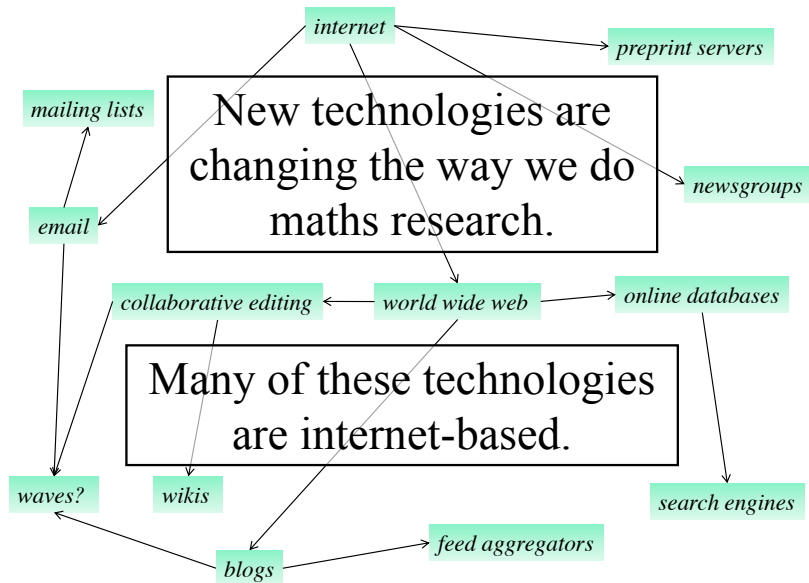




David Zureick-Brown  
Emory Univeristy

Slides available at <http://www.mathcs.emory.edu/~dzb/slides/>

# Introduction



# Introduction



1947



1969

Maple™

1980

MATLAB



1984

L<sup>A</sup>T<sub>E</sub>X 1983

Mathematica™ 1988

MAGMA 1993  
COMPUTER ALGEBRA



1989



1995



sage

2005

sci.math

1987

sci.math.research

1991



1999

arXiv.org

1991



1995



1999

PlanetMath.org

2000



2001

WIKIPEDIA  
The Free Encyclopedia

MOVABLE TYPE 4 2001  
Publishing Platform

WordPress 2003

Google 2004  
Book Search BETA

AMERICAN MATHEMATICAL SOCIETY  
MathSciNet

1995

Google 2004  
Scholar BETA

Tricki 2009  
polymath 2009

# Mathematical collective consciousness

“I assume everybody has dreams about organizing and sharing everything they ever think of, or of how great it would be if everybody in your field shared a big brain like the borg”

– Anton Geraschenko

# Massively collaborative mathematics – Polymath

11. One can start with any point (since every point of  $S$  should be pivot infinitely often), the direction of line that one starts with however matters!



👍 8 🚫 0 ⓘ Rate This

*Comment by Anonymous — July 19, 2011 @ 8:19 pm | Reply*

In other words, we can start with any point and 'just' need to choose a second point through which will we draw a line.



👍 0 🚫 0 ⓘ Rate This

*Comment by Nemanja — July 19, 2011 @ 8:28 pm | Reply*

Perhaps even the line does not matter! Is it possible to prove that any point and any line will do?



👍 0 🚫 1 ⓘ Rate This

*Comment by Anonymous — July 19, 2011 @ 8:31 pm | Reply*

No, if you start with two points on the convex hull (ordered in the right way) you stay on the convex hull.



👍 2 🚫 0 ⓘ Rate This

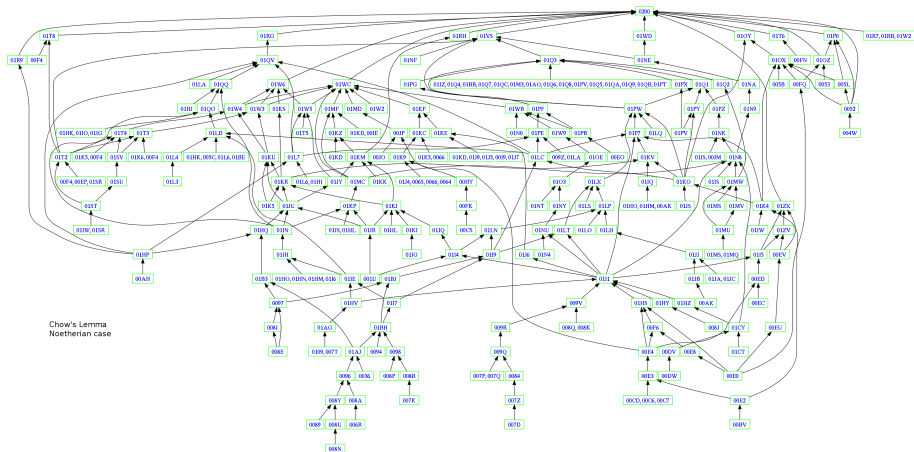
*Comment by Thomas H — July 19, 2011 @ 8:35 pm | Reply*

It is not possible, two consecutive points on convex hull will not do.



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# Stacks Project




# Motivation: math on the internet « getting buried!

Learn and relearn your field « What's new

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terrytao.wordpress.com/career-advice/learn-and-relearn-yo



## What's new

Updates on my research and expository papers, discussion of open problems, and other maths-related topics. By Terence Tao

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## Learn and relearn your field

Even fairly good students, when they have obtained the solution of the problem and written down nearly the argument, shut their books and look for something else. Doing so, they miss an important and instructive phase of the work. ... A good teacher should understand and impress on his students the view that no problem whatever is completely exhausted. One of the first and foremost duties of the teacher is not to give his students the impression that mathematical problems have little connection with each other, and no connection at all with anything else. We have a natural opportunity to investigate the connections of a problem when looking back at its solution. (George Pólya, "How to Solve It")

Learning never really stops in this business, even in your chosen specialty; for instance I am still learning surprising things about basic harmonic analysis, more than ten years after writing my thesis in the topic.

Just because you know a statement and proof of Fundamental Lemma X, you shouldn't take that lemma for granted; instead, you should dig deeper until you really understand what the lemma is all about:

- Can you find alternate proofs?
- If you know two proofs of the lemma, do you know to what extent the proofs are equivalent? Do they generalise in different ways? What theorems do the proofs have in common? What are the other relative strengths and weaknesses of the two proofs?
- Do you know why each of the hypotheses are necessary?
- What kind of generalizations are known/conjectured/heuristic?
- Are there weaker and simpler versions which can suffice for some applications?
- What are some model examples demonstrating that lemma in action?
- When is it a good idea to use the lemma, and when isn't it?
- What kind of problems can it solve, and what kind of problems are beyond its ability to assist with?
- Are there analogues of that lemma in other areas of mathematics?

Learn and relearn your field « What's new

Learn and relearn your field « W...

terrytao.wordpress.com/career-advice/learn-and-relearn-yo

## 33 comments

Comments feed for this article

7 March, 2008 at 10:06 am  
[...] Learn and relearn the field: learning the strength and weakness of tools, learning what else is going on in mathematics; learning how to solve problems rigorously.

7 March, 2008 at 11:32 am  
[...] NO. In order to make good and useful contributions to mathematics, one does need to work hard, learn one's field well, learn other fields and tools, ask questions, talk to other mathematicians, and think about the [...]

6 September, 2008 at 9:04 pm  
Dear Prof. Tau,  
First of all, I should thank you for your nice and useful hints and advice. Then, I would like to tell you a serious problem I'm facing with and ask you to help, if you don't mind:  
I'm a PhD student and my field is arithmetic algebraic geometry. As you know, the literature in this area is vast. So if I want to learn my field and go through all the details of all results and proofs, then I guess, I can never (i.e., in a reasonable time) work on my own thesis problem and produce anything. But, not learning and reading that way give me the feeling that I'm missing something and I'm not confident anymore.  
I would really appreciate if you could give me some advice. Thank you in advance

7 September, 2008 at 8:48 pm  
Dear Anonymous,  
I hope you won't mind someone else providing you with some advice.

Most workers in arithmetic algebraic geometry (and not just students) suffer from the problem you describe to various degrees. The literature is indeed vast, and to read everything as a student, even everything that you might need in solving your particular thesis problem, is essentially impossible.

I would suggest the following: a good grounding in algebraic geometry is essential. Most students in algebraic geometry, of all flavours, go through the rite of passage known as "Hartshorne": reading Hartshorne's book, especially chapters 2 and 3, and solving vast numbers of exercises. It is more or less impossible, and in any case probably unwise, to avoid doing this. And once you have solved many/most of the Hartshorne problems, you should have some baseline confidence in algebraic geometry, scheme theory, and cohomology.

At the same time, there are other texts that it is good to look at because they emphasize certain functorial aspects of algebraic geometry more than Hartshorne, aspects which are particularly important in arithmetic algebraic geometry – e.g. Mumford's red book. It is advisable to supplement your Hartshorne reading with such books.

Another standard text to read is Cornell-Silverman (and these days, depending on your precise direction of interest, Cornell-Silverman-Stevens – but this is more number-theoretic, while Cornell-Silverman is more geometric). This is not such a long book, and has a lot of information in it. Furthermore, since it is

# Introduction

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# About the site

- Created in October, 2009 (2 Berkeley grad students, 1 postdoc)
- Draws questions and advice from each extreme – Fields medalists and gifted high school students
- (Sanitized) database dumps are publicly available, fun to grep for statistics of site usage

# Fun facts

- **35000** questions, **60000** answers, at least **10000** 'active' users;
- Time before getting an answer:
  - Average: 4.40 hours
  - Median: 1.75,
  - Standard deviation: 5.70
- Time before getting an 'accepted' answer:
  - Average: 5.39 hours
  - Median : 2.61
  - Standard Deviation: 6.16

## How many mathematicians are there?

26

11

Although we are not so numerous as other respected professionals, like for example lawyers, I wonder if we could come up with a reasonable estimate of our population.

Needless to say, the question more or less amounts to the definition of "mathematician".

Since I should like to count only research mathematicians (and not, say, high-school teachers) some criterion of publishing should be applied. But it should not be too strict in order not to exclude Grothendieck, for example, who has not published any mathematics for a long time.

An excuse for asking a question so soft as to verge on the flabby is that it might be considered an exercise in Fermi-type order of magnitude estimation.

soft-question

mod | edit | close | delete | flag | cite

asked Nov 14 2009 at 8:27

community wiki



Georges Elencwajg

24 Time to break out the Drake equation. – [Ryan Budney](#) Nov 14 2009 at 8:35

7 On a related topic: does there exist two mathematicians with the same number of hairs on their heads? – [Douglas S. Stones](#) Mar 4 2010 at 4:53

22 Doug, the answer is yes. I know several completely bald mathematicians. – [Ryan Budney](#) Aug 18 at 19:24

4 wow between 2009 and now MO has changed (matured) a lot!! – [Suvrit](#) Aug 18 at 19:33

tagged

soft-question × 888

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Tip: You can see the source for MathJax output by right clicking it and selecting "View Source". [See more tips and tricks.](#)

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Cures for mathematician's block (as in writer's block)

(Preferably rare) Audio/Video recordings of famous

## 6 Answers

oldest

newest

votes



Current count of [Mathematics Genealogy Project](#) is 137672 (I am assuming that the PhD students that graduated are ranked as "research mathematicians"). But the problem is.. Mathematics Genealogy is mostly for universities of developed countries. There could be some really good university in Russia, China or Korea out there that doesn't give us the correct statistics. Another problem is.. Mathematics Genealogy Project counts even the dead mathematicians (like Hilbert, Hasse, Kepler and so on).. and I am assuming you want a report of living mathematicians.. but hey, I'm quite surprised by the number even 200k is pretty low for the living!

mod | link | edit | delete | flag | cite

answered Nov 14 2009 at 8:45

community wiki



Jose Capco

- 2 The MGP used to be utterly inadequate for those who got their PhDs in the UK before the 1980s, it may have improved now. Also, there are odd gaps/bugs in some of the entries. It's useful and interesting but I'd be wary of using it for head counts – [Yemon Choi](#) Nov 14 2009 at 9:01
- 3 The dead mathematicians are probably neglegable, because of the exponential growth of the mathematics community. – [Martin](#) Mar 8 2011 at 8:03
- 5 I'd be careful using the MGP. I'll give some examples from my family, so I am very sure of the facts - one of my grandfathers, who was a chemist, and never published a math paper in his life, is listed in the MGP twice, as distinct persons - once as a student (his also listed advisor was not a mathematician either) and once as an advisor. My father, who is a physicist, and wrote exactly one paper that could be called math, is listed. So are 13 of his students - probably at most 1 or 2 is reasonably considered a mathematician, even if one regards many theoretical physicists as mathematicians. – [Dan Fox](#) Jul 16 2011 at 9:48

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Mathematicians and writing

Famous mathematicians with background in arts/humanities/law etc

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### How to write math

You can just type LaTeX formulas between dollar signs! There are some occasional strange behaviors: see the [FAQ](#) and this [meta.MO thread](#) for details. **Basic solution:** if you're having problems with the preview (or the post looks wrong), put backticks around any math that contains underscores or asterisks. E.g. write `$f_n=g_{n+1}$`.



In [an article](#) written a few years ago, Jean-Pierre Bourguignon estimates that there are around 80 000 mathematicians worldwide, with the AMS having about 45 000 members.

## About the site – features

- **Badges** - mostly exist to reward exploring the site and figuring out how to do everything;
- **Reputation** - gain more ability to use site;
- Big boon – the community is **self moderating**;
- **Wiki effect** – edit others' answers;

Things you get to do with **a little** reputation:

- **Up-voting**
- **Down-voting**
- Ability to **leave comments**

Things you get to do with a **lot of** reputation

- **“Moderator”** privileges

(e.g., **“vote to close”** a bad question)

- **retag** questions
- **edit posts**
- **edit answers**

Easy to **cut through the clutter**:

- **Tags**
- **Watched**
- **Avoided**
- **RSS** (for questions, users, tags, etc.)



# Introduction

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## About the site - quote from Anton

“One thing that I like to point out in conversation about MO is that putting a question or answer out there without posing it towards some specific person often leads to meaningful interactions with awesome people. Some people start collaborations based on MO questions, but even if you don't, you get to know a lot of people pretty well, which feels great. Also, there is something about interacting with famous people on MO that humanizes my internal representation of them.”

– Anton Geraschenko

# Typical questions

- Specific mathematical questions
  - Research oriented
  - Idle (e.g., “Is this theorem still true if I weaken hypothesis  $X'$ ?”)
- Historical questions
- Reference requests
- “What’s the point of...?”
- Career advice
- Crowdsourcing typos
- Gossip (discouraged)

## MO – keeping current

“I started reading mathoverflow a few months ago, and currently for me it is by far the best online way to find out about current events in math research (at least in my area – number theory). It’s just stunning the number of new results and links to key papers I’ve found on mathoverflow.”

– William Stein (Mathematician, creator of SAGE)

# Why successful for pure mathematics?

“Using MathOverflow should be an extension of the way you normally do mathematics, and the same rules you use to effectively solve problems can be used to make good MO questions. Just like solving problems, crafting good questions requires you to put in some effort!”

– “How to ask” page

Thank you!

Thank you!

**For more:**

- ① See [whats-the-story-behind-mathoverflow](#)
- ② [Atlantic article](#) – “Beyond Facebook: How the World’s Mathematicians Organize Online”
- ③ Terry Tao’s talk [mathematical research and the internet](#)