385, Adjusted R-squared: 0.6514
## F-statistic: 3.269 on 28 and 6 DF, p-value: 0.07143
```

```
coded.model.reduced <- lm(CV~.^2 - replace - ntree:cutoff - nodesize:classwt, data = extraction.data.co
summary(coded.model.reduced)
```

```
##
## Call:
## lm.default(formula = CV ~ .^2 - replace - ntree:cutoff - nodesize:classwt,
      data = extraction.data.coded)
##
## Residuals:
##
        Min
                        Median
                   1Q
                                      30
                                               Max
## -0.038524 -0.017245 0.001948 0.016683 0.031684
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    6.211e-01 7.098e-03 87.497 1.69e-14 ***
                    -6.066e-03 1.137e-02 -0.534 0.606545
## ntree
                    1.133e-02 7.925e-03 1.430 0.186634
## mtry
## nodesize
                    -8.473e-04 9.091e-03 -0.093 0.927785
                    -5.316e-02 9.640e-03 -5.515 0.000373 ***
## classwt
## cutoff
                    2.427e-02 1.307e-02 1.857 0.096238
## maxnodes
                    2.278e-02 8.839e-03 2.577 0.029829 *
                   -7.443e-03 9.543e-03 -0.780 0.455447
## ntree:mtry
## ntree:replace
                   1.879e-05 1.063e-02 0.002 0.998628
## ntree:nodesize
                    3.485e-03 8.933e-03 0.390 0.705503
## ntree:classwt
                   -4.611e-03 7.716e-03 -0.598 0.564855
## ntree:maxnodes
                   -1.949e-03 1.008e-02 -0.193 0.850944
                   -6.899e-04 9.718e-03 -0.071 0.944957
## mtry:replace
```

```
## mtry:nodesize
                 2.595e-03 1.054e-02 0.246 0.811071
## mtry:classwt
                   7.224e-03 8.286e-03 0.872 0.405959
                  -6.749e-03 8.709e-03 -0.775 0.458259
## mtry:cutoff
## mtry:maxnodes
                  1.079e-03 8.602e-03 0.125 0.902951
## replace:nodesize 3.623e-04 1.053e-02 0.034 0.973305
## replace:classwt -6.758e-03 9.476e-03 -0.713 0.493821
## replace:cutoff
                  -2.464e-03 1.035e-02 -0.238 0.817231
## replace:maxnodes 1.105e-02 1.185e-02 0.933 0.375143
## nodesize:cutoff
                   1.095e-03 9.777e-03 0.112 0.913312
## nodesize:maxnodes 8.395e-04 1.000e-02 0.084 0.934932
## classwt:cutoff
                1.780e-02 7.783e-03 2.287 0.047981 *
## classwt:maxnodes 3.619e-02 8.609e-03 4.204 0.002293 **
## cutoff:maxnodes 2.293e-02 9.889e-03 2.319 0.045576 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.04054 on 9 degrees of freedom
## Multiple R-squared: 0.9355, Adjusted R-squared: 0.7564
## F-statistic: 5.223 on 25 and 9 DF, p-value: 0.006921
### summary(coded.model.reduced) gives us some significant effects
coded.model.reduced.two <- lm(CV~(classwt + maxnodes + classwt:cutoff + classwt:maxnodes + cutoff:maxno
                       data = extraction.data.coded)
summary(coded.model.reduced.two)
##
## Call:
## lm.default(formula = CV ~ (classwt + maxnodes + classwt:cutoff +
##
      classwt:maxnodes + cutoff:maxnodes), data = extraction.data.coded)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                    3Q
## -0.093783 -0.007918 -0.001815 0.015728 0.056058
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  ## classwt
                  ## maxnodes
## classwt:cutoff
                   0.015943 0.005859
                                      2.721 0.010887 *
## classwt:maxnodes 0.037794 0.005842
                                      6.470 4.43e-07 ***
## maxnodes:cutoff
                   0.017898 0.005859
                                      3.055 0.004795 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.03449 on 29 degrees of freedom
## Multiple R-squared: 0.8496, Adjusted R-squared: 0.8237
## F-statistic: 32.77 on 5 and 29 DF, p-value: 4.386e-11
```

Figure C.10

Normal Q-Q Plot

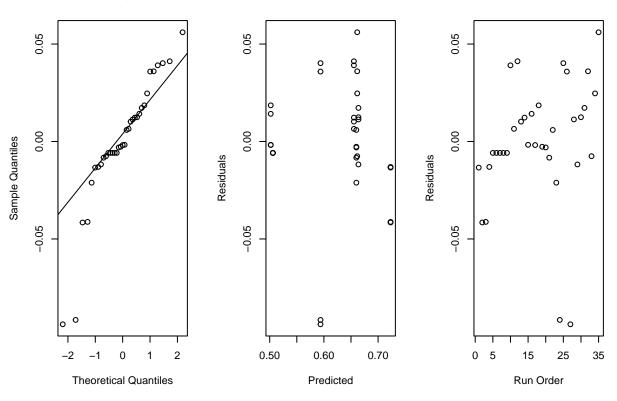


Figure C.11

classwt
maxnodes

classwt:maxnodes

```
X.frac_new <- model.matrix(~(classwt + maxnodes + classwt:cutoff + classwt:maxnodes + cutoff:maxnodes)^
var.eff.one.3 <- diag(solve(t(X.frac_new)%*%X.frac_new))

results.frac.3 <- data.frame('Var.35run' = var.eff.one.3, 'VIF.35run' = nrow(X.frac_new)*var.eff.one.3)

print.data.frame(results.frac.3)</pre>

##

Var.35run VIF.35run
```

0.02886513 1.010280

0.02886513 1.010280 0.02869152 1.004203

```
## classwt:cutoff 0.02886513 1.010280
## maxnodes:cutoff 0.02886513 1.010280
## classwt:maxnodes:cutoff 0.02869152 1.004203
```

Section D: TA's Design

Figure D.1

```
source("CrossValidation_RF.R")
TAdesign \leftarrow data.frame(c(100,550,1000,1000,1000)
                        100,1000,100,100,100,
                        100,1000,100,550,100,
                        1000,1000,1000,100,1000,
                        550,550)
,c(2,2,4,6,6,
   2,2,2,6,6,
   4,2,6,4,6,
   6,2,6,2,2,
   4,6)
,c(1,0,1,1,0,
   0,0,0,1,0,
   0,1,1,0,0,
   0,0,1,1,1,
   1,1)
,c(11,1,1,1,1,
   1,6,11,1,1,
   11,11,6,6,11,
   11,11,11,1,1,
   6,11)
,c(0.5,0.5,0.5,0.5,0.9,
   0.5,0.9,0.9,0.7,0.9,
   0.9,0.5,0.5,0.7,0.5,
   0.5,0.7,0.9,0.9,0.9,
   0.7, 0.9)
,c(0.8,0.2,0.2,0.8,0.2,
   0.8,0.8,0.2,0.8,0.5,
   0.8,0.5,0.2,0.5,0.2,
   0.8,0.2,0.2,0.2,0.8,
   0.5, 0.8)
,c(10,10,10,1000,1000,
   1000,10,10,10,10,
   1000,1000,1000,505,505,
   10,1000,10,1000,505,
   505,1000))
colnames(TAdesign) <- c("ntree", "mtry", "replace", "nodesize", "classwt", "cutoff", "maxnodes")</pre>
print(TAdesign, row.names = FALSE)
##
   ntree mtry replace nodesize classwt cutoff maxnodes
##
      100
             2
                     1
                              11
                                     0.5
                                            0.8
      550
                     0
                                            0.2
                                                       10
##
             2
                              1
                                     0.5
##
     1000
                                     0.5
                                            0.2
                                                       10
                                     0.5
##
     1000
                     1
                             1
                                            0.8
                                                   1000
             6
```

```
1000
                                        0.9
                                                0.2
                                                         1000
##
##
      100
              2
                       0
                                        0.5
                                                0.8
                                                         1000
                                  1
     1000
                                                0.8
##
                                        0.9
                                                            10
      100
                                        0.9
                                                0.2
##
              2
                       0
                                11
                                                            10
##
      100
              6
                       1
                                 1
                                        0.7
                                                0.8
                                                            10
##
      100
                       0
                                        0.9
                                                0.5
                                                            10
              6
                                 1
##
      100
                       0
                                11
                                        0.9
                                                0.8
                                                         1000
##
     1000
                                11
                                        0.5
                                                0.5
                                                         1000
              2
                       1
##
      100
              6
                       1
                                  6
                                        0.5
                                                0.2
                                                         1000
##
      550
                       0
                                 6
                                        0.7
                                                0.5
                                                          505
##
      100
              6
                       0
                                11
                                        0.5
                                                0.2
                                                          505
     1000
                                        0.5
                                                0.8
##
                       0
                                11
                                                            10
              6
     1000
                                                0.2
##
              2
                       0
                                11
                                        0.7
                                                         1000
##
     1000
                                        0.9
                                                0.2
              6
                       1
                                11
                                                            10
##
      100
              2
                                        0.9
                                                0.2
                                                         1000
                       1
                                 1
##
     1000
                       1
                                  1
                                        0.9
                                                0.8
                                                          505
##
      550
                                  6
                                        0.7
                                                0.5
                                                          505
              4
                       1
      550
##
                                11
                                        0.9
                                                0.8
                                                         1000
```

TAresults # matrix with CV as a response variable

1

ntree mtry replace nodesize classwt cutoff maxnodes

11

Figure D.2

1

100

2

```
load("diabetes.RData")
TAresults <- cv.rf(TAdesign, y, X)
## Collecting response on test combination 1
## Collecting response on test combination 2
## Collecting response on test combination
## Collecting response on test combination 4
## Collecting response on test combination 5
## Collecting response on test combination 6
## Collecting response on test combination
## Collecting response on test combination 8
## Collecting response on test combination 9
## Collecting response on test combination 10
## Collecting response on test combination 11
## Collecting response on test combination 12
## Collecting response on test combination
## Collecting response on test combination 14
## Collecting response on test combination 15
## Collecting response on test combination
## Collecting response on test combination
## Collecting response on test combination
## Collecting response on test combination 19
## Collecting response on test combination
## Collecting response on test combination
## Collecting response on test combination
```

0.8

0.5

CV

10 0.6635911

```
## 2
        550
                2
                         0
                                   1
                                          0.5
                                                  0.2
                                                             10 0.6820796
## 3
       1000
                4
                                          0.5
                         1
                                   1
                                                  0.2
                                                             10 0.7031909
## 4
       1000
                6
                         1
                                   1
                                          0.5
                                                  0.8
                                                           1000 0.6509424
       1000
                6
                         0
                                                  0.2
                                                           1000 0.6349065
## 5
                                   1
                                          0.9
## 6
        100
                2
                         0
                                   1
                                          0.5
                                                  0.8
                                                           1000 0.6743822
## 7
                2
                         0
                                   6
       1000
                                          0.9
                                                  0.8
                                                             10 0.5002134
## 8
        100
                2
                         0
                                  11
                                          0.9
                                                  0.2
                                                             10 0.5000000
## 9
        100
                6
                         1
                                   1
                                          0.7
                                                  0.8
                                                             10 0.7222842
## 10
        100
                6
                         0
                                   1
                                          0.9
                                                  0.5
                                                             10 0.5004667
                         0
## 11
        100
                4
                                  11
                                          0.9
                                                  0.8
                                                           1000 0.7128980
## 12
       1000
                2
                         1
                                  11
                                          0.5
                                                  0.5
                                                           1000 0.7394889
                                   6
## 13
        100
                6
                         1
                                          0.5
                                                  0.2
                                                           1000 0.6258453
## 14
        550
                4
                         0
                                   6
                                          0.7
                                                  0.5
                                                            505 0.7083643
## 15
        100
                6
                         0
                                  11
                                          0.5
                                                  0.2
                                                            505 0.6544887
       1000
                         0
## 16
                6
                                  11
                                          0.5
                                                  0.8
                                                             10 0.6939424
## 17
       1000
                2
                         0
                                  11
                                          0.7
                                                  0.2
                                                           1000 0.5447868
## 18
       1000
                6
                         1
                                  11
                                          0.9
                                                  0.2
                                                             10 0.5000001
## 19
        100
                2
                         1
                                   1
                                          0.9
                                                  0.2
                                                           1000 0.5022178
## 20
       1000
                2
                                   1
                                          0.9
                                                  0.8
                                                            505 0.7002000
                         1
## 21
        550
                4
                         1
                                   6
                                          0.7
                                                  0.5
                                                            505 0.7176668
                                                           1000 0.7160623
## 22
        550
                6
                         1
                                  11
                                          0.9
                                                  0.8
```

Figure D.3

```
TA.coded.data <- TAresults
TA.coded.data[,1][TA.coded.data[,1]==100] \leftarrow -1
TA.coded.data[,1][TA.coded.data[,1]==550] \leftarrow 0
TA.coded.data[,1][TA.coded.data[,1]==1000] \leftarrow 1
TA.coded.data[,2][TA.coded.data[,2]==2] \leftarrow -1
TA.coded.data[,2][TA.coded.data[,2]==4] \leftarrow 0
TA.coded.data[,2][TA.coded.data[,2]==6] <- 1
TA.coded.data[,3][TA.coded.data[,3]==0] \leftarrow -1
TA.coded.data[,3][TA.coded.data[,3]==1] \leftarrow 1
TA.coded.data[,4][TA.coded.data[,4]==1] \leftarrow -1
TA.coded.data[,4][TA.coded.data[,4]==6] \leftarrow 0
TA.coded.data[,4][TA.coded.data[,4]==11] \leftarrow 1
TA.coded.data[,5][TA.coded.data[,5]==0.5] \leftarrow -1
TA.coded.data[,5][TA.coded.data[,5]==0.7] \leftarrow 0
TA.coded.data[,5][TA.coded.data[,5]==0.9] \leftarrow 1
TA.coded.data[,6][TA.coded.data[,6]==0.2] \leftarrow -1
TA.coded.data[,6][TA.coded.data[,6]==0.5] \leftarrow 0
TA.coded.data[,6][TA.coded.data[,6]==0.8] \leftarrow 1
TA.coded.data[,7][TA.coded.data[,7]==10] \leftarrow -1
TA.coded.data[,7][TA.coded.data[,7]==505] <- 0
TA.coded.data[,7][TA.coded.data[,7]==1000] \leftarrow 1
```

print(TA.coded.data) # data with coded vales

```
ntree mtry replace nodesize classwt cutoff maxnodes
                                                            CV
                                                   -1 0.6635911
## 1
        -1
             -1
                                    -1
                                           1
                     1
                             1
## 2
             -1
                    -1
                            -1
                                    -1
                                           -1
                                                   -1 0.6820796
## 3
         1
             0
                     1
                            -1
                                    -1
                                           -1
                                                   -1 0.7031909
## 4
                            -1
                                                    1 0.6509424
         1
             1
                     1
                                    -1
                                           1
## 5
             1
                    -1
                            -1
                                                   1 0.6349065
         1
                                    1
                                          -1
## 6
        -1
            -1
                    -1
                            -1
                                    -1
                                          1
                                                   1 0.6743822
## 7
                            0
                                    1
                                          1
                                                   -1 0.5002134
        1
            -1
                    -1
                            1
## 8
        -1
             -1
                    -1
                                    1
                                           -1
                                                   -1 0.5000000
## 9
        -1
                    1
                            -1
                                    0
                                          1
                                                   -1 0.7222842
           1
## 10
        -1
            1
                    -1
                            -1
                                    1
                                          0
                                                   -1 0.5004667
                    -1
## 11
        -1
             0
                                                   1 0.7128980
                             1
                                    1
                                          1
## 12
        1
                    1
                             1
                                    -1
                                           0
                                                   1 0.7394889
            -1
## 13
                             0
        -1
           1
                    1
                                   -1
                                          -1
                                                   1 0.6258453
## 14
        0
             0
                    -1
                             0
                                   0
                                           0
                                                   0 0.7083643
## 15
        -1
                    -1
                                   -1
                                           -1
                                                   0 0.6544887
             1
                             1
                                          1
## 16
        1
            1
                    -1
                            1
                                   -1
                                                   -1 0.6939424
## 17
                                    0
                                          -1
            -1
                    -1
                            1
                                                   1 0.5447868
## 18
                                          -1
                                                   -1 0.5000001
        1
             1
                    1
                             1
                                    1
## 19
        -1
             -1
                     1
                            -1
                                     1
                                          -1
                                                   1 0.5022178
## 20
         1
            -1
                     1
                            -1
                                     1
                                          1
                                                    0 0.7002000
## 21
             0
                     1
                                     0
         0
                             0
                                          0
                                                    0 0.7176668
## 22
         0
             1
                     1
                             1
                                     1
                                          1
                                                    1 0.7160623
```

