
Recurrent Neural Network - 1

(순환 신경망)

조윤상

목차

- ❖ 순환 신경망 개요
- ❖ 순환 신경망 학습(Backpropagation Trough Time)
- ❖ 순환 신경망 모델링
- ❖ 순환 신경망 한계

목차

❖ 순환 신경망 개요

❖ 순환 신경망 학습(Backpropagation Trough Time)

❖ 순환 신경망 모델링

❖ 순환 신경망 한계

순환 신경망 개요

❖ 기계학습 모델

$$f(\cdot) = \text{Model}$$

설명 변수(X)

$f(X) = y$ 반응 변수(y)

변수 관측치	x_1	x_2	...	x_{p-1}	x_p		y
N_1						학습	
N_2							
...							
N_{n-1}							
N_n							

순환 신경망(recurrent neural network, RNN) 이란?

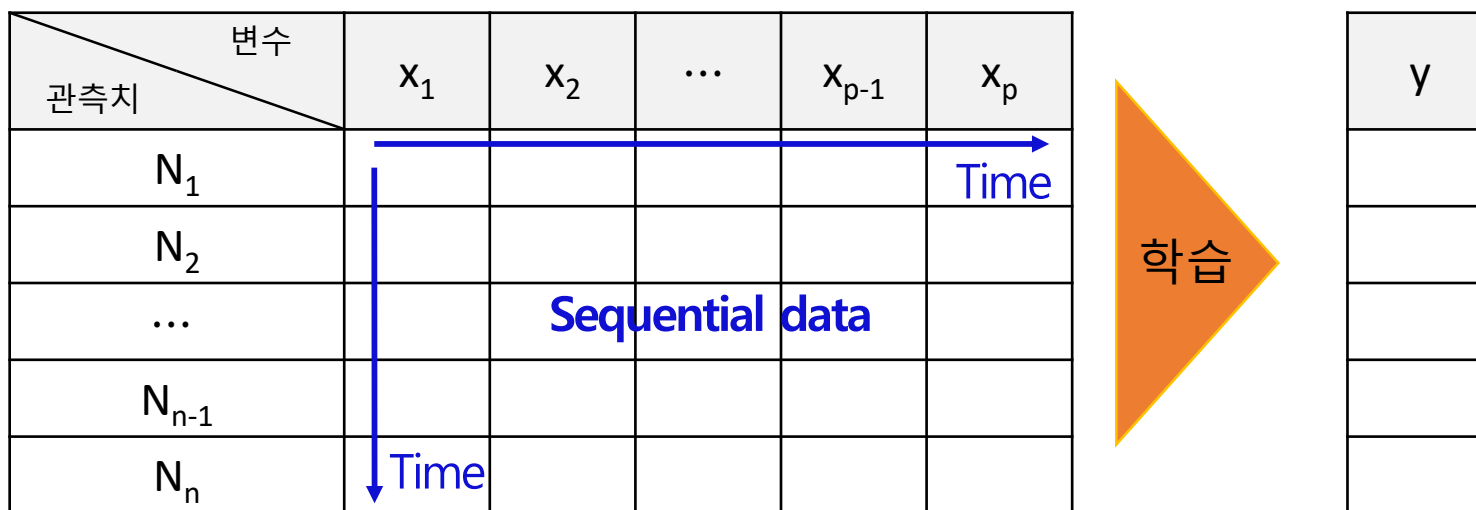
순환 신경망 개요

- ❖ 순환 신경망(recurrent neural network, RNN)

$$f(\cdot) = \text{RNN Model}$$

설명 변수(X)

$f(X) = y$ 반응 변수(y)

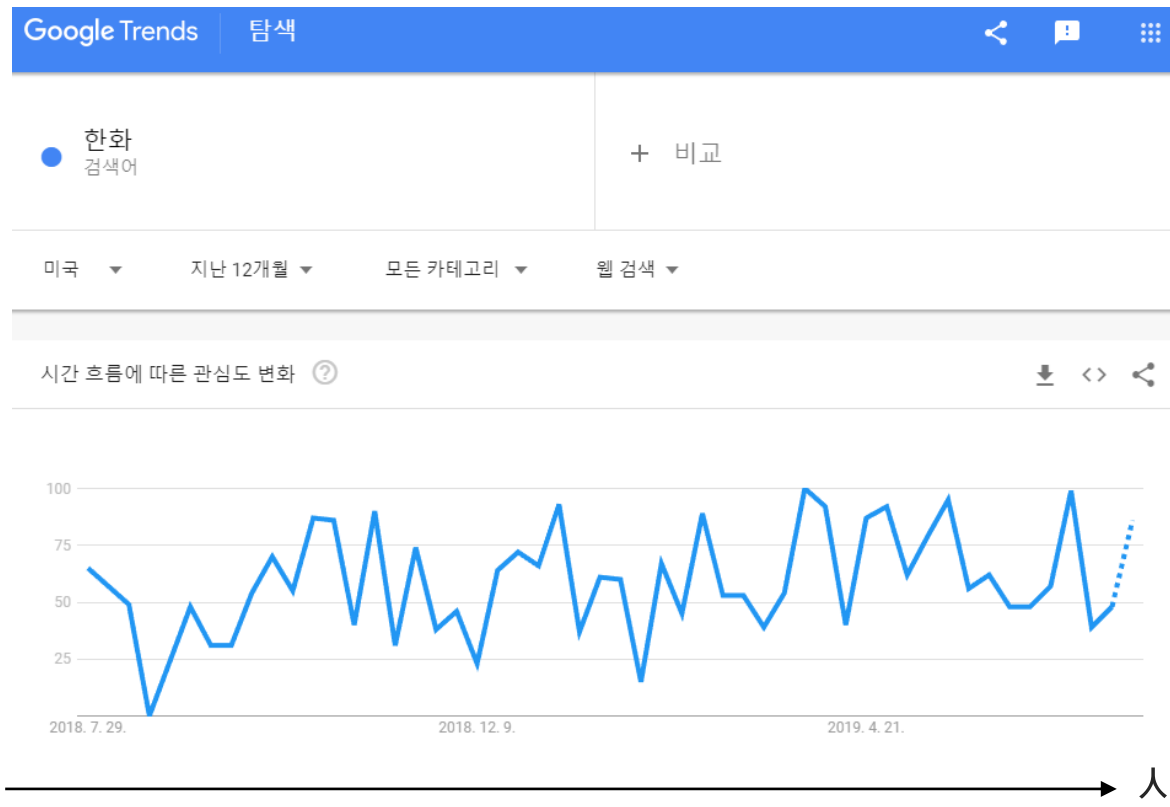


순차 데이터(sequential data) 모델링을 위한 인공 신경망(neural network) 모델

순환 신경망 개요

- ❖ 순차 데이터(sequential data)
 - 변수 간 or 관측치 간 순서가 있는 데이터

구글 트렌드 데이터

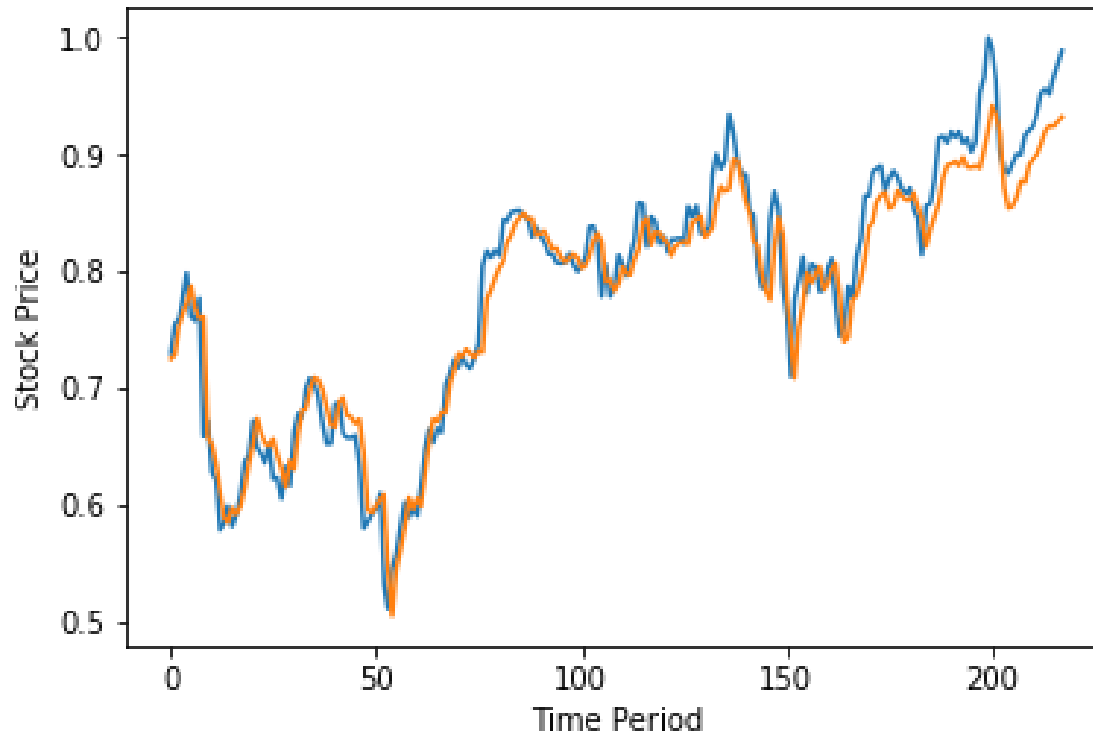


순환 신경망 개요

❖ 순차 데이터(sequential data)

- 변수 간 or 관측치 간 순서가 있는 데이터

주가 데이터



순환 신경망 개요

- ❖ 순차 데이터(sequential data)
 - 변수 간 or 관측치 간 순서가 있는 데이터

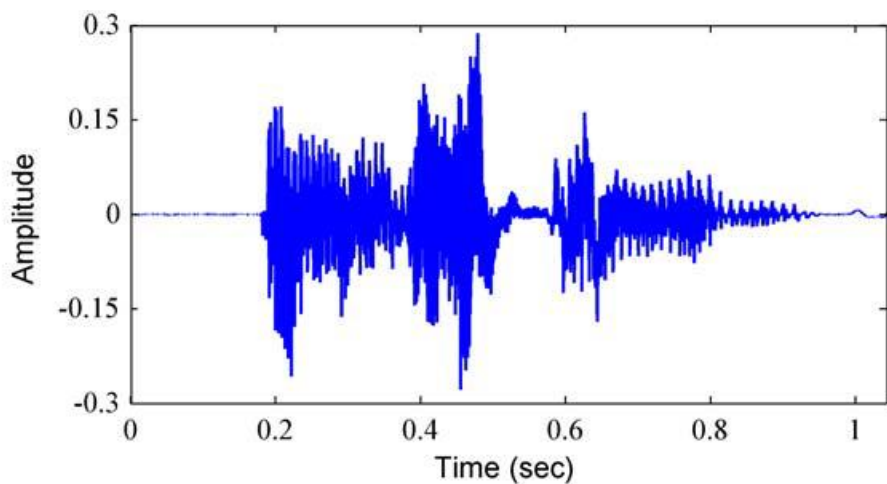
텍스트 데이터

	Review	Rating
0	excellent service, great price, an...	5
1	Comfortable seating with adequate ...	5
2	I like Flix Bus. It seems like an ...	4
3	Very good service, clean bus, big,...	4
4	Great first trip! Great price, cle...	5
5	It was a very bad trip. The bus de...	1
6	Im first time by flibus, it's nic...	4
7	Good way to travel	4
8	Very fast, very cheap and rather c...	4
9	Booked bus from Bayreuth in German...	1

순환 신경망 개요

- ❖ 순차 데이터(sequential data)
 - 변수 간 or 관측치 간 순서가 있는 데이터

음성 데이터



b	ey	z	th	ih	er	em
Bayes'			Theorem			

순환 신경망 개요

❖ 순환 신경망(recurrent neural network, RNN) 이란?

- 순차 데이터(sequential data) 모델링을 위한 인공 신경망(neural network) 모델
- 순차 데이터(sequential data): **변수** 간 or **관측치** 간 순서가 있는 데이터

인공신경망

- 1943: Neural networks
- 1957: Perceptron
- 1974-86: Backpropagation, RBM, RNN
- 1989-98: CNN, MNIST, LSTM, Bidirectional RNN
- 2006: "Deep Learning", DBN
- 2009: ImageNet
- 2012: AlexNet, Dropout
- 2014: GANs
- 2014: DeepFace
- 2016: AlphaGo
- 2017: AlphaZero, Capsule Networks
- 2018: BERT

* Dates are for perspective and not as definitive historical record of invention or credit

순환 신경망 구조

No	RNN Architectures
1	Fully Recurrent Neural Network
2	Recursive Neural Network
3	Hopfield Network
4	Elman Networks And Jordan Networks or Simple Recurrent Network (SRN)
5	Echo State Network
6	Neural History Compressor
7	Long Short-Term Memory (LSTM)
8	Gated Recurrent Unit
9	Bi-Directional Recurrent Neural Network
10	Continuous-Time Recurrent Neural Network (CTRNN)
11	Hierarchical Recurrent Neural Network
12	Recurrent Multilayer Perceptron Network
13	Multiple Timescales Model
14	Neural Turing Machines (NTM)
15	Differentiable Neural Computer (DNC)
16	Neural Network Pushdown Automata (NNPDA)

<https://www.rsisinternational.org/journals/ijrsi/digital-library/volume-5-issue-3/124-129.pdf>

순환 신경망 개요

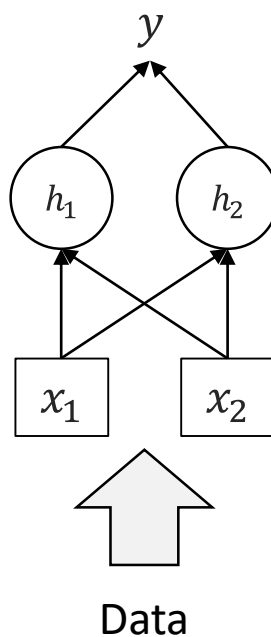
❖ 신경망(NN) vs 순환 신경망(RNN)

$f(\cdot)$ = Neural Network

반응 변수

은닉층

설명 변수



→ y 를 잘 예측하는 방향으로.

→ 더 좋은 특징을 추출

→ 변수 2개를 조합

순환 신경망 개요

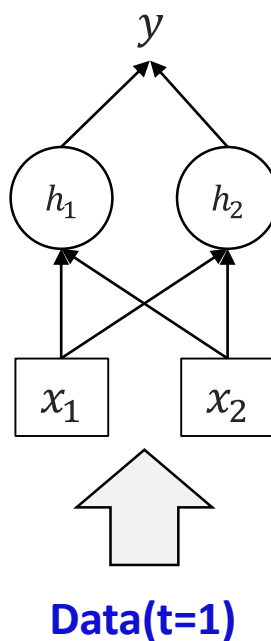
❖ 신경망(NN) vs 순환 신경망(RNN)

$f(\cdot)$ = Recurrent Neural Network

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→ y를 잘 예측하는 방향으로.

→ 더 좋은 특징을 추출

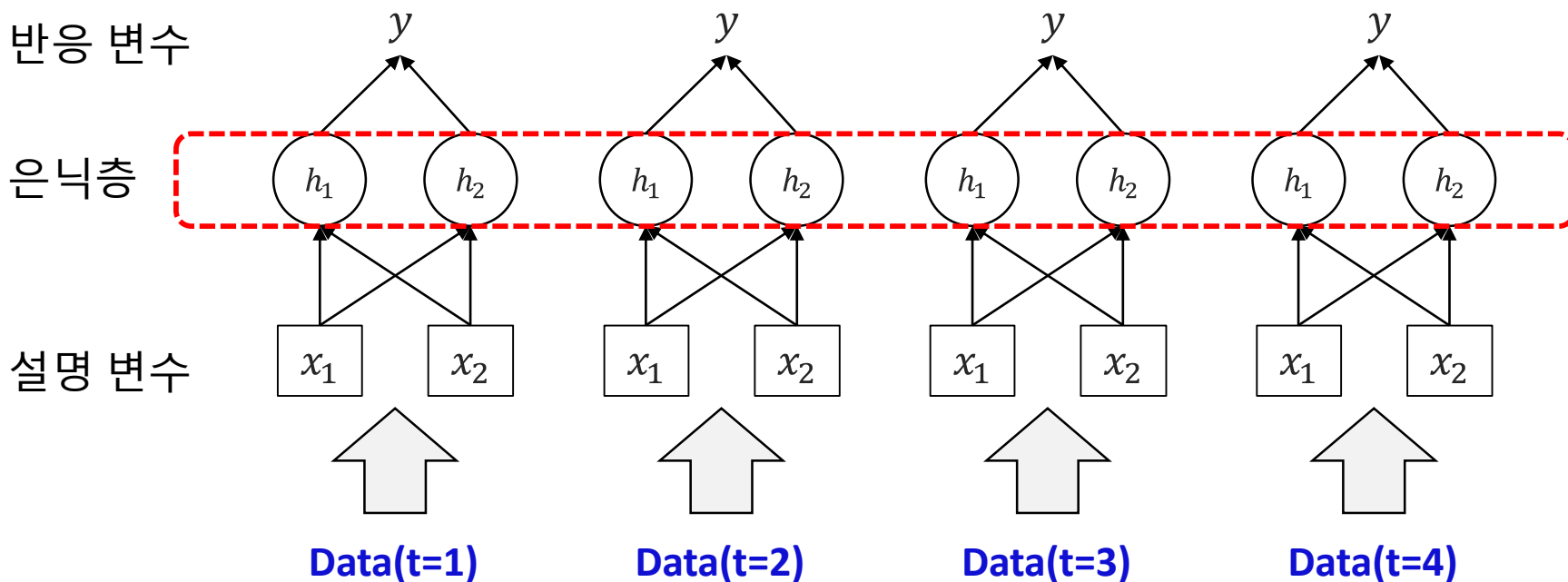
→ 변수 2개를 조합

순환 신경망 개요

❖ 신경망(NN) vs 순환 신경망(RNN)

$f(\cdot)$ = Recurrent Neural Network

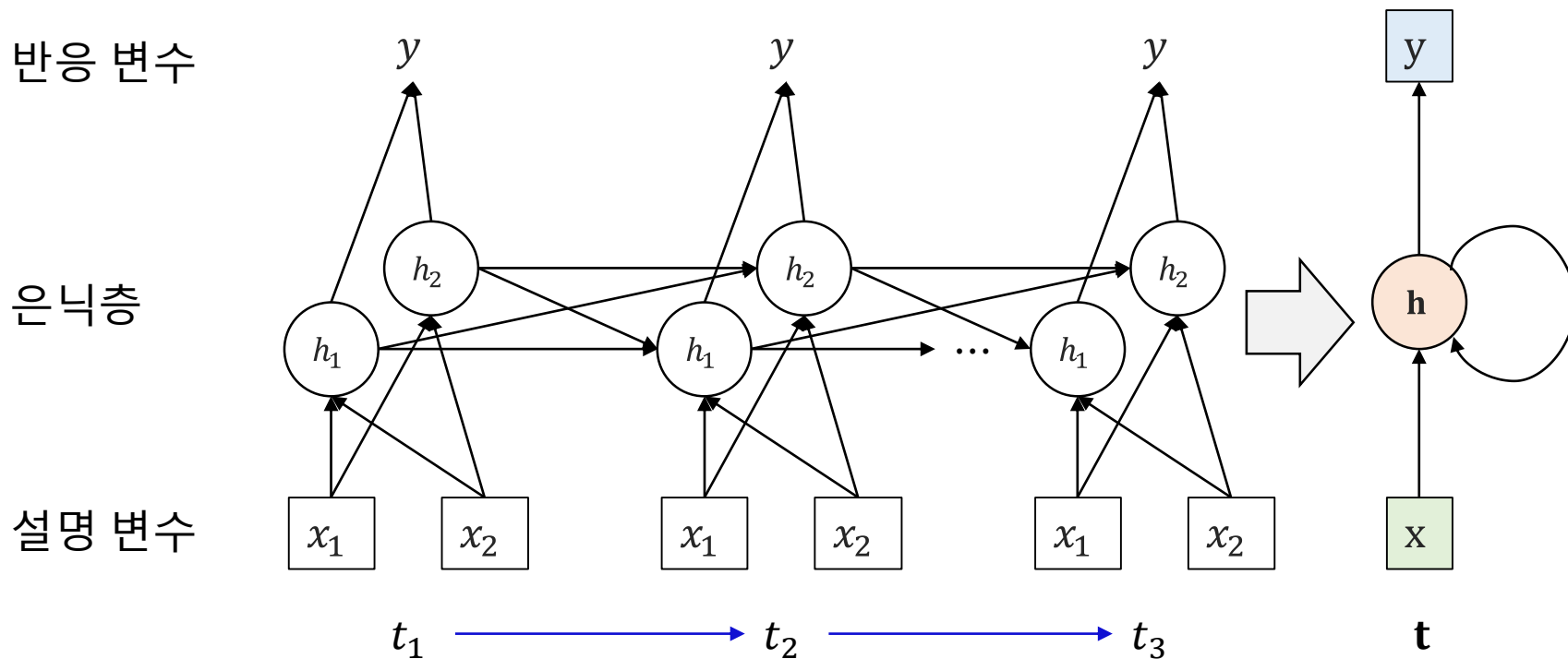
시간을 반영하는 것은 Hidden layer, 어떻게?



순환 신경망 개요

❖ 신경망(NN) vs 순환 신경망(RNN)

$f(\cdot)$ = Recurrent Neural Network

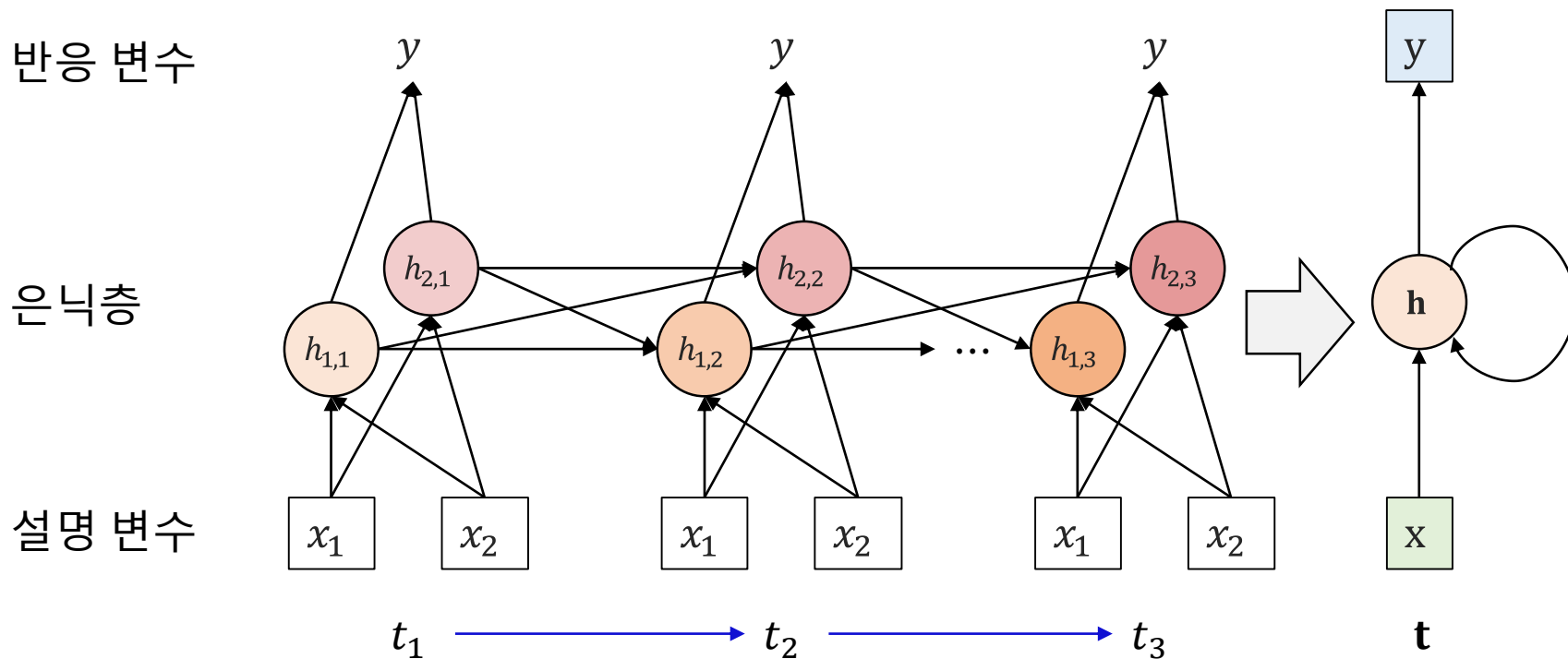


순환 신경망 개요

❖ 순환 신경망(RNN)

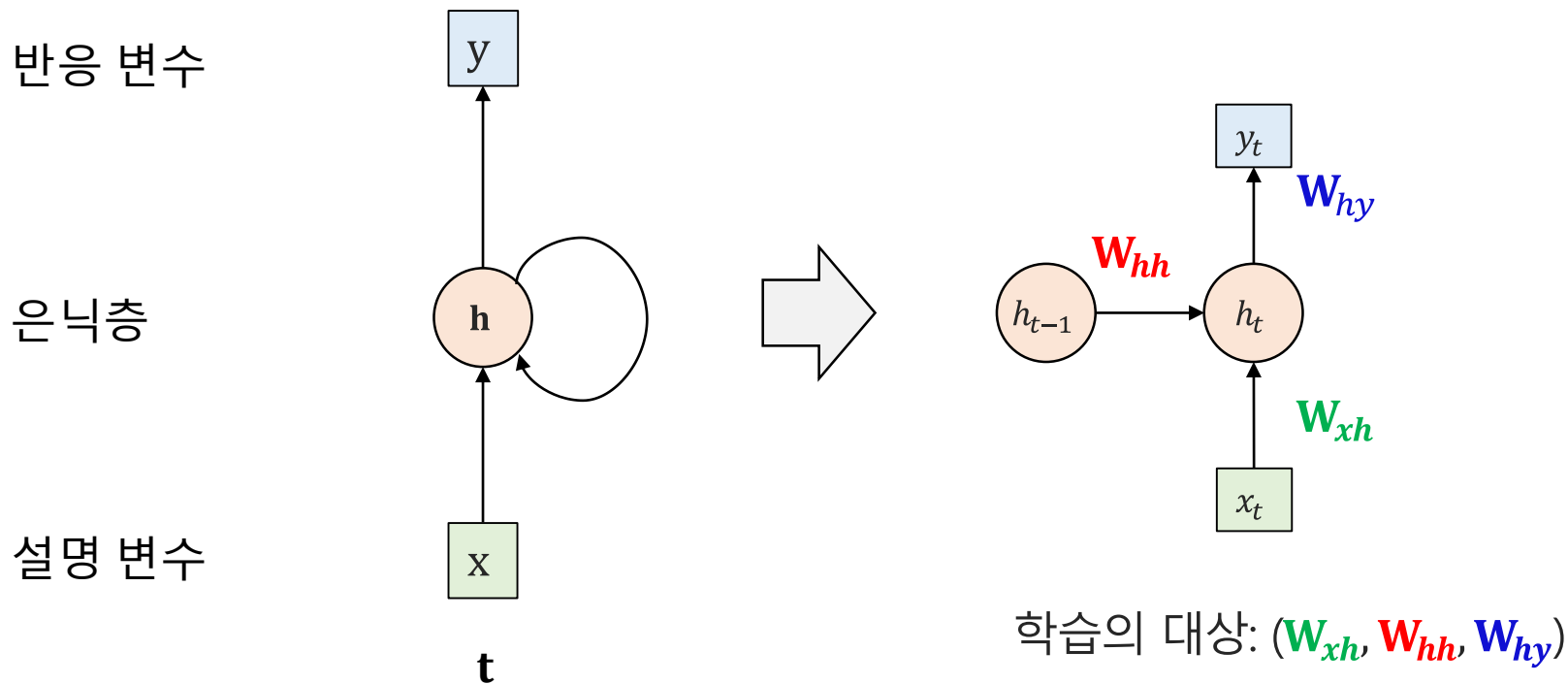
t 시점 y를 예측

$f(\cdot) = \text{Recurrent Neural Network}$



순환 신경망 개요

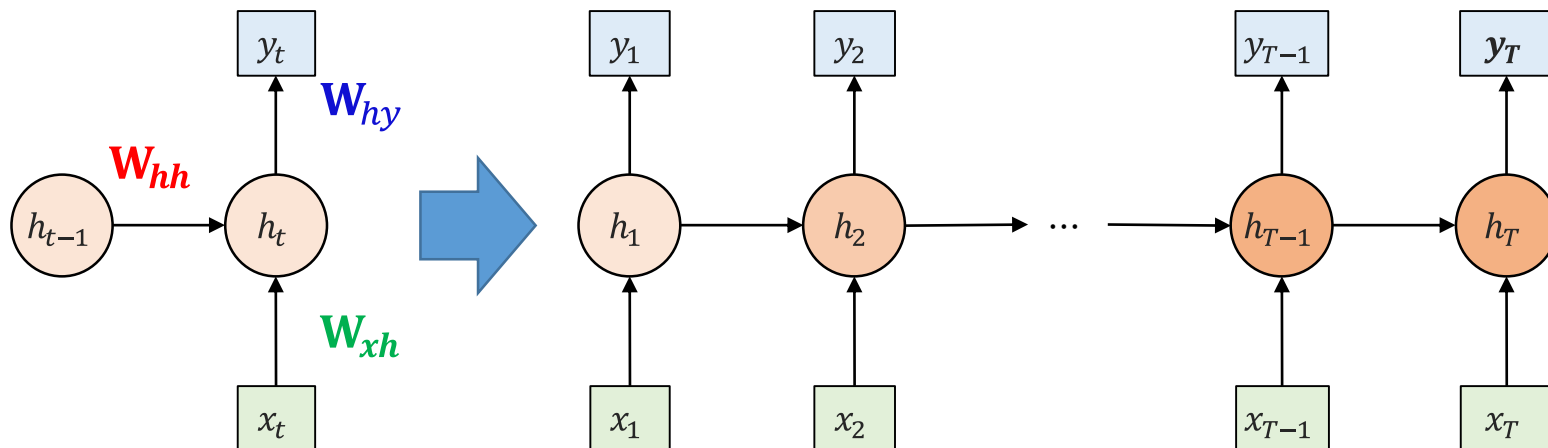
- ❖ t 시점 이전 정보와, → hidden layer로부터 전달되는 weight(W_{hh})
- ❖ t 시점 input 데이터 정보를 가지고 → W_{xh}
- ❖ t 시점의 y를 예측 → W_{hy}



순환 신경망 개요

❖ RNN 구조: t 시점 이전 정보, t시점 데이터 x_t 를 가지고 t 시점 y_t 를 예측

- $y_t = g(W_{xh}h_t + b_y)$
- $h_t = f(W_{hh}h_{t-1} + W_{xh}x_t + b_x)$



학습의 대상: (W_{xh} , W_{hh} , W_{hy})

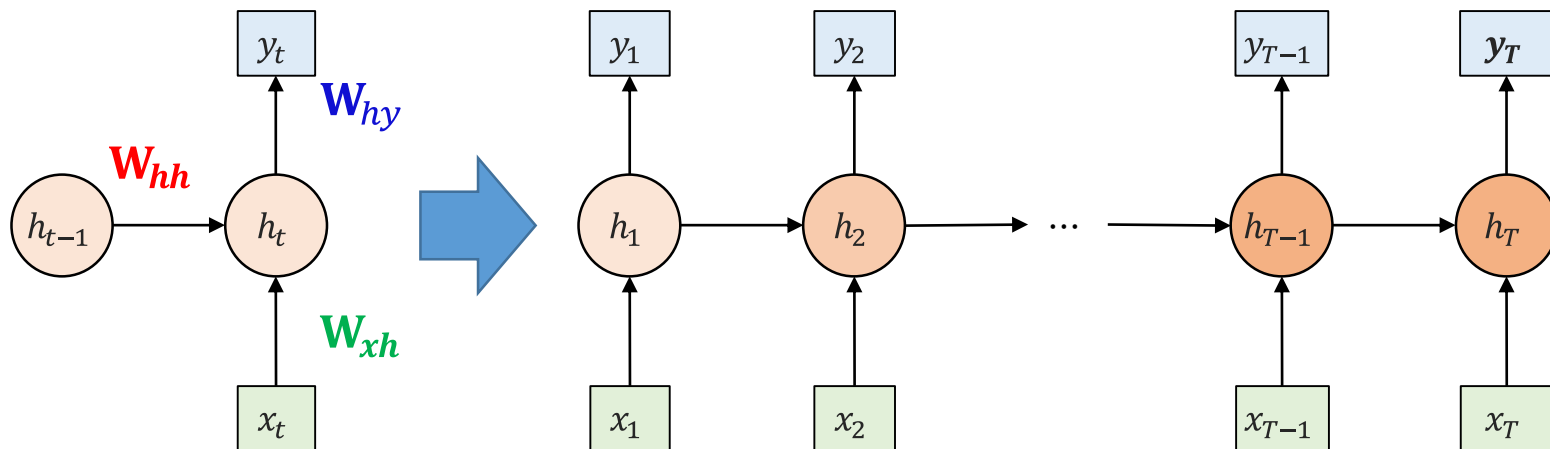
학습 방법: Backpropagation Trough Time

순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to Many RNN



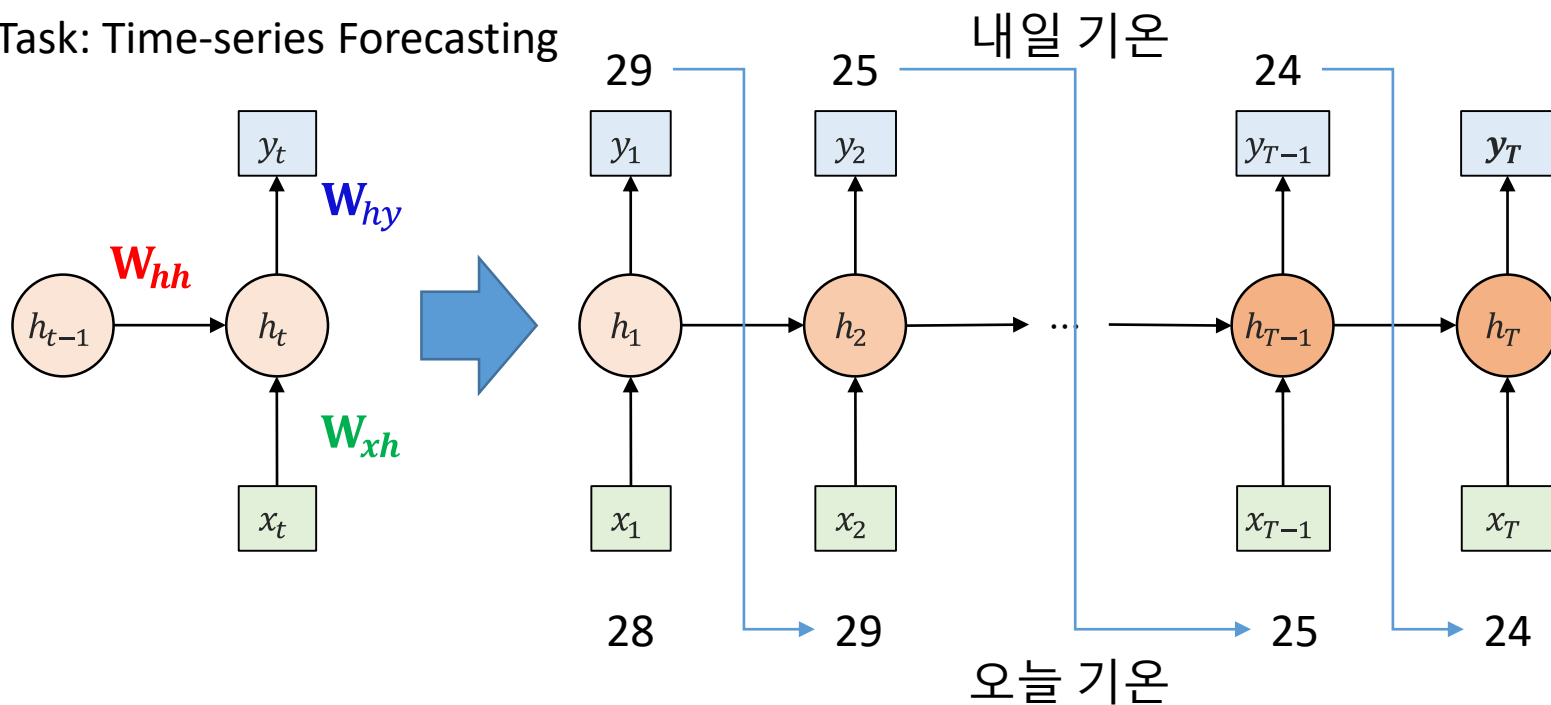
순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to Many RNN

Task: Time-series Forecasting



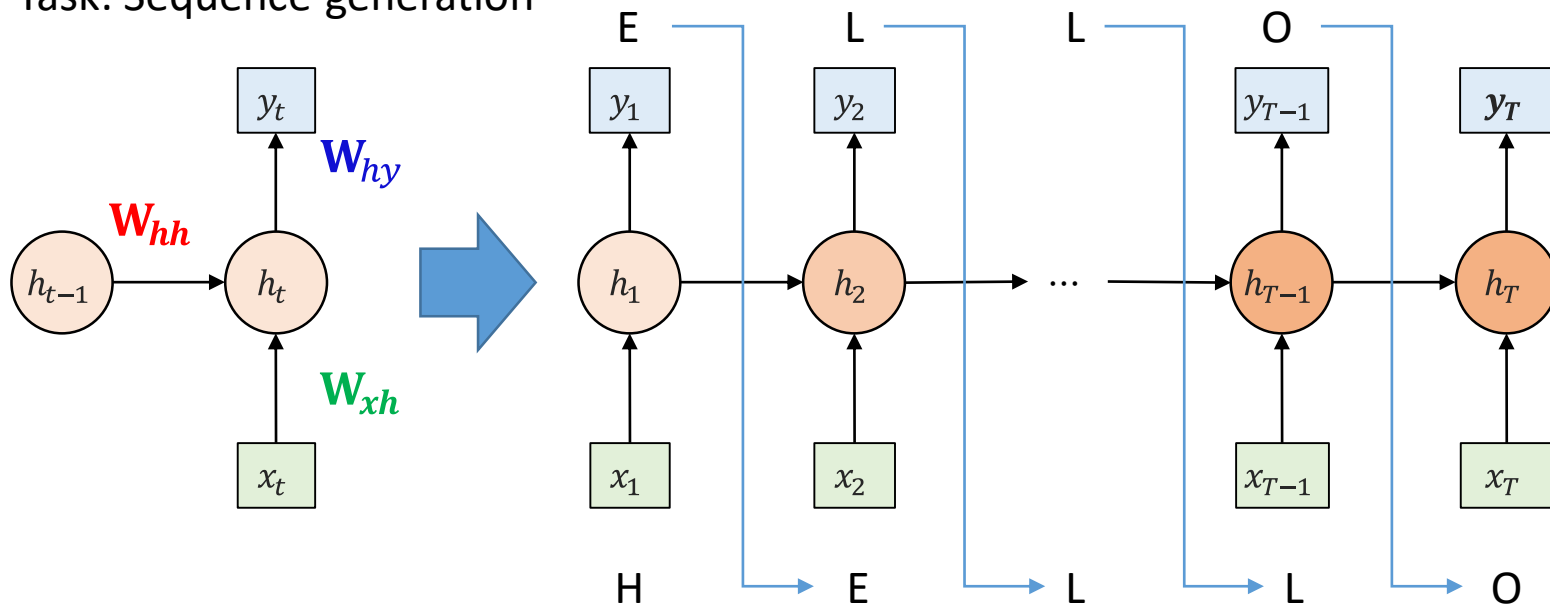
순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to Many RNN

Task: Sequence generation

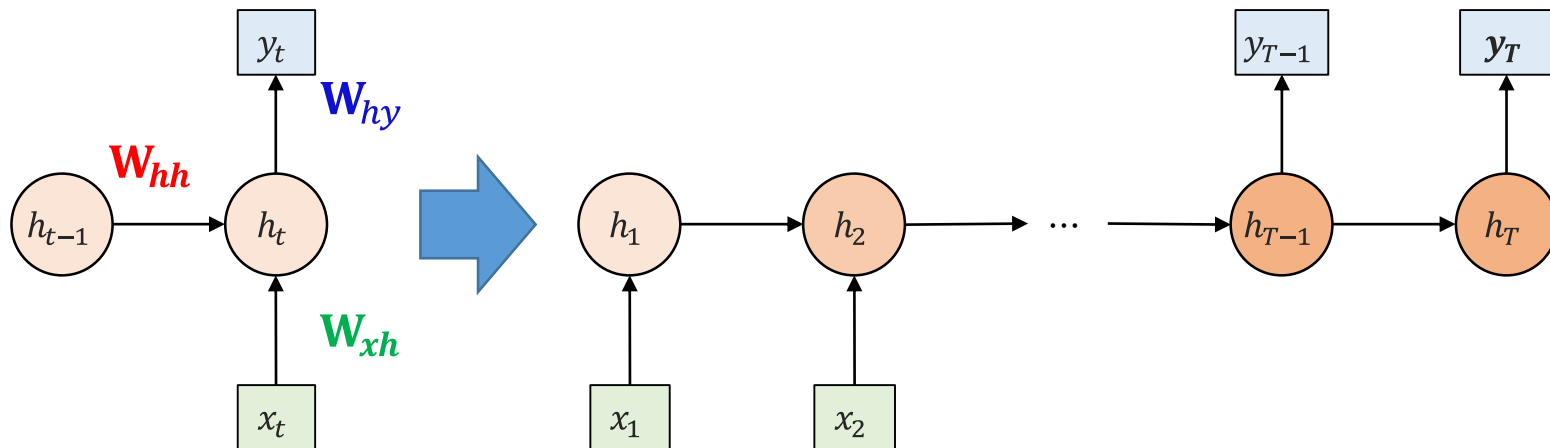


순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to Many RNN



순환 신경망 개요

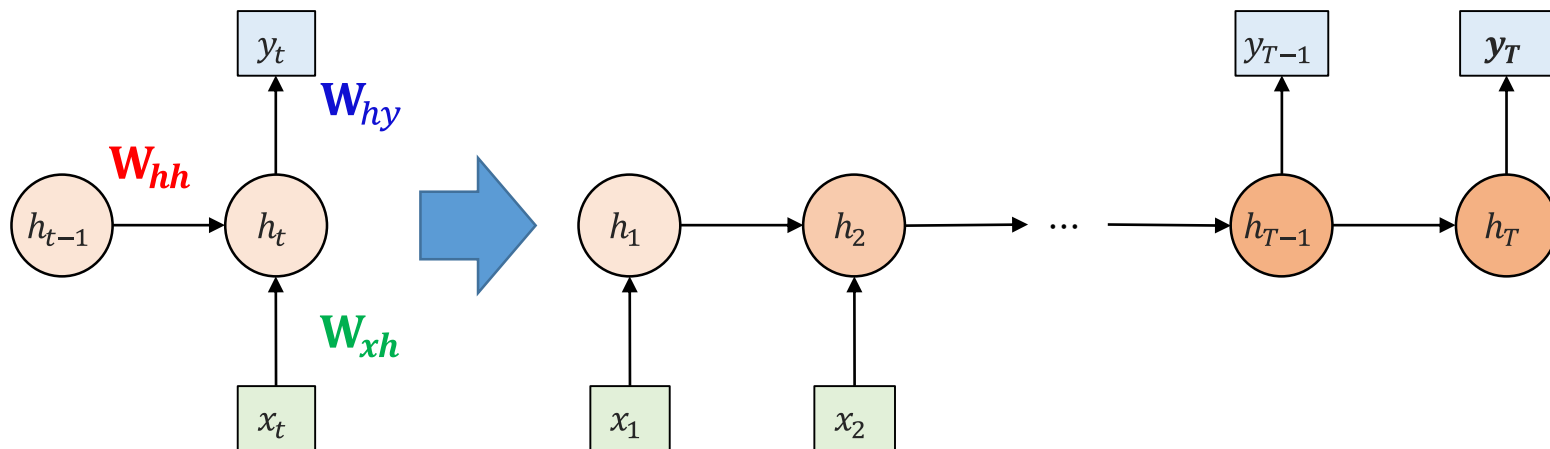
학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to Many RNN

Task: Machine Translation

(한국어) 안녕하세요 조 박사님, 한화입니다.

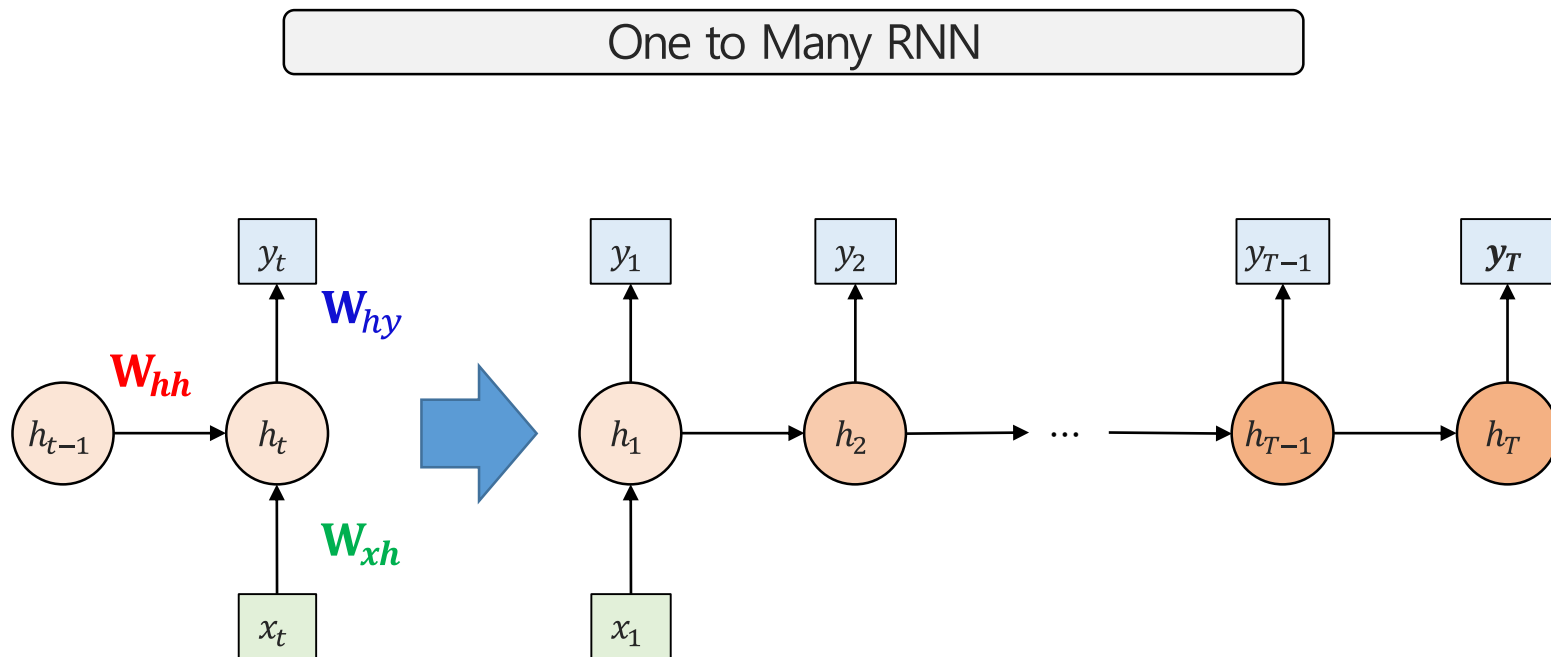


(English) Hello Dr. Cho, This is Hanhwa.

순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조



순환 신경망 개요

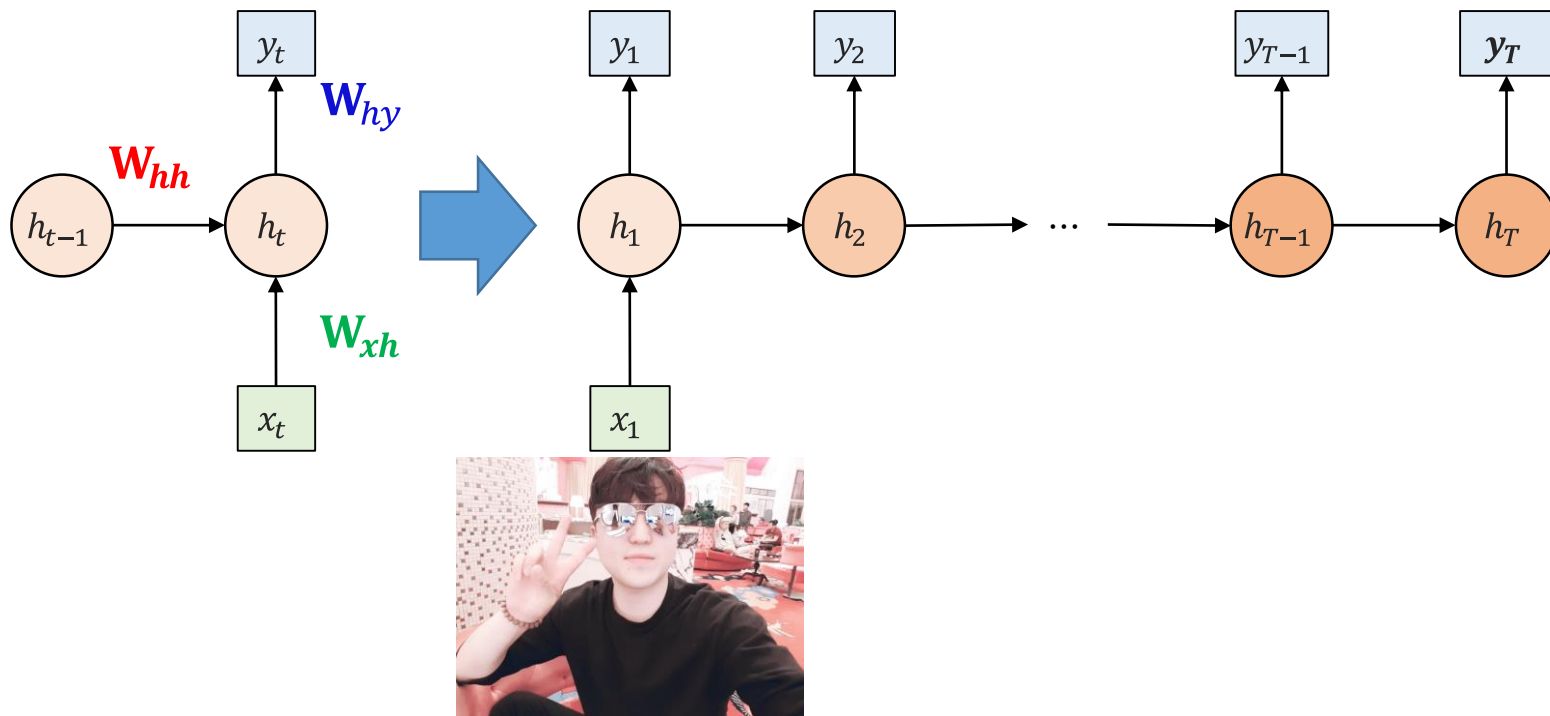
학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

One to Many RNN

Task: Image Captioning

... 선글라스 낀 남자가 v 를 하고 있다. ...

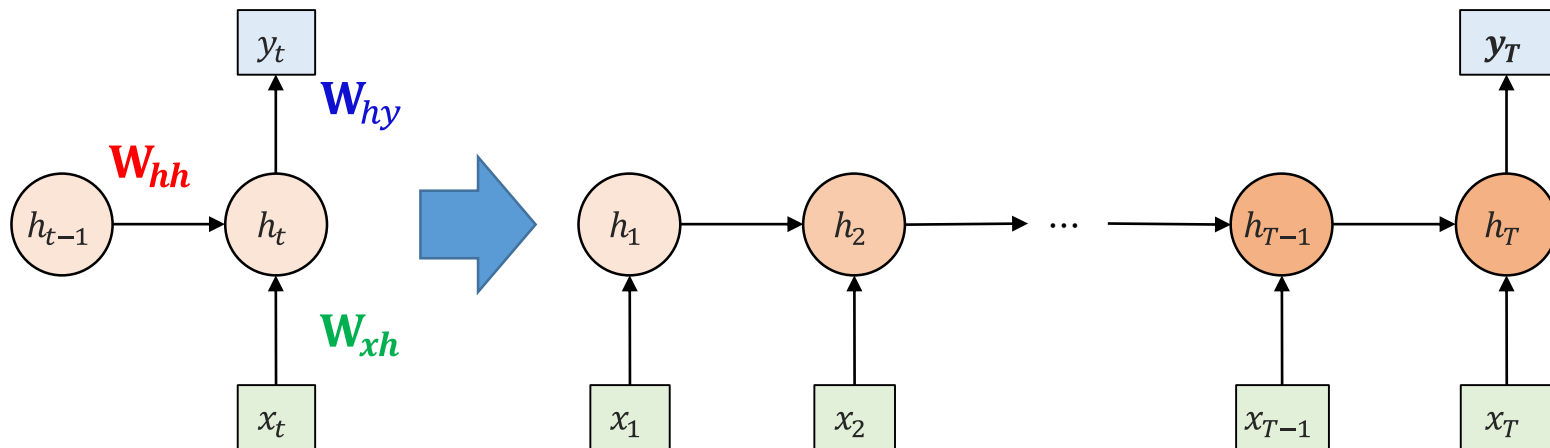


순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to One RNN



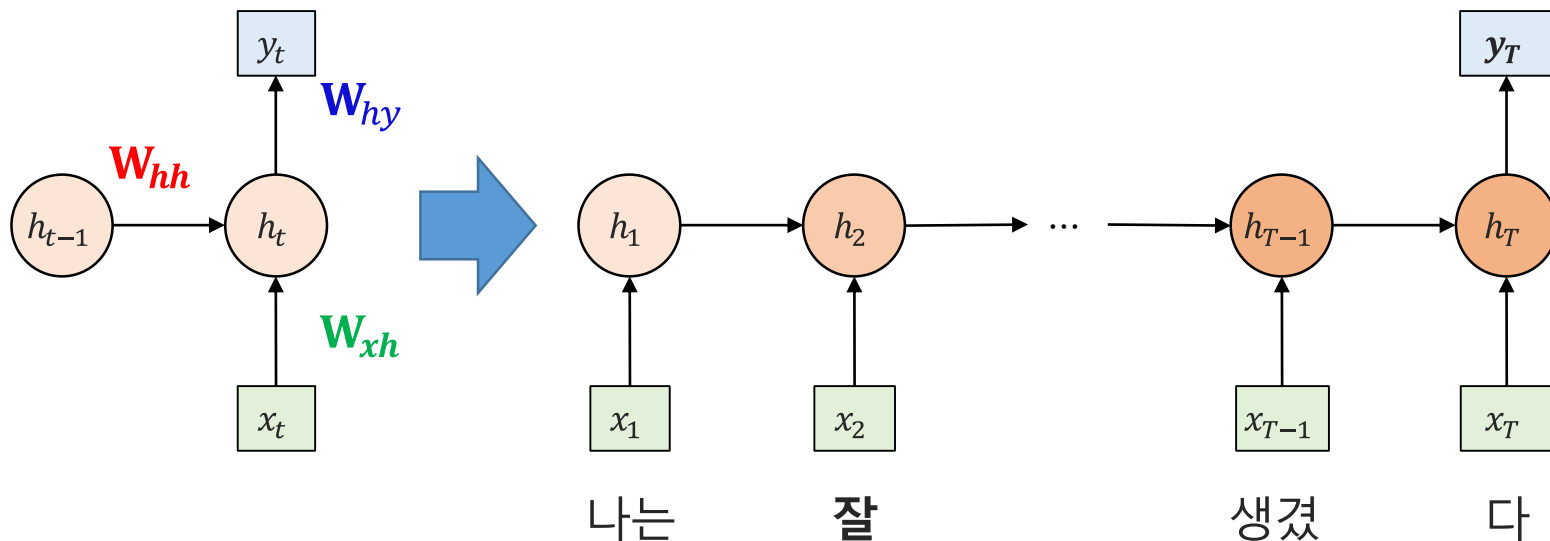
순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to One RNN

Task: Sequence Classification



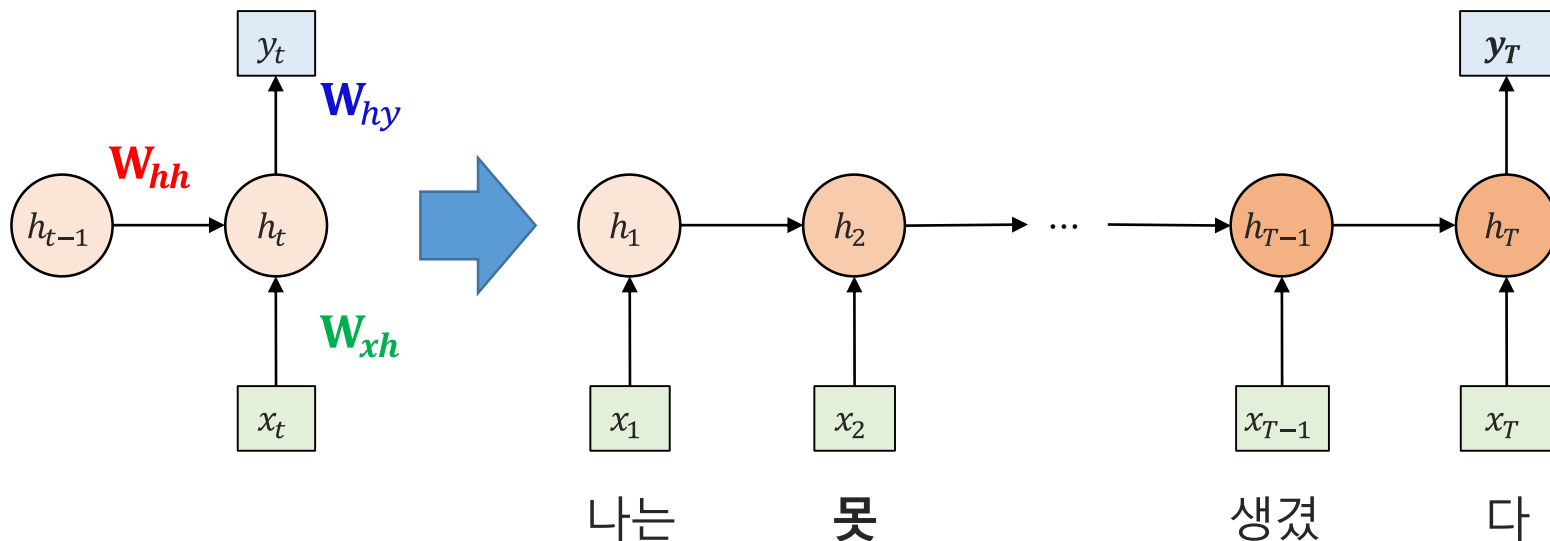
순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조

Many to One RNN

Task: Sequence Classification



목차

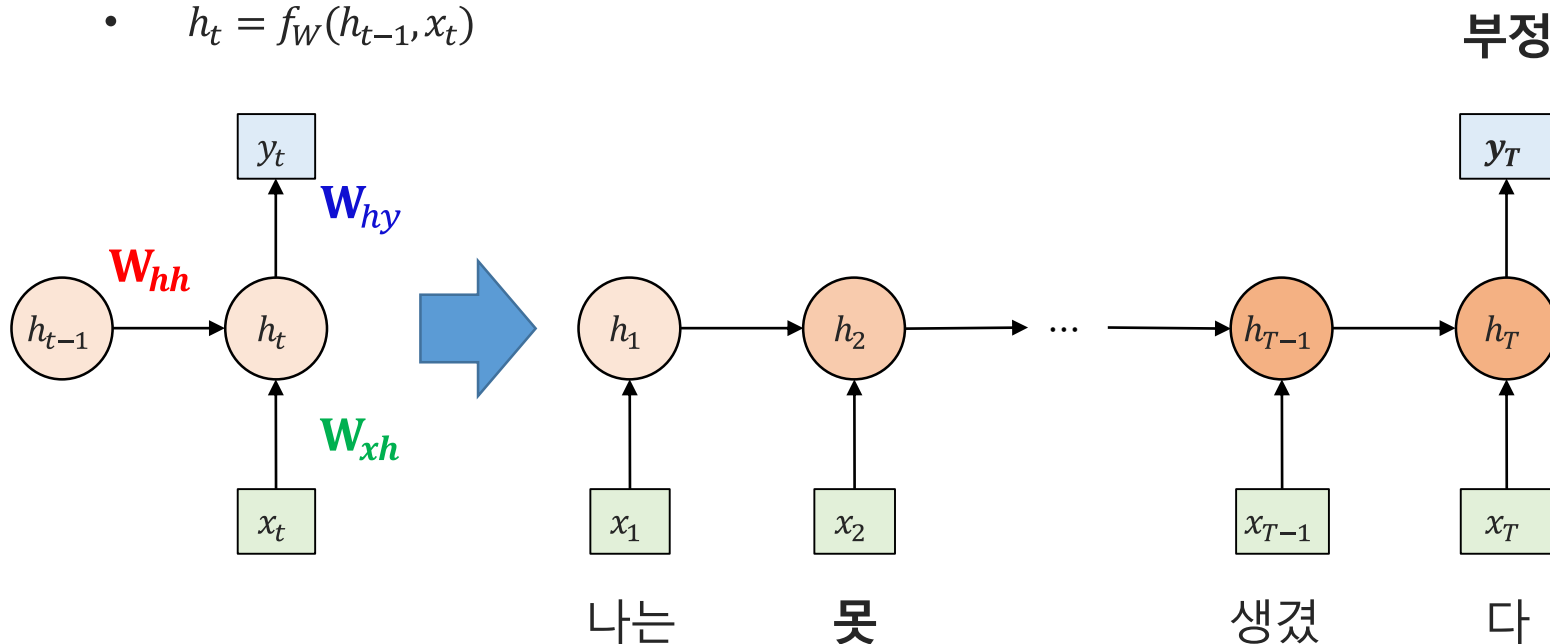
- ❖ 순환 신경망 개요
- ❖ 순환 신경망 학습(Backpropagation Trough Time)
- ❖ 순환 신경망 모델링
- ❖ 순환 신경망 한계

순환 신경망 개요

학습의 대상: (W_{xh} , W_{hh} , W_{hy})

❖ RNN 구조: t 시점 이전 정보, t시점 데이터 x_t 를 가지고 t 시점 y_t 를 예측

- $y_t = g(W_{xh}h_t + b_y)$
- $h_t = f(W_{hh}h_{t-1} + W_{xh}x_t + b_x)$
 - $h_t = f_W(h_{t-1}, x_t)$



학습의 대상: (W_{xh} , W_{hh} , W_{hy})

학습 방법: Backpropagation Trough Time

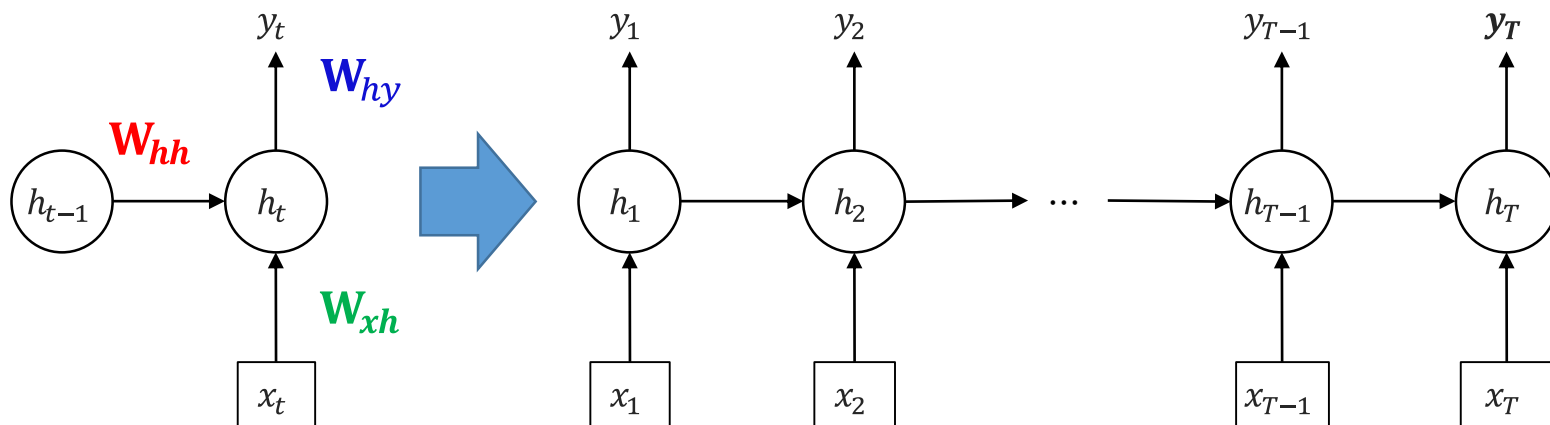
순환 신경망 개요

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Many to Many RNN



학습의 대상: (W_{xh} , W_{hh} , W_{hy})

학습 방법: Backpropagation Trough Time

순환 신경망 학습

❖ RNN 학습 방식: 시간 흐름에 따라 파라미터 업데이트

❖ Backpropagation Trough Time (BPTT)

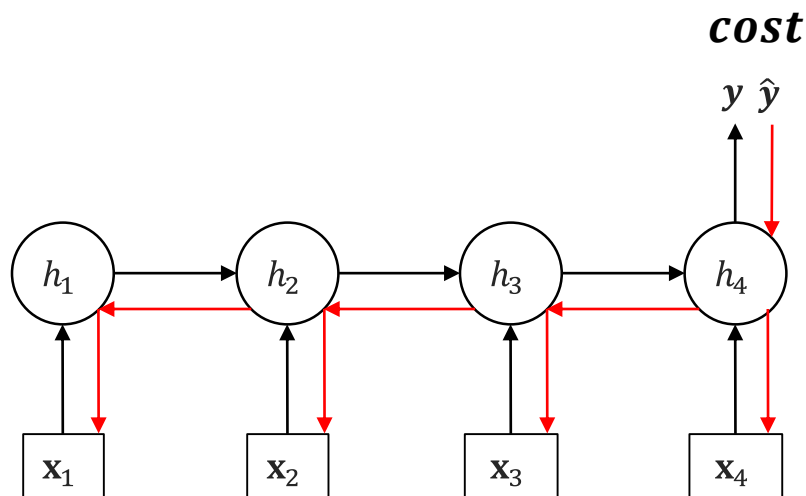
학습의 대상: (W_{xh} , W_{hh} , W_{hy})

- $y_t = g(W_{xh}h_t + b_y)$

- $h_t = f(W_{hh}h_{t-1} + W_{xh}x_t + b_x) \rightarrow f(\cdot)$ 를 tanh 함수라 하자

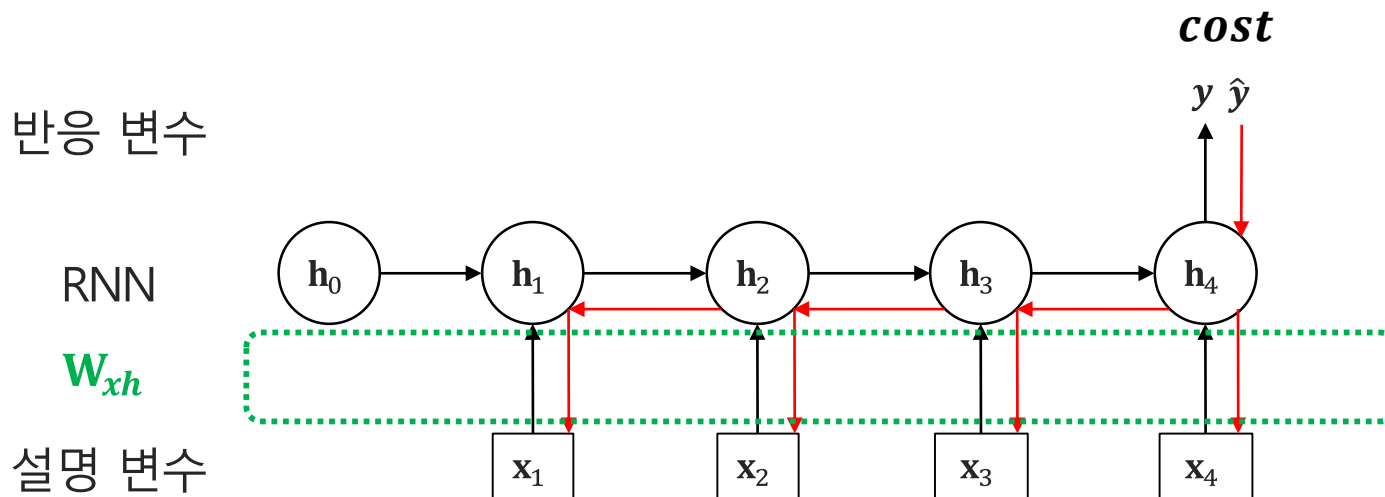
반응 변수

설명 변수



순환 신경망 학습

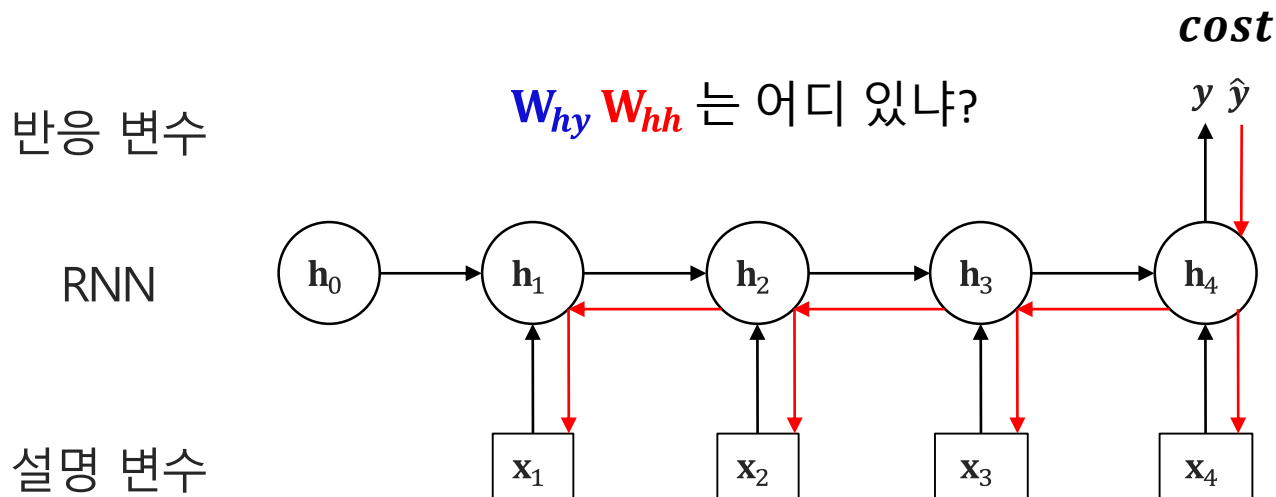
- ❖ RNN 학습 방식: Backpropagation Trough Time (BPTT)
- ❖ 학습의 대상: (W_{xh} , W_{hh} , W_{hy})



$$\begin{aligned}
 \frac{\partial Cost}{\partial W_{xh}} &= \frac{\partial Cost}{\partial y} \times \frac{\partial y}{\partial h_4} \times \frac{\partial h_4}{\partial W_{xh}} + \frac{\partial Cost}{\partial y} \times \frac{\partial y}{\partial h_4} \times \frac{\partial h_4}{\partial h_3} \times \frac{\partial h_3}{\partial W_{xh}} + \\
 &\quad \frac{\partial Cost}{\partial y} \times \frac{\partial y}{\partial h_4} \times \frac{\partial h_4}{\partial h_3} \times \frac{\partial h_3}{\partial h_2} \times \frac{\partial h_2}{\partial W_{xh}} + \frac{\partial Cost}{\partial y} \times \frac{\partial y}{\partial h_4} \times \frac{\partial h_4}{\partial h_3} \times \frac{\partial h_3}{\partial h_2} \times \frac{\partial h_2}{\partial h_1} \times \frac{\partial h_1}{\partial W_{xh}}
 \end{aligned}$$

순환 신경망 학습

- ❖ RNN 학습 방식: Backpropagation Trough Time (BPTT)
- ❖ 학습의 대상: (\mathbf{W}_{xh} , \mathbf{W}_{hh} , \mathbf{W}_{hy})



$$\frac{\partial Cost}{\partial \mathbf{W}_{xh}} = \sum_{i=1}^n \frac{\partial Cost}{\partial y} \cdot \frac{\partial y}{\partial \mathbf{h}_n} \cdot \left(\prod_{j=i}^{n-1} \frac{\partial \mathbf{h}_{j+1}}{\partial \mathbf{h}_j} \right) \cdot \frac{\partial \mathbf{h}_i}{\partial \mathbf{W}_{xh}}$$

순환 신경망 학습

- ❖ RNN 학습 방식: Backpropagation Trough Time (BPTT)
- ❖ 학습의 대상: (\mathbf{W}_{xh} , \mathbf{W}_{hh} , \mathbf{W}_{hy})

$$\frac{\partial Cost}{\partial \mathbf{W}_{xh}} = \sum_{i=1}^n \frac{\partial Cost}{\partial y} \cdot \frac{\partial y}{\partial \mathbf{h}_n} \cdot \left(\prod_{j=i}^{n-1} \frac{\partial \mathbf{h}_{j+1}}{\partial \mathbf{h}_j} \right) \cdot \frac{\partial \mathbf{h}_i}{\partial \mathbf{W}_{xh}}$$

$$\mathbf{h}_t = f(\mathbf{W}_{hh}\mathbf{h}_{t-1} + \mathbf{W}_{xh}\mathbf{x}_t + \mathbf{b}_x) = \tanh(\mathbf{z}_t)$$

$$\frac{\partial \mathbf{h}_t}{\partial \mathbf{h}_{t-1}} = \frac{\partial \mathbf{h}_t}{\partial \mathbf{z}_t} \times \frac{\partial \mathbf{z}_t}{\partial \mathbf{h}_{t-1}} = (1 - \tanh^2(\mathbf{z}_t)) \cdot \mathbf{W}_{hh}$$

$$\frac{\partial \mathbf{h}_t}{\partial \mathbf{W}_{xh}} = \frac{\partial \mathbf{h}_t}{\partial \mathbf{z}_t} \times \frac{\partial \mathbf{z}_t}{\partial \mathbf{W}_{xh}} = (1 - \tanh^2(\mathbf{z}_t)) \cdot \mathbf{x}_t$$

순환 신경망 학습

❖ RNN 구조

One-to-Many

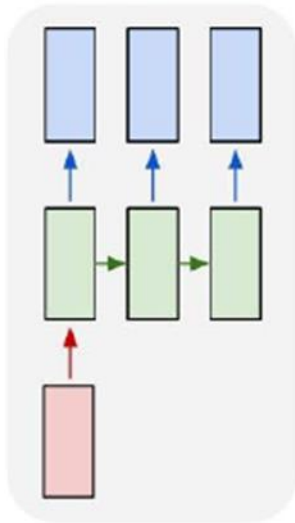
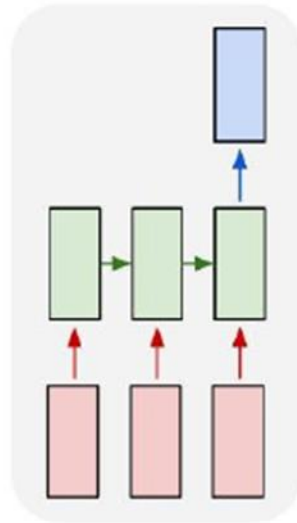


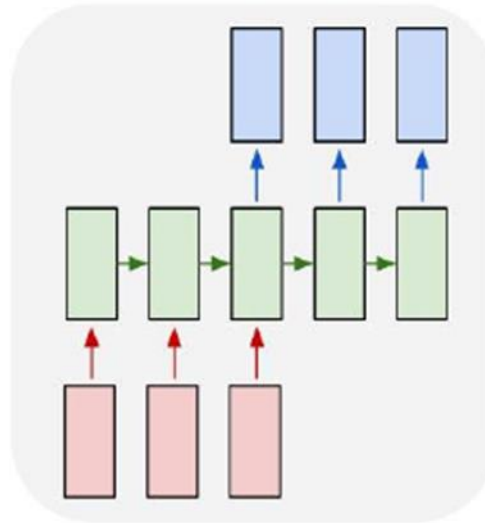
Image Captioning
→ Image to sequence of words

Many-to-One



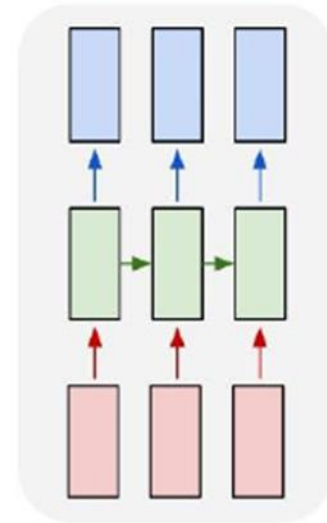
감정 분류

Many-to-Many



기계 번역

Many-to-Many



비디오 분류
(프레임단위)

순환 신경망 모델링

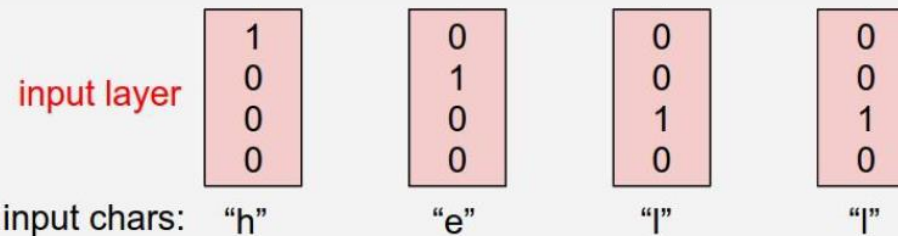
- ❖ Many to Many RNN for Language modeling

wxh			
0.287027	0.84606	0.572392	0.486813
0.902874	0.871522	0.691079	0.18998
0.537524	0.09224	0.558159	0.491528

target chars: “e” “l” “l” “o”

<https://www.analyticsvidhya.com/blog/2017/12/introduction-to-recurrent-neural-networks/>

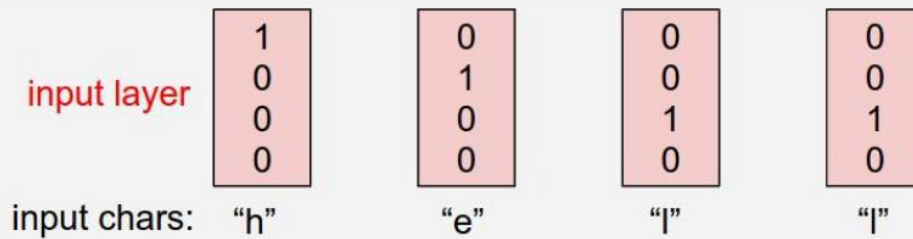
W_{hy}
 W_{hh}
 W_{xh}



- <https://cs224d.stanford.edu/>

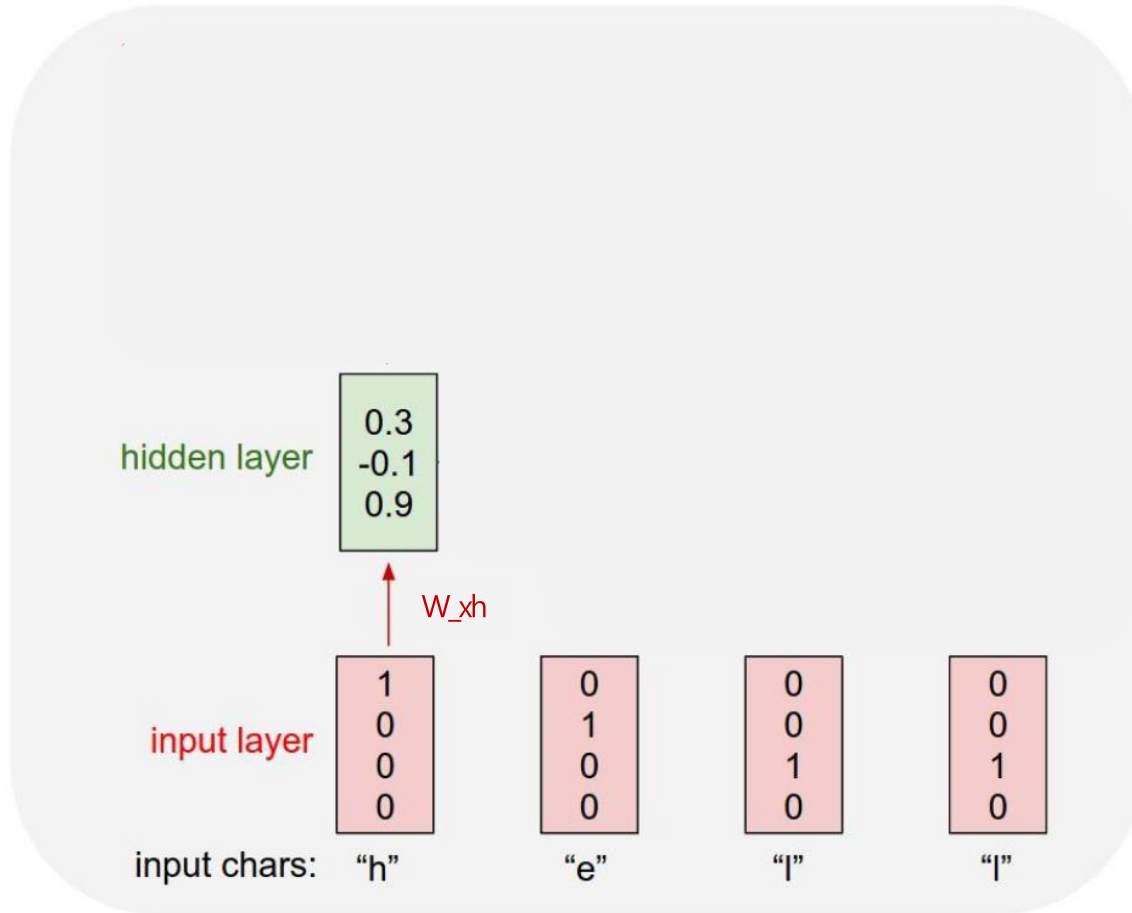
순환 신경망 모델링

❖ Many to Many RNN for Text modeling



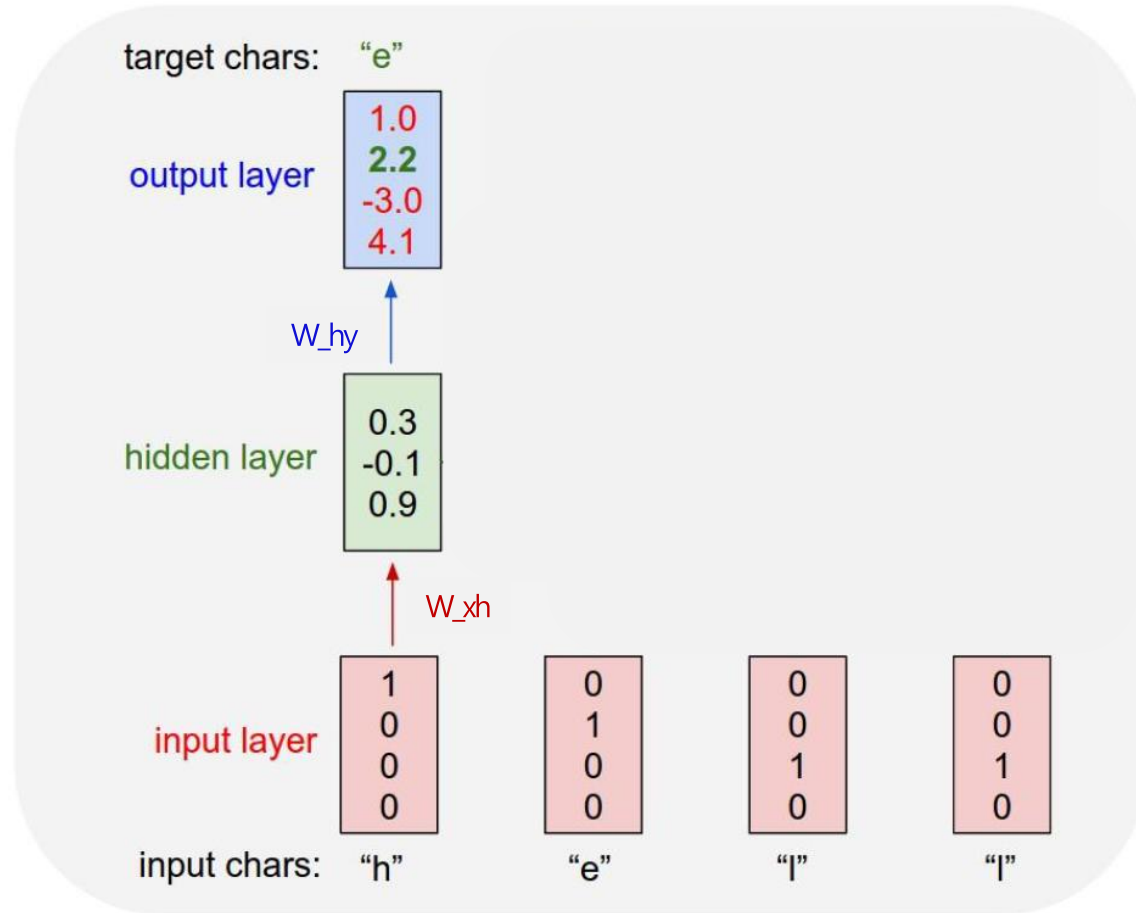
순환 신경망 모델링

❖ Many to Many RNN for Text modeling



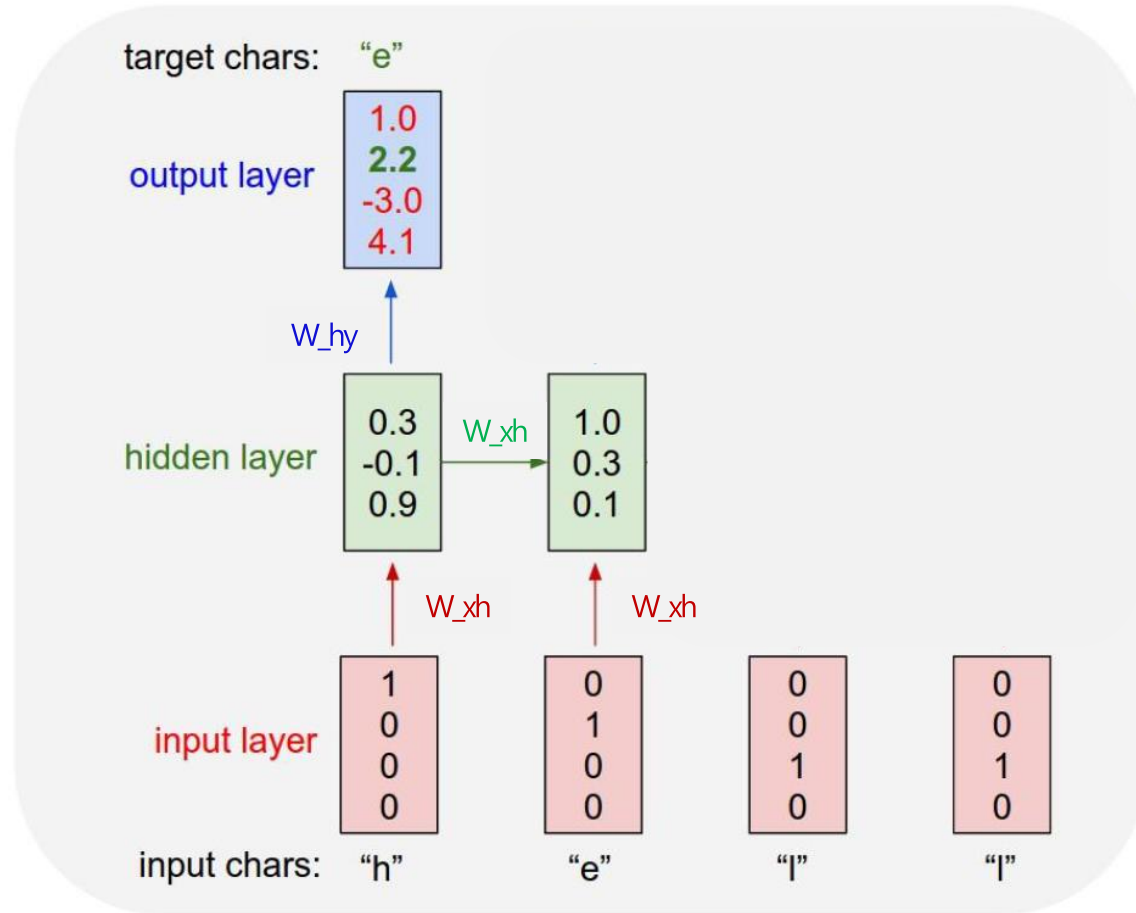
순환 신경망 모델링

❖ Many to Many RNN for Text modeling



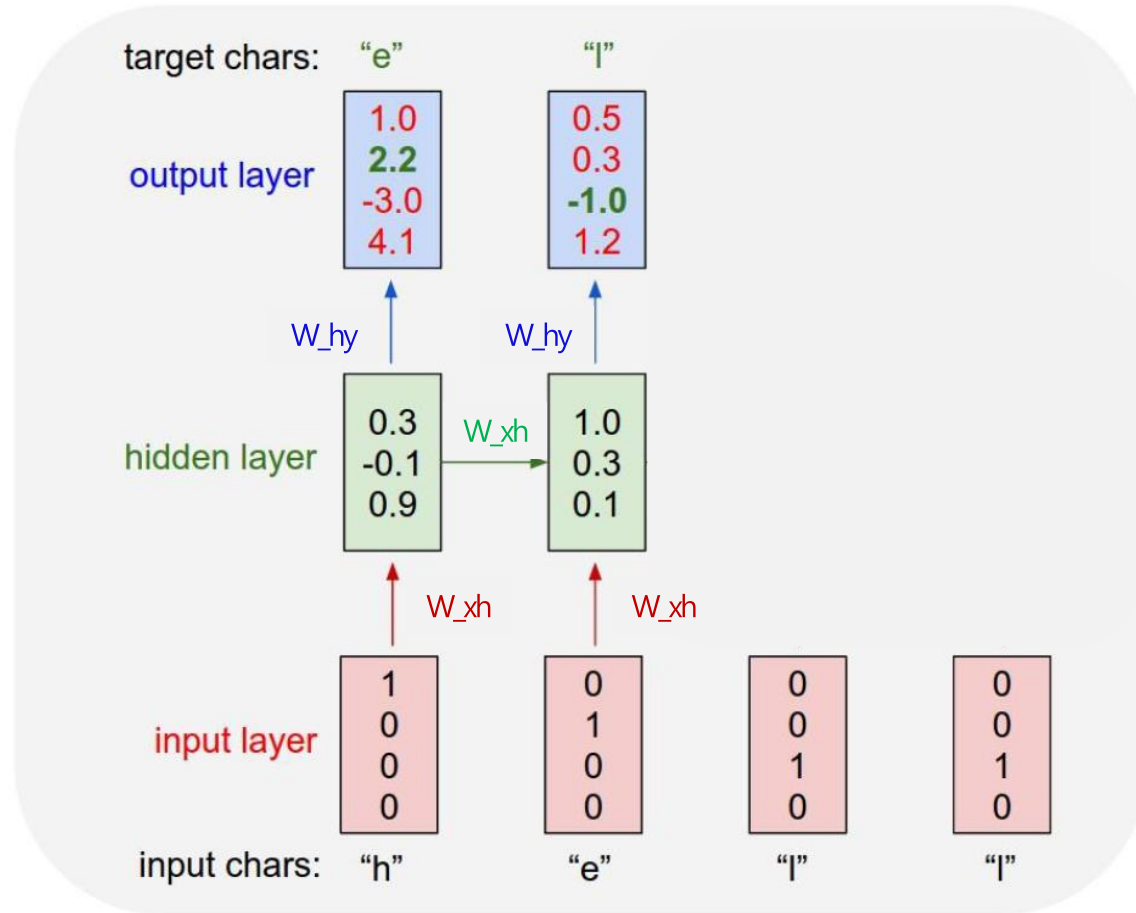
순환 신경망 모델링

❖ Many to Many RNN for Text modeling



순환 신경망 모델링

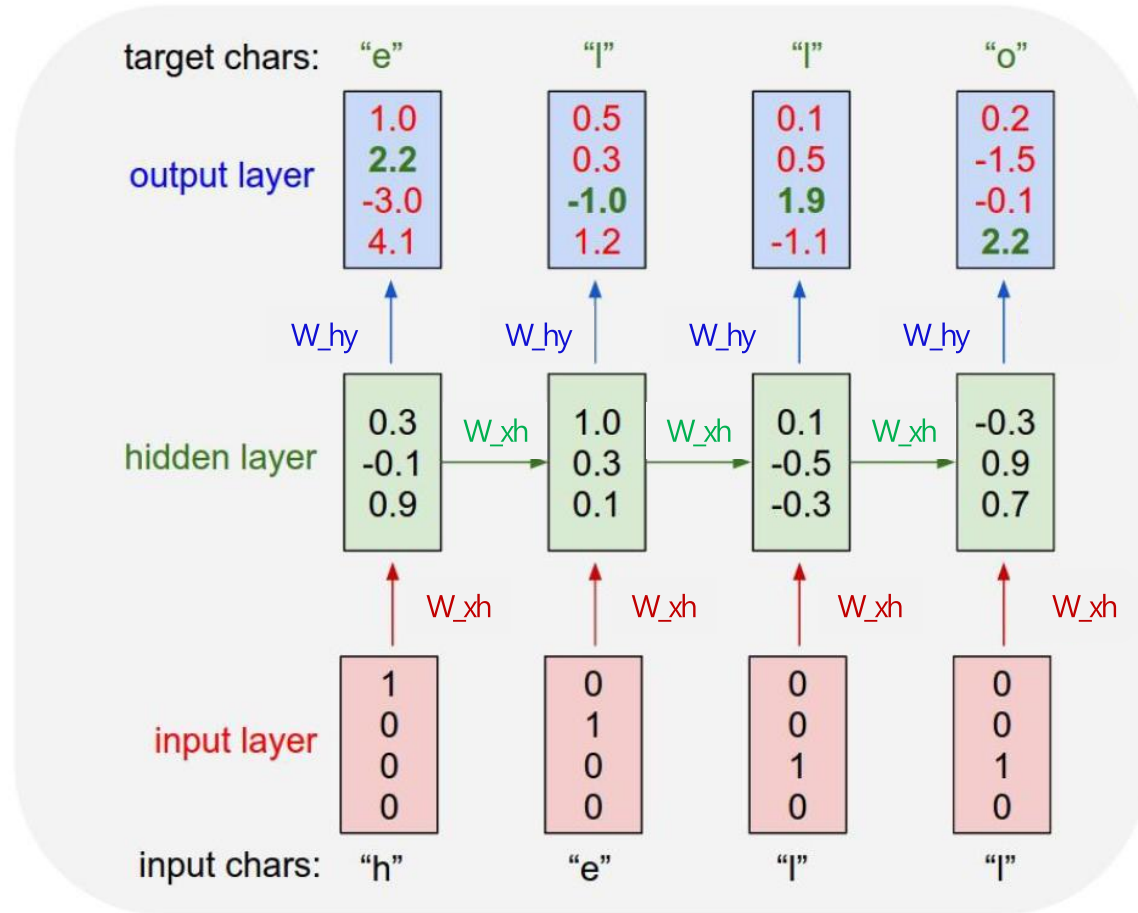
❖ Many to Many RNN for Text modeling



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순환 신경망 모델링

❖ Many to Many RNN for Text modeling



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목차

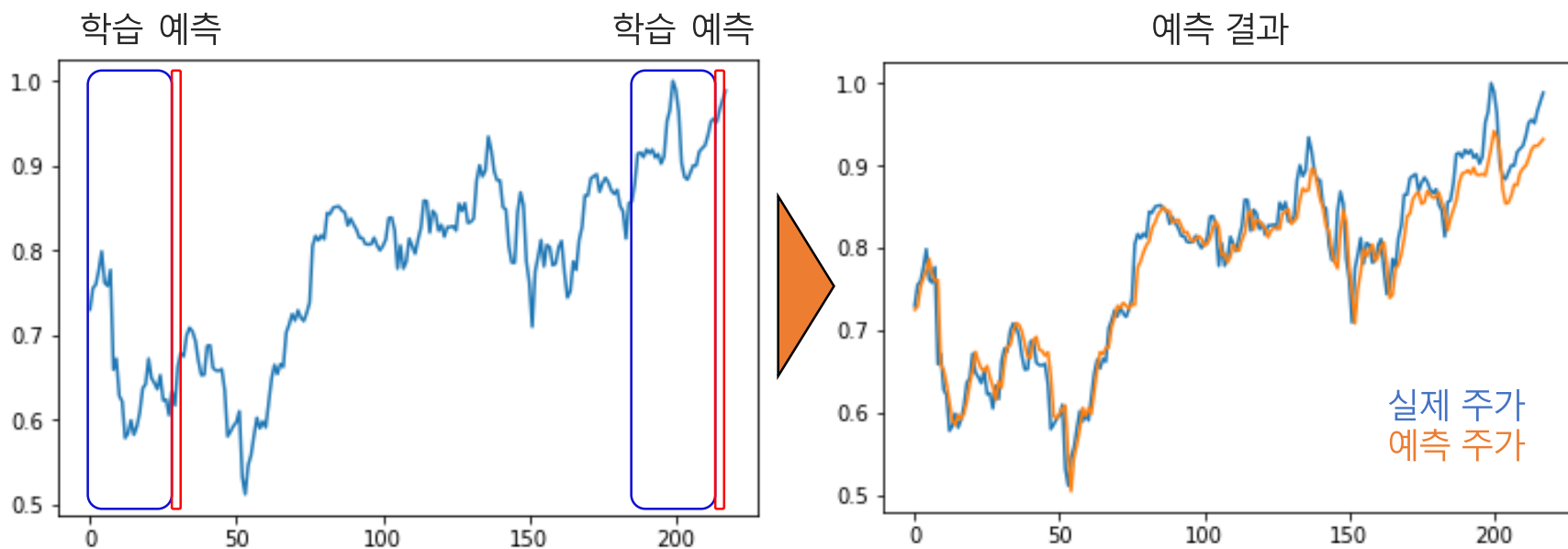
- ❖ 순환 신경망 개요
- ❖ 순환 신경망 학습(Backpropagation Trough Time)
- ❖ 순환 신경망 모델링
- ❖ 순환 신경망 한계

순환 신경망 모델링

❖ Many to Many RNN for Time series data modeling: Univariate

- 설명 변수 (y_{t-10}, \dots, y_{t-1}) : 주가 (이전 시점)
- 반응 변수 (y_t) : 주가 건수 (현재 or 예측 시점)
- 하이퍼파라미터(hyperparameter): 주기 (time length) = 10

주가 예측

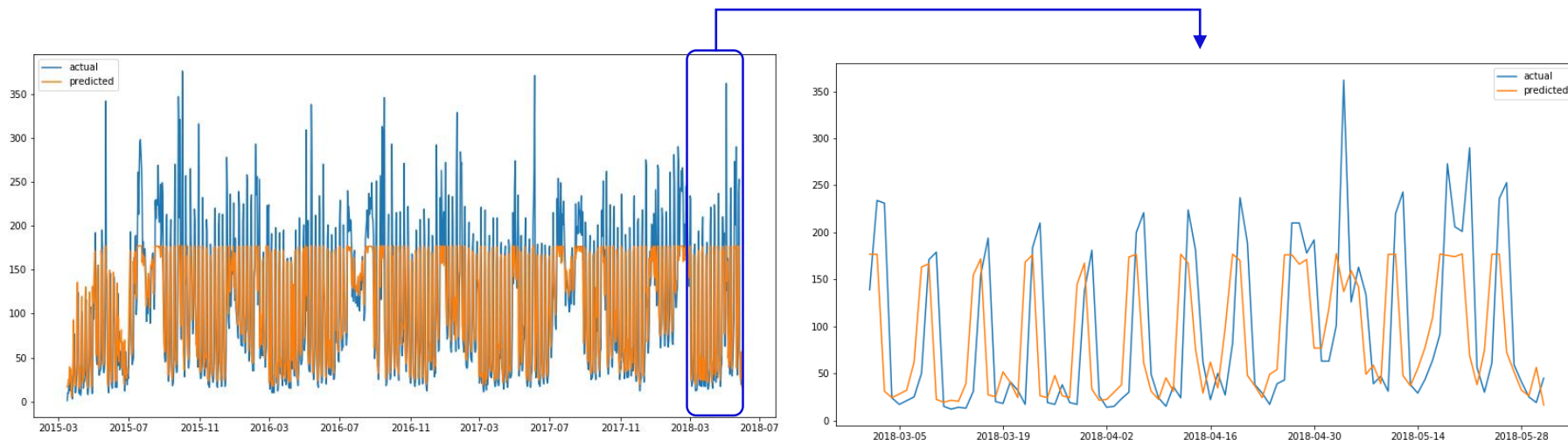


순환 신경망 모델링

❖ Many to Many RNN for Time series data modeling: Univariate

- 설명 변수 (y_{t-10}, \dots, y_{t-1}) : 리조트 취소 건수 (이전 시점)
- 반응 변수 (y_t) : 리조트 취소 건수 (현재 or 예측 시점)
- 하이퍼파라미터(hyperparameter): 주기 (time length) = 10

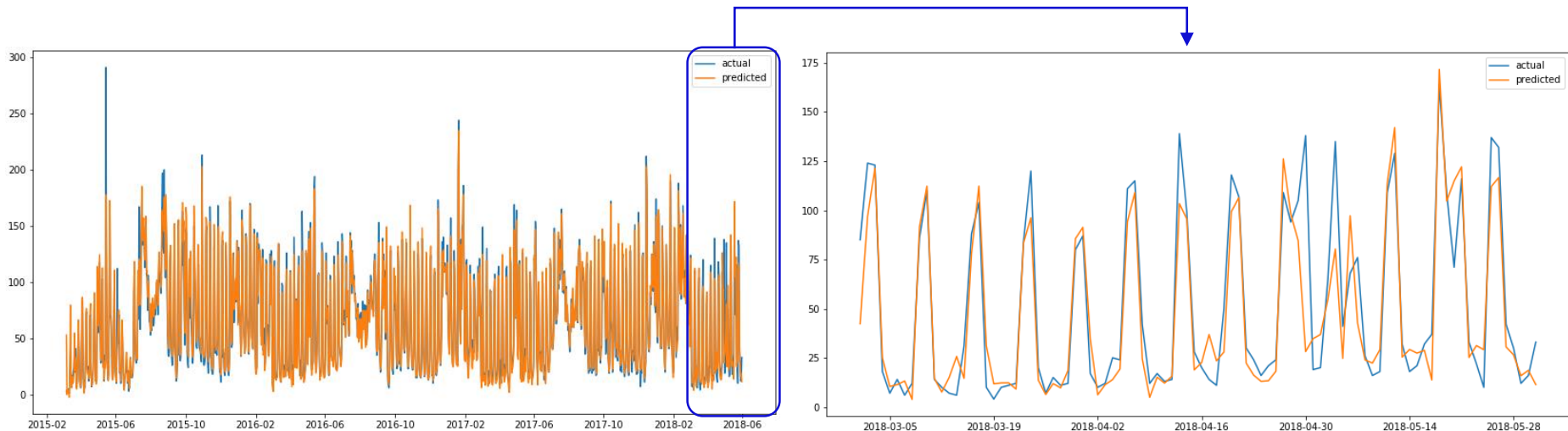
한화 리조트 객실 취소 건수 예측(단변량)



순환 신경망 모델링

- ❖ Many to Many RNN for Time series data modeling: Multivariate
 - 설명 변수 ($x_{1,t}, \dots, x_{i,t}$): 예약자 정보, 객실 정보(평수, 방 개수 등) 등
 - 반응 변수 (y_t): 리조트 취소 건수

한화 리조트 객실 취소 건수 예측(다변량)

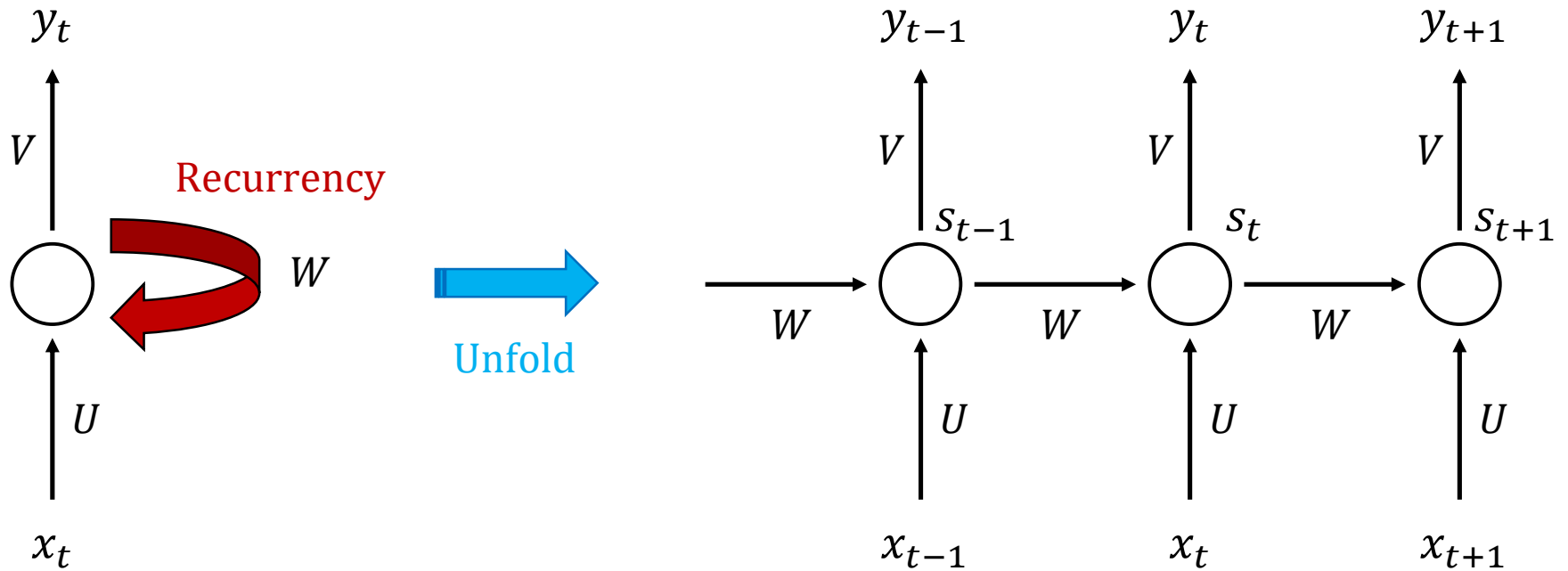


목차

- ❖ 순환 신경망 개요
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- ❖ 순환 신경망 한계

순환 신경망 한계

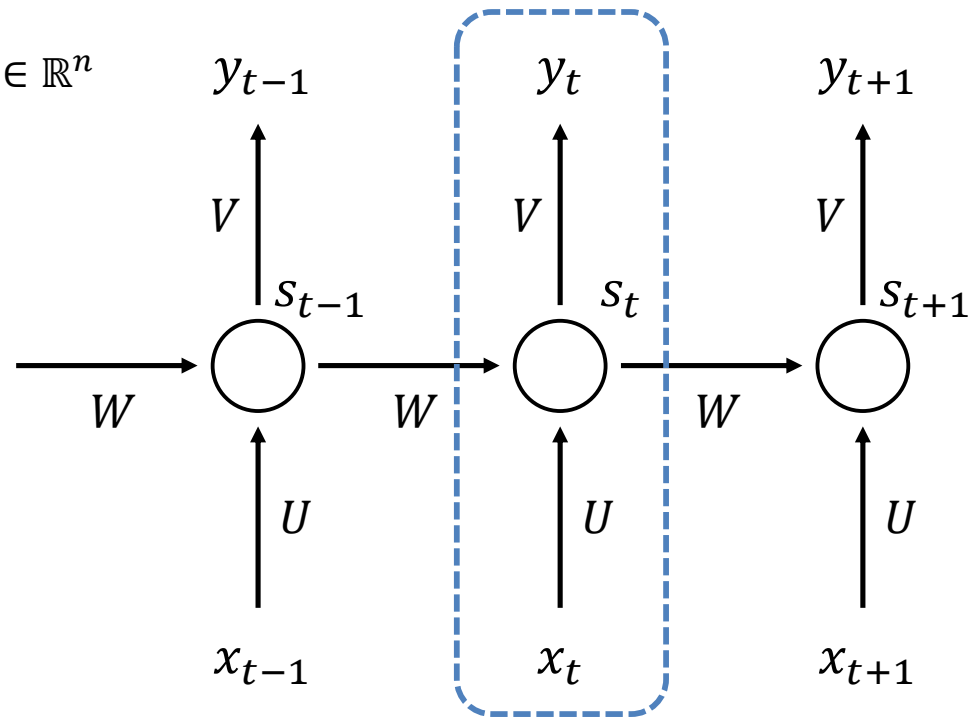
❖ RNN 용어



순환 신경망 한계

❖ RNN 용어: 약어 표시 예시

- x_t : input at time step $t \in \mathbb{R}^m$
- s_t : hidden state at time step $t \in \mathbb{R}^n$
- y_t : output at time step $t \in \mathbb{R}^l$
- $U \in \mathbb{R}^{n \times m}$
- $V \in \mathbb{R}^{l \times n}$
- $W \in \mathbb{R}^{n \times n}$
- $s_t = \tanh(Ux_t + Ws_{t-1})$
- $y_t = \text{softmax}(Vs_t)$
- $L(y, \hat{y}) = \sum_t L_t(y_t, \hat{y}_t) = -\sum_t y_t \ln \hat{y}_t$



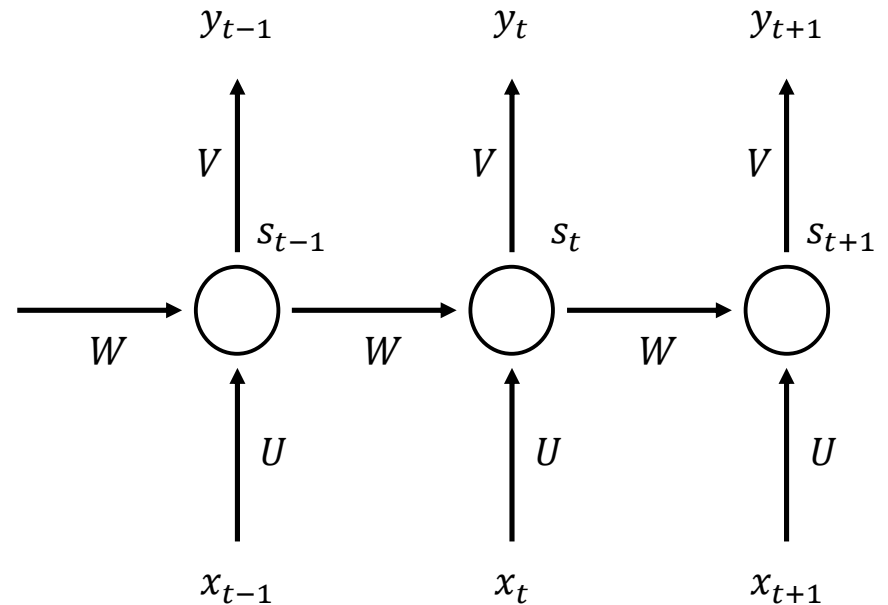
순환 신경망 한계

❖ RNN 용어: 약어 표시 예시

$$1) \frac{\partial L_t}{\partial V} = \frac{\partial L_t}{\partial \hat{y}_t} \times \frac{\partial \hat{y}_t}{\partial V s_t} \times \frac{\partial V s_t}{\partial V}$$

$$2) \frac{\partial L_t}{\partial W} = \sum_{k=0}^t \left(\frac{\partial L}{\partial \hat{y}_t} \times \frac{\partial \hat{y}_t}{\partial s_t} \times \frac{\partial s_t}{\partial s_k} \times \frac{\partial s_k}{\partial W} \right)$$

$$3) \frac{\partial L_t}{\partial U} = \sum_{k=0}^t \left(\frac{\partial L}{\partial \hat{y}_t} \times \frac{\partial \hat{y}_t}{\partial s_t} \times \frac{\partial s_t}{\partial s_k} \times \frac{\partial s_k}{\partial U} \right)$$

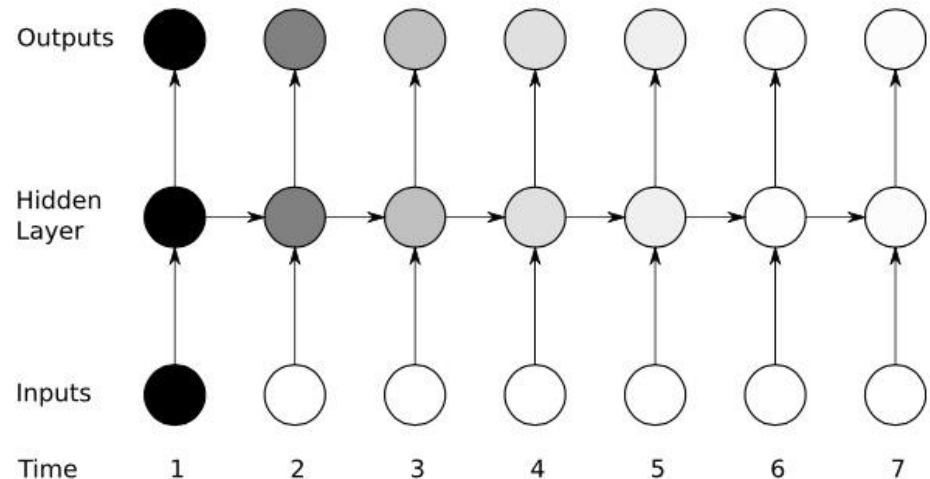
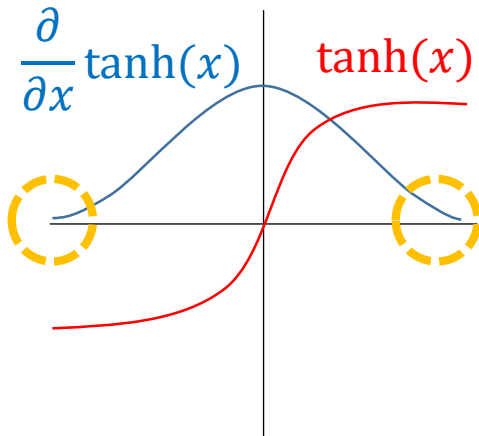


순환 신경망 한계

- ❖ 길이가 긴 sequence 의 경우 Gradient Vanishing / Exploding 문제 발생
 - Vanishing gradient: 다른 모델 사용 → (LSTM, GRU 등)
 - Exploding gradient: clip gradient

$$\frac{\partial \mathcal{E}_3}{\partial \hat{y}_3} \frac{\partial \hat{y}_3}{\partial s_3} \left(\frac{\partial s_3}{\partial W} + \frac{\partial s_3}{\partial s_2} \frac{\partial s_2}{\partial W} + \frac{\partial s_3}{\partial s_2} \frac{\partial s_2}{\partial s_1} \frac{\partial s_1}{\partial W} + \frac{\partial s_3}{\partial s_2} \frac{\partial s_2}{\partial s_1} \frac{\partial s_1}{\partial s_0} \frac{\partial s_0}{\partial W} \right)$$

Long-Term Dependency problem



EOD