

Surrogate-enabled inference

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1 Setup

Consider a model $Z(\mathbf{x}, t, \lambda)$ that produces discretized output for a given QoI (in this case, GPP only is considered) Z over a period of time $t \in \Omega_t$ and over space $\mathbf{x} = (x, y) \in \Omega_x$ (typically a rectangular region)*, for a given parameter vector $\lambda \in \mathbb{R}^d$.

- Raw data: ensemble of daily simulations is available, i.e. $\{Z(\mathbf{x}_i, t_j, \lambda_n)\}$ for $i = 1, \dots, I$, $j = 1, \dots, J$ and $n = 1, \dots, N$, where $I = 61 \times 41$, $J = N_y \times 365$ and $N = 2000$. Number of years is set to $N_y = 24$.
- Monthly averages are taken first, so, with some abuse of notation, let us set $J = N_y \times 12$.
- The actual QoI to be analyzed is the month-by-month average over all years, i.e., for $j = 1, \dots, 12$

$$\bar{Z}_j(\mathbf{x}, \lambda) = \frac{1}{N_y} \sum_{k=0}^{N_y-1} Z(\mathbf{x}, t_{j+12k}, \lambda) \quad (1)$$

- We have several sites available, and for the $S = 8$ sites that are in the region Ω_x , we identify the closest \mathbf{x}_i , see Figure 1. Therefore, the QoIs for which we build surrogates are

$$Q_{ij}(\lambda) = \bar{Z}_j(\mathbf{x}_i, \lambda), \text{ for } i = 1, \dots, S \text{ and } j = 1, \dots, 12 \quad (2)$$

2 Surrogates

A total of $12S = 96$ surrogates are build, using BCS and second order Legendre-basis. A subset of inputs lead to 0 GPP - we ignored those inputs (in fact we ignored all below 0.02) for surrogate construction. The surrogates have shown relative errors between 5% – 15%, as demonstrated in two example plots in Figure 2.

The sensitivities for the eight sites over 12 months are shown in Figure 3 (minus the winter months with zero GPP for all ensemble members.).

3 Inference

*where x is longitude, y is latitude.

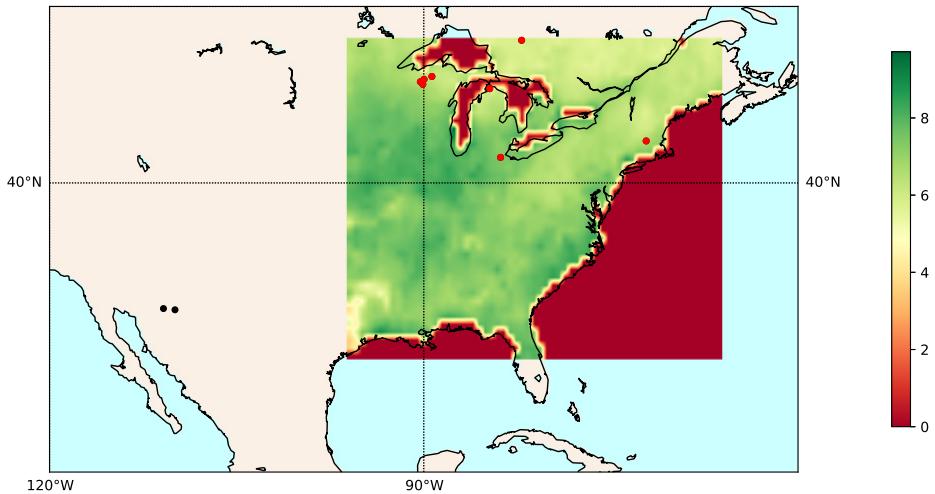


Figure 1: The 8 sites that lie in the region where we have model evaluations. The average GPP field for a month of June (?) is shown.

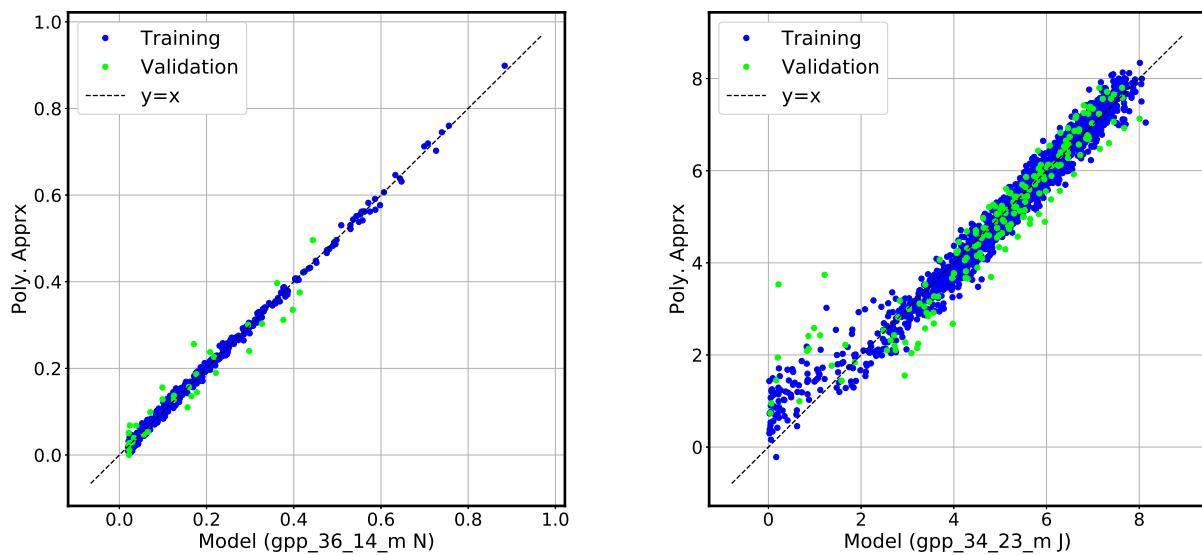


Figure 2: Two representative surrogates.

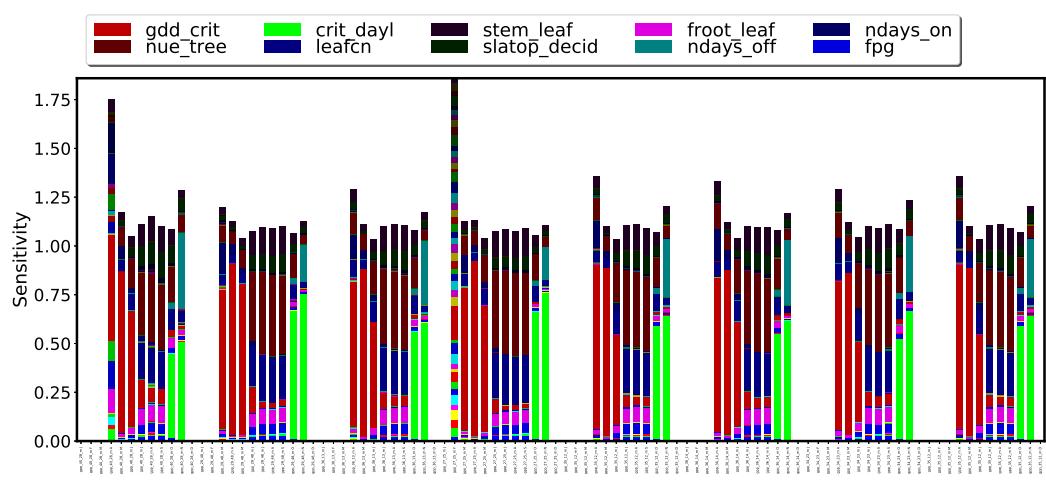


Figure 3: Sensitivities of GPP for 8 sites (the winter sites are not shown due to dominantly zero-ed GPP).

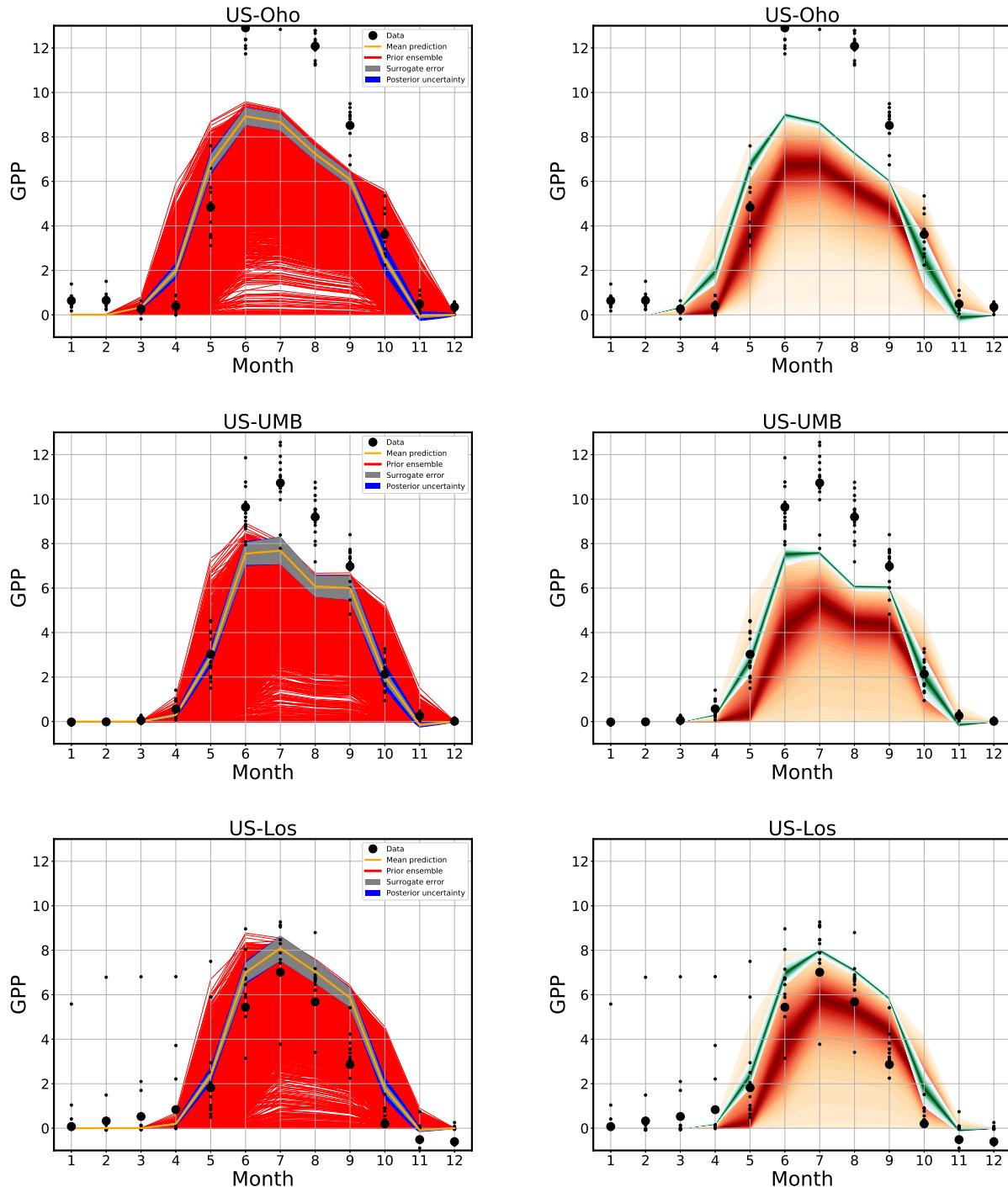


Figure 4: Inference1.

