

AI5031: Machine learning, exercise sheet 3

1 Preparations

Download the file `linclass_skeleton.py` from the E-Learning site and execute it with `python3`. If you are on a non-graphical terminal, download the Python file via

```
wget http://www.gepperth.net/alexander/downloads/linclass_skeleton.py
```

The program should load the data into `traind` and `trainl`. Please inspect the code!

2 ReLU

Implement the ReLU function as a Python function `r(X)` where `X` is a numpy array of arbitrary shape. Call the function from `__main__` and print out results for $X = \begin{pmatrix} -1 & -1 & 5 \\ 1 & 1 & 2 \end{pmatrix}$. Hint: use mask indexing to set the negative parts of `X` to zero!

3 Softmax

Implement the softmax function in the method `LinearClassifier.S`. It should accept a 2D np.array `X` and return a np.array of the same dimensions. The usual assumptions that rows of `X` contain data samples holds here as well. Caution: you may need to work with reshape and broadcasting here to implement the softmax formula! Call the function from `__main__` and print out results for $X = \begin{pmatrix} -1 & -1 & 5 \\ 1 & 1 & 2 \end{pmatrix}$. Perform the computation on paper to verify your results!

4 Implementing the cross-entropy loss

Implement the cross-entropy loss in the method `LinearClassifier.loss`. It should receive two 2D np.array's `Y` and `T`, where `Y` is computed by `LinearClassifier.f`. Test it, from `__main__`, with the first digit and first label of the train data! Test with 2D matrices as well, each having a single row. The first row of `Y` should be `(0,0,0,0.5,0,0.3,0,0.2, 0, 0)`, the first row of `T` should be `(0,0,0,0,1,0,0,0,0,0)`.

5 Implementing the model function

Implement a linear classifier in the method `LinearClassifier.f`. It should receive a 2D np.array with `N` rows and 784 columns, and produce a 2D np.array of `N` rows and 10 columns (why?). Test it, from `__main__`, with the first digit from the training data!