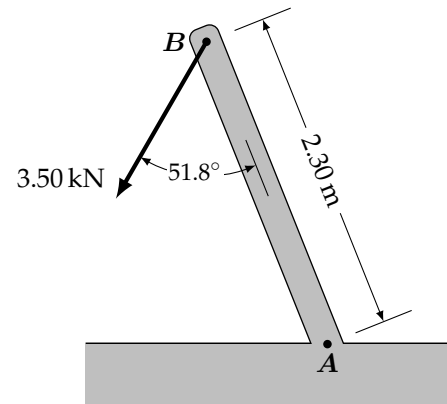
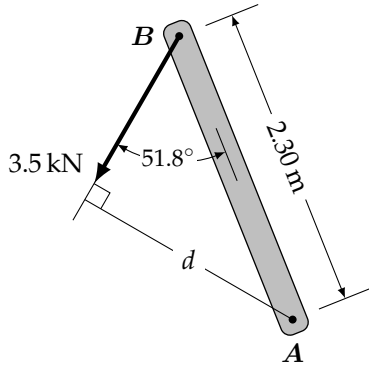


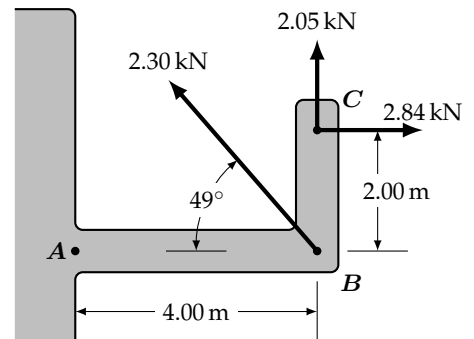
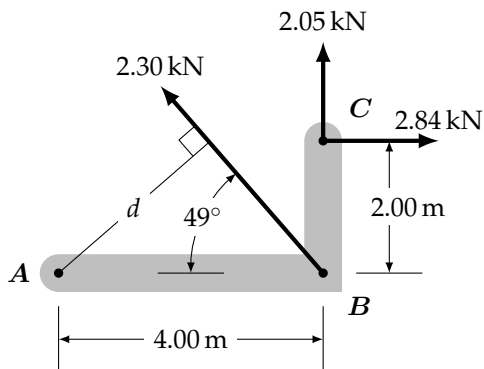
Engineering Statics - 05 Moments - Instructor Copy

Example 1: Determine the moment, M_A , of the 3.5 kN force applied at B , about the point A .



$$\begin{aligned}
 M_A &= F \cdot d \\
 &= (3.5 \text{ kN}) \cdot (2.30 \text{ m}) (\sin 51.8^\circ) \\
 &= 6.3261 \text{ kN} \cdot \text{m} \\
 &\approx 6.33 \text{ kN} \cdot \text{m}
 \end{aligned}$$

Example 2: Determine the sum of the moments of the forces, acting at B and C , about the point A .
Also, sum the moments of the forces about the point B .

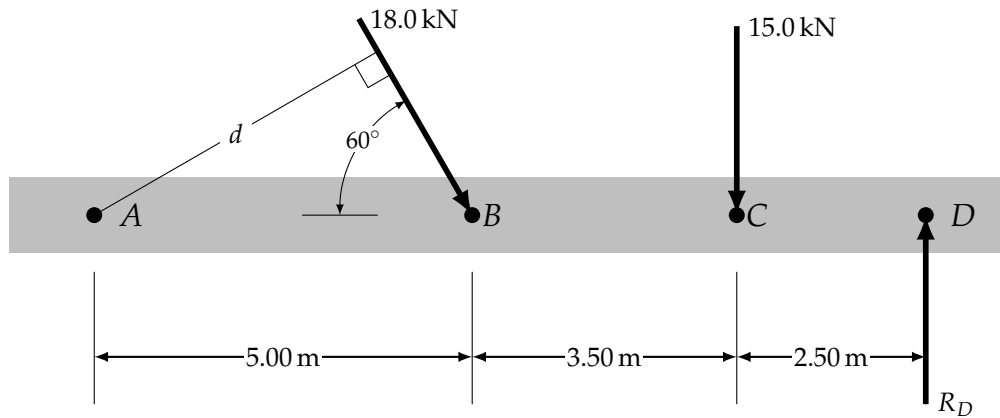
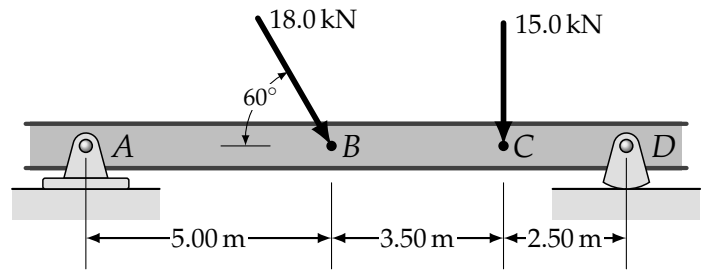


$$\begin{aligned}
 \Sigma M_A &= \Sigma F \cdot d \\
 &= (2.30 \text{ kN}) \cdot (4.00 \text{ m}) (\sin 49^\circ) \\
 &\quad + (2.05 \text{ kN}) \cdot (4.00 \text{ m}) - (2.84 \text{ kN}) \cdot (2.00 \text{ m}) \\
 &= 9.4633 \text{ kN} \cdot \text{m} \approx 9.46 \text{ kN} \cdot \text{m}
 \end{aligned}$$

$$\Sigma M_B = 0 + 0 - (2.84 \text{ kN}) \cdot (2.00 \text{ m}) = -5.6800 \text{ kN} \cdot \text{m} = -5.68 \text{ kN} \cdot \text{m}$$

Exercise 1: Rigid beam $ABCD$ is supported at A and at D , and is subjected to the two forces shown at B and C .

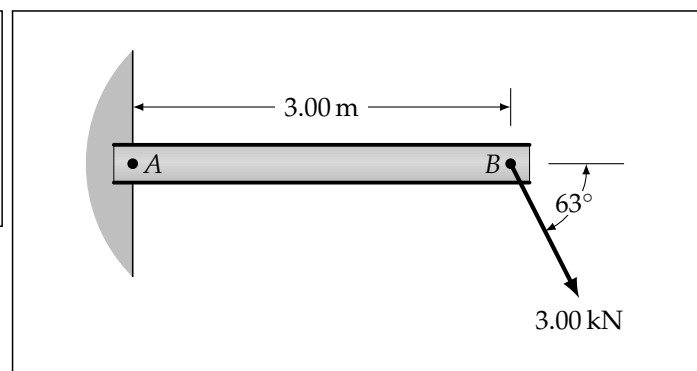
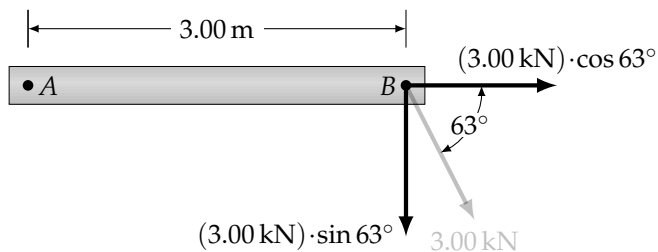
Determine the value of the reaction at D , R_D , if the sum of the moments about A , ΣM_A , is zero and the reaction at D is vertically upwards.



$$\begin{aligned}\Sigma M_A &= -(18.0 \text{ kN})(5.00 \text{ m})(\sin 60^\circ) - (15.0 \text{ kN})(8.50 \text{ m}) + R_D(11.00 \text{ m}) = 0 \\ \Rightarrow R_D &= \frac{(18.0 \text{ kN})(5.00 \text{ m})(\sin 60^\circ) + (15.0 \text{ kN})(8.50 \text{ m})}{11.00 \text{ m}} \\ &= 18.677 \text{ kN} \approx 18.7 \text{ kN}\end{aligned}$$

Example 3:

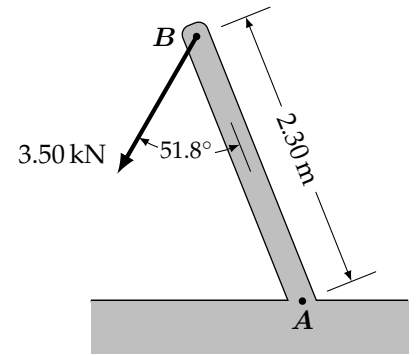
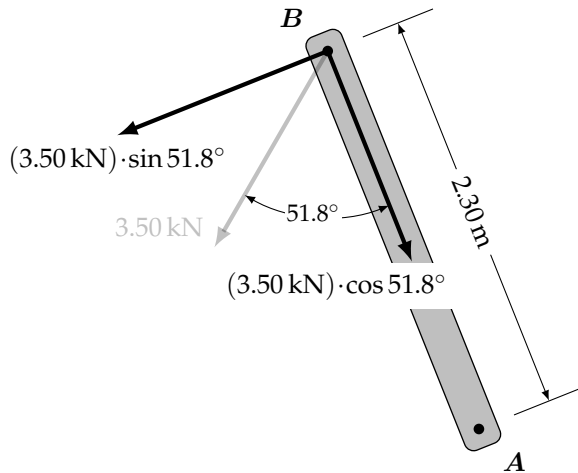
Determine the moment about A of the force applied to B by resolving the force at B into horizontal and vertical components.



$$\Sigma M_A = (3.00 \text{ kN}) \cdot \cos 63^\circ \cdot 0 + (3.00 \text{ kN}) \cdot \sin 63^\circ \cdot 3.00 \text{ m} = 8.0191 \text{ kN} \cdot \text{m} \approx 8.02 \text{ kN} \cdot \text{m}$$

Example 4:

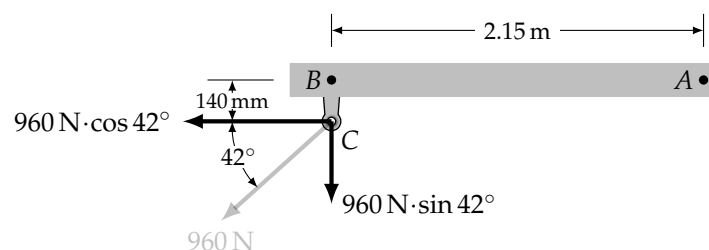
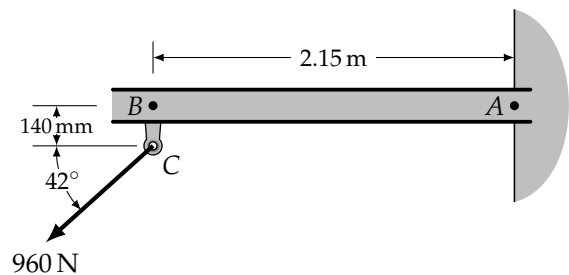
Determine the moment about A of the force at B by resolving the force into components parallel to and perpendicular to AB .



$$\begin{aligned}\Sigma M_A &= (3.50 \text{ kN}) \cdot \cos 51.8^\circ \cdot 0 \\ &\quad + (3.50 \text{ kN}) \cdot \sin 51.8^\circ \cdot 2.30 \text{ m} \\ &= 6.3261 \text{ kN} \approx 6.33 \text{ kN}\end{aligned}$$

Exercise 2:

Determine the moment about A of the force acting on D . Then determine the moment about B for the same force.

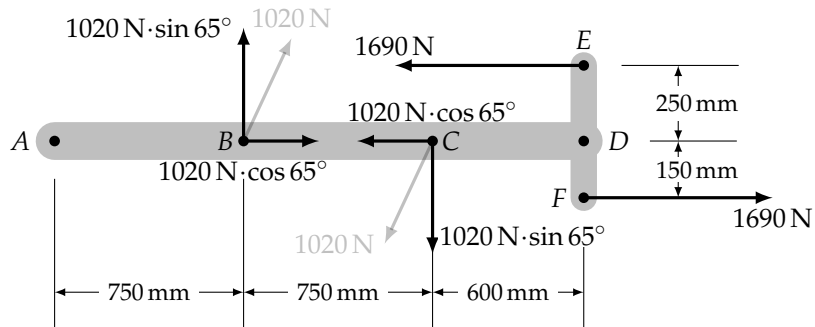
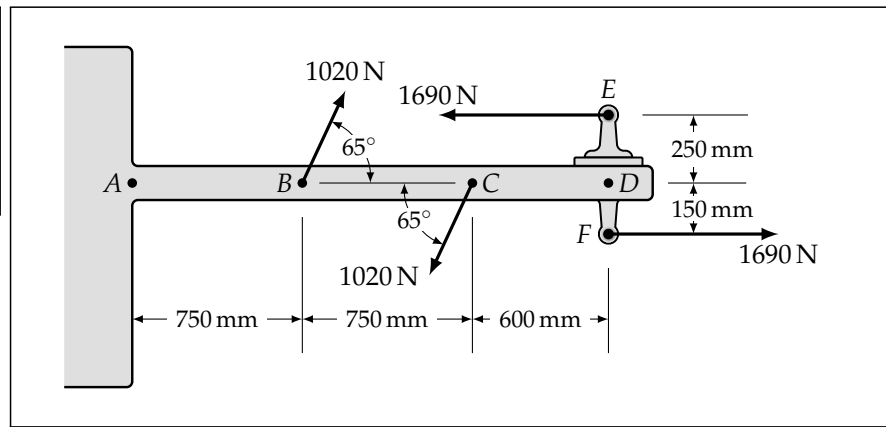


$$\Sigma M_A = 960 \text{ N} \cdot \sin 42^\circ \cdot (2.15 \text{ m}) - 960 \text{ N} \cdot \cos 42^\circ \cdot (0.14 \text{ m}) = 1281.2 \text{ N} \cdot \text{m} \approx 1280 \text{ N} \cdot \text{m}$$

$$\Sigma M_B = -960 \text{ N} \cdot \cos 42^\circ \cdot (0.14 \text{ m}) = 99.879 \text{ N} \cdot \text{m} \approx 99.9 \text{ N} \cdot \text{m}$$

Exercise 3:

Determine the sum of the moments about A , about C and about F of the forces shown.



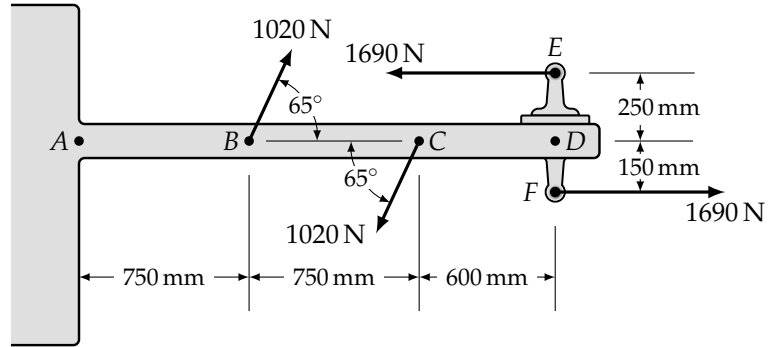
$$\begin{aligned}\Sigma M_A &= (1020 \text{ N} \cdot \sin 65^\circ)(750 \text{ mm}) - (1020 \text{ N} \cdot \sin 65^\circ)(1500 \text{ mm}) \\ &\quad + (1690 \text{ N})(250 \text{ mm}) + (1690 \text{ N})(150 \text{ mm}) \\ &= -(1020 \text{ N} \cdot \sin 65^\circ)(750 \text{ mm}) + (1690 \text{ N})(400 \text{ mm}) \\ &= -17325 \text{ N} \cdot \text{mm} \approx -17.3 \text{ N} \cdot \text{m}\end{aligned}$$

$$\begin{aligned}\Sigma M_C &= -(1020 \text{ N} \cdot \sin 65^\circ)(750 \text{ mm}) + (1690 \text{ N})(250 \text{ mm}) + (1690 \text{ N})(150 \text{ mm}) \\ &= -17325 \text{ N} \cdot \text{mm} \approx -17.3 \text{ N} \cdot \text{m}\end{aligned}$$

$$\begin{aligned}\Sigma M_F &= (1020 \text{ N} \cdot \sin 65^\circ)(600 \text{ mm}) - (1020 \text{ N} \cdot \sin 65^\circ)(1350 \text{ mm}) + (1690 \text{ N})(400 \text{ mm}) \\ &= -17325 \text{ N} \cdot \text{mm} \approx -17.3 \text{ N} \cdot \text{m}\end{aligned}$$

Example 5:

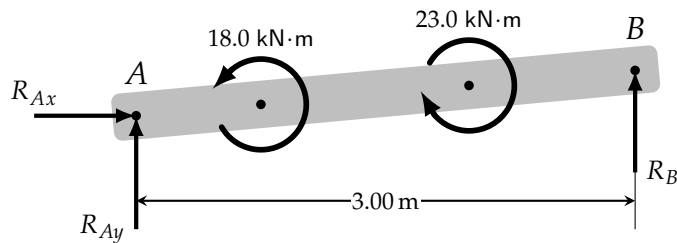
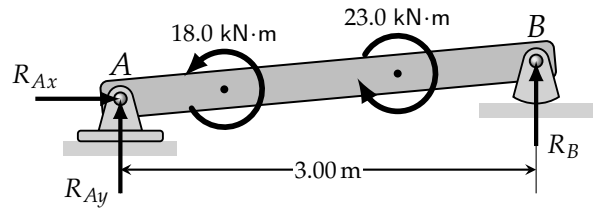
Determine ΣM , the sum of the moments, of the couples shown.



$$\Sigma M = (-1020 \text{ N})(750 \text{ mm}) + (1690 \text{ N})(400 \text{ mm}) = -17325 \text{ N}\cdot\text{mm} \approx -17.3 \text{ N}\cdot\text{m}$$

Example 6: Considering beam AB:

1. Determine the magnitude of R_D if $\Sigma M_A = 0$.
2. Determine the magnitude of R_{Ay} if $\Sigma F_y = 0$.
3. Determine the magnitude of R_{Ax} if $\Sigma F_x = 0$.



1.

$$\Sigma M_A = 18.0 \text{ kN}\cdot\text{m} - 23.0 \text{ kN}\cdot\text{m} + R_B(3.00 \text{ m}) = 0 \Rightarrow R_B = 1.6667 \text{ kN} \Rightarrow R_B \approx 1.67 \text{ kN}$$

2.

$$\Sigma F_y = R_{Ay} + R_B = 0 \Rightarrow R_{Ay} = -1.6667 \text{ kN} \Rightarrow R_{Ay} \approx -1.67 \text{ kN}$$

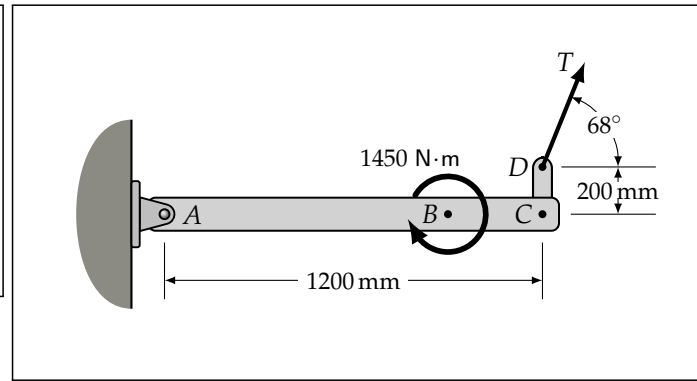
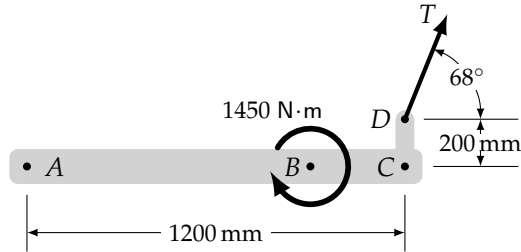
3.

$$\Sigma F_x = R_{Ax} = 0$$

Exercise 4:

$ABCD$ has a negative couple applied at B and is supported by a cable at D .

1. Determine the magnitude of T if $\Sigma M_A = 0$.
2. Determine the reaction at A if $\Sigma F_x = \Sigma F_y = 0$.



1.

$$\begin{aligned}\Sigma M_A &= -1450 \text{ N}\cdot\text{m} - (T \cos 68^\circ)(200 \text{ mm}) \\ &\quad + (T \sin 68^\circ)(1200 \text{ mm}) = 0 \\ \Rightarrow T &= \frac{1450 \text{ N}\cdot\text{m}}{(1.200 \text{ m}) \sin 68^\circ - (0.200 \text{ m}) \cos 68^\circ} \\ &= 1397.3 \text{ N} = 1400 \text{ N}\end{aligned}$$

2. $R_A = 1400 \text{ N}$ at 248° measured ccw from the positive x -axis. Why?

Example 7:

Determine the moment of the distributed load about O .

