

Final Project

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Task 1

1 Statement of Problem

2 Hypotheses and Theories

3 Solution of the Problem

4 Conclusion

Task 2

5 Statement of Problem

Task 2 utilizes a wave ray tracing algorithm and local bathymetry information, provided for Narragansett Bay, in order to propagate storm waves determined from task 1. In order to complete this task, simulations are conducted for the 20 and 50 year storms along with creating rays that intersect along the shoreline of Narragansett Beach. For the 20 year storm simulations, use the ray spacing on the beach to calculate a refraction coefficient for each section of beach. Then, using bathymetry data from a chart near the beach, estimate the beach slope. This is used along with the deep water wave properties and refraction coefficient to estimate the shoaling coefficient, breaking depth, and breaker height.

6 Hypotheses and Theories

When waves propagate over a non uniform sea floor, some parts of the wave travel faster than others. The parts of the wavefront that propagate more quickly shift the overall direction of the front. Depending on the local bathymetry, wavefronts can become focused or de-focused as they approach the shoreline. Seen in 1, the refraction coefficient can be determined by observing the distance between two wave rays propagating through a region.

$$K_r = \sqrt{\frac{b_o}{b}} \quad (1)$$

In shallow water, waves slow down and experience an increase in wave height due to shoaling. The degree of wave refraction, and the shoaling coefficient dictate breaking wave height and water depth. Seen in 4,

the ratio of phase speed and group celerity changes as water depth approaches the shallow water condition. With the deep water characteristics, and angle of incidence, breaker depth and wave height can be found iteratively.

$$c = c_o * \tanh(kh); \quad (2)$$

$$c_g = \frac{c}{2} * \left(1 + \frac{2kh}{\sinh(2kh)} \right) \quad (3)$$

$$K_s = \sqrt{c/2c_g} \quad (4)$$

$$H_b = H_o K_{sb} K_{rb} = \kappa h_b \quad (5)$$

$$K_{sb} = F(L, h) \quad (6)$$

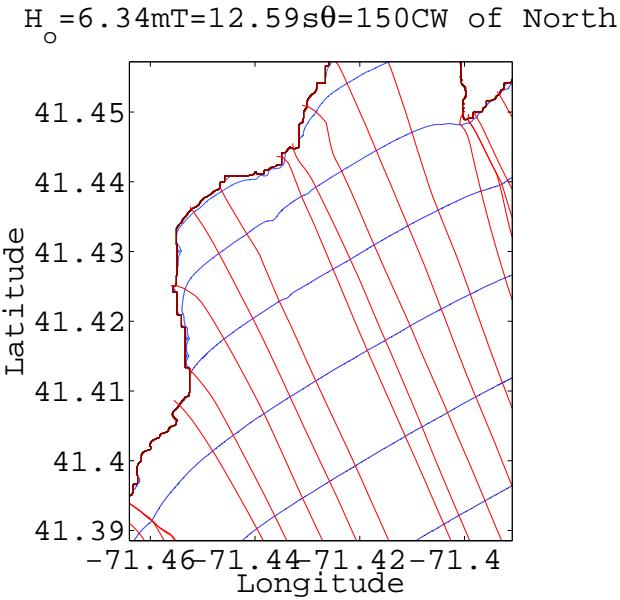
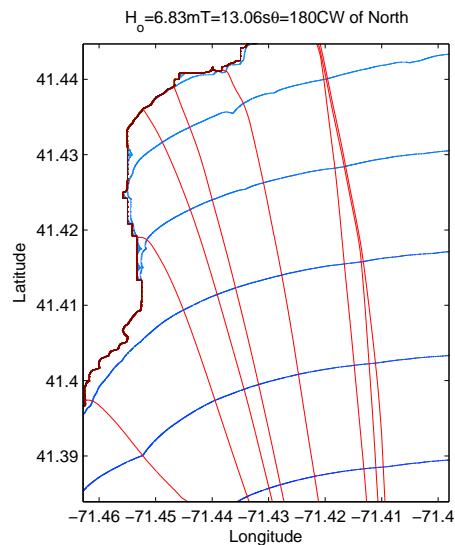
$$K_{rb} = F(L, h, \theta_o) \quad (7)$$

The programs supplied for the problem simulated waves propagating into the region of coastline surrounding Narragansett Beach. The programs required deep water wave characteristics, and latitude-longitude grid resolution.

7 Solution of the Problem

Using the supplied C functions and waveray.m, wave rays were propagated into Narragansett Beach under the conditions determined in Task 1. Twenty and fifty year predicted wave parameters were used to simulate the path lines extreme waves followed. Seen in CITE WAVEDIR FIGURE HERE, three predominant angles of incidence were determined from the supplied data. Waveray.m was non-intuitive, and didn't allow for manipulation of the rendered area without disrupting the ray simulation. As a result, most of the renders did not intersect Narragansett Beach with more than two or three rays.

The 20 year predicted wave conditions were simulated at for each of the three predominant angles of incidence. De-focusing was observed in each simulation, and was most extreme in 3. Figures 1 and 2 indicated a large degree of local de-focusing in the bathymetry of Narragansett Beach. Wave rays can be seen spreading out as they approached the shoreline.

Figure 1: 20y Predicted Wave Rays at 150° angle of incidenceFigure 2: 20y Predicted Wave Rays at 180° angle of incidence

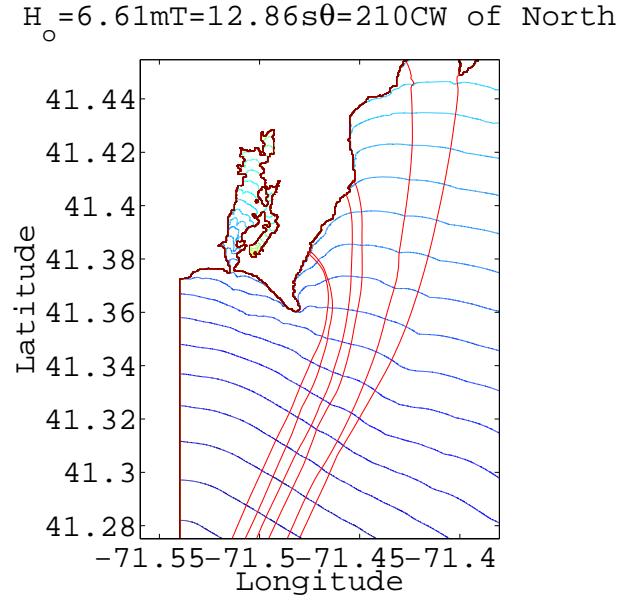


Figure 3: Breaking Wave Characteristics for 20 Year extreme wave at 210° angle of incidence

Seen below, the simulated wave rays for the 50 year predicted conditions were very similar to their 20 year counterparts. The bathymetry of Narragansett Beach caused most of the wave rays to de-focus as they propagated into the coastline. Figures 4 and 5 supported the simulations run for the 20 year predicted wave characteristics. The wave rays de-focused as they approached the coastline. Similarly, 6 confirmed that large amounts of de-focusing occurred before the wave fronts got close to Narragansett Beach.

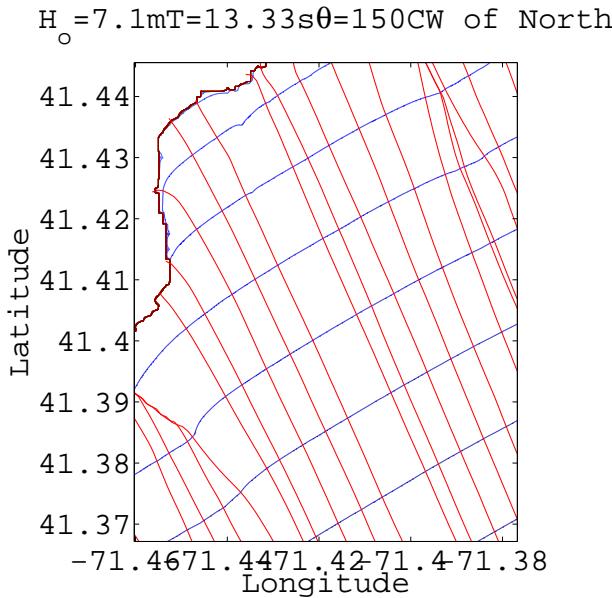
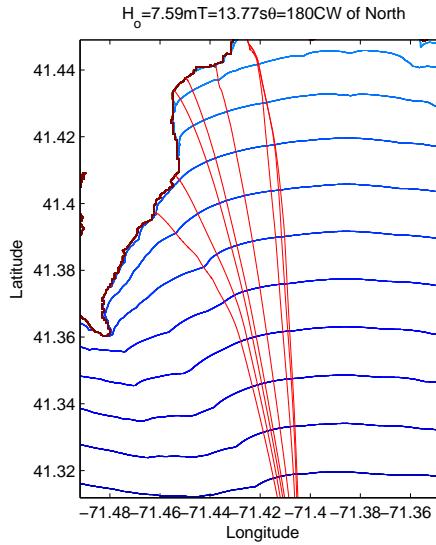
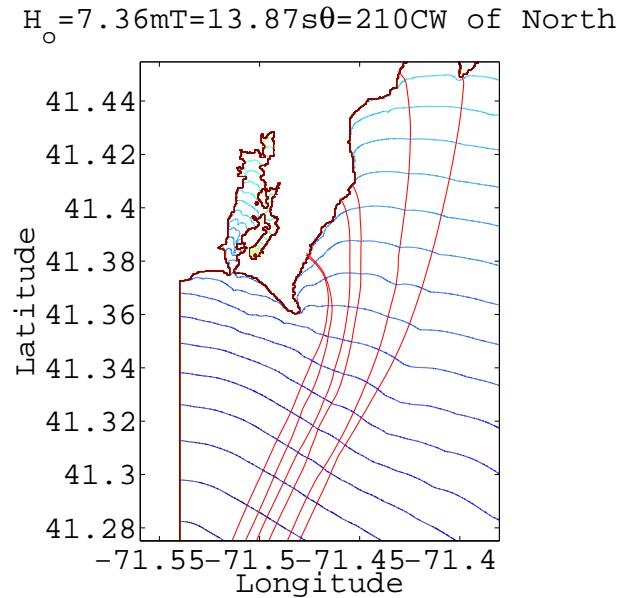


Figure 4: 50y Predicted Wave Rays at 150° angle of incidence

Figure 5: 50y Predicted Wave Rays at 180° angle of incidenceFigure 6: 50y Predicted Wave Rays at 180° angle of incidence

The predicted breaking wave characteristics were not accurate. The calculated shoaling coefficients were extremely small, and indicated that the breaking wave characteristics were not evaluated properly. Due to the nature of the program, it was difficult to render wave rays across short regions. As such, the resolutions required to fully map the beach were not achieved. It was not possible to evaluate the characteristics of the 210° angle of incidence wave fronts. Seen in 3 and 6 the rays that propagated close to the beach de-shoaled significantly before they got to the coastline.

Ray:	K_r	K_s	H_b , m.	h_b , m.	$\frac{H_b}{h_b}$
1	1.0	0.1	5.2	7.6	0.7
2	1.0	0.0	3.4	7.5	0.5

Table 1: Breaking Wave Characteristics for 20 Year extreme wave at 150° angle of incidence

Ray:	K_r	K_s	H_b , m.	h_b , m.	$\frac{H_b}{h_b}$
1	1.0	0.1	5.8	8.2	0.7
2	1.0	0.1	4.9	8.2	0.6

Table 2: Breaking Wave Characteristics for 20 Year extreme wave at 180° angle of incidence

Ray:	K_r	K_s	H_b , m.	h_b , m.	$\frac{H_b}{h_b}$
1	1.0	0.1	6.2	8.6	0.7
2	1.0	0.0	4.0	8.5	0.5

Table 3: Breaking Wave Characteristics for 50 Year extreme wave at 150° angle of incidence

Ray:	K_r	K_s	H_b , m.	h_b , m.	$\frac{H_b}{h_b}$
1	1.0	0.1	6.8	9.2	0.7
2	1.0	0.0	4.2	9.0	0.5

Table 4: Breaking Wave Characteristics for 50 Year extreme wave at 180° angle of incidence

Diffraction modeling would have influenced our 210° angle of incidence waves. Bloc

8 Conclusion

After manually evaluating the breaking wave characteristics, it indicated that the simulated wave rays would experience de-focusing. From the data in task 1, the simulated wave rays for the 50 year extreme showed similarity to their 20 year counterparts. Narragansett Beach also de-focused the rays that hit the beach. The degree of de-focusing can be observed to increase as the angle of incidence approaches 210° . Overall, using the supplied functions given, the wave ray analysis on Narragansett Beach under the conditions determined in task 1 proved that the simulated wave rays experienced de-focusing.

Appendices

A MATLAB Calculations