6.009 Quiz 2: Practice Quiz A

Fall 2021

Name:
Kerberos/Athena Username:

5 questions

1 hour and 50 minutes

- Please WAIT until we tell you to begin.
- This quiz is closed-book, but you may use two 8.5×11 sheets of paper (both sides) as a reference.
- You may **NOT** use any electronic devices (including computers, calculators, phones, etc.).
- If you have questions, please **come to us at the front** to ask them.
- Enter all answers in the boxes provided. Work on other pages with QR codes may be taken into account when assigning partial credit. **Please do not write on the QR codes.**
- If you finish the exam more than 10 minutes before the end time, please quietly bring your exam to us at the front of the room. If you finish within 10 minutes of the end time, please remain seated so as not to disturb those who are still finishing their quizzes.
- You may not discuss the details of the quiz with anyone other than course staff until final quiz grades have been assigned and released.

1 Generators

Consider the following three generators:

```
def numbers():
    i = 1
    while True:
        yield i
        i += 1
def squared(gen):
    for x in gen:
        yield x ** 2
def first(gen, count):
    for ix, x in enumerate(gen):
        yield x
        if ix >= count:
            return
and the following three functions:
def run_generator_1(gen):
    for x in gen:
        print(x)
        if x > 10:
            pass
def run_generator_2(gen):
    for x in gen:
        print(x)
        if x > 10:
            break
def run_generator_3(gen):
    for x in gen:
        print(x)
        if x > 10:
            continue
```

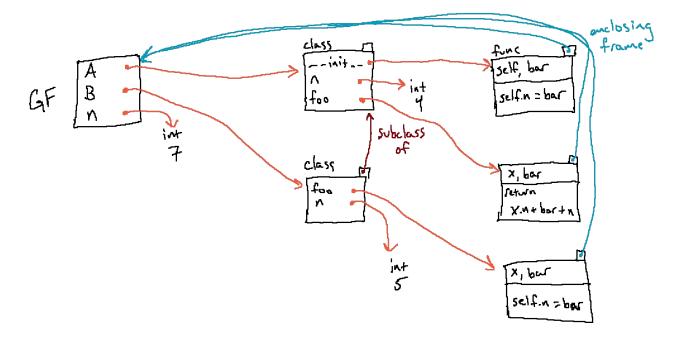
For each function call on the facing page, indicate how many numbers will ultimately be printed to the screen. Write ∞ if the function call never terminates, and write ERROR if the program function call raises an exception.

<pre>run_generator_1(numbers)</pre>	How many nu	mbers?		
<pre>run_generator_2(numbers)</pre>	How many nu	mbers?		
<pre>run_generator_3(numbers)</pre>	How many nu	mbers?		
<pre>run_generator_1(numbers())</pre>	How many	numbers?		
<pre>run_generator_2(numbers())</pre>	How many	numbers?		
<pre>run_generator_3(numbers())</pre>	How many	numbers?		
<pre>run_generator_1(squared(numbers</pre>	s())) H	How many r	numbers?	
run_generator_2(squared(numbers	s())) H	Iow many r	numbers?	
<pre>run_generator_3(squared(numbers</pre>	s())) H	How many r	numbers?	
<pre>run_generator_1(first(numbers()</pre>	, 8))	How many	numbers?	
<pre>run_generator_2(first(numbers()</pre>	, 8))	How many	numbers?	
<pre>run_generator_3(first(numbers()</pre>	, 8))	How many	numbers?	

2 Environment Diagrams

Part a.

The following environment diagram represents the state of a program after executing some code:



Consider evaluating the expressions on the facing page, one after another, after running the code that led to the diagram above. In each box, write the result of evaluating the expression that preceded it. If an expression would result in an infinite loop, write INFINITE LOOP. If it would result in an error, write ERROR.

Note that the three angle brackets on each line represent the Python prompt, and the expressions to be evaluated are shown after the prompt.

>>> b = B(9)	
>>> B.n	
>>> b.n	
>>> b.foo(10)	
>>> B.foo(b, 10)	
>>> A.foo(b, 3)	

Part b.

Consider the following piece of code:

```
01 |
       class Counter:
02 |
           id = 0
03 |
           def get_id(self):
               self.id += 1
04 |
05 |
               return self.id
06 |
07 |
       class Counter2(Counter):
           def get_id(self):
08
               self.id += 2
09 |
               return self.id
10 |
11 |
       if __name__ == "__main__":
12 |
13 |
           c2 = Counter2()
           print(c2.get_id())
14 |
15 |
           Counter2.id += 2
```

In the box on the facing page, draw the environment diagram corresponding to the state of this program after line 15 has executed.

Additionally, in the boxes below, write the value that will be printed by each of these print statements, starting after having run the code above. If an expression would result in an infinite loop, write INFINITE LOOP instead. If it would result in an error, write ERROR.

```
print(Counter().get_id())

print(Counter2().get_id())

print(c2.get_id())
```

Environment Diagram:	

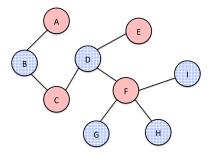
3 Graph Coloring

In this problem, we will consider the goal of "coloring" nodes in a graph with two colors, such that each node receives a color of either "red" or "blue", subject to the constraint that no two nodes that are directly connected have the same color.

In this problem, we will represent a graph as a dictionary, mapping each node label to a list of the labels of the nodes that are directly connected to it. Your goal is to check whether the graph can be colored using two colors subject to the constraint mentioned above.

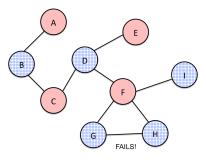
If the graph *cannot* be colored in this way, your function should return an empty dictionary {}. If the graph *can* be colored in this way, your function should return a dictionary mapping each node label to either the string "red" or the string "blue", representing a valid coloring.

Examples of function invocation and return are given below:



```
alternating_colors({'A': ['B'], 'B': ['A', 'C'], 'C': ['B', 'D'], 'D': ['C', 'E', 'F'], 'E': ['D'], 'F': ['D', 'G', 'H', 'I'], 'G': ['F'], 'H': ['F'], 'I': ['F']}, 'A')
```

could return {'A': 'red', 'B': 'blue', 'C': 'red', 'D': 'blue', 'E': 'red', 'F': 'red', 'G': 'blue', 'H': 'blue', 'I': 'blue'} or a different valid coloring with 'red' and 'blue' interchanged.



```
alternating_colors({'A': ['B'], 'B': ['A', 'C'], 'C': ['B', 'D'], 'D': ['C', 'E', 'F'],

'E': ['D'], 'F': ['D', 'G', 'H', 'I'], 'G': ['F', 'H'],

'H': ['F', 'G'], 'I': ['F']}, 'A')
```

should return an empty dictionary since there is no valid coloring.

The facing page contains a partial definition of a function designed to solve this problem. Fill in the blanks to complete the function so that it works as described above.

def	<pre>alternating_colors(graph, start): coloring = {}</pre>
	<pre># color in nodes (by mutating the coloring dictionary) # return True if the coloring is OK, False otherwise def color_node(node, color): # base case if we're trying to color a node that has already been colored in (what # should we return here?) if node in coloring:</pre>
	<pre># color the node (mutating the dictionary from above) coloring[node] = color other_color = 'blue' if color == 'red' else 'red'</pre>
	<pre># recursively try neighbors for neighbor in graph[node]:</pre>
	# back outside the loop, what should we do/return (if anything)?
	# call the helper function and return the appropriate # result

return coloring if color_node(start,'red') else {}

4 Expressions Puzzle

In this problem, we will explore an interesting kind of arithmetic puzzle.

Given a number target number T and a single-digit number n, we want to form a mathematical expression containing only the number n that evaluates to T. For example, with T=7 and n=4, one such expression is ((((4+4)+4)/4)+4)=7. In particular, we want to find a minimal expression of this form (i.e., the one that contains the fewest instances of n).

We will consider the function $find_expression(T, n, limit=None)$ on the second-to-last page of this handout, which was written to solve this problem (you may remove that page). $find_expression$ takes integers representing T and n as inputs, as well as a third optional argument limit; if limit is specified, the code should not consider expressions that contain more than limit number of operations.

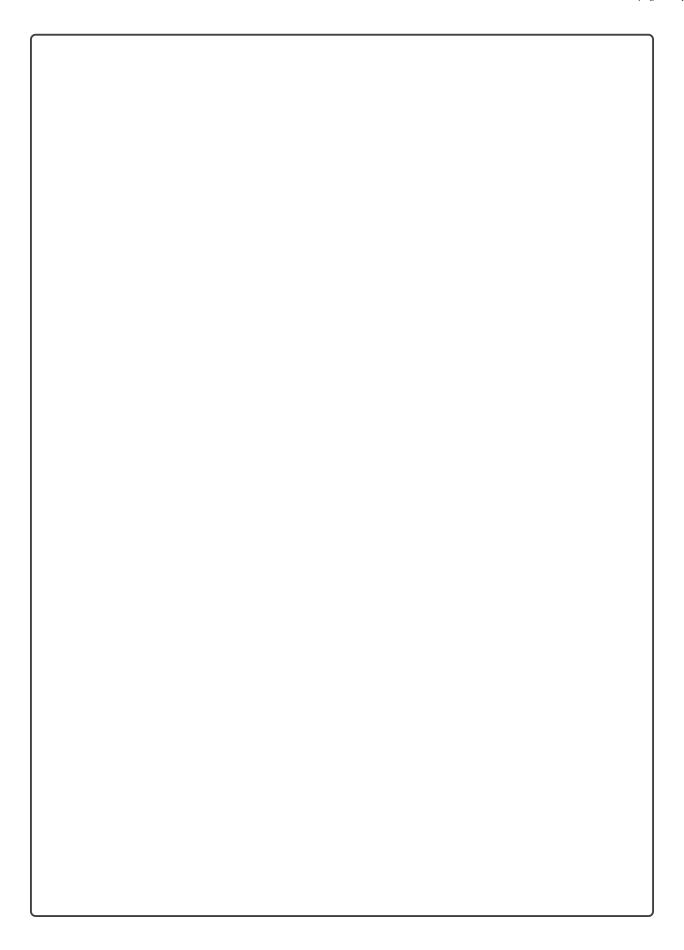
Ultimately, the goal is to return the answer as a tuple of symbols, where each symbol is either '*', '/', '%', '+', or '-'. This tuple represents a sequence of operations that should be performed left-to-right. For example, the tuple ('*', '-', '/', '+') represents the expression $((((n \times n) - n)/n) + n)$. Note that in this setup, the empty tuple represents n.

If there are no possible answers, we want to return None.

Here are some examples of the desired behavior (not necessarily the code that the given implementation produces):

```
>>> find_expression(7, 4, 10)
('+', '+', '/', '+')
>>> find_expression(7, 4, 4)
('+', '+', '/', '+')
>>> find_expression(7, 4, 3) is None
True
>>> find_expression(102, 9, 10)
('*', '+', '+', '*', '+', '+', '+', '/')
>>> find_expression(102, 9, 5) is None
True
>>> find_expression(3, 3, 5)
()
>>> find_expression(1, 20, 5)
(''/',)
>>> find_expression(300, 20, 10)
('*', '-', '-', '-', '-')
```

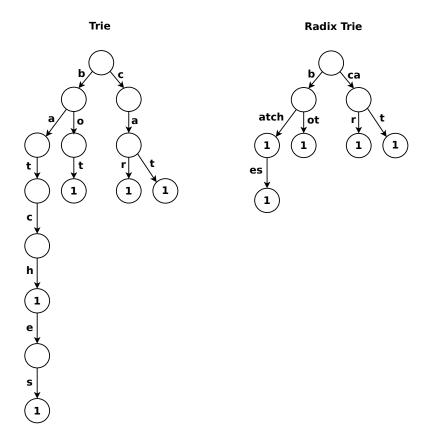
The given implementation of find_expression contains a number of deficiencies. There may be issues with correctness, efficiency, and/or style. On the facing page, briefly describe any issues you find with the given implementation, as well as how to fix them (if appropriate).



5 Radix Tries

A *radix trie* is a variant of the trie data structure we explored in lab 6. In a radix trie, each node that has no value and has only one child is merged with that child. One effect of this is that the edge labels (the keys in the children dictionary) are no longer necessarily of length 1; another effect is that it is often possible to make a radix trie with many fewer nodes than the original trie.

For example, consider the following example trie, and a radix trie containing the same keys ('car', 'cat', 'bot', 'batch', and 'batches'):



Note that we have provided a complete implementation of Trie on the last page of this quiz (which you may remove). We have also provided a placeholder for a class called RadixTrie (which inherits from Trie) to represent radix tries. You should not modify either class.

In the box on the facing page, write a function called <code>compress_trie(trie)</code>. This function should take an instance of the <code>Trie</code> class as its input, and it should return an instance of the <code>RadixTrie</code> class, representing the corresponding radix trie (where nodes have been merged as described above).

Your function should not modify the structure that was passed in, but rather should make an entirely new instance of RadixTrie. All nodes internal to the structure should also be RadixTrie instances.

Your function only needs to handle keys that are strings. (Unlike the lab implementation, you do not need to handle tuples as valid keys.)

<pre>class RadixTrie(Trie): pass</pre>	
<pre>def compress_trie(trie):</pre>	

Code for find_expression

```
01 |
       operations = {
02 |
           '+': lambda x, y: x+y,
           '-': lambda x, y: x-y,
03 |
04 |
           '/': lambda x, y: x//y,
           '*': lambda x, y: x*y,
05 |
06 |
           '%': lambda x, y: x%y,
07 |
       }
08 |
09 |
       def evaluate(expr, num):
           out = num
10 |
11 |
           for op in expr:
12 |
               out = operations[op](out, num)
13 |
           return out
14 |
15 |
16 |
       def find_expression(target, num, limit=None):
17 |
           to_do = [()]
           while to_do:
18 |
               expr = to_do.pop(0)
19 |
20 |
               val = evaluate(expr, num)
21 |
               if val == target:
22 |
                   return expr
23 |
               for op in operations:
24 |
                   to_do.append(expr + (op,))
```

Code For Tries

```
class Trie:
   def __init__(self, key_type):
        self.key_type = key_type
        self.children = {}
        self.value = None
   def _get_node(self, key, make_new=False):
        if not isinstance(key, self.key_type):
            raise TypeError
        if not key:
            return self
        if key[:1] not in self.children:
            if not make_new:
                raise KeyError
            self.children[key[:1]] = Trie(self.key_type)
        return self.children[key[:1]]._get_node(key[1:], make_new)
   def __setitem__(self, key, value):
        self._get_node(key, make_new=True).value = value
   def __getitem__(self, key):
        out = self._get_node(key).value
        if out is not None:
            return out
       raise KeyError
   def __delitem__(self, key):
       node = self._get_node(key)
        if node.value is None:
            raise KeyError
       node.value = None
   def __contains__(self, key):
        try:
            return bool(self[key] or True)
        except:
            return False
   def __iter__(self):
        if self.value:
            yield (self.key_type(), self.value)
        for child, ctree in self.children.items():
            yield from ((child + key, val) for key, val in ctree)
```