

1. Order the following list of functions by their big-Oh notation. Simplify the function notation using basic rules for logarithms and exponents in order to make their relative complexity evident.

$6n \log n$

2^{100}

$\log \log n$

$\log^2 n$

$2^{\log n}$

2^{2n}

$5n$

$n^{0.01}$

$\frac{1}{n}$

2^n

$3n^{0.5}$

$4^{\log n}$

$n^2 \log n$

$\sqrt{\log n}$

$n \log_4 n$

4^n

Function	Simplified function	
		Slowest growing
		Fastest growing

2. Suppose we perform a sequence of operations on a queue data structure. After every n operations we make a copy of the entire queue for debugging purposes. Show that the cost of n operations (including the copy) is $O(n)$ using the accounting method.

3. Suppose we have implemented a k -bit counter with a k -element binary array. The counter is initially 0. The only available operation is `increment(A)` which adds 1 to the current number.

- What is the worst-case running time of `increment`?
- What is the worst-case complexity for a sequence of k -`increment`?
- Use the potential method to find a better estimate.

4. Suppose we have 20 singleton sets, numbered 0 through 19, and we call the operation $\text{union}(\text{find}(i), \text{find}(i+5))$, for $i = 0, 1, 2, \dots, 14$. Draw a picture of the tree-based representation of the sets that result, assuming we don't implement the union-by-size and path compression techniques.

5. Repeat exercise (4) assuming that we now implement both techniques