

Let  $f: \mathbb{R}^n \to \mathbb{C}$  be a continuous function. Then the support of f, denoted supp f, is the closure of the set on which  $f(x) \neq 0$ . That is,

$$\operatorname{supp} f = \overline{\{x \in \mathbb{R}^n \mid f(x) \neq 0\}}.$$

 $C^k(\Omega)$  is the set of k-times differentiable functions on  $\Omega$ . Functions in  $C^k(\Omega)$  for every k > 0 are said to be in  $C^{\infty}(\Omega)$ , that is, infinitely differentiable functions.  $C_C^{\infty}(\Omega)$  is the set of infinitely differentiable functions on  $\Omega$  which have support bounded and contained in  $\Omega$  (compact when  $\Omega = \mathbb{R}^n$ ). That is,

$$C^{k}(\Omega) = \left\{ f : \Omega \to B \mid \frac{\partial^{i} f}{\partial x^{i}} \text{ for } i = 0, \dots, k \in C(\Omega) \right\}$$

$$C^{\infty}(\Omega) = \{ f : \Omega \to B \mid f \in C^k(\Omega) \text{ for } k \in \mathbb{N} \}$$

$$C_C^\infty(\Omega) = \{f \in C^\infty(\Omega) \mid \operatorname{supp}\,(f) \text{ is compact}\}$$

Let  $\Omega \subset \mathbb{R}^n$  be an open set and let  $K \subset \Omega$  be compact. Then there exists a nonnegative function  $\psi \in C_C^{\infty}$  with  $\psi(x) = 1$  for  $x \in K$ .

Define $\sigma$ -algebra
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(i)	E be a collection of subsets of Ω. Then Σ is called a $\sigma$ -algebra if If $A \in \Sigma$ , then $A^C \in \Sigma$ ;	
(ii)	If $A_1, A_2, \ldots$ is a countable family of sets in $\Sigma$ , then $\bigcup_{n=1}^{\infty} A_i \in \Sigma$ ;	
(iii) and $\Omega \in \Sigma$ . n English,		
		(i)
(ii)	$\Sigma$ is closed under countable unions;	
(iii)	and $\Sigma$ contains the entire set $\Omega$ .	