Lexemes, or what Dictionaries Know about Morphology

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February 10, 2025

Take a corpus of text, tokenized by punctuation and whitespace, and identify all of the word types (unique words). Then take all of the headwords in a dictionary and compare these two lists. Are all the common words on the first list in the second list? What is missing?

- (1) a. houses
 - b. drinks
 - c. passed
 - d. moving

Note that the dictionary does have entries for

- (2) a. house
 - b. drink
 - c. pass
 - d. move

Why are the examples in (1) present but those in (2) absent? Are the wordforms in (1) not covered?

The dictionary has one entry for *drink*, *drinks*, *drank*, *drunk*, and *drinking*. Together, these form what is called a LEXEME. The other words shown above are treated similarly. A lexeme is a set of wordforms that are related by inflection. One of the forms is often used to identify the whole set, like *drink*. This is called the LEMMA. The headwords in dictionaries are lemmas.

Lexemes are not simply sets, though. They have structure. The structure a lexeme has is called its paradigm. Take an English verb like *drink*. Leaving aside the past participle *drunk* and the present participle *drinking*, their are three parameters in which English verbs can vary: person, number, and tense (which we say in the lecture on inflection). We can then ask what the form of the verb *drink* is for each of the combinations of properties. We often lay this out as a table to make it easier to visualize, as in Table 1: Note that this English paradigm is rather monotonous—most of the cells are just *drink*. Consider the equally boring paradigm for *move* in Table 2: Note that everywhere where the first paradigm has *drink*, the second paradigm has *move*, wherever the first paradigm has *drinks*, the second paradigm has *moved*, and wherever the first paradigm has *drinks*, the second paradigm has *moves*. We can look at paradigms in two ways:

From the perspective of a lemma or another "base" form
 1sg is lemma and 3sg is lemma + s



Figure 1: A dictionary entry with the headword *virus*.

	PAST	PRES	FUT
1sg	drank	drink	drink
2sg	drank	drink	drink
3sg	drank	drinks	drink
1pl	drank	drink	drink
2 _{PL}	drank	drink	drink
3PL	drank	drink	drink
	PAST	PRES	FUT
1sg	moved	move	move
2sg	moved	move	move
3sg	moved	moves	move
1pl	moved	move	move
2 _{PL}	moved	move	move
3 _{PL}	moved	move	move

Table 1: A paradigm for drink (person, number, and tense)

Table 2: A paradigm for move (person, number, and tense)

• From the perspective of paradigm cells The other past cells are always the same as, e.g., the 1sg.past and 3sg.pres is always 1sg.pres + s.

The verb paradigms in Totonac are much more complicated than the English noun paradigms. A partial paradigm is shown in Table 3.

'SWIM, BATHE'	IMPERFECT	PERFECTIVE	PERFECT
1sg	kpá∫	kpáſł	kpa∫nį́:t
2sg	páſa	pa∫t	pa∫nį́:ta̯
3sg	pá∫	paſł	pa∫nį́:t
1pl.excl	kpaſáw	kpaſw	kpaſnį:táw
1PL.INCL	paſáw	pa∫w	pa∫nį:tą́w
2PL	paſá:ti̯t	pá∫t <u>i</u> t	paʃni̯:táti̯t
3PL	pa∫qóh	paſqó:ł	pa∫qo:nį́:t

As a lemma, would choose 3sG—all of the other wordforms can be inferred easily from this one. The relationships are much more complicated, but the principles are the same. One can either infer each of the cells given the lemma and the properties (like first person, plural, inclusive, or perfective) or infer some cells in the paradigm given wordforms in the other cells.

Table 3: Partial paradigm for Totonac paf 'swim, bathe'

Computational Tasks with Paradigms

One can infer all of the cells in (this part of) a Totonac verb paradigm (roughly) by substituting the lemma for the Xs in Table 4.

'SWIM, BATHE' IMPERFECT PERFECTIVE PERFECT 1s_G kX kX} kXnį:t 2s_G Xt Xa Xní:ta Xł 3s_G X Xní:t 1PL.EXCL kXáw kXw kXnj:táw Xáw Xw Xnj:táw 1PL.INCL Xtit 2_{PL} Xá:tit Xni:tátit Xqó:ł 3pt. Xqóh Xqo:ní:t

Table 4: Partial paradigm for Totonac

Alternatively, given a subset of wordforms in a paradigm, we can fill in the missing cells by analogy with other paradigms (Table 5).

'SWIM, BATHE'	IMPERFECT	PERFECTIVE	PERFECT
1sg	kpá∫	kpáſł	kpaʃní̯:t
2sg	páſa	paſt	pa∫nį́:ta̯
3sg	[mask]	paſł	pa∫nį́:t
1pl.excl	kpaſáw	kpaſw	[mask]
1pl.incl	pa∫áౖw	pa∫w	pa∫nį:tá́w
2PL	pa∫á:ti̯t	páſti̯t	pa∫nį:táti̯t
3PL	paſqóh	[mask]	paſqo:nį́:t

Table 5: Partial paradigm for Totonac paf 'swim, bathe'

These two tasks are called REINFLECTION and PARADIGM COMPLE-TION.

Morphemes, Paradigms, and Theories of Morphology

In the previous section, we concentrated on MORPHEMES as minimal signs and treated words as the concatenation of strings of morphemes. This approach to morphology is called ITEM-AND-ARRANGEMENT morphology. We further saw that non-concatenative processes could act like morphemes. A kind of morphological theory that generalizes morphemes to processes (treats concatenation of morphemes as a special case of string-to-string, or rather sign-to-sign, functions) is called ITEM-AND-PROCESS morphology.

WORD-AND-PARADIGM morphology is a much different morphological theory in which morphology is understood not in terms of morphemes but in terms of relationship between wordforms within a paradigm.

item-and-arrangement Words are built up by concatenating morphemes. Meaning is computed compositionally.

item-and-process Words are build up by applying zero or more functions of the type $f: \Sigma * \to \Sigma *$ to a root morpheme. Meaning is computed compositionally.

word-and-paradigm Wordforms are realizations of lexemes given inflectional properties (within a paradigm). Morphemes, as such, do not exist.

Lexemes, Paradigms, and Subword Representations

Lexemes are sets of signifiers than have only one signified. They also tend to share a common substring (so the signifiers are not completely distinct). What does this mean for tokenization?

- If words have a similar meaning, we expect them to have a similar representation.
- It would help words have a similar representation if there were an overlap between subword units
- If the lemma is a distinct unit, most or all wordforms belonging to a lexeme will share a token in common
- Is is less clear what this means for other subword units of a wordform

UniMorph and Paradigms in Computational Morphology

Perhaps the best-know multilingual computational resource for morphological analysis is UniMorph (https://unimorph.github.io/). It is a collaborative effort to collect and annotate paradigms of the world's languages. It consists of wordforms, the corresponding lemmas, and the corresponding bundle of inflectional properties. An excerpt from the Catalan dataset (a few wordforms for the verb abaixar 'lower') is given below:

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abaixar abaixada V.PTCP;PST;SG;FEM
abaixar abaixades V.PTCP;PST;PL;FEM
abaixar abaixant V.PTCP;PRS
abaixar abaixaran V;IND;FUT;3;PL
abaixar abaixaràs V;IND;FUT;2;SG
abaixar abaixarà V; IND; FUT; 3; SG
abaixar abaixarem V;IND;FUT;1;PL
abaixar abaixàrem V; IND; PST; 1; PL; PFV
abaixar abaixaren V;IND;PST;3;PL;PFV
abaixar abaixares V; IND; PST; 2; SG; PFV
abaixar abaixareu V;IND;FUT;2;PL
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abaixar abaixàreu V;IND;PST;2;PL;PFV
abaixar abaixaré V;IND;FUT;1;SG
abaixar abaixaria V;COND;1;SG
abaixar abaixaria V;COND;3;SG
abaixar abaixaríem V;COND;1;PL
abaixar abaixarien V;COND;3;PL
abaixar abaixaries V;COND;2;SG
abaixar abaixaríeu V;COND;2;PL
abaixar abaixar V;NFIN
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The first column is the lemma; the second column is the inflected wordform; the third column is a list of inflectional properties in standardized representation, separated by semicolons. Part of speech, represented by V for verb, is treated as a property. A complete catalog of all of these labels, and their definitions, is provided by the UniMorph Schema.

UniMorph has provided the framework for a number of shared tasks. The most prominent of these are reinflection and paradigm completion, as mentioned above. In reinflection, the model is provided with the lemmas, properties, and wordforms for a subset of the dataset as training data. At test time, the model is required to generate a wordform given the lemma and the properties. For example, given *abaixar* as a lemma and *V;IND;FUT;1;PL* as properties, the model is expected to generate abaixarem.