



Fully automated inductive invariants inference for Solidity smart contracts

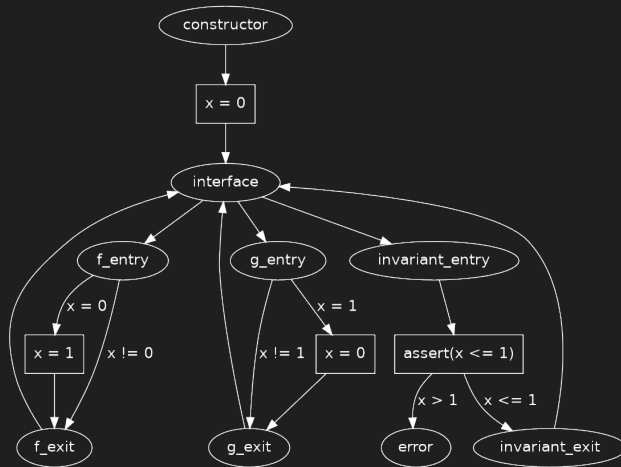
Leonardo Alt

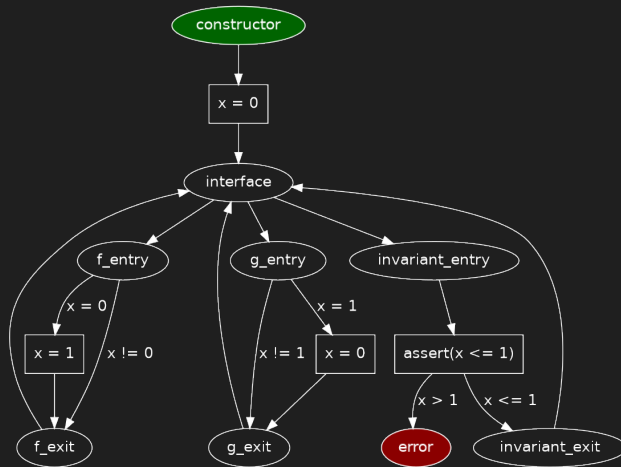
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Demo

$x \leq 2$ is Inductive!

$x \leq 2 \wedge \text{local behavior} \implies x \leq 2$

Inductive invariants

can summarize a relevant piece of code without relying on prior information

Inductive invariants

are particularly useful to summarize the behavior of loops

Demo

Loop invariants

```
y = 0;  
while (y < x)  
    ++x;  
assert(x == y);
```

🎨 $y \leq x$ is the core property of the the loop

🎨 After the loop, its condition is false: $y \geq x$

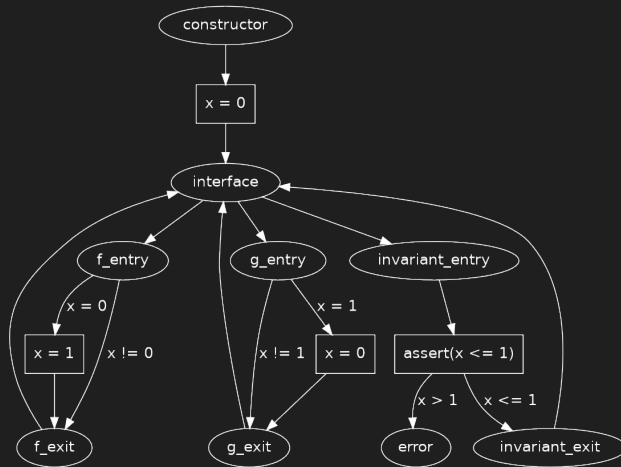
🎨 Which leads to $y \leq x \wedge y \geq x \implies y = x$.

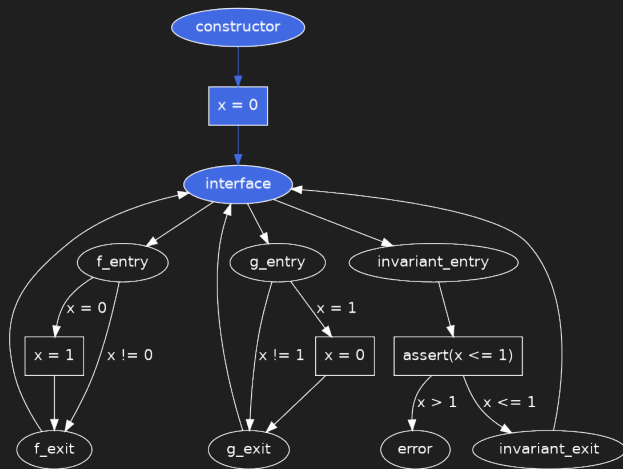
Inductive invariants

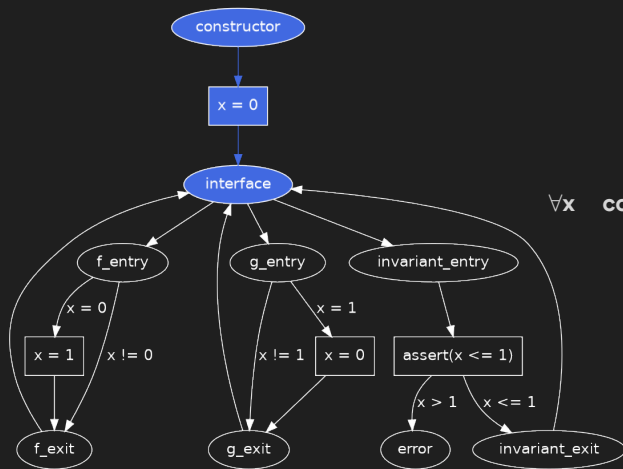
can also be applied to recursive programs, as the inductive hypothesis to be proven.

How can we use inductive invariants for smart contract verification?

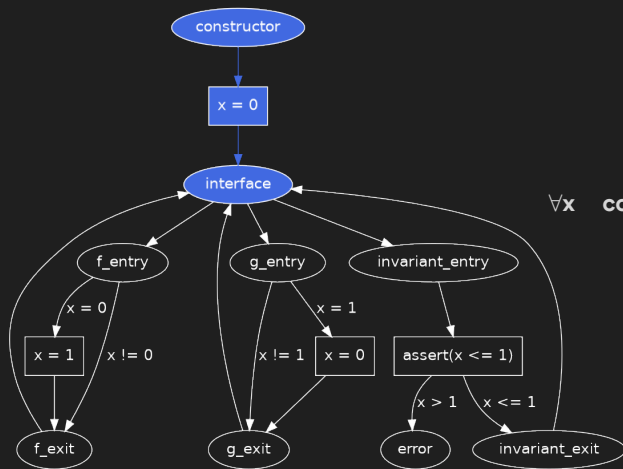
The lifecycle of a smart contract can also be seen as a control-flow containing a loop



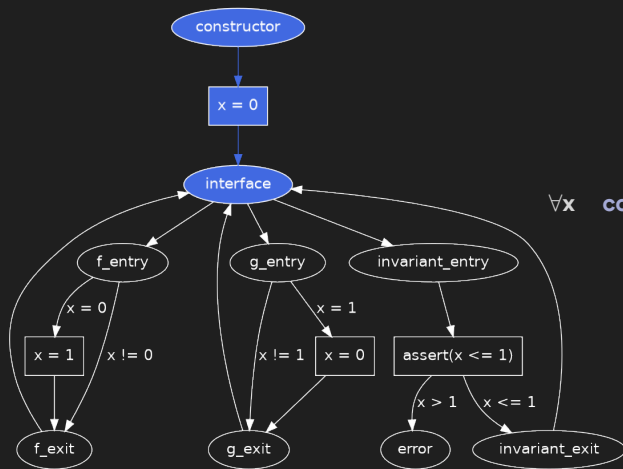




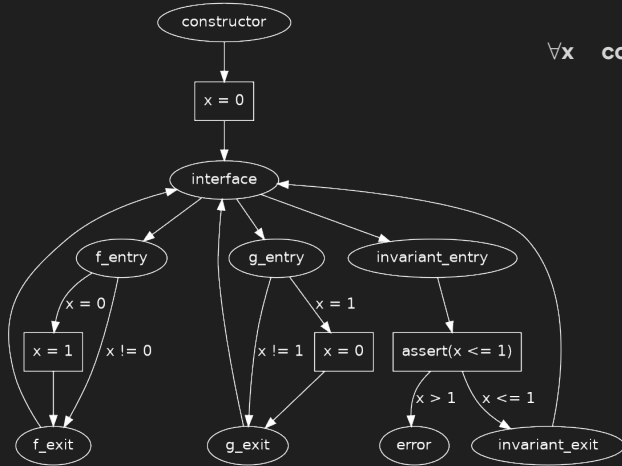
$$\forall x \quad \text{constructor}(x) \wedge x = 0 \implies \text{interface}(x)$$



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$$\forall x \text{ constructor}(x)$$

$$\forall x \text{ constructor}(x) \wedge x = 0 \implies \text{interface}(x)$$

$$\forall x \text{ interface}(x) \implies f(x)$$

$$\forall x \text{ interface}(x) \implies g(x)$$

$$\forall x \text{ interface}(x) \implies \text{invariant}(x)$$

$$\forall x f_{\text{entry}}(x) \wedge x = 0 \implies f_{\text{body}}(x)$$

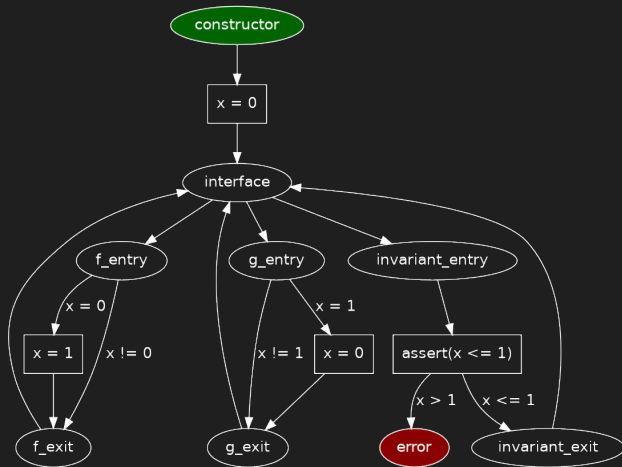
$$\forall x f_{\text{body}}(x) \wedge x' = 1 \implies f_{\text{exit}}(x')$$

$$\forall x f_{\text{entry}}(x) \wedge x = 1 \implies f_{\text{exit}}(x)$$

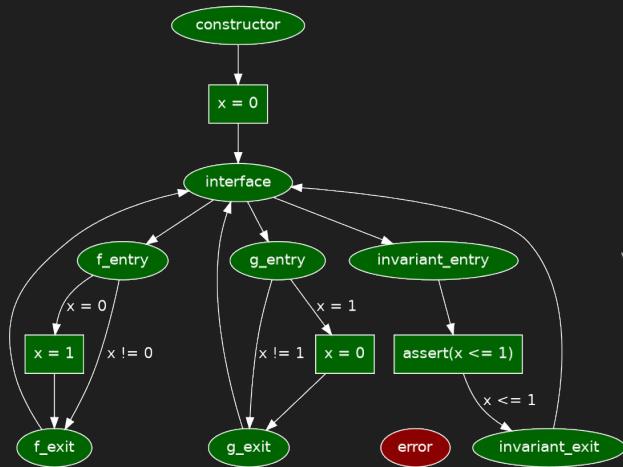
$$\forall x f_{\text{exit}}(x) \implies \text{interface}(x)$$

$$\forall x \text{ invariant}(x) \wedge x > 1 \implies \text{error}(x)$$

$$\forall x \text{ invariant}(x) \wedge x \leq 1 \implies \text{interface}(x)$$



error(x)?



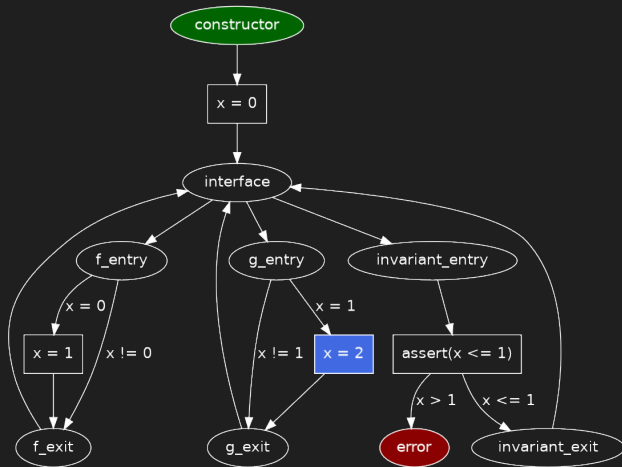
$\forall x. \text{error}(x)$ is unreachable

🎨 Existential positive Least Fixed-Point logic (E+LFP) matches Hoare logic

Blass, A., Gurevich, Y.: Existential fixed-point logic. In: Computation Theory and Logic, In Memory of Dieter Rödding. pp. 20-36 (1987)

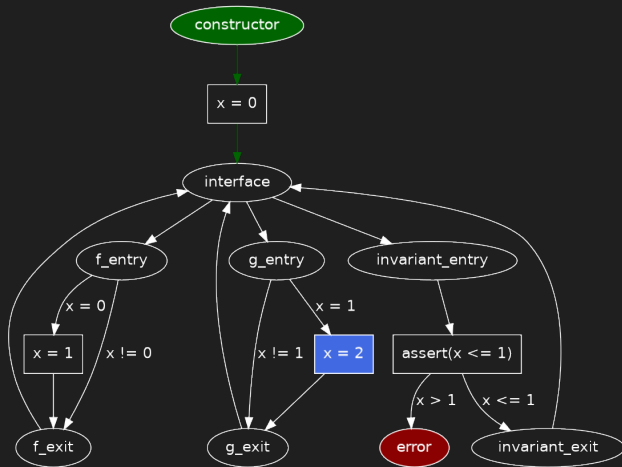
🎨 E+LFP solved by CHCs satisfiability

Bjørner, N., Gurfinkel, A., McMillan, K.L., Rybalchenko, A.: Horn clause solvers for program verification. In: Fields of Logic and Computation II. pp. 24-51 (2015)

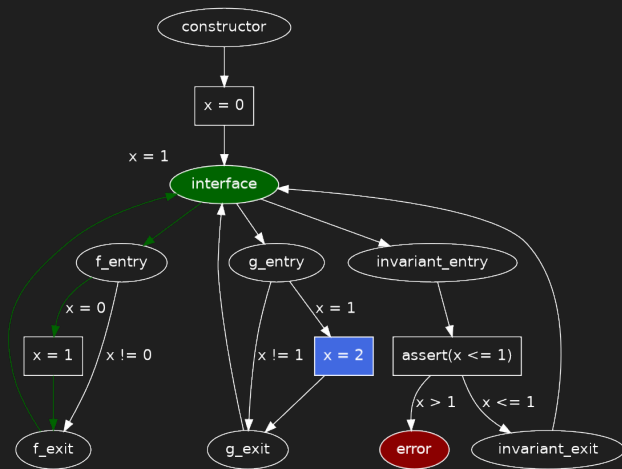


error(x)?

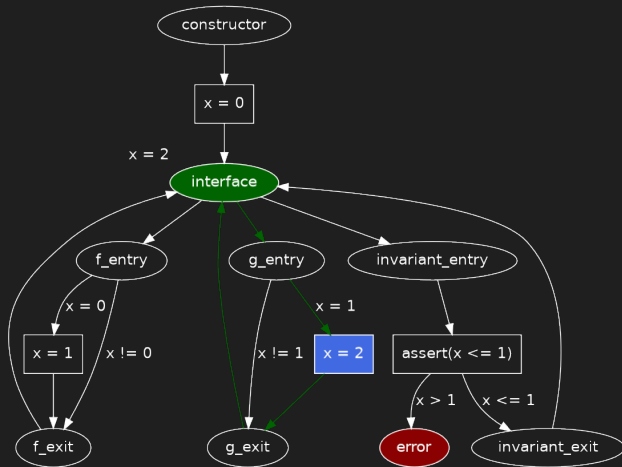
Demo



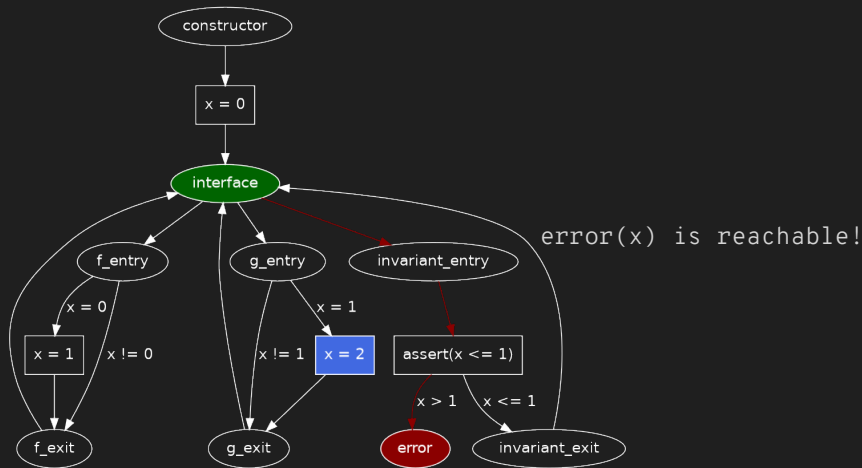
error(x)?



error(x)?







error(x)?







error(x) is reachable!

The sequence that leads to the error is
deployment, f(), g(), invariant().

Horn solvers

-  Predicate abstraction
-  Abstract interpretation
-  Maximal inductive subsets
-  Machine learning

Horn solvers

-  SMT-based unbounded model checking – PDR/IC3
-  Spacer – spacer.bitbucket.io
-  Backwards reachability
-  Quantifier-free SMT queries and interpolation to find predecessors and new lemmas

What's next

- Function calls!
 - Function summaries
 - No changes in the state of the caller contract
 - Synthesis of external functions
 - Multi-contract-unbounded-transactions properties
 - Maybe entire state?
- Nice looking counterexamples and invariants
- Better usability
- Simple formal spec language –
github.com/ethereum/smart-contract-spec-lang

Final remarks

- 🎨 SMT solvers are powerful and fast (hopefully as powerful as we sell them)
- 🎨 Unbounded model checking with PDR
- 🎨 Unbounded transaction properties and counterexamples
- 🎨 Embedded in the Solidity compiler
- 🎨 Contract inductive invariants can further help verification of bytecode (added lemmas)

Thank you!