# 04 — The General Energy Equation

Water Resources, CIVL318

Last revision on September 23, 2018

#### Introduction

In the module on Bernoulli's Equation, we assumed that energy remained constant throughout the system: no energy was added to or removed from the system, and any losses due to friction were insignificant and could be ignored.



#### Introduction

- In the module on Bernoulli's Equation, we assumed that energy remained constant throughout the system: no energy was added to or removed from the system, and any losses due to friction were insignificant and could be ignored.
- ▶ In this section, Bernoulli's Equation is modified to include terms for:
  - lacktriangle Head added,  $h_A$ , the energy added to a system by a device such as a pump
  - Head removed, h<sub>R</sub>, the energy removed from a system by a turbine or fluid motor
  - lacktriangle Head lost,  $h_L$ , due to friction in pipes and flow through valves and fittings



#### Introduction

- In the module on Bernoulli's Equation, we assumed that energy remained constant throughout the system: no energy was added to or removed from the system, and any losses due to friction were insignificant and could be ignored.
- ▶ In this section, Bernoulli's Equation is modified to include terms for:
  - ightharpoonup Head added,  $h_A$ , the energy added to a system by a device such as a pump
  - Head removed, h<sub>R</sub>, the energy removed from a system by a turbine or fluid motor
  - lacktriangle Head lost,  $h_L$ , due to friction in pipes and flow through valves and fittings
- ▶ The modified Bernoulli's Equation is called the General Energy Equation



# General Energy Equation

#### **General Energy Equation (GEE)**

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} + h_A - h_R - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$$



# General Energy Equation

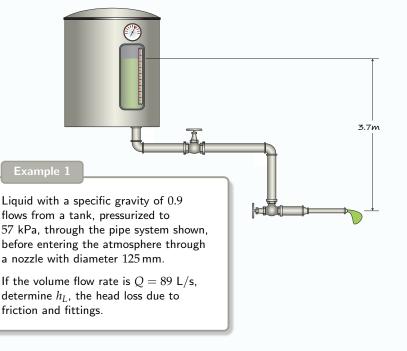
#### **General Energy Equation (GEE)**

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} + h_A - h_R - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$$

**Note**: It is now **critically** important that the equation be applied in the direction of the flow: section 1 must be "upstream" of section 2.

"Upstream" means earlier in the flow, not necessarily at a higher elevation!







# **Pumps**

- A pump is a mechanical device, normally powered by electricity, that drives a rotating shaft in the pump.
- A pump adds energy to a flowing liquid.
- Note that a pump increases flow through the whole system: the volume flow rate at the pump outlet is the same as at the pump inlet.
- This is a centrifugal pump.



Water distribution, Banff



# Centrifugal Pumps

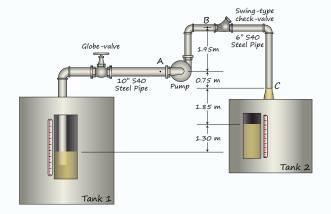
The centrifugal pump is the most common type of dynamic pump used in industry; a centrifugal pump contains a rotating part (axle and impeller) and a stationary part (casing, bearings, etc.).

We shall look at centrifugal pumps in more detail later in this course.



http://commons.wikimedia.org/wiki/File: Warman\_centrifugal\_pump.jpg

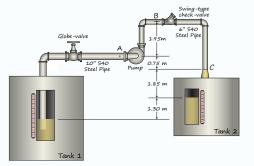




Liquid with a specific gravity of 0.87 is pumped from Tank 1; the liquid exits the pipe into the atmosphere, at C, before dropping into Tank 2 at 180 L/s.

Determine the head added by the pump and the pressure at A. (You may neglect any head losses due to friction and valves.)





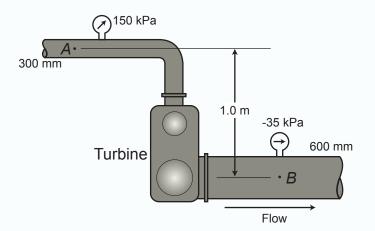
#### Exercise 1

As before, liquid with a specific gravity of 0.87 is pumped from Tank 1; the liquid exits the pipe into the atmosphere, at C, before dropping into Tank 2 at  $180\,L/s$ . (Neglect any head losses due to friction and valves.)

Determine the pressure at *B*:

- $\blacksquare$  First, by applying the GEE between the surface of Tank 1 and B;
- $\blacksquare$  Second, by applying the GEE between A and B;
- $\blacksquare$  Finally, by applying the GEE between B and C.





Water flows from A to B at the rate of 120 L/s. Determine the head removed by the turbine.



# Power Added by a Pump

- Power is the rate of doing work
- In fluid mechanics, power is considered the rate at which energy is transferred to the system
- The unit for power is the watt (W) which is 1.0 N·m/s or, equivalently, 1.0 joule (J)/s



# Power Added by a Pump

- Power is the rate of doing work
- In fluid mechanics, power is considered the rate at which energy is transferred to the system
- ▶ The unit for power is the watt (W) which is  $1.0 \text{ N} \cdot \text{m/s}$  or, equivalently, 1.0 joule (J)/s

$$\begin{split} P_A &= \frac{\mathbf{N} \cdot \mathbf{m}}{\mathbf{s}} \\ &= \mathbf{m} \times \frac{\mathbf{N}}{\mathbf{s}} \\ &= h_A \times W \text{(weight flow rate)} \\ &= h_A \gamma Q \end{split}$$

Note:  $h_A$  is the energy added N·m per N of fluid flowing through the pump and W, the weight flow rate, is N/s.



# Mechanical Efficiency of a Pump

Efficiency is the ratio of power added by the pump to the power supplied to the pump:

$$e_M = \frac{\text{Power added to the fluid}}{\text{Power input to the pump}} = \frac{P_A}{P_I}$$

- Efficiency is always less than 1
- Efficiency is expressed as a number or as a percentage



#### **Turbines**

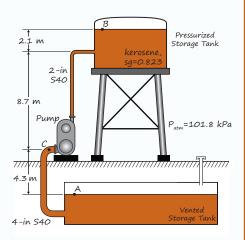
Similarly, the power removed by a turbine/fluid motor is given by:

$$P_R = h_R \gamma Q$$

and the efficiency of a turbine/fluid motor is given by:

$$e_M = \frac{\text{Power output from turbine}}{\text{Power removed from the fluid}} = \frac{P_O}{P_R}$$

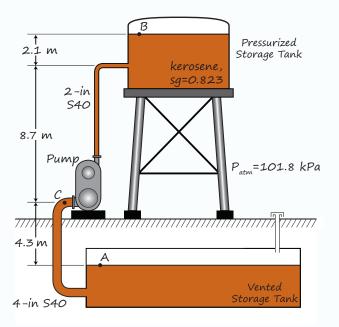




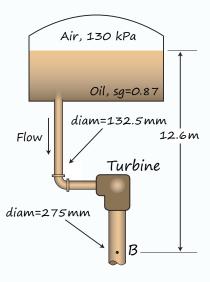
A pump produces a flow of  $1024\,\mathrm{L/min}$  of kerosene with a specific gravity of 0.823 from vented underground storage to an elevated tank pressurized to  $512\,\mathrm{kPa}$ . Energy loss between the underground storage and the pump is  $0.95\,\mathrm{m}$  and energy loss between the pump and the elevated tank is  $4.9\,\mathrm{m}$ .

- Determine the power added to the fluid by the pump.
- If the pump has an efficiency of 73%, determine the (electrical) power drawn by the pump.
- Determine the gauge and the absolute pressure at the pump inlet.









#### Exercise 2

Oil, with sg=0.87, flows from a tank pressurized at 130 kPa at a rate of 72 L/s and powers a fluid motor as shown. Energy losses due to friction and fittings between the tank and B are estimated to be 1.81 m.

If the pressure at B is found to be  $-56~\mathrm{kPa}$  and the motor has an efficiency of 78%, determine the power output from the motor.



# fuel pump to engine

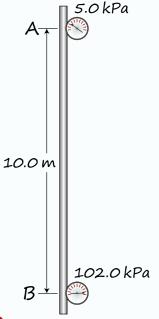
#### Example 5

A car fuel pump pumps  $1\,\mathrm{L}$  of gasoline every  $45\mathrm{s}$  when is has a suction pressure of  $155\,\mathrm{mm}$  of mercury vacuum and a discharge pressure of  $32\,\mathrm{kPa}$ . Both the suction and the discharge lines have the same diameter.

If the pump efficiency is 68%, determine the power drawn from the engine.



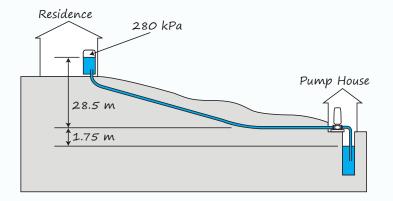




There are no pumps or turbines and the pipe is of constant diameter. Determine which of the following is true:

- flow is upward
- there is no flow
- III flow is downward





#### Exercise 3

A rural house relies upon a shallow well for its water supply. The pump at the well is required to supply 210~L/min of water. The water tank at the house maintains a pressure of 280~kPa. Friction losses in the pipe amount to 4.35~m.

If the pump is 72% efficient, determine the power delivered to the pump by the electrical supply and the power added to the water by the pump.

