Module 1: The Nature of Fluids/Pressure Measurement (CIVL 318)

Some useful results:

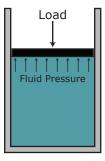
Table A: Properties of Water

Table B: Properties of Common Liquids (at 101 kPa and 25°C)

Temperature	Specific Weight	Density	Dynamic Viscosity
	γ	ho	η
(°C)	(kN/m^3)	(kg/m^3)	$(Pa \cdot s)$
0	9.81	1000	1.75×10^{-3}
5	9.81	1000	1.52×10^{-3}
10	9.81	1000	1.30×10^{-3}
15	9.81	1000	1.15×10^{-3}
20	9.79	998	1.02×10^{-3}
25	9.78	997	8.91×10^{-4}
30	9.77	996	9.00×10^{-4}
35	9.75	994	7.18×10^{-4}
40	9.73	992	6.51×10^{-4}
45	9.71	990	5.94×10^{-4}
50	9.69	988	5.41×10^{-4}
55	9.67	986	4.98×10^{-4}
60	9.65	984	4.60×10^{-4}
65	9.62	981	4.31×10^{-4}
70	9.59	978	4.02×10^{-4}
75	9.56	975	3.73×10^{-4}
80	9.53	971	3.50×10^{-4}
85	9.50	968	3.30×10^{-4}
90	9.47	965	3.11×10^{-4}
95	9.44	962	2.92×10^{-4}
100	9.40	958	2.82×10^{-4}

	Specific	Specific		Dynamic
Liquid	Gravity	Weight	Density	Viscosity
		γ	ho	η
		(kN/m^3)	(kg/m^3)	(Pa·s)
Acetone	0.787	7.72	787	3.16×10^{-4}
Alcohol, Ethyl	0.787	7.72	787	1.00×10^{-3}
Alcohol, Methyl	0.789	7.74	789	5.60×10^{-4}
Alcohol, Propyl	0.802	7.87	802	1.92×10^{-3}
Benzene	0.876	8.59	876	6.03×10^{-4}
Carbon Tetrachloride	1.590	15.60	1590	9.10×10^{-4}
Castor Oil	0.960	9.42	960	6.51×10^{-1}
Ethylene Glycol	1.100	10.79	1100	1.62×10^{-2}
Gasoline	0.68	6.67	680	2.87×10^{-4}
Glycerine	1.258	12.34	1258	9.60×10^{-1}
Kerosene	0.823	8.07	823	1.64×10^{-3}
Linseed Oil	0.930	9.12	930	3.31×10^{-2}
Mercury	13.54	132.8	13540	1.53×10^{-3}
Propane	0.495	4.86	495	1.10×10^{-4}
Seawater	1.030	10.10	1030	1.03×10^{-3}
Turpentine	0.870	8.53	870	1.37×10^{-3}
Fuel Oil, medium	0.852	8.36	852	2.99×10^{-3}
Fuel Oil, heavy	0.906	8.89	906	1.07×10^{-1}

Example 1:



A piston confines oil in a closed circular cylinder. The maximum operating pressure for the piston is 17.8 MPa. The piston has a diameter of 62.5 mm. What is the maximum load that the piston can support?

Solution:

$$\begin{split} F &= P \times A \\ &= 17.8 \times 10^6 \text{ N/m}^2 \times \frac{\pi (0.0625 \text{ m})^2}{4} \\ &= 54610 \text{ N} \\ &\approx 54.6 \text{ kN} \end{split} \tag{3 sig digs}$$

Alternative units:

$$F = P \times A$$

$$= 17.8 \text{ N/mm}^2 \times \frac{\pi (6.25 \text{ mm})^2}{4}$$

$$= 54610 \text{ N}$$

$$\approx 54.6 \text{ kN}$$

Exercise 1:

A press used to produce coins requires a force of $8.20\ kN$.

The hydraulic cylinder has a diameter of 63.5 mm.

What is the oil pressure needed to generate this force?

Solution:

$$\begin{split} P &= \frac{F}{A} \\ &= \frac{8.20 \text{ kN}}{\pi (0.0635 \text{ m})^2 / 4} \\ &= 2589.3 \text{ kN/m}^2 \\ &\approx 2.59 \text{ MPa} \end{split}$$

Alternative units:

$$P = \frac{F}{A}$$
= $\frac{8200 \text{ N}}{\pi (6.35 \text{ mm})^2 / 4}$
= 2.5893 N/mm²
 $\approx 2.59 \text{ MPa}$

Example 2:

An empty barrel with an inside diameter of 900 mm weighs 205 N.

What does the barrel weigh when it is filled to a depth of 750 mm with water at 25° C?

Solution:

The volume of water is the volume of a cylinder with diameter 900 mm and height 750 mm:

$$v = \frac{\pi d^2}{4} \cdot h$$

$$= \frac{\pi (0.900 \text{ m})^2}{4} \cdot (0.75 \text{ m})$$

$$= 0.47713 \text{ m}^3$$

(Use 5 significant digits for interim calculations and 3 significant digits for solutions.)

The specific weight of water at 25° C is 9.78 kN/m^3 (Table A.1) so

$$w = \gamma V$$

= 9.78 kN/m³ × 0.47713 m³
= 4.6663 kN

The combined weight of the barrel and the water is given by:

$$0.205 \text{ kN} + 4.6663 \text{ kN} \approx 4.87 \text{ kN}$$

Example 3:

Calculate the density and the specific weight of benzene if it has a specific gravity of 0.876.

Solution:

$$0.876 = \frac{
ho_b}{
ho_{water@4^{\circ}C}}$$
 $ho_b = 0.876 \times 1000 \text{ kg/m}^3$
 $= 876 \text{ kg/m}^3$
 $0.876 = \frac{\gamma_b}{\gamma_{water@4^{\circ}C}}$
 $\gamma_b = 0.876 \times 9.81 \text{ kN/m}^3$
 $= 8.59 \text{ kN/m}^3$

Example 4:

An open cylindrical tank with diameter $5.75~\mathrm{m}$ and depth $3.30~\mathrm{m}$ is filled to the top with water at $10^{\circ}\mathrm{C}$. The water is heated to $55^{\circ}\mathrm{C}$. Assuming that the tank dimensions remain constant and there are no losses due to evaporation, calculate the mass of water that overflows.

Solution:

Volume of tank:

$$V_{tank} = \frac{\pi (5.75 \text{ m})^2}{4} \times 3.30 \text{ m}$$

= 85.692 m³

Mass of the water in the tank at 10° C:

$$m =
ho_{10^{\circ}\text{C}} imes V_{10^{\circ}\text{C}}$$

= 1000 kg/m³ × 85.692 m³
= 85 692 kg

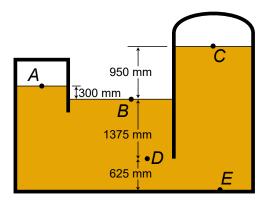
Mass of the water in the tank at 70°C :

$$m =
ho_{55^{\circ}\text{C}} imes V_{55^{\circ}\text{C}} = 986 \text{ kg/m}^3 imes 85.692 \text{ m}^3 = 84492 \text{ kg}$$

Mass of water that overflows:

$$\begin{split} m_{overflow} &= 85\,692~\mathrm{kg} - 84\,492~\mathrm{kg} \\ &= 1\,200~\mathrm{kg} \end{split}$$

Example 5:



A tank, open to the atmosphere in the centre, contains medium fuel oil. Atmospheric pressure is 102.1 kPa. Calculate the gauge pressure and the absolute pressure for locations *A*, *B*, and *D*.

Solution:

Pressure at *B*: *B* is open to the atmosphere so

$$P_B=0$$
 and $P_{B(abs)}=P_{(atm)}=102.1\,\mathrm{kPa}$

Note that pressure is assumed to be gauge pressure unless otherwise specified.

Also, atmospheric pressure is generally specified to four significant digits if over 100; there is a distinct difference in pressure between $100.5\,\mathrm{kPa}$ and $101.4\,\mathrm{kPa}$ (which are the same to 3 sig digs).

Pressure at A:

$$P_{A} = P_{B} - \Delta p$$
 $= 0 - \gamma h$
 $= -(8.36 \,\mathrm{kN/m^{3}})(0.30 \,\mathrm{m})$
 $= -2.5080 \,\mathrm{kPa}$
 $\approx -2.51 \,\mathrm{kPa}$
 $P_{A(abs)} = P_{atm} + P_{A(gauge)}$
 $= 102.1 \,\mathrm{kPa} - 2.5080 \,\mathrm{kPa}$
 $= 99.592 \,\mathrm{kPa}$
 $\approx 99.6 \,\mathrm{kPa}$

Pressure at D:

$$P_D = P_B + \Delta p$$

 $= 0 + \gamma h$
 $= (8.36 \text{ kN/m}^3)(1.375 \text{ m})$
 $= 11.495 \text{ kPa}$
 $\approx 11.50 \text{ kPa}$
 $P_{D(abs)} = P_{atm} + P_{D(gauge)}$
 $= 102.1 \text{ kPa} + 11.495 \text{ kPa}$
 $= 113.60 \text{ kPa}$
 $= 113.6 \text{ kPa}$

Exercise 2:

Calculate the gauge pressure and the absolute pressure for locations C and E for the previous example.

Pressure at *C*:

$$P_{C} = P_{C} - \Delta p$$

 $= 0 - \gamma h$
 $= -(8.36 \,\mathrm{kN/m^3})(0.950 \,\mathrm{m})$
 $= -7.9420 \,\mathrm{kN/m^2}$
 $\approx -7.94 \,\mathrm{kPa}$
 $P_{C(abs)} = P_{atm} + P_{C(gauge)}$
 $= 102.1 \,\mathrm{kPa} - 7.9420 \,\mathrm{kPa}$
 $= 94.158 \,\mathrm{kPa}$
 $\approx 94.2 \,\mathrm{kPa}$

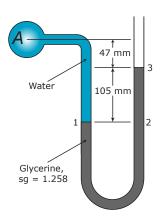
Pressure at *E*:

$$P_{E} = P_{B} + \Delta p$$

 $= 0 + \gamma h$
 $= (8.36 \,\mathrm{kN/m^{3}})(2.0 \,\mathrm{m})$
 $= 16.720 \,\mathrm{kPa}$
 $P_{E(abs)} = P_{atm} + P_{D(gauge)}$
 $= 102.1 \,\mathrm{kPa} + 16.72 \,\mathrm{kPa}$
 $= 118.82 \,\mathrm{kPa}$
 $\approx 118.8 \,\mathrm{kPa}$

Example 6:

Determine the pressure at A given that the temperature of the water is 25° C.



Solution:

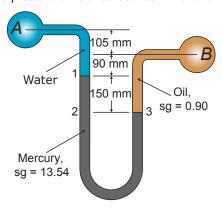
$$P_3 = 0$$

 $P_2 = P_3 + \gamma h$
 $= 0 + (1.258)(9.81 \text{ kN/m}^3)(0.105 \text{ m})$
 $= 1.2958 \text{ kPa}$
 $P_1 = 1.2958 \text{ kPa}$
 $P_A = P_1 - \gamma h$
 $= 1.2958 \text{ kPa} - (9.78)(0.152) \text{ kPa}$
 $= -0.1907 \text{ kPa}$

Note: There is not much difference in pressure for a difference in levels of 0.105 m. For this reason, a gauge fluid with a higher specific gravity, such as mercury, is usually used to measure larger pressure differences.

Example 7:

Find the pressure difference between A and B



Solution:

$$\begin{array}{rcl} P_1 &=& P_A + \gamma h \\ &=& P_A + (9.81 \text{ kN/m}^3)(0.195 \text{ m}) \\ &=& P_A + 1.913 \text{ kPa} \\ P_2 &=& P_1 + (13.54)(9.81 \text{ kN/m}^3)(0.15 \text{ m}) \\ &=& P_A + (1.913 + 19.924) \text{ kPa} \\ &=& P_A + 21.837 \text{ kPa} \\ P_3 &=& P_A + 21.837 \text{ kPa} \\ P_B &=& P_3 - (0.90)(9.81 \text{ kN/m}^3)(0.240 \text{ m}) \\ &=& P_A + 21.837 \text{ kPa} - 2.119 \text{ kPa} \\ \Delta p &=& 19.72 \text{ kPa} \end{array}$$