

Lens Examples for Locks and Constraints

Sums

This section is motivated by the following example. We are given sales data for a number of stores in a company, with each store identified by its state. The regional managers of the company can view the sum of their own region's sales data and change that number, indicating a wish to increase future sales. If the manager wishes to change the sales figures from n to N , each store's figures will be multiplied by $\frac{N}{n}$ to make the change. Similarly, the CEO can see the total sum of national sales and adjust that number accordingly.

However, the sales data for an individual store or region may be fixed or *locked*, meaning that its sales data may not be changed.

Flat Sums

We start with a lens which takes a single list of numbers to its sum. The default case, assuming no locks on the elements of the list, distributes $n - \sum_{i=1}^m x_i$ among the list in proportion to each x_i .

Input	Output	
$200 \rightarrow [10, 20, 30, 40], \text{FFFF}$	$[20, 40, 60, 80]$	(1)

In the presence of locks on $\{x_j \mid j \in J\}$, we produce a list which is the result of fixing the locked entries and distributing $n - \sum_{i=1}^m x_i$ values among the $m - |J|$ locked elements of the list.

$200 \rightarrow [10, 20, 30, 40], \text{TFFF}$	$[10, 42.2, 63.3, 84.4]$	(2)
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To keep the first element of the list locked, we must scale the other elements by a factor of $\frac{19}{9}$.

If the constraints do not allow the elements of the list to be mutated to satisfy the sum, there are two possibilities of output. The first option is to fail if the list cannot be mutated in-place.

$200 \rightarrow [10, 20, 30, 40], \text{TTTT}$	fail	(3)
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The second option is to add elements to the list so that the sum holds.

$200 \rightarrow [10, 20, 30, 40], \text{TTTT}$	$[10, 20, 30, 40, 100]$	(4)
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In what context would this notion of sum be appropriate?

Split Sum

Next we consider the lens which maps an ordered pair to a labeled list, with each element of the list labeled as either L(left) or R(right). The left-labeled elements of the list should sum up to the left element of the ordered pair, and vice versa.

The default case with no locks behaves like an extension of the sum lens above.

$(50, 50) \rightarrow [\text{L}10, \text{L}20, \text{R}30, \text{R}40], \text{FFFF}$	$[\text{L}16.67, \text{L}33.33, \text{R}21.43, \text{R}28.57]$	(5)
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Similarly, with the case for locks...

$$(50, 50) \rightarrow [L10, L20, R30, R40], \text{TFFT} \quad [L10, L40, R10, R40] \quad (6)$$

If locks prevent us from mutating either section of the list to fit the constraint, we default to the options presented for plain sums in this situation.

$$(50, 70) \rightarrow [L10, L20, R30, R40], \text{TTF} \quad \text{fail} \quad (7)$$

$$(50, 70) \rightarrow [L10, L20, R30, R40], \text{TTF} \quad [L10, L20, L20, R30, R40] \quad (8)$$

Multi-Level Lenses

We can represent the full sales example described in the beginning of this section as a lens with multiple levels. From the CEO's point of view, this lens stretches between the total sales data and a labelled list of store sales data.

When neither intermediary region is completely locked, a change from n to N first scales up the intermediary regions by a factor of N/n . The changes to each individual region must be accounted for, even if some of its sub-elements are locked.

$$200 \rightarrow (30, 70), [L10, L20, R30, R40], \text{TFFF} \quad (60, 140), [L10, L50, R60, R80] \quad (9)$$

When an entire region is locked however, we must propagate the locks up to the regional level.

$$200 \rightarrow (30, 70), [L10, L20, R30, R40], \text{TTF} \quad (30, 170), [L10, L20, R72.9, R97.1] \quad (10)$$

Cumulative Average

A student is given some number of grades in a class, and she wants to know what grades she needs to get in the future to obtain a desired average. The constraints on this problem may go beyond locking to illuminate different environments.

Given that all grades fall within a certain range, how many assignments must the student complete to raise her average?

$$95 \rightarrow [80, 100], \{\text{lists like } [80, 100, x_0, x_1, x_2, \dots] \text{ where } 0 \leq x_i \leq 100\} \quad [80, 100, 100, 100] \quad (11)$$

The constraint might limit the number of future assignments.

$$95 \rightarrow [80, 100], \{\text{lists like } [80, 100, x_0, \dots, x_{n-1}] \text{ where } 0 \leq x_i \leq 100 \text{ and } n \leq 1\} \quad \text{fail} \quad (12)$$

Partition

Constraints on the partition lens can be stated in a very general form, and might be able to guide the lens's alignment/update policy. Let A , B and C be the following lists:

A		B	C
L	Bach	Bach	Asimov
R	Asimov	Beethoven	Austin
L	Beethoven		

For example, we can use the constraint to model the structure of the merge.

$$B, C \rightarrow A, \{\text{lists with authors first}\} \quad \begin{array}{l} \text{R} \quad \text{Asimov} \\ \text{R} \quad \text{Austin} \\ \text{L} \quad \text{Bach} \\ \text{L} \quad \text{Beethoven} \end{array} \quad (13)$$

$$B, C \rightarrow A, \{\text{lists like } A++Z \text{ where elements in } Z \text{ do not appear in } A\}$$

L	Bach
R	Asimov
L	Beethoven
R	Austin

(14)