

- Fórmulas útiles para resolver recurrencias:

$$\log_a(x^y) = y \cdot \log_a(x)$$

$$x^{\log_a(y)} = y^{\log_a(x)}$$

$$(x^y)^z = (x^z)^y \quad \text{si } 0 \neq 0 \rightarrow x^{(y^z)} \neq x^{(z^y)}$$

$$\log_a(x) = \frac{\log_b(x)}{\log_b(a)}$$

↓ $\log_b(a)$

se puede cambiar de base considerando una constante multiplicativa, $\log_b(a)$

$$\log_a(x \cdot y) = \log_a(x) + \log_a(y)$$

$$\log_a\left(\frac{x}{y}\right) = \log_a(x) - \log_a(y)$$

$$x^{(y+z)} = x^y \cdot x^z$$

$$x^{(y-z)} = \frac{x^y}{x^z}$$

$$(x^y)^z = x^{(y \cdot z)}$$

- Fórmulas útiles para bucles anidados:

Progresión aritmética

$$a_{i+1} = a_i + d$$

$$\sum_{i=1}^n a_i = \frac{n(a_1 + a_n)}{2}$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}$$

Progresión geométrica

$$a_{i+1} = a_i \cdot d$$

$$\sum_{i=1}^n a_i = \frac{a_{n+1} - a_1}{d - 1}$$

$$\sum_{i=1}^n b^i = \frac{b^{(n+1)} - b}{b - 1}$$

$$\sum a + b = \sum a + \sum b$$

$$\sum_{i=1}^n a = a \cdot n$$

$$\sum_{i=1}^n a \cdot f(i) = a \cdot \sum_{i=1}^n f(i)$$

$$\sum_{i=p}^q i = \frac{(q+p)(q-p+1)}{2}$$

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{i=1}^n i^3 = \left[\frac{n(n+1)}{2} \right]^2$$

$$\sum_{i=1}^n i \cdot (i+1) = \frac{n \cdot (n+1)(n+2)}{3}$$