# Module 1: The Nature of Fluids/Pressure Measurement (CIVL 318)

# Some useful results:

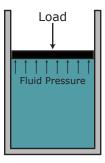
Table A: Properties of Water

Table B: Properties of Common Liquids (at 101 kPa and 25°C)

Temperature	Specific Weight	Density	Dynamic Viscosity
	$\gamma$	ho	η
(°C)	$(kN/m^3)$	$(kg/m^3)$	$(Pa \cdot s)$
0	9.81	1000	$1.75\times10^{-3}$
5	9.81	1000	$1.52\times10^{-3}$
10	9.81	1000	$1.30\times10^{-3}$
15	9.81	1000	$1.15\times10^{-3}$
20	9.79	998	$1.02\times10^{-3}$
25	9.78	997	$8.91\times10^{-4}$
30	9.77	996	$9.00\times10^{-4}$
35	9.75	994	$7.18\times10^{-4}$
40	9.73	992	$6.51\times10^{-4}$
45	9.71	990	$5.94\times10^{-4}$
50	9.69	988	$5.41\times10^{-4}$
55	9.67	986	$4.98\times10^{-4}$
60	9.65	984	$4.60\times10^{-4}$
65	9.62	981	$4.31\times10^{-4}$
70	9.59	978	$4.02\times10^{-4}$
75	9.56	975	$3.73\times10^{-4}$
80	9.53	971	$3.50\times10^{-4}$
85	9.50	968	$3.30\times10^{-4}$
90	9.47	965	$3.11\times10^{-4}$
95	9.44	962	$2.92\times10^{-4}$
100	9.40	958	$2.82 \times 10^{-4}$

	Specific	Specific		Dynamic
Liquid	Gravity	Weight	Density	Viscosity
		$\gamma$	ho	η
		$(kN/m^3)$	$(kg/m^3)$	(Pa·s)
Acetone	0.787	7.72	787	$3.16\times10^{-4}$
Alcohol, Ethyl	0.787	7.72	787	$1.00\times10^{-3}$
Alcohol, Methyl	0.789	7.74	789	$5.60\times10^{-4}$
Alcohol, Propyl	0.802	7.87	802	$1.92\times10^{-3}$
Benzene	0.876	8.59	876	$6.03\times10^{-4}$
Carbon Tetrachloride	1.590	15.60	1590	$9.10\times10^{-4}$
Castor Oil	0.960	9.42	960	$6.51\times10^{-1}$
Ethylene Glycol	1.100	10.79	1100	$1.62\times10^{-2}$
Gasoline	0.68	6.67	680	$2.87\times10^{-4}$
Glycerine	1.258	12.34	1258	$9.60 \times 10^{-1}$
Kerosene	0.823	8.07	823	$1.64\times10^{-3}$
Linseed Oil	0.930	9.12	930	$3.31\times10^{-2}$
Mercury	13.54	132.8	13540	$1.53\times10^{-3}$
Propane	0.495	4.86	495	$1.10\times10^{-4}$
Seawater	1.030	10.10	1030	$1.03\times10^{-3}$
Turpentine	0.870	8.53	870	$1.37\times10^{-3}$
Fuel Oil, medium	0.852	8.36	852	$2.99\times10^{-3}$
Fuel Oil, heavy	0.906	8.89	906	$1.07\times10^{-1}$

# Example 1:



A piston confines oil in a closed circular cylinder. The maximum operating pressure for the piston is 17.8 MPa. The piston has a diameter of 62.5 mm. What is the maximum load that the piston can support?

#### Solution:

$$\begin{split} F &= P \times A \\ &= 17.8 \times 10^6 \text{ N/m}^2 \times \frac{\pi (0.0625 \text{ m})^2}{4} \\ &= 54610 \text{ N} \\ &\approx 54.6 \text{ kN} \qquad \text{(3 sig digs)} \end{split}$$

#### Alternative units:

$$\begin{split} F &= P \times A \\ &= 17.8 \text{ N/mm}^2 \times \frac{\pi (6.25 \text{ mm})^2}{4} \\ &= 54610 \text{ N} \\ &\approx 54.6 \text{ kN} \end{split}$$

#### Exercise 1:

A press used to produce coins requires a force of  $8.20\ kN$ .

The hydraulic cylinder has a diameter of 63.5 mm.

What is the oil pressure needed to generate this force?

# Solution:

$$P = \frac{F}{A}$$
=  $\frac{8.20 \text{ kN}}{\pi (0.0635 \text{ m})^2/4}$ 
= 2589.3 kN/m<sup>2</sup>
 $\approx 2.59 \text{ MPa}$ 

# Alternative units:

$$P = \frac{F}{A}$$
=  $\frac{8200 \text{ N}}{\pi (6.35 \text{ mm})^2/4}$ 
= 2.5893 N/mm<sup>2</sup>
 $\approx 2.59 \text{ MPa}$ 

#### Example 2:

An empty barrel with an inside diameter of 900 mm weighs 205 N.

What does the barrel weigh when it is filled to a depth of 750 mm with water at  $25^{\circ}$ C?

#### Solution:

The volume of water is the volume of a cylinder with diameter 900 mm and height 750 mm:

$$v = \frac{\pi d^2}{4} \cdot h$$

$$= \frac{\pi (0.900 \text{ m})^2}{4} \cdot (0.75 \text{ m})$$

$$= 0.47713 \text{ m}^3$$

(Use 5 significant digits for interim calculations and 3 significant digits for solutions.)

The specific weight of water at  $25^{\circ}$ C is  $9.78 \text{ kN/m}^3$  (Table A.1) so

$$w = \gamma V$$
  
= 9.78 kN/m<sup>3</sup> × 0.47713 m<sup>3</sup>  
= 4.6663 kN

The combined weight of the barrel and the water is given by:

$$0.205 \text{ kN} + 4.6663 \text{ kN} \approx 4.87 \text{ kN}$$

## Example 3:

Calculate the density and the specific weight of benzene if it has a specific gravity of 0.876.

#### Solution:

$$0.876 = \frac{
ho_b}{
ho_{water@4^{\circ}C}}$$
 $ho_b = 0.876 \times 1000 \text{ kg/m}^3$ 
 $= 876 \text{ kg/m}^3$ 
 $0.876 = \frac{\gamma_b}{\gamma_{water@4^{\circ}C}}$ 
 $\gamma_b = 0.876 \times 9.81 \text{ kN/m}^3$ 
 $= 8.59 \text{ kN/m}^3$ 

#### Example 5:

An open cylindrical tank with diameter  $5.75~\mathrm{m}$  and depth  $3.30~\mathrm{m}$  is filled to the top with water at  $10^{\circ}\mathrm{C}$ . The water is heated to  $55^{\circ}\mathrm{C}$ . Assuming that the tank dimensions remain constant and there are no losses due to evaporation, calculate the mass of water that overflows.

#### Solution:

Volume of tank:

$$\begin{split} v_{tank} &= \frac{\pi (5.75 \text{ m})^2}{4} \times 3.30 \text{ m} \\ &= 85.692 \text{ m}^3 \end{split}$$

Mass of the water in the tank at  $10^{\circ}\text{C}$ :

$$\begin{split} m &= \rho_{10^{\circ}\text{C}} \times v_{10^{\circ}\text{C}} \\ &= 1000 \text{ kg/m}^3 \times 85.692 \text{ m}^3 \\ &= 85\,692 \text{ kg} \end{split}$$

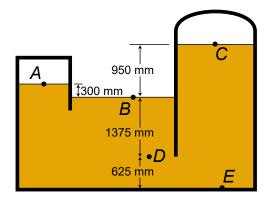
Mass of the water in the tank at  $70^{\circ}$ C:

$$\begin{split} m &= \rho_{55^{\circ}\text{C}} \times v_{55^{\circ}\text{C}} \\ &= 986 \text{ kg/m}^3 \times 85.692 \text{ m}^3 \\ &= 84\,492 \text{ kg} \end{split}$$

Mass of water that overflows:

$$\begin{split} m_{overflow} &= 85\,692~\mathrm{kg} - 84\,492~\mathrm{kg} \\ &= 1\,200~\mathrm{kg} \end{split}$$

#### Example 6:



A tank, open to the atmosphere in the centre, contains medium fuel oil. Atmospheric pressure is 102.1 kPa. Calculate the gauge pressure and the absolute pressure for locations *A*, *B*, *C*, *D* and *E*.

#### Solution:

**Pressure at B**: B is open to the atmosphere so

$$P_B=0$$
 and  $P_{B(abs)}=P_{(atm)}=102.1$  kPa

Note that pressure is assumed to be gauge pressure unless otherwise specified.

Also, atmospheric pressure is generally specified to four significant digits; there is a distinct difference in pressure between 100.5 kPa and 101.4 kPa.

#### Pressure at A:

$$P_A = P_B - \Delta p$$
  
=  $0 - \gamma h$   
=  $-(8.36 \text{ kN/m}^3)(0.30 \text{ m})$   
=  $-2.5080 \text{ kPa}$   
 $\approx -2.51 \text{ kPa}$ 

$$P_{A(abs)} = P_{atm} + P_{A(gauge)}$$
  
= 102.1 kPa - 2.5080 kPa  
= 99.592 kPa  
 $\approx$  99.6 kPa

## Pressure at *C*:

$$P_C = P_C - \Delta p$$
  
=  $0 - \gamma h$   
=  $-(8.36 \text{ kN/m}^3)(0.950 \text{ m})$   
=  $-7.9420 \text{ kN/m}^2$   
 $\approx -7.94 \text{ kPa}$ 

$$P_{C(abs)} = P_{atm} + P_{C(gauge)}$$
  
= 102.1 kPa - 7.9420 kPa  
= 94.158 kPa  
 $\approx$  94.2 kPa

# Pressure at D:

$$P_D = P_B + \Delta p$$
  
 $= 0 + \gamma h$   
 $= (8.36 \text{ kN/m}^3)(1.375 \text{ m})$   
 $= 11.495 \text{ kPa}$   
 $\approx 11.50 \text{ kPa}$   
 $P_{D(abs)} = P_{atm} + P_{D(gauge)}$   
 $= 102.1 \text{ kPa} + 11.495 \text{ kPa}$   
 $= 113.60 \text{ kPa}$   
 $= 113.6 \text{ kPa}$ 

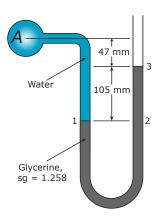
# Pressure at *E*:

$$P_E = P_B + \Delta p$$
  
=  $0 + \gamma h$   
=  $(8.36 \text{ kN/m}^3)(2.0 \text{ m})$   
=  $16.720 \text{ kPa}$ 

$$P_{E(abs)} = P_{atm} + P_{D(gauge)}$$
  
= 102.1 kPa + 16.72 kPa  
= 118.82 kPa  
 $\approx$  118.8 kPa

# Example 7:

Determine the pressure at A given that the temperature of the water is  $25^{\circ}\text{C}$ .

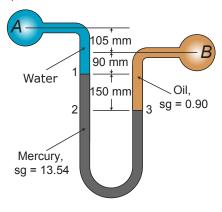


#### Solution:

$$P_3 = 0$$
  
 $P_2 = P_3 + \gamma h$   
 $= 0 + (1.258)(9.81 \text{ kN/m}^3)(0.105 \text{ m})$   
 $= 1.2958 \text{ kPa}$   
 $P_1 = 1.2958 \text{ kPa}$   
 $P_A = P_1 - \gamma h$   
 $= 1.2958 \text{ kPa} - (9.78)(0.152) \text{ kPa}$   
 $= -0.1907 \text{ kPa}$ 

**Note**: There is not much difference in pressure for a difference in levels of 0.105 m. For this reason, a gauge fluid with a higher specific gravity, such as mercury, is usually used to measure larger pressure differences.

# **Example 8**: Find the pressure difference between A and B



#### Solution:

$$\begin{array}{lll} P_1 &=& P_A + \gamma h \\ &=& P_A + (9.81 \; \mathrm{kN/m^3})(0.195 \; \mathrm{m}) \\ &=& P_A + 1.913 \; \mathrm{kPa} \\ P_2 &=& P_1 + (13.54)(9.81 \; \mathrm{kN/m^3})(0.15 \; \mathrm{m}) \\ &=& P_A + (1.913 + 19.924) \; \mathrm{kPa} \\ &=& P_A + 21.837 \; \mathrm{kPa} \\ P_3 &=& P_A + 21.837 \; \mathrm{kPa} \\ P_B &=& P_3 - (0.90)(9.81 \; \mathrm{kN/m^3})(0.240 \; \mathrm{m}) \\ &=& P_A + 21.837 \; \mathrm{kPa} - 2.119 \; \mathrm{kPa} \\ \Delta p &=& 19.72 \; \mathrm{kPa} \end{array}$$