A Review and Meta-Analysis of Multimodal Affect Detection Systems

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Affect detection is an important pattern recognition problem that has inspired researchers from several areas. The field is in need of a systematic review due to the recent influx of Multimodal (MM) affect detection systems that differ in several respects and sometimes yield incompatible results. This article provides such a survey via a quantitative review and meta-analysis of 90 peer-reviewed MM systems. The review indicated that the state of the art mainly consists of person-dependent models (62.2% of systems) that fuse audio and visual (55.6%) information to detect acted (52.2%) expressions of basic emotions and simple dimensions of arousal and valence (64.5%) with feature- (38.9%) and decision-level (35.6%) fusion techniques. However, there were also person-independent systems that considered additional modalities to detect nonbasic emotions and complex dimensions using model-level fusion techniques. The meta-analysis revealed that MM systems were consistently (85% of systems) more accurate than their best unimodal counterparts, with an average improvement of 9.83% (median of 6.60%). However, improvements were three times lower when systems were trained on natural (4.59%) versus acted data (12.7%). Importantly, MM accuracy could be accurately predicted (cross-validated R^2 of 0.803) from unimodal accuracies and two system-level factors. Theoretical and applied implications and recommendations are discussed.

Categories and Subject Descriptors: I.5.m [Pattern Recognition]: Miscellaneous

General Terms: Measurement, Performance

Additional Key Words and Phrases: Affective computing, human-centered computing, evaluation, methodology, survey

ACM Reference Format:

Sidney K. D'Mello and Jacqueline Kory. 2015. A review and meta-analysis of multimodal affect detection systems. ACM Computing Surveys. ACM Comput. Surv. 47, 3, Article 43 (February 2015), 36 pages. DOI: http://dx.doi.org/10.1145/2682899

1. INTRODUCTION

Affect detection (or affect recognition or affect classification) is an emerging research area of considerable practical and theoretical interest to a number of fields including signal processing, machine learning, computational linguistics, computer vision, neuroscience, and cognitive and social psychology [Picard 2010]. From a practical

This work is supported by the National Science Foundation (NSF) (ITR 0325428, HCC 0834847, DRL 1235958) and the Bill & Melinda Gates Foundation via grants to the first author and NSF Graduate Research Fellowship under 1122374 to the second author. Any opinions, findings and conclusions, or recommendations expressed in this article are those of the authors and do not necessarily reflect the views of the funding agencies.

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© 2015 ACM 0360-0300/2015/02-ART43 \$15.00

DOI: http://dx.doi.org/10.1145/2682899

standpoint, affect detection is a cornerstone of affect-aware interfaces that aim to automatically detect and intelligently respond to users' affective states in order to increase usability and effectiveness [Brave and Nass 2002; Picard 1997]. From a theoretical standpoint, affect detection is ultimately a signal processing and pattern recognition problem because it involves the development of a classifier or regressor to detect an ill-defined phenomenon (affect) from observable signals. The problem is extremely challenging because affective states are psychological constructs (conceptual variables) that are not directly observable and are embedded in a noisy context-sensitive expressive and communicative system that has been fine-tuned over millions of years. The challenge is to detect an elusive and fleeting signal (affect) embedded in a system with multiple sources of noise exacerbated by context sensitivity, social masking, and individual and cultural variability [Elfenbein and Ambady 2002; Russell 1994; Russell et al. 2003].

The aforementioned complexities make affect detection an interesting and worth-while problem to pursue as witnessed by numerous efforts toward detecting affective states from a variety of modalities, such as facial expressions, acoustic-prosodic cues, body movements, gesture, contextual cues, text and discourse, physiology, and neural circuitry (see Calvo and D'Mello [2010], Pantic and Rothkrantz [2003], and Zeng et al. [2009] for reviews). While early affect detection systems focused primarily on individual modalities and on emotional expressions portrayed by actors, many contemporary systems emphasize Multimodal (MM) detection of naturalistic affective expressions [Zeng et al. 2009], which is a novel problem in its own right.

Despite the impressive progress made so far, it is safe to say that there is still considerable ground to be covered before affect detectors can be integrated into everyday interfaces and devices and can be more readily deployed into real-world contexts. The field is still confronted with a number of persistent problems, such as (a) intrusive, expensive, and noisy sensors, some of which have scalability concerns; (b) technical challenges associated with detecting latent psychological constructs (i.e., affect) from weak signals embedded in noisy channels; (c) difficulties associated with collecting adequate realistic training data for machine learning [Douglas-Cowie et al. 2007]; (d) the persistent problem of obtaining ground truth labels for supervised classification, when interobserver agreement is generally low [Afzal and Robinson 2011; Graesser et al. 2006]; (e) challenges of incorporating top-down models of context with bottom-up body-based sensing [Conati and Maclaren 2009]; (f) issues of generalizability across contexts, time, individuals, and cultures [Calvo and D'Mello 2010]; (g) lack of clarity of the affective phenomenon being modeled (e.g., moods vs. emotions, categorical vs. dimensional representations, partly due to a difficulty in defining affect [Izard 2010]); and (g) many others as articulated in previous reviews [Calvo and D'Mello 2010; Pantic and Rothkrantz 2003; Zeng et al. 2009].

As researchers are well aware, this daunting list of challenges and open problems is more the norm than the exception given the difficulty of affect detection and the relative infancy of the field (about 15 years old). Numerous innovative solutions to address some of the aforementioned challenges have been extensively reviewed in both early (prior to 2009—see Cowie et al. [2001], Jaimes and Sebe [2007], Pang and Lee [2008], and Pantic and Rothkrantz [2003]) and more recent surveys (2009 to present—see Calvo and D'Mello [2010], D'Mello and Kory [2012], Valstar et al. [2012], and Zeng et al. [2009]), and will not be repeated here. Instead, the present focus is on *MM affect detection*, a strategy that is gaining momentum because it is expected to yield several advantages over unimodal (UM) affect detection. The remainder of the section briefly introduces the area of MM affect detection along with an overview of the issues addressed in this article.

1.1. MM Affect Detection

While UM detection involves the use of a single modality (e.g., facial features, gestures), MM systems fuse two or more modalities for affect detection. This raises a number of unique challenges and opportunities. The main challenges include (a) deciding which modalities to combine; (b) collecting MM training data; (c) handling missing data, different sampling rates, and modality interdependence when building models; (d) deciding how to fuse data from different modalities; and (e) deciding how to evaluate MM affect detectors. The hypothesized advantages of MM approaches to affect detection include (a) a higher-fidelity model of human affective expression, (b) a potential solution to address missing data caused by UM sensors, and (c) a solution to the noisy channel problem that plagues UM approaches.

With respect to the first advantage, it is widely acknowledged that human affective expression consists of a complex coordination of signals encompassing mostly involuntary (e.g., physiology), semivoluntary (facial expressions, body movements), and voluntary (e.g., overt actions such as key presses) responses [Ekman 1992; Rosenberg and Ekman 1994]. Analyzing multiple signals and their mutual interdependence is expected to yield models that more accurately reflect the underlying nature of human affective expression.

Second, UM signals suffer from notable problems associated with missing data. For example, a speech-based affect detector is virtually useless when the user is not speaking, while facial expressions cannot be reliably tracked when the face is out of view or occluded. MM approaches can provide more continuous affect detection capabilities by basing their decisions on the available channels.

The third hypothesized advantage of MM systems stems from the fact that UM affect detectors are inherently noisy since the link between specific signals and affective states is tenuous at best [Barrett et al. 2007; Russell et al. 2003]. This is partially the case because there is no one-to-one mapping between an expression and an affective state. For example, a furrowed brow caused by squinting to focus at something in the distance is diagnostic of a different cognitive state (information seeking) than a furrowed brow that accompanies an expression of confusion [D'Mello and Graesser 2014]. Furthermore, the same affective state can be differentially expressed as a function of the underlying eliciting stimulus. For example, a nearby spider (about to strike) and a spider across the room elicit different responses because they require different actions even though the underlying affective state (fear) elicited by both situations might be the same [Coan 2010]. In general, there is a loose coupling between observable expressions and specific affective states; hence, UM affect detectors are expected to yield moderate accuracies as best. MM affect detectors should yield improvements over UM systems because they are more suited to modeling the weak coupling between expression and experience of affect.

1.2. Goals and Overview of the Present Article

It is generally expected that incorporating MM signals should yield improvements in affect detection accuracies over UM signals. Although this assumption has obvious face validity, it has not always been supported. For example, when compared to the accuracies obtained by the best UM classifiers, some studies have reported impressive MM improvements (e.g., Jiang et al. [2011], Kessous et al. [2010], Lin et al. [2012], Paleari et al. [2009], and Wöllmer et al. [2010]), others have reported negligible or null improvements (e.g., Emerich et al. [2009], Kim [2007], and Metallinou et al. [2012]), and some have even reported negative effects (e.g., Glodek et al. [2011], Gunes and Piccardi [2005], and Khalali and Moradi [2009]). The considerable interstudy variance

in the results of MM affect detection makes it difficult to appropriately gauge what advantages (if any) MM detection yields over UM detection. In addition, there is the question of whether situations can be identified where MM detectors yield impressive improvements, and whether these situations can be differentiated from those that result in null or negative effects. The present article attempts to address these questions by analyzing 90 MM and UM affect detection accuracies reported in published studies.

Research Questions. We focus on answering three specific research questions pertaining to state-of-the-art MM affect detection systems. First, what are the major trends in contemporary MM affect detectors? More specifically, can any general conclusions be drawn with respect to the various components (called system-level factors) of MM affect detection systems (e.g., type of training data, modality fusion methods, affect representation models)? Second, what is the added improvement (if any) in MM over the best UM detection accuracy (called MM1 effect size or MM1 effects)? Third, can we identify system-level factors that correlate with MM1 effects and can they be used to predict MM accuracies in a manner that generalizes across our sample of 90 studies (called moderation analyses)?

Preliminary Analyses. We have made an initial attempt to answer some of these questions (specifically the second and partially the first and third questions) by performing a preliminary analysis of 30 published MM affect detectors [D'Mello and Kory 2012]. The results of this initial analysis indicated that MM accuracies were consistently (26 out of 30 studies) better than UM accuracies, and on average, yielded an 8.12% improvement over the best UM detectors. The present article substantially expands on this initial study, both in terms of distributive breadth (the number of studies analyzed) and analysis depth (the types of questions that can be answered with a larger sample of studies).

Focus of Current Analyses. The focus of this article is on quantifying study-level factors and statistically analyzing MM accuracies rather than qualitatively describing individual affect detection systems; the latter has been extensively done in previous surveys, although mainly on UM and/or audio-visual detection (see Calvo and D'Mello [2010], Jaimes and Sebe [2007], Pantic and Rothkrantz [2003], and Zeng et al. [2009]). Hence, we do not discuss individual systems and approaches in depth, but focus on identifying general trends across systems with descriptive statistics and analyzing MM accuracies and effects with both descriptive and inferential statistics.

It is sometimes argued that meta-analyses of this type are not feasible because it is improper to compare accuracies across studies that differ in multiple respects. Hence, it is important to emphasize that the present article does not make such comparisons. Instead, MM1 effects are computed by comparing MM accuracies to UM accuracies from the *same* study, a comparison that is justifiable because study-level factors are held constant. The distribution of MM1 effects from individual studies is then statistically analyzed, an approach recommended by standard texts on meta-analyses (e.g., Borenstein et al. [2009] and Lipsey and Wilson [2001]). In addition, the variability in datasets, methods, and metrics used is, in fact, a major strength of meta-analytical approaches because it allows one to estimate "population effects" from individual "study effects" by averaging across interstudy variability.

To summarize, with the exception of our preliminary study [D'Mello and Kory 2012], this article represents the first major attempt to quantify and statistically analyze a large set of MM affect detectors in order to make generalizable conclusions.

2. METHOD

The methodology used to search for relevant articles, the inclusion/exclusion criteria, the data coding, and data treatment procedures are discussed in some detail in this section to enable replication as more studies emerge in the literature.

2.1. Search Process and Inclusion/Exclusion Criteria

A three-pronged approach was used for study selection. First, relevant journals and conference proceedings were searched using a targeted search strategy. The journals included IEEE Transactions on Affective Computing, IEEE Transactions on Multimedia, and IEEE Transactions on Pattern Analysis and Machine Intelligence. Conferences included the International Conference on Affective Computing and Intelligent Interaction (ACII), IEEE International Conference on Automatic Face and Gesture Recognition (FG), IEEE International Conference on Multimedia and Expo (ICME), ACM International Conference on Multimodal Interfaces (ICMI), and INTERSPEECH. The secondary search commenced by identifying additional articles from the reference sections of articles retrieved from the targeted search and from recent survey articles [Calvo and D'Mello 2010; Zeng et al. 2009]. Finally, the *informal search* proceeded by querying Google Scholar with the following search queries: (multimodal OR bimodal) fusion; (affect OR emotion) AND (detection OR recognition). We restricted our targeted search to articles published within the last 5 years (2009-2013), but earlier articles could have been retrieved in the secondary and informal searches as long as they were published in the last 10 years (2003 and beyond).

A rather liberal inclusion/exclusion criterion was adopted in order to maximize the number of studies considered. Any peer-reviewed publication that reported both UM and MM affect detection accuracies in a clearly accessible format (i.e., accuracy metrics could be easily obtained from the text, tables, or figures) was included in the analysis. Failure to report both UM and MM accuracies unfortunately led to the exclusion of some relevant and highly cited studies (e.g., Kapoor et al. [2007]), but this was unavoidable due to the nature of the analytic strategy. Selection bias was avoided by never excluding a study based on the results, publication outlet, or authors.

In all, 84 articles were selected based on the search and inclusion/exclusion criteria. These 84 articles yielded 90 viable systems since some articles reported more than one unique multimodal affect detector. There was a strong positive correlation between the year (2004–2013) and the number of studies, r=0.727, suggesting that recent studies were more frequent in the sample. More than 60% of the studies were from the 2009–2013 period and 42% of all studies were from the 2011–2013 period.

2.2. Data Coding

The studies were coded along several system-level (or study-level) factors. The coding process was initially performed by one of the authors and then independently checked by the second author. Disagreements were resolved via discussion among the authors. Table I describes how each study was coded with respect to the factors discussed in the following.

Data type addresses whether training and validation data consisted of affective expressions that were (a) obtained by asking actors to portray various emotions (e.g., Castellano et al. [2008], Cueva et al. [2011], Dobrišek et al. [2013], Lingenfelser et al. [2011], and Metallinou et al. [2012]), (b) collected via experimental methods that induced specific emotions (e.g., Bailenson et al. [2008], Glodek et al. [2013], Koelstra et al. [2012], Soleymani et al. [2012], and Wöllmer et al. [2013a]), or (c) naturalistic displays of affect (i.e., nonacted and not induced—e.g., Castellano et al. [2009], D'Mello and Graesser [2010], Kapoor and Picard [2005], Litman and Forbes-Riley [2004], and Wöllmer et al. [2013b]).

While the criteria for a dataset to be categorized as acted or natural is quite clear, the induced category requires some clarification. This designation was applied to datasets where specific emotions were induced using well-established techniques such as showing participants films (e.g., Soleymani et al. [2012]) or images (e.g., Hussain et al.

Table I. Details of Individual Study Characteristics (Sorted by Author and Year)

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2 act disc class 7 disc basic Voice + Text 42 act disc class 4 disc basic Face + Voice 42 act disc class 6 disc basic Face + Voice 28 nat disc class 5 disc nonbasic Content 28 nat disc class 5 disc nonbasic Face + Body 43 act disc class 6 disc basic Face + Voice 44 ind dim reg dim simple Voice + Text 45 act disc class 6 dim simple Voice + Text 46 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 28 act disc class 6 disc basic Face + Voice 29 act disc class 6 disc basic Face + Voice 20 dim complex Face + Voice 21 act disc class 6 dim complex Face + Voice 22 dim complex Face + Voice 23 act disc class 6 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body 5 disc mixed Face + Body 6 disc mixed Face + Body	Chetty and Wagner [2008]	44	act	$_{ m disc}$	class	4	disc basic	Face + Voice	hybrid	$_{ m deb}$
42 act disc class 4 disc basic Face + Voice 42 act disc class 6 disc basic Face + Voice 28 nat disc class 5 disc nonbasic Content 28 nat disc class 5 disc nonbasic Face + Body 43 act disc class 6 disc basic Face + Voice 28 act disc class 6 disc basic Face + Voice 4 ind dim reg dim simple Voice + Text 42 act disc class 6 dim simple Voice + Text 42 act disc class 6 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc basic Face + Voice 24 act disc class 6 disc basic Face + Voice 25 act disc class 6 dim complex Face + Voice 26 disc basic Face + Voice 27 dim complex Face + Voice 28 act disc class 6 disc basic Face + Voice 29 act disc class 7 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	Chuang and Wu [2004]	2	act	$_{ m disc}$	class	7	disc basic	Voice + Text	dec	$_{ m deb}$
42 act disc class 6 disc basic Face+Voice 28 nat disc class 4 disc nonbasic Body+ 28 nat disc class 5 disc nonbasic Face+Body 43 act disc class 6 disc basic Face+Voice 28 act disc class 6 disc basic Face+Voice 4 ind dim reg dim simple Voice+Text 42 act disc class 6 dim simple Voice+Text 42 act disc class 6 dim complex Face+Voice 16 ind dim class 2 dim complex Face+Voice 16 ind dim class 2 dim complex Face+Voice 23 act disc class 6 disc basic Face+Voice 24 act disc class 6 disc basic Face+Voice 25 dim complex Face+Voice 26 disc mixed Face+Body 27 disc mixed Face+Body	Cueva et al. [2011]	42	act	disc	class	4	disc basic	Face + Voice	dec	$_{ m deb}$
28 nat disc class 4 disc nonbasic Body + 28 nat disc class 5 disc nonbasic Face + Body 43 act disc class 6 disc basic Face + Voice 28 act disc class 6 disc basic Face + Voice 4 ind dim reg dim simple Voice + Text 42 act disc class 6 dim simple Face + Voice 16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc basic Face + Voice 24 act disc class 6 disc basic Face + Voice 25 dim complex Face + Voice 26 dim complex Face + Voice 27 disc mixed Face + Body 28 act disc class 6 disc mixed Face + Body	Datcu and Rothkrantz [2011]	42	act	$_{ m disc}$	class	9	disc basic	Face + Voice	feat	$_{ m deb}$
28 nat disc class 5 disc nonbasic Face + Body 43 act disc class 6 disc basic Face + Voice 28 act disc class 6 disc basic Face + Voice 4 ind dim reg dim simple Voice + Text 42 act disc class 6 disc basic Face + Voice 16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc basic Face + Voice 24 act disc class 6 disc basic Face + Voice 25 act disc class 6 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	D'Mello and Graesser [2007]	28	nat	disc	class	4	disc nonbasic	Body +	feat	$_{ m deb}$
28 nat disc class 5 disc nonbasic Face + Body + Content 43 act disc class 6 disc basic Face + Voice 28 act disc class 6 disc basic Face + Voice 4 ind dim class 6 dim simple Voice + Text 42 act disc class 6 dim simple Voice + Text 44 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body 6 disc mixed Face + Body								Content		
43 act disc class 6 disc basic Face + Voice 28 act disc class 6 disc basic Face + Voice 4 ind dim reg disc class 3 dim simple Voice + Text 17 nat disc class 6 disc basic Face + Voice 16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc mixed Face + Voice 24 act disc class 6 disc mixed Face + Voice 25 act disc class 6 disc mixed Face + Fort 26 disc mixed Face + Fort 27 disc mixed Face + Fort 28 act disc class 6 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	D'Mello and Graesser [2010]	28	nat	disc	class	ស	disc nonbasic	${ m Face} + { m Body} \ + { m Content}$	feat	indep
act disc class 5 disc basic Face + Voice 4 ind dim reg disc class 6 dim simple Voice + Text 17 nat disc class 3 dim simple Voice + Text 42 act disc class 6 disc basic Face + Voice 16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 6 disc mixed Face + Voice 4 act disc class 6 disc mixed Face + Body 5 disc mixed Face + Body 6 disc mixed Face + Body 7 disc mixed Face + Body 8 disc mixed Face + Body	Dobrišek et al. [2013]	43	act	$_{ m disc}$	class	9	disc basic	Face + Voice	dec	$_{ m dep}$
28 act disc class 6 disc basic Face+Voice 4 ind dim reg dim simple Voice+Text 17 nat disc class 3 dim simple Voice+Text 42 act disc class 6 disc basic Face+Voice 16 ind dim class 2 dim complex Face+Voice 16 ind dim class 2 dim complex Face+Voice 23 act disc class 7 disc mixed Face+Body 4 act disc class 6 disc mixed Face+Body	Dy et al. [2010]		nat	$_{ m disc}$	$_{ m class}$	ರ	disc basic	Face + Voice	dec	$_{ m deb}$
4 ind dim reg dim simple Voice+Text 17 nat disc class 3 dim simple Voice+Text 42 act disc class 6 disc basic Face+Voice 16 ind dim class 2 dim complex Face+Voice 16 ind dim class 2 dim complex Face+Voice 23 act disc class 7 disc mixed Face+Body 4 act disc class 6 disc mixed Face+Body	Emerich et al. [2009]	28	act	$_{ m disc}$	class	9	disc basic	Face + Voice	feat	$_{ m deb}$
17 nat disc class 3 dim simple Voice + Text 42 act disc class 6 disc basic Face + Voice 16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 7 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	Eyben et al. [2010]	4	ind	dim	reg		dim simple	Voice + Text	model	$_{ m deb}$
42 act disc class 6 disc basic Face+Voice 16 ind dim class 2 dim complex Face+Voice 16 ind dim class 2 dim complex Face+Voice 23 act disc class 7 disc mixed Face+Body 4 act disc class 6 disc mixed Face+Body	Forbes-Riley and Litman [2004]	17	nat	$_{ m disc}$	class	က	dim simple	Voice + Text	feat	$_{ m deb}$
16 ind dim class 2 dim complex Face + Voice 16 ind dim class 2 dim complex Face + Voice 23 act disc class 7 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	Gajsek et al. [2010]	42	act	$_{ m disc}$	$_{ m class}$	9	disc basic	Face + Voice	dec	$_{ m deb}$
16 ind dim class 2 dim complex Face + Voice 23 act disc class 7 disc mixed Face + Body 4 act disc class 6 disc mixed Face + Body	Glodek et al. [2011]	16	ind	dim	class	2	dim complex	Face + Voice	dec	indep
di [2005] 23 act disc class 7 disc mixed Face + Body di [2005] 4 act disc class 6 disc mixed Face + Body	Glodek et al. [2013]	16	ind	dim	class	2	dim complex	Face + Voice	dec	indep
4 act disc class 6 disc mixed Face + Body	Gong et al. [2007]	23	act	$_{ m disc}$	$_{ m class}$	7	disc mixed	Face + Body	feat	$_{ m deb}$
	Gunes and Piccardi [2005]	4	act	$_{ m disc}$	$_{ m class}$	9	disc mixed	Face + Body	feat	$_{ m deb}$

Table I. Continued

		Data	Rep.	Class		Affect		Fusion	Validation
Reference	N	Type	Model	Model	k	States	Modalities	Type	Method
Gunes and Piccardi [2009]	10	act	disc	class	12	disc mixed	Face + Body	feat	deb
Han et al. [2007]	14	act	$_{ m disc}$	class	5	disc basic	Face + Voice	dec	deb
Haq et al. [2008]	1	act	disc	class	7	disc basic	Face + Voice	feat	deb
Haq and Jackson [2009]	4	act	$_{ m disc}$	class	7	disc basic	Face + Voice	dec	deb
Hoch et al. [2005]	7	act	$_{ m disc}$	class	4	disc mixed	Face + Voice	dec	deb
Hommel et al. [2013]	4	act	$_{ m disc}$	class	5	disc basic	Face + Voice	dec	deb
Hussain et al. [2012]	19	ind	dim	$_{\rm class}$	က	dim simple	Face + PPhy	dec	deb
Jiang et al. [2011]	42	act	disc	class	9	disc basic	Face + Voice	model	deb
Joo et al. [2007]	5	act	$_{ m disc}$	class	5	disc basic	Face + Voice	dec	deb
Kanluan et al. [2008]	20	nat	dim	reg		dim complex	Face + Voice	dec	deb
Kapoor and Picard [2005]	8	nat	disc	class	2	disc nonbasic	Face + Body	model	$_{ m deb}$
							+ Content		
Karpouzism et al. [2007]	4	ind	dim	class	4	dim simple	Face + Voice	feat	deb
Kessous et al. [2010]	10	act	$_{ m disc}$	class	œ	disc mixed	Face + Voice	feat	deb
							+ Body		
Khalali and Moradi [2009]	2	ind	$_{ m disc}$	class	က	disc mixed	CPhy + PPhy	feat	$_{ m deb}$
Kim et al. [2005]	က	ind	dim	class	4	dim simple	Voice + PPhy	feat	deb
Kim [2007]	က	ind	dim	$_{\rm class}$	4	dim simple	Voice + PPhy	feat	indep
Kim and Lingenfelser [2010]	က	ind	dim	class	4	dim simple	Voice + PPhy	dec	$_{ m deb}$
Koelstra et al. [2012]	22	ind	dim	class	2	dim complex	CPhy +	dec	deb
							$\begin{array}{c} {\rm Content} + \\ {\rm PPhy} \end{array}$		
Krell et al. [2013]	13	ind	disc	class	2	disc nonbasic	Face + Voice	dec	indep
Lin et al. [2012]	7	act	$_{ m disc}$	class	4	disc basic	Face + Voice	model	indep
Lin et al. [2012]	4	ind	dim	class	4	dim simple	Face + Voice	model	indep
Lingenfelser et al. [2011]	8	act	$_{ m disc}$	class	7	disc basic	Face + Voice	dec	indep
Lingenfelser et al. [2011]	13	ind	dim	class	က	dim simple	Face + Voice	dec	indep
Litman and Forbes-Riley [2004]	15	nat	dim	class	က	dim simple	Voice + Text	feat	$_{ m deb}$
Litman and Forbes-Riley [2006a]	14	nat	dim	class	3	dim simple	Voice + Text	feat	deb
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		Data	Rep.	Class		Affect		Fusion	Validation
Reference	N	Type	Model	Model	k	States	Modalities	$_{\mathrm{Type}}$	Method
Litman and Forbes-Riley [2006a]	20	nat	dim	class	က	dim simple	Voice + Text	feat	deb
Lu and Jia [2012]	5	act	dim	class	2	dim simple	Face + Voice	model	indep
Mansoorizadeh and Charkari [2010]	12	act	$_{ m disc}$	class	9	disc basic	Face + Voice	hybrid	deb
Mansoorizadeh and Charkari [2010]	42	act	$_{ m disc}$	class	9	disc basic	Face + Voice	hybrid	$_{ m deb}$
Metallinou et al. [2008]	10	act	$_{ m disc}$	class	4	disc basic	Face + Voice	dec	deb
Metallinou et al. [2012]	10	act	dim	class	က	dim simple	Face + Voice	model	indep
Monkaresi et al. [2012]	20	ind	dim	class	2	dim simple	Face + PPhy	feat	$_{ m deb}$
Nicolaou et al. [2011]	4	ind	dim	reg		dim simple	Face + Voice + Body	model	deb
Pal et al. [2006]		nat	disc	class	5	disc mixed	Face + Voice	dec	deb
Paleari et al. [2009]	44	act	$_{ m disc}$	$_{\rm class}$	9	disc basic	Face + Voice	model	indep
Park et al. [2012]	10	act	$_{ m disc}$	class	4	disc basic	Face + Voice	dec	deb
Rabie et al. [2009]	œ	act	disc	class	7	disc basic	Face + Voice	model	indep
Rashid et al. [2012]	42	act	disc	class	9	disc basic	Face + Voice	dec	deb
Rigoll et al. [2005]	13	act	$_{ m disc}$	class	7	disc basic	Voice + Text	dec	indep
Rosas et al. [2013]	92	nat	dim	class	2	dim simple	Face + Voice $\perp Toxt$	feat	indep
Desce et el [9019]	0.7	+		200	c	والمصنين مبياه	Too - Meio	£004	
Kosas et al. [2013]	91	nat	di di	class	N	dim simple	race + voice + Text	Ieat	ındep
Rozgic et al. [2012]	10	act	disc	class	4	disc basic	$\mathrm{Face} + \mathrm{Voice} \\ + \mathrm{Text}$	feat	indep
Savran et al. [2012]	16	pui	dim	reg		dim complex	$\mathrm{Face} + \mathrm{Voice} \\ + \mathrm{Text}$	model	indep
Schuller et al. [2007]	21	nat	disc	class	က	disc nonbasic	Face + Voice	feat	indep
Schuller [2011]	47	nat	dim	reg		dim complex	Voice + Text	feat	indep
Sebe et al. [2006]	38	act	$_{ m disc}$	class	11	disc mixed	Face + Voice	model	deb
Seppi et al. [2008]	51	ind	$_{ m disc}$	class	4	disc mixed	Voice + Text	feat	indep
Shan et al. [2007]	2	act	$_{ m disc}$	class	7	disc mixed	Face + Body	feat	$_{ m deb}$
Soleymani et al. [2012]	24	ind	dim	class	က	dim simple	CPhy + Gaze	qec	indep
Tu and Yu [2012]	42	act	$_{ m disc}$	class	9	disc basic	Face + Voice	dec	deb
									Continued

Table I. Continued

		Data	Kep.	Class		Affect		Fusion	Validation
Reference	N	Type	Model	Model	k	States	Modalities	$_{\mathrm{Type}}$	Method
Vu et al. [2011]	2	act	disc	class	4	disc mixed	Voice + Body	qec	deb
Wagner et al. [2011]	21	act	dim	class	4	dim simple	Face $+$ Voice $+$ Body	dec	indep
Walter et al. [2011]	10	ind	dim	class	2	dim complex	Voice + PPhy	qec	deb
Wang and Guan [2005]	00	act	disc	class	9	disc basic	Face + Voice	feat	indep
Wang and Guan [2008]	00	act	disc	class	9	disc basic	Face + Voice	feat	indep
Wang et al. [2013]	28	ind	dim	class	73	dim simple	$\operatorname{CPhy} + \operatorname{Content}$	feat	dep
Wimmer et al. [2008]	8	ind	disc	class	9	disc nonbasic	Face + Voice	feat	deb
Wöllmer et al. [2010]	10	act	dim	class	က	dim simple	Face + Voice	feat	indep
Wöllmer et al. [2013a]	16	ind	dim	class	2	dim complex	Face + Voice	model	indep
Wöllmer et al. [2013b]	343	nat	dim	class	73	dim simple	$\mathrm{Face} + \mathrm{Voice} \ + \mathrm{Text}$	hybrid	indep
Wu and Liang [2011]	00	act	disc	class	4	disc basic	Voice + Text	qec	deb
Zeng et al. [2005]	20	act	disc	class	11	disc mixed	Face + Voice	model	indep
Zeng et al. [2006]	2	nat	disc	class	2	dim simple	Face + Voice	model	deb
Zeng et al. [2007]	20	act	disc	class	11	disc mixed	Face + Voice	model	indep

otherwise blank); Affect states (disc basic = discrete basic emotions; disc nonbasic = discrete nonbasic emotions; disc mixed = discrete basic + nonbasic emotions; dim simple = dimensional simple; dim complex = dimensional complex); Modalities (PPhy = peripheral physiology, CPhy = central physiology, Notes: N = number of participants (blank when not specified); Data Type (act = acted; ind = induced; nat = natural); Representation Model (disc = discrete; dim = dimensional); Classification Model (class = classification, reg = regression); k = Number of affective states (only for classification tasks,Content = content/context); Fusion Type (feat = feature; dec = decision); Validation Method (dep = subject dependent; indep = subject independent). [2012]) that were previously validated as being reliable elicitors of affect [Kory and D'Mello 2014]. It was also applied to studies where individuals were required to participate in interactions that were intentionally affectively charged, thereby increasing the likelihood that they would respond emotionally. For example, the SEMAINE dataset [McKeown et al. 2012] was constructed by asking individuals to engage in a conversation with an animated agent that had one of four affective dispositions (or personalities): angry, happy, gloomy, or pragmatic. Studies that utilized this dataset (e.g., Karpouzis et al. [2007] and Nicolaou et al. [2011]) were categorized as "induced" because it is likely that the affective disposition of the agent induced specific emotions in the individual. In fact, this was the main motivation toward using agents with four specific affective dispositions.

Number of participants simply refers to the number of unique individuals in the training/validation dataset. It is an important factor because generalizability is related to the number of individuals used to train the detector due to individual differences in affect expression.

Affect representation model refers to whether ground truth affect measures for the supervised classifiers consisted of discrete or dimensional representations. Discrete models consider emotional episodes as belonging to one of m distinct categories (e.g., judging if a 30 second video of an individual's face represents anger, sadness, or fear). Discrete ratings do not need to be mutually exclusive since affective blends are often experienced, yet most studies use mutually exclusive ratings for convenience (e.g., D'Mello and Graesser [2010], Krell et al. [2013], and Rashid et al. [2012]). Dimensional models represent affect along one or more dimensions, primarily valence (positive-negative) and activation/arousal (sleepy vs. awake or inactive vs. active) (e.g., Hussain et al. [2012], Lu and Jia [2012], and Wang et al. [2013]), but occasionally extending to other dimensions such as expectancy, power, and dominance (e.g., Baltrušaitis et al. [2013], Glodek et al. [2013], and Wöllmer et al. [2013a]).

The affect representation model is a conceptual entity that is concerned with the affective representation and not with the measurement scale per se. Hence, studies involving ordinal or continuous ratings of discrete emotions were coded as discrete, as was the case where the intensity of amusement (a discrete state) was rated via a 0 (neutral) to 8 (amused) scale (e.g., Bailenson et al. [2008]). Similarly, studies with categorical ratings of dimensions (e.g., low vs. high ratings of valence) were coded as dimensional (e.g., Bailenson et al. [2008]).

Affect detection model pertains to whether the machine learning models were classifiers or regressors. In most cases, classifiers and regressors were used when affect models were discrete (e.g., D'Mello and Graesser [2010], Hommel et al. [2013], and Rashid et al. [2012]) and continuous (e.g., Eyben et al. [2011], Kanluan et al. [2008], and Savran et al. [2012]), respectively. However, a number of studies used dimensional representations and collected ordinal or continuous ratings, but performed classifications instead of regressions by discretizing the scales into high versus low or high versus medium versus low categories (e.g., Glodek et al. [2011] and Wöllmer et al. [2013a]). For example, Wöllmer et al. [2010] used a five-point scale to measure valence and activation, but then performed a categorical classification by performing a tripartite split on each dimension (i.e., dividing the scale into low, medium, and high sections). Similarly, ordinal or continuous activation-valence values were often discretized by clustering prior to classification (e.g., Karpouzis et al. [2007]).

Number of affective states detected only applies to classification tasks and is simply the number of discrete affective states considered. It is an important factor as the affect detection problem ostensibly becomes more challenging as the number of discriminations increases.

Affective states/dimensions detected pertains to the specific affective states/dimensions in the classification/regression models. Researchers in the affective sciences have proposed a number of taxonomies to categorize the discrete affective states that occur in everyday experiences [Ekman 1992; Ortony et al. 1988; Plutchik 2001]. Broadly, the affective states can be divided into discrete basic and discrete nonbasic states. States such as anger, surprise, happiness, disgust, sadness, and fear are typically considered to be basic affective states [Ekman 1992]. States such as boredom, confusion, frustration, engagement, and curiosity share some, but not all, of the features commonly attributed to basic emotions (see Ekman [1992]). Consequently, these are labeled as nonbasic states. Some studies used a combination of both (e.g., Castellano et al. 2008; Sebe et al. 2006] and these were coded as discrete mixed.

With respect to affective dimensions, most researchers agree that valence and arousal (activation) are two essential dimensions to represent affect [Barrett et al. 2007; Russell 2003]. Beyond this, there is considerable debate as to which other dimensions are needed [Fontaine et al. 2007; Kaernbach 2011]. Most studies detected valence and arousal (coded as *dimensional simple*), but expectancy, power, and dominance were also considered in some studies (coded as *dimensional complex*).

Number of modalities simply refers to whether the MM detectors fused two (bimodal) or three (trimodal) modalities.

Modalities refer to the specific modalities used for affect detection. In communication theory, modality is considered to be distinct from medium because the former focuses on the sense via which a message is communicated (e.g., facial expression, pitch), while the latter is concerned with the means of message communication [Sutdiffe 2008]. For example, facial expressions and gestures are different modalities that can be communicated via the same medium (video). The present coding scheme focused on modality instead of medium.

The specific modalities used in the 90 studies included (a) facial features extracted from video, (b) paralinguistic or acoustic-prosodic features from the voice, (c) linguistic or semantic features from written or spoken language, (d) body movements consisting of postures and gestures (excluding facial features), (e) eye gaze, (f) central physiology (only Electroencephalography—EEG), (g) peripheral physiology (e.g., Electrodermal activity (EDR), Electrocardiography (ECG), Electromyography (EMG), respiration), and (h) content and context.

While modalities (a)–(f) were straightforward, peripheral physiology and content/context require some clarification. With respect to peripheral physiology, although individual channels, such as EDR, ECG, EMG, and so forth, can be analyzed independently and treated as separate modalities, most studies fused features from these various channels instead of considering each signal individually. For example, Chanel et al. [2011] built (a) a peripheral model by combining galvanic skin response, blood volume pulse, heart rate, chest cavity expansion, and skin temperature; (b) a central physiology model (EEG); and (c) a combined peripheral + central physiology model. In this and similar cases, the combination of the individual peripheral physiological channels was taken as a UM detector.

Content features were gleaned from a multimedia content analysis of affect-elicitation stimuli (e.g., low-level video features such as color, lighting [Koelstra et al. 2012]). Context features were obtained by analyzing the situation in which the affective interaction was embedded. For example, D'Mello and Graesser [2010] tracked a number of contextual cues, such as session length, system feedback, and so on, when individuals completed a learning session with a computer tutor. Both content and context features are unique from the other modalities in that they are obtained from the stimuli and situation rather than the individuals themselves. They were grouped as

context/context features since there were not a sufficient number of studies to sustain an independent analysis of each.

Fusion method pertains to the method used to fuse modalities. Possible options include data-level, decision-level, score-level, hybrid, and model-level fusion. In datalevel fusion, individual data streams are fused prior to feature engineering (e.g., fusing video data from two cameras). Feature-level fusion consists of independently computing features from each modality and then fusing the features prior to classification (e.g., Castellano et al. [2008], D'Mello and Graesser [2010], and Litman and Forbes-Riley [2006a]). In decision-level fusion, classification is first performed on the individual features and the outputs (decisions) are fused via one of several voting rules (e.g., Kanluan et al. [2008], Koelstra et al. [2012], and Walter et al. [2011]). Score-level fusion is related to decision-level fusion in that affect likelihoods (or probabilities) computed by classifiers operating on independent modalities are fused (e.g., Gajsek et al. [2010]). Only a small number of systems relied on score-level fusion, so these were coded as decision-level fusion due to the similarity between these two methods. Hybrid fusion combines both feature- and decision-level fusion, for example, by combining independent decisions of individual UM classifiers with the decisions of a featurelevel fused MM classifier (e.g., Chetty and Wagner [2008] and Mansoorizadeh and Charkari [2010]). Finally, model-level fusion takes advantage of the interdependencies among the various modalities during the fusion process (e.g., Caridakis et al. [2006], Eyben et al. [2010], and Metallinou et al. [2012]). When multiple fusion techniques were implemented and compared in a single study, the fusion method that yielded the highest accuracy was analyzed.

Validation method is concerned with whether the affect detectors are expected to generalize to new individuals (person independent) or not (person dependent). This is a critical distinction because (for the most part) affect detectors are intended to be person independent but developing such systems is more challenging due to large interindividual variability in affect. Designation of an affect detector as person dependent or independent was rarely articulated in the papers, but could be inferred from the methods used to validate the detectors. Studies that used leave-one-person-out or leave-several-people-out validation techniques, where instances from the same individual were either in the training or testing sets but never both, were deemed to be person independent (e.g., D'Mello and Graesser [2010], Savran et al. [2012], and Schuller [2011]). Studies that cross-validated within an individual, or studies where person independence across training and testing sets was not carefully controlled were coded as person dependent (e.g., Castellano et al. [2008], Litman and Forbes-Riley [2006a], and Monkaresi et al. [2012]).

2.3. Encoding Affect Detection Accuracy

Table II provides several measures of UM and MM affect detection accuracies. The key measures were detection accuracy of the best, second-best, and worst UM detectors (Max1, Max2, and Min, respectively) and MM accuracy (MM). Most studies that performed a categorical classification used classification accuracy (i.e., the proportion of correctly classified instances) as the evaluation metric. In rare cases where both classification accuracy and the F1 measure were reported, classification accuracy was taken to be the metric in order to increase consistency among studies. The correlation coefficient was taken as the performance metric for regression models.

MM1 effect was the key effect size metric. If a_1 and a_2 are accuracies associated with two UM detectors, and a_{12} is the MM accuracy, then the MM1 effect was computed as the percent improvement over the best UM detector (see Equation (1)). This metric affords a unified analysis framework for studies that used classification accuracies, F1

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49.7

49.3 23.098.3 46.8 0.001 45.2

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6.0

275.0

24.4

MMMin

154.8

25.7

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0.9540.668

Hag and Jackson [2009]

Ian et al. [2007] Haq et al. [2008] Hommel et al. [2013]

0.525

0.817 0.983 0.868

20.1

MM Effect Size (%) 36.8 23.0 46.8 100.0 134.9 275.0 49.3 43.7 45.2 30.3 12.5 -14.28.01 13.4 15.4 0.8150.775 0.800 0.713 0.7900.9480.6300.840 0.970 0.7500.5630.407 0.4870.930 0.530 0.8370.470 0.6430.8961.000 0.9770.8910.7830.9640.827Table II. Classification Accuracy and Multimodal (MM) Effect Sizes (Sorted by Author + Year) Content 0.781 0.381 CPhyPPhy 0.5900.280Gaze Body 0.3310.3160.7461.000 0.7690.671 0.655Text 0.832 Voice 0.7090.7300.7640.6500.5590.5050.7620.6290.5060.644 0.4000.7910.571 0.877 0.2480.9520.6700.4830.2000.377 0.5280.8600.6200.8090.8290.3520.4050.8510.9380.8500.8200.3520.907 0.5470.500Acc Acc Acc AccAcc Acc CC Forbes-Riley and Litman [2004] Oatcu and Rothkrantz [2011] D'Mello and Graesser [2010] D'Mello and Graesser [2007] Sanda and Robinson [2011] Chetty and Wagner [2008] Chetty and Wagner [2008] Junes and Piccardi [2005] Gunes and Piccardi [2009] Baltrušaitis et al. [2013] Chuang and Wu [2004] Castellano et al. [2008] Castellano et al. [2009] Caridakis et al. [2006] Sailenson et al. [2008] Dobrišek et al. [2013] Emerich et al. [2009] Chanel et al. [2011] Gajsek et al. [2010] Glodek et al. [2011] Glodek et al. [2013] Sueva et al. [2011] Eyben et al. [2010] Busso et al. [2004] Chen et al. [2005] Jong et al. [2007] Oy et al. [2010] Reference

Table II. Continued

		IIM									MM	MW Effect Size (%)	(%)
Reference	Meas.	Face	Voice	Text	Body	Gaze	PPhy	CPhy	Content	\overline{MM}	MM1	MM2	MMMin
Hussain et al. [2012]	Acc	0.585					0.495			0.624	6.5	25.9	25.9
Jiang et al. [2011]	Acc	0.468	0.522							0.665	27.4	42.1	42.1
Joo et al. [2007]	Acc	0.534	0.630							0.704	11.7	31.8	31.8
Kanluan et al. [2008]	CC	0.590	0.710							0.780	8.6	36.0	36.0
Kapoor and Picard [2005]	Acc	0.668			0.820				0.572	0.865	5.5	29.5	51.2
Karpouzis et al. [2007]	Acc	0.670	0.730							0.820	12.3	22.4	22.4
Kessous et al. [2010]	Acc	0.483	0.571		0.671					0.783	16.7	37.1	62.1
Khalali and Moradi [2009]	Acc						0.517	0.667		0.622	-6.7	20.3	20.3
Kim et al. [2005]	Acc		0.520				0.530			0.660	24.5	26.9	26.9
Kim [2007]	Acc		0.540				0.510			0.550	1.9	7.8	7.8
Kim and Lingenfelser [2010]	Acc		0.711				0.640			0.724	1.7	13.0	13.0
Koelstra et al. [2012]	F1						0.560	0.549	0.619	0.627	1.2	9.5	17.9
Krell et al. [2013]	Acc	0.553	0.605							0.798	31.9	44.4	44.4
Lin et al. [2012]	Acc	0.713	0.710							0.906	27.0	27.6	27.6
Lin et al. [2012]	Acc	0.621	0.603							0.781	25.7	29.5	29.5
Lingenfelser et al. [2011]	Acc	0.480	0.450							0.550	14.6	22.2	22.2
Lingenfelser et al. [2011]	Acc	0.530	0.610							0.610	0.0	15.1	15.1
Litman and Forbes-Riley [2004]	Acc		0.555	0.580						0.612	5.6	10.3	10.3
Litman and Forbes-Riley [2006a]	Acc		0.695	0.745						0.750	0.7	7.9	7.9
Litman and Forbes-Riley [2006a]	Acc		0.520	0.545						0.570	4.5	9.6	9.6
Lu and Jia [2012]	Acc	0.622	0.760							0.911	20.0	46.8	46.8
Mansoorizadeh and Charkari [2010]	Acc	0.540	0.510							0.770	42.6	51.0	51.0
Mansoorizadeh and Charkari [2010]	Acc	0.370	0.330							0.710	91.9	115.2	115.2
Metallinou et al. [2008]	Acc	0.654	0.544							0.754	15.4	38.8	38.8
Metallinou et al. [2012]	Acc	0.562	0.559							0.630	2.5	24.5	24.5
Monkaresi et al. [2012]	F1	0.582					0.512			0.612	5.1	19.6	19.6
Nicolaou et al. [2011]	CC	0.603	0.515		0.502					0.719	10.7	32.4	8.7.9
Pal et al. [2006]	Acc	0.640	0.742							0.752	1.3	17.5	17.5
												7	

Table II. Continued

		TIME									אראער	MIN DEC. + C.:- (0)	(10)
Defenses	Mood	7 C.M.	170:00	Ė	Dodr	2	DDb	CDb	+400	JATA	TATTAT	MANGO SIZ	
Neierence	Meas.	race	volce	Text	Doay	caze	ггиу	Criiy	Content	IMIMI	TIMIN	1VIIVI 2	IMIMIMI
Paleari et al. [2009]	Acc	0.321	0.361							0.430	19.1	34.0	34.0
Park et al. [2012]	Acc	0.771	0.773							0.814	5.3	5.6	5.6
Rabie et al. [2009]	Acc	0.745	0.619							0.782	4.9	26.3	26.3
Rashid et al. [2012]	Acc	0.742	0.674							0.803	8.3	19.1	19.1
Rigoll et al. [2005]	Acc		0.742	0.596						0.920	24.0	54.4	54.4
Rosas et al. [2013]	Acc	0.610	0.468	0.649						0.750	15.5	22.9	60.4
Rosas et al. [2013]	Acc	0.540	0.486	0.540						0.649	20.0	20.0	33.3
Rozgic et al. [2012]	Acc	0.513	0.609	0.486						0.694	14.0	35.3	42.8
Savran et al. [2012]	CC	0.178	0.092	0.162						0.280	41.9	121.9	217.6
Schuller et al. [2007]	Acc	0.312	0.621							0.639	2.9	104.8	104.8
Schuller [2011]	CC		0.683	0.685						0.776	2.6	28.8	28.8
Sebe et al. [2006]	Acc	0.560	0.450							0.900	60.7	100.0	100.0
Seppi et al. [2008]	Acc		0.631	0.629						0.664	5.2	5.6	9.6
Shan et al. [2007]	Acc	0.792			0.726					0.885	11.7	21.9	21.9
Soleymani et al. [2012]	Acc					0.689		0.563		0.725	5.2	29.3	29.3
Tu and Yu [2012]	Acc	0.600	0.570							0.720	20.0	26.3	26.3
Vu et al. [2011]	Acc		0.700		0.885					0.854	-3.5	22.0	22.0
Wagner et al. [2011]	Acc	0.480	0.510		0.420					0.550	7.8	14.6	31.0
Walter et al. [2011]	Acc		0.764				0.722			0.778	1.8	7.8	7.8
Wang and Guan [2005]	Acc	0.493	0.664							0.700	5.4	42.0	42.0
Wang and Guan [2008]	Acc	0.493	0.664							0.700	5.4	42.0	42.0
Wanget al. [2013]	Acc							969.0	0.658	0.774	7.7	22.4	22.4
Wimmer et al. [2008]	Acc	0.611	0.737							0.818	11.0	33.9	33.9
Wöllmer et al. [2010]	Acc	0.497	0.511							0.672	21.6	48.3	48.3
Wöllmer et al. [2013a]	Acc	0.545	0.596							0.616	8.0	17.1	17.1
Wöllmer et al. [2013b]	Acc	0.612	0.644	0.730						0.720	-1.4	11.8	17.6
Wu and Liang [2011]	Acc		0.800	0.809						0.836	3.3	4.4	4.4
Zeng et al. [2005]	Acc	0.390	0.69.0							0.750	8.7	92.3	92.3
Zeng et al. [2006]	Acc	0.862	0.701							0.899	4.3	28.2	28.2
Zeng et al. [2007]	Acc	0.386	0.664							0.724	9.0	87.6	87.6

Notes: Measure (Acc = Percent correct; CC = correlation coefficient; F1 = F measure), UM (PPhy = peripheral physiology; CPhy = central physiology; Content = Content/Context); MM = MM accuracy; MM Effect Size (MM1 and MM2 = percent MM improvement over best and second-best UM, respectively, MMMin = percent MM improvement over worst UM).

scores, or correlation coefficients to quantify performance.

MM1 effect =
$$100 * \frac{a_{12} - \max(a_1, a_2)}{\max(a_1, a_2)}$$
. (1)

In addition to the MM1 effect, MM2 and MMMin effects were also computed as the percent MM improvement over the second-best and worst UM detectors. These are important metrics to test for inhibition effects, which occur when MM accuracies are lower than underperforming UM detectors.

It is important to note three points about the data presented in Table II. First, accuracy scores associated with the best-performing detector were used when *multiple detectors* or *multiple fusion techniques* were considered for the *same* classification task. For example, Soleymani et al. [2012] reported both feature-level and decision-level MM accuracies. Decision-level fusion yielded higher accuracies, so only decision-level fusion results were used in the subsequent analyses.

Second, several studies performed *multiple discriminations* on the same set of affective states. For example, D'Mello and Graesser [2010] developed one classifier to predict four affective states and another to predict an overlapping but different set of five affective states. Similarly, the study by Eyben et al. [2011] contributed five data points by independently predicting five affect dimensions (i.e., activation, expectancy, intensity, power, and valence). In general, one data point was obtained for the studies that performed a categorical classification. It was the dimensional studies that contributed multiple data points because the number of models increases proportional to number of dimensions considered. In all, data from 124 classification tasks was obtained. These 124 data points were reduced to the 90 shown in Table II after the aggregation procedure discussed next.

Third, when *multiple* classification tasks on the *same* dataset were performed, the one closest to real-world performance was retained. For example, if text-based models were built on automatically recognized and human-transcribed speech (e.g., Litman and Forbes-Riley [2006b]), then the former was analyzed. Similarly, person-independent validation results were used when both person-dependent and person-independent validation methods were reported (e.g., D'Mello and Graesser [2010]). For the same reason, event-level or segment-level analyses with a temporal resolution in seconds were preferred over frame-level analyses with a temporal resolution in milliseconds because affective phenomena operate across a coarser time span ranging from a few seconds to tens of seconds [D'Mello and Graesser 2011; Rosenberg 1998].

2.4. Data Treatment

Data from 124 classification tasks were subjected to aggregation, winsorization, and standardization procedures as noted in the following.

Aggregation. Studies that performed multiple classification tasks on the same dataset would bias the results and would violate independence assumptions of the inferential statistical analyses applied to the data. Therefore, the data reported in Table II consists of average scores across multiple classification tasks on the same dataset. For example, the five correlation coefficients from the Eyben et al. [2011] study discussed previously were averaged to yield one data instance. Studies that reported multiple classification tasks on different datasets were analyzed as separate data instances (e.g., Rosas et al. [2013] where results corresponding to two distinct datasets were reported in the same article).

Winsorization (Outlier Treatment). An examination of the MM, Max1, Max2, and Min accuracy distributions did not yield any outliers, which, following standard conventions, were defined as values exceeding three standard deviations from the mean. However, the MM1, MM2, and MMMin effects yielded two, one, and two outliers,

respectively. These outliers were replaced with the values corresponding to three standard deviations from the means of each distribution (60.7% \rightarrow 55.5%; 91.9% \rightarrow 55.5% for MM1 effect; 275% \rightarrow 168% for MM2 effect; and 217% \rightarrow 182% and 275% \rightarrow 182% for MM-Min effect), akin to a Winsorization procedure [Tukey and McLaughlin 1963], which is a widely used technique for outlier treatment. Paired-sample t-tests on the distributions before and after outlier replacement did not yield significant differences (p > 0.10) for any of the three MM effects, thereby indicating that this method of treating outliers had no unintended effects.

Standardization. The three MM effects represent percent improvements over a baseline, so they are not sensitive to differences in accuracy metrics. However, raw detector accuracy scores were quantified in terms of percent correct (recognition accuracy), correlation coefficient, or F1 measure. These different metrics raised issues for the statistical methods used to analyze the raw detection accuracy scores (Max1, Max2, and Min). Hence, these measures were standardized (i.e., z-scores were computed) within each metric prior to the analyses.

3. RESULTS AND DISCUSSION

The results are presented with respect to the three major research questions listed in the Introduction: (a) What are the major trends in contemporary MM affect detectors? (b) What is the added improvement (if any) of MM affect detection accuracy (MM1 effects) over the best UM detectors? (c) Can we identify system-level factors identified in (a) that are predictive of MM1 effects analyzed in (b)?

It is useful to clarify our terminology before proceeding. *System* and *study* are used to refer to a multimodal affect detector (system) and its validation (study). *Effects* refer to percent improvement in MM accuracies over UM accuracies (MM1, MM2, and MMMin effects), while *accuracies* refer to affect detector performance represented as z-scores following metric-level standardization of percent correct, F1, and correlation coefficient (see Section 2.4).

3.1. Major Trends in MM Affect Detectors

Table III lists descriptive statistics on the various system-level factors described in Section 2.2.

Data Sources. We note that on average MM detectors were constructed from affective data from 21.2 participants (not shown in Table III). There was also considerable variability (SD = 37.8) in the number of participants used for model building, ranging from a single participant [Busso et al. 2004; Haq et al. 2008] to 343 participants [Wöllmer et al. 2013b]. An examination of the distribution indicated that 25% of the studies had five participants or fewer, 50% had 12 participants or fewer, and 97% of studies had fewer than 50 participants.

The data also indicated that the MM detectors were more likely to be trained on actor-portrayed affective displays (>50% of studies) rather than on more spontaneous expressions that were either experimentally induced or naturally occurred.

Affect Models. As is evident in Table III, approximately two thirds of the affect detectors focused on discrete (or categorical) affect models and performed classification tasks. Even though one third of the studies used dimensional models of affect, only 7.8% performed regressions. This was because several studies either collected categorical measures of affect dimensions (e.g., low or high arousal) or discretized continuous measures (e.g., via median splits or by applying clustering). On average, the classifiers discriminated 4.71 affective states (SD = 2.28; median = 4 states), with a minimum of 2 and a maximum of 12 (not shown in Table III). The results also revealed that approximately one third of the affect detectors exclusively focused on discriminating the basic emotions, while less than 10% primarily focused on nonbasic emotions. Even

Dimension	Prop.	Dimension	Prop.
Data type		Measure. model	
Acted	0.522	Disc.	0.644
Induced	0.278	Dim.	0.356
Natural	0.200		
Detection model		Affect detected	
Classification	0.922	Disc. basic	0.367
Regression	0.078	Disc. nonbasic	0.078
		Disc. mixed	0.178
No. of modalities		Dim. simple	0.278
Bimodal	.867	Dim. complex	0.100
Trimodal	.133		
		Fusion method	
Modality		Feature	0.389
Face	0.767	Decision	0.356
Voice	0.822	Hybrid	0.056
Text	0.167	Model	0.200
Body	0.133		
Eye Gaze	0.011	Validation method	
Peri. physio.	0.111	Person indep.	0.378
Central physio.	0.056	Person dep.	0.622
Content	0.067		

Table III. Descriptive Statistics on Study Features

Notes: Prop. = Proportion; Peri = Peripheral; Physio. = Physiology; Content = Content/Context; Measure. = Measurement; Disc. = Discrete; Dim. = Dimensional; Indep. = Independent; Dep. = Dependent.

though 17.8% of the studies included a mixture of basic and nonbasic emotions, these studies mainly focused on basic emotions with one or two nonbasic emotions. Hence, more than 50% of the studies had a primary focus on the basic emotions.

The two primary dimensions of valence and arousal dominated the dimensional models (approximately 30% of studies) with 10% of studies modeling more complex dimensions. In all, 48 affective states (including dimensions) were modeled in the 90 studies (not shown in Table III). Only nine of the 48 affective states (18.8%) appeared in more than 5% of the studies, and these nine states collectively accounted for 76% of the states detected across all studies. The nine frequent states were (a) the six basic emotions—anger (12%), sadness (11%), happiness (9%), fear (7%), disgust (7%), and surprise (7%); (b) the two primary dimensions of valence (8%) and arousal (7%); and (c) the state of no apparent feeling (8%) or neutral.

Modalities. The face and voice were the most commonly used modalities, each occurring in over 75% of the studies. Text, body movements, and peripheral physiology were individually used in at least 10% of the studies. Eye gaze, central physiology, and context/content models were relatively infrequent.

Fifteen unique MM combinations were noted in the 90 studies. Of these, most were bimodal (86.7%) systems, while a handful were trimodal systems. Audiovisual systems (face + voice) comprised 55.6% of the MM systems, followed by speech + text (11.1%) and face + speech + text (5.6%). These three combinations accounted for 72.3% of the systems. In addition, voice + peripheral physiology, face + body movements, and face + voice + body movements each accounted for 4.4% of the MM systems. In all, these six MM combinations accounted for 85.6% of the systems, while the remaining nine combinations were quite infrequent (each observed in <4% of the studies).

Fusion Methods. Several studies tested multiple fusion methods, so it was difficult to accurately estimate if a particular method was used more frequently than others.

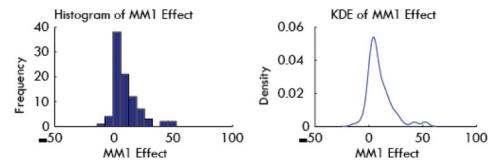


Fig. 1. Histogram (left) and kernel smoothing density estimation (right) of distribution of MM1 effects.

When multiple methods were used in the same study, we only recorded the method that yielded the best performance, because the final detector would presumably use the best-performing method. As noted in Table III, feature-level and decision-level fusion were dominant and were collectively observed in approximately 75% of the studies. Model-level fusion was somewhat less frequent (20%), but occurred at nontrivial rates. Data-level fusion was nonexistent and hybrid fusion was rare.

The most common feature-level fusion strategy simply involved concatenating feature vectors from individual modalities (e.g., D'Mello and Graesser [2010] and Forbes-Riley and Litman [2004]) with or without feature selection. The decision-level fusion methods usually relied on simple voting rules (e.g., Dy et al. [2010] and Gajsek et al. [2010]), but more nuanced ways of decision making were also proposed. Some of these include metadecision trees [Wu and Liang 2011], cascading specialists [Kim and Lingenfelser 2010; Wagner et al. 2011], Kalman filters [Glodek et al. 2013], Bayesian belief integration [Chanel et al. 2011], and Markov decision networks [Krell et al. 2013]. There was considerable variation in model-level fusion methods, but bidirectional long short-term memories [Eyben et al. 2010; Metallinou et al. 2012; Wöllmer et al. 2010, 2013a], various HMM-based approaches (error-weighted semicoupled HMMs [Lin et al. 2012], multistream HMMs [Zeng et al. 2005, 2007], boosted multistream HMMs [Zeng et al. 2006], boosted coupled HMMs [Lu and Jia 2012]) and Bayesian-based approaches (e.g., Jiang et al. [2011], Paleari et al. [2009], Sebe et al. [2006], and Wang et al. [2013]) were most prominent.

Validation Methods. Tenfold cross-validation at the segment (or frame) level was the most popular validation method. This method was used in 62.2% of the studies. This validation method is problematic when the goal is to build person-independent models (which is usually the goal), since instances from the same individual are in both the training and testing sets. In contrast, leave-one-subject-out or leave-several-subjects-out validation methods guarantee training and testing independence, but were used with considerably less frequency (37.8% of studies).

3.2. MM Effects and Accuracy

The data were analyzed in terms of (a) MM improvement over best UM accuracies (MM1 effects), (b) MM improvement over second-best (MM2 effects) and worst (MMMin effects) UM accuracies, and (c) relationships between UM and MM accuracies.

Overall MM Effects (MM1 Effect). The distribution of MM1 effects is presented in Figure 1. A one-sample t-test indicated that the mean MM1 effect of 9.83% significantly differed from zero, t(89) = 8.08, p < 0.001, d = 0.85 sigma (large effect¹). This suggests

¹Cohen's d is a common effect size statistic in standard deviation units (sigma) between two samples with means $\overline{M_1}$ and $\overline{M_2}$ and standard deviations $\overline{s_1}$ and $\overline{s_2}$ [Cohen 1992]. According to Cohen, effect

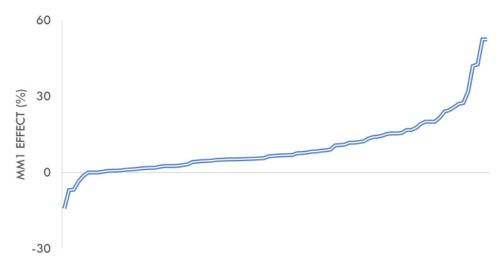


Fig. 2. MM1 effects (Y axis) by study number (X axis) ordered by effect size (ascending order).

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	Number of	Percent of	Cumulative
Group	Studies	Studies (%)	Percent (%)
$\overline{\mathrm{MM1}} \leq -1$	5	5.56	5.56
$-1 < MM1 \leq 1$	8	8.89	14.4
$1 < MM1 \leq 5$	21	23.3	37.8
$5 < MM1 \leq 10$	23	25.6	63.3
$10 < MM1 \leq 20$	20	22.2	85.6
$20 < MM1 \leq 30$	8	8.89	94.4
MM1 > 30	5	5.56	100.0

Table IV. Grouping of MM1 Effects

that, on average, the MM detectors yield positive improvements in performance compared to the best UM detectors.

There was considerable variance in the MM1 effect distribution. MM1 effects ranged from -14.2% to 52.5% with a standard deviation of 11.5%. The large range and the fact that the standard deviation was greater than the mean, suggests that the *median value of* 6.60% might provide a more accurate estimate of the central tendency of the distribution than the mean.

To examine the distribution of MM1 effects more closely, we sorted the distribution (see Figure 2), divided it into several categories of practical interest (see Table IV) and computed the percent of studies falling into each category. This analysis indicated that 14.4% of the studies either yielded negative or negligible ($\leq 1\%$) MM1 effects. Results for the remaining 85% of the studies were much more positive in that roughly half of the studies yielded either small 1%–5% or medium-sized (5%–10%) MM1 effects. Approximately 35% of the studies yielded impressively large effects (> 10%).

MM2 and MMMin Effects. MM2 and MMMin effects are identical for the studies that only considered two modalities (87% of studies), yet we analyze these effects separately because there were some subtle differences in their distributions. MM2 effects ranged from 4.40% to 168.4% with an impressive mean of 40.0% (SD = 36.9%). MMMin effects had a mean of 43.7% (SD = 40.0%) and a range of 4.40%–182.3%. Given the large

sizes approximately equal to 0.3, 0.5, and 0.8 represent small, medium, and large effects, respectively. $d = (M_1 - M_2) / \sqrt{\frac{s_1^2 + s_2^2}{z}}.$

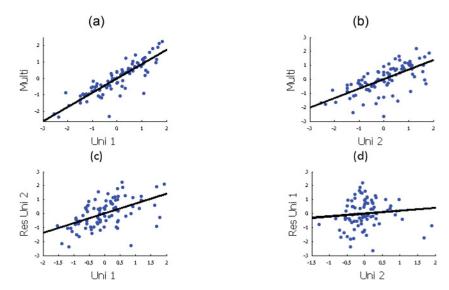


Fig. 3. Scatter plots denoting relationships between MM and UM accuracy along with regression line for (a) regression of MM (Multi) on best UM (Uni 1) accuracy; (b) regression of MM (Multi) on second-best UM (Uni 2) accuracy; (c) same as (a) but after controlling for second-best UM accuracy; and (d) same as (b) but after controlling for best UM accuracy.

standard deviations, the median values of 27.9% and 29.4% for MM2 and MMMin effects, respectively, might be a more accurate summary statistics of these distributions. One-sample t-tests indicated that the mean MM2 effect significantly differed from zero, $t(89)=10.3,\ p<0.001,\ d=0.1.08$ sigma, as did the mean MMMin effect, $t(89)=10.4,\ p<0.001,\ d=1.09$ sigma. Furthermore, paired samples t-tests indicated that the mean MM2 effect was significantly, $t(89)=8.18,\ p<0.001,\ and$ substantially t(d=1.11) sigma) greater than the mean MM1 effect (9.83%) A similar finding was discovered when MMMin effects were compared to MM1 effects, $t(89)=8.59,\ p<0.001,\ d=1.15$ sigma. In general, MM2 and MMMin effects were approximately four times greater than MM1 effects, so MM detectors were substantially more accurate than their less effective UM counterparts.

Relationships between UM and MM Accuracies. There was a very robust correlation between best UM and MM accuracies, r(88) = 0.870, p < 0.001. The correlation between second-best UM and MM accuracies was notable, but smaller, r(88) = 0.681. Best and second-best UM accuracies were also strongly correlated, r(88) = 0.725, p < 0.001.

We simultaneously regressed MM accuracy (dependent or predicted variable) on best and second-best UM accuracies (independent or predictor variables). The model was significant, $F(2,87)=139.7,\ p<0.001,$ and explained a robust amount of the variance, $R^2=0.763$; $R^2=3.22$. The best UM accuracy was a significant predictor ($R^2=0.795,\ p<0.001$) but second-best UM accuracy was not ($R^2=0.104,\ p=0.174$). This indicates that much of the variance in MM accuracy can be explained by the best UM accuracy.

These patterns are shown in Figure 3, where we note that the linear relationship between MM and best UM accuracy (Figure 3(a)) is retained after controlling for second-best UM accuracy (Figure 3(c)). However, the linear relationship between MM and

 $^{^2}R^2$ or the coefficient of determination is used to assess goodness of fits of regression models. Using Cohen's recommended conventions [Cohen 1992], effect sizes are expressed as Cohen's $\overline{f^2 = \frac{R^2}{1-R^2}}$ and values of 0.02, 0.15, and 0.35 are taken to signify small, medium, and large effects, respectively.

second-best UM accuracy (Figure 3(b)) essentially disappears after controlling for best UM accuracy (flat line in Figure 3(d)).

Hence, the final model simply consisted of predicting MM accuracy from best UM accuracy. This model was significant, F(1,88) = 274.8, p < 0.001, and robust, $R^2 = 0.757$, $f^2 = 3.12$. The standardized model coefficient (β weight) was 0.870, which indicates that a 1 unit (in standard deviation units) increase in best UM accuracy results in a 0.870 unit increase in MM accuracy.

To address the question of whether this regression model generalizes to new studies, we performed a between-study 10-fold cross-validation analysis, which yielded an R^2 of 0.746, which was very similar to R^2 on the entire training set (0.757). The very small discrepancy of 0.011 suggests that the regression model is expected to generalize to new studies.

There is the question of whether MM accuracy increases, decreases, or remains unchanged as a function of the difference between best and second-best UM accuracies. To address this question, we retained the residuals (prediction errors or unexplained variance) after regressing best on second-best UM accuracies. MM accuracy was then regressed on the residual. The resultant model was significant and explained a modest amount of variance, F(1,88) = 37.6, p < 0.001, $R^2 = 0.299$, $f^2 = 0.43$, $\beta = 0.574$. This finding suggests that MM accuracy improves in relation to the difference between best and second-best UM accuracies. Put simply, MM accuracy was higher when UM accuracies were more independent.

3.3. Moderation Analysis

Section 3.1 analyzed general trends in the design of MM affect detectors (system-level factors) while Section 3.2 quantified performance in terms of MM effects. In this section, we assess whether the system-level factors can predict MM performance.

The analyses proceeded by independently regressing MM1 effects and MM accuracy on the eight system-level factors listed in Table III plus the number of participants and number of affective states (10 total). Eight out of these 10 factors were categorical variables, so these were dummy coded prior to constructing the models. It was not possible to consider every unique modality combination given that there were 15 modality combinations and only 90 data points. However, since 55.6% of the modality combinations were face + voice, we created a new indicator variable and coded it as a 1 for face + voice and a 0 for other modality combinations. Furthermore, given that only five studies reported hybrid fusion, these studies were removed prior to constructing the model for fusion method.

Predicting MM1 Effects. The resultant models for predicting MM1 effects are shown in Table V, where k is the number of studies used to construct each model. F is the test statistic for model significance (p value is in parentheses) and R^2 is the measure of model fit. Significant (p < 0.05) models were discovered for data type, number of affective states, and classifier fusion method, but not for the remaining seven factors.

The significant model for data type yielded a small- to medium-sized effect ($f^2 = 0.087$). A test of model coefficients indicated that MM1 effects for detectors built from natural data were statistically equivalent to those built from induced data (p = 0.299), but were significantly (p = 0.009) lower than detectors built from acted data. The induced models yielded quantitatively lower MM1 effects than the acted models, but the difference was not quite significant (p = 0.102). These patterns are graphically depicted in Figure 4(a), where we note a negative linear relationship between MM1 effects and authenticity of training and validation data (mean MM1 effects = 12.7%, 8.19%, and 4.59% for acted, induced, and natural data, respectively). More precisely, if data type is numerically coded along an authenticity dimension, with 1, 2, and 3

		Significance and	Fit
Dimension	k	F(p)	R^2
Number of participants	88	0.004 (0.947)	0.000
Data type	90	**3.80 (0.026)	0.080
Affect representation model	90	1.25(0.267)	0.014
Affect detection model	90	0.329(0.567)	0.004
Affect states detected	90	0.828(0.511)	0.037
Number of affective states	83	**6.77 (0.011)	0.077
Number of modalities	90	1.02 (.316)	.011
Modality (face + voice vs. other)	90	2.08 (.153)	.023
Fusion method	85	**4.96 (0.009)	0.108
Validation method	90	0.133(0.716)	0.002

Table V. Regression Models for Predicting MM1 Effects

Note: **denotes significant models at the p < 0.05 level.

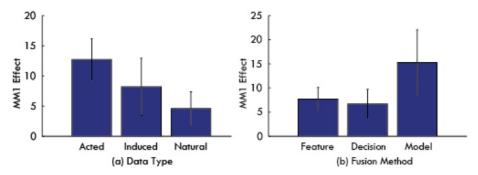


Fig. 4. Mean MM1 effect by (a) data type and (b) fusion method. Error bars are 95% confidence intervals.

representing acted, induced, and natural data, respectively, then there is a negative -0.245 (p = 0.020) correlation between data authenticity and MM1 effects.

The results also indicated that MM1 effects could be predicted from the number of affective states in the 85 studies that built classifiers instead of regressors. This model also yielded a small- to medium-sized effect ($f^2 = 0.083$). Interestingly, the number of affective states was a positive predictor ($\beta = 0.278$), so MM1 effects improved when more affective states were considered. One tentative interpretation of this finding is that the classification problem becomes more difficult when more affective states are considered and the additional modalities have more to contribute in this situation.

The third significant model had MM fusion type as the predictor and also yielded with a small- to medium-sized effect ($f^2=0.121$). An analysis of the model coefficients indicated that MM1 effects associated with feature- (M=7.73%) and decision-level (M=6.68%) fusion were statistically equivalent (p=0.661), but were lower than MM1 effects for model-based fusion (M=15.3%, p<.05; see Figure 4(b)). This finding should be interpreted with caution because it does not represent direct comparisons of different fusion techniques on the same datasets and classification tasks. Instead, it simply suggests that, on average, model-level fusion yielded higher MM1 effects than feature-level and decision-level fusion.

Predicting MM Accuracy. In Section 3.2, we reported that 75.7% of the variance in MM accuracy was explained by the best UM accuracy. We investigated if this model could be improved by adding system-level factors. The analyses proceeded by testing if each system-level factor explained unique variance in MM accuracy after accounting for best UM accuracy (our previous model). This was accomplished with 10 hierarchical linear regressions with UM accuracy as the predictor for the Step 1 models and each

system-level factor as individual predictors in the Step 2 models. A significant change in \mathbb{R}^2 from Step 1 to Step 2 would indicate that the system-level feature under consideration explained additional variance in MM accuracy above and beyond best UM accuracy.

The results yielded significant R^2 changes (ΔR^2) for data type ($\Delta R^2 = 0.034$, p = 0.002), affect representation model ($\Delta R^2 = 0.011$, p = 0.046), number of affective states classified ($\Delta R^2 = 0.025$, p = 0.005), and fusion method ($\Delta R^2 = 0.014$, p = 0.041), but not for number of subjects ($\Delta R^2 = 0.001$, p = 0.633), affect detection model ($\Delta R^2 = 0.00$, p = 1.00), affect states detected ($\Delta R^2 = 0.019$, p = 0.144), number of modalities ($\Delta R^2 = 0.00$, p = 0.936), modality (face + voice vs. other: $\Delta R^2 = .009$, p = .068), and validation method ($\Delta R^2 = 0.06$, p = 0.137).

Examining coefficients of models with significant ΔR^2 indicated that (a) detectors developed from induced and natural affect had MM accuracies that were on par but significantly (p < 0.01) lower than detectors developed from acted data, (b) detectors that used discrete affect models yielded significantly (p = 0.043) higher accuracies than their dimensional counterparts, (c) MM accuracies increased (p = 0.005) when more affective states were classified, and (d) model-level fusion resulted in significantly (p < 0.05) higher MM accuracies than feature- and decision-level fusion.

Next, we created a model that predicted MM accuracy when these four key factors (data type, affect representation model, number of affective states, and fusion method) were considered simultaneously. This model was constructed using a forward feature selection approach, where features were incrementally added if they improved model fit. It should be noted that due to missing data (elimination of five studies that used hybrid fusion and number of states not applicable in the seven studies that developed regressors), this model was constructed from 78 out of the 90 studies. The Step 1 model on these 78 studies with the best UM accuracy as a predictor yielded an $R^{\bar{2}}$ of 0.796 (note the difference from the $0.757 R^2$ reported earlier on all 90 studies). The Step 2 model had an R^2 of 0.832, which represented a significant improvement ($\Delta R^2 = 0.036$, p = 0.014) from the Step 1 model. The significant predictors that were retained by forward feature selection were best UM accuracy ($\beta = 0.879$, p < 0.001), whether the training data was acted (coded as 1) or not (coded as 0) ($\beta = 0.138$, p = 0.006), and whether model-level fusion (coded as 1) was used in lieu of feature and decision fusion (coded as 0) ($\beta = 0.122$, p = 0.014). Finally, 10-fold cross-validation yielded an R^2 of 0.803. The very small discrepancy of 0.029 from R^2 on entire training data is suggestive of excellent generalizability of the final model.

4. GENERAL DISCUSSION

Timely surveys that synthesize research are critical in any burgeoning research area. The qualitative nature of surveys can be complemented with quantitative meta-analyses, an invaluable scientific tool for approximating a population variable from effects obtained in individual studies that vary along multiple dimensions [Borenstein et al. 2009]. In this article, we identified 90 contemporary MM affect detectors from the peer-reviewed literature, coded and descriptively analyzed each detector along 10 dimensions, performed a meta-analysis on MM accuracy as compared to UM accuracy (MM effects), and identified important system-level moderators of MM1 effects. In this section, we summarize our major findings along with their applied implications, discuss their theoretical implications, address limitations, offer recommendations for future work, and make concluding remarks.

4.1. Major Findings and Applied Implications

The major findings are organized with respect to the three research questions listed in the Introduction: (a) identifying major trends in MM affect detectors, (b) analyzing

MM effects and MM accuracy, and (c) identifying the factors that moderate MM effects and accuracies.

Major Trends in MM Affect Detectors. The first surveys on automated affect detection emerged over a decade ago [Cowie et al. 2001; Pantic and Rothkrantz 2003]. According to these pioneering surveys, and at the risk of overgeneralization, the state of the art in affect detection in 2003 and earlier could be summarized as "the use of basic signal processing and machine learning techniques, independently applied to still frames (but occasionally to sequences) of facial or vocal data, to detect exaggerated contextfree expressions of a few basic affective states that are acted by a small number of individuals with no emphasis on generalizability." Based on the present analysis, subjective interpretation, and somewhat overgeneralization, the 2013 state of the art can be summarized as "the use of basic and advanced signal processing and machine learning techniques, independently and jointly applied to sequences of primarily facial and vocal data, to detect exaggerated and naturalistic context-free and context-sensitive expressions of a modest number of basic affective states and simple dimensions that are acted or experienced by a modest number of individuals with some emphasis on generalizability." The italicized items in the previous summary reflect important changes in the state of the art from 2003 to 2013. Based on this comparison, it is clear that considerable progress has been made, although there is still more to be done. We discuss some of the remaining issues with respect to the following four aspects: authenticity, utility, scope, and generalizability.

Authenticity refers to the naturalness of training and validation data and is directly related to the extent to which an affect detector developed in the lab can be applied in the real world. The fact that more than 50% of the affect detectors were based on acted data is of some concern since spontaneous and acted expressions differ in surprising ways. A striking example is a study that found that individuals rarely smile when generating posed expressions of frustration, but smiles were discovered in 90% of instances of spontaneous frustration [Hoque and Picard 2011].

Utility refers to whether the affect detectors can be expected to be useful in real-world contexts. Assuming that detection accuracy will eventually be sufficiently accurate, the question is whether the affective states that are detected are relevant in the real-world contexts of use (e.g., editing a word document on a computer). This is a critical issue since more than 50% of the studies primarily focused on detecting the basic emotions of anger, sadness, fear, frustration, disgust, and surprise. This is a bit unfortunate because it has been asserted that many interactions with computers and even human-human interpersonal communication rarely involve the basic emotions [Cowie et al. 2005; Zeng et al. 2009]. Some recent evidence for this assertion can be found in a meta-analysis on 24 studies that collectively tracked the emotions of over 1,700 students during interactions with a range of learning technologies [D'Mello 2013]. The major finding was that engagement, confusion, boredom, curiosity, frustration, and happiness were the most frequent affective states. With the exception of happiness, which occurred with some frequency, the basic emotions were rarely observed in over 1,200 hours of interaction.

Scope (in this context) simply refers to the landscape of configurations that were covered by the affect detectors. In addition to the basic versus nonbasic emotion imbalance discussed previously, perhaps the greatest disparity emerges in the modality combinations. More specifically, the eight modalities identified in Table III afford 28 and 56 unique bimodal and trimodal combinations, respectively. However, only 15 out of the possible 84 (28 + 56) combinations (17.9%) were observed at least once in the data. Six of these (7.14% of possible combinations) were represented in more than 85% of the studies, while the face + voice, which represents a mere 1.19% of possible modality combinations, was the focus of more than half of the studies. Indeed, the explored

MM space is sparse and there is both the room for and the need to consider different modality combinations.

Generalizability pertains to an affect detector's ability to maintain its level of accuracy when applied to new individuals and to new or related contexts. One way to facilitate generalizability is to collect training data in diverse contexts and from a large number of individuals. There is clearly more work to be done in this respect since 97% of the studies collected training and validation data from fewer than 50 individuals and usually in a single context (e.g., watching videos, interacting with a specific interface). Generalizability across the individual can be assessed via person-independent models, where training and validation data are completely independent. As noted in Table III, about 40% of the studies used person-independent validation methods, so there is some confidence on their generalizability (across individuals). Unfortunately, no clear case for generalizability can be made for the remaining 60% of studies that used persondependent validation methods. Furthermore, no notable efforts were made to assess generalizability across tasks, situational contexts, datasets, and cultures. This is particularly important since emerging data suggests that models trained on individuals from one demographic do not necessarily generalize to another [Ocumpaugh et al. 2014].

MM Effects and Accuracy. A number of important conclusions can be drawn from the analysis of MM effects and MM and UM accuracies. Over 85% of the studies resulted in MM1 effects greater than at least 1%. This provides important evidence that MM classifiers do outperform their best UM counterparts. The sizes of the mean (9.83%) and median (6.60%) MM1 effects resemble modest improvements over UM accuracy. Importantly, however, MM1 effects associated with detectors trained on naturalistic data (4.59%) were three times lower than detectors trained on acted data (12.7%). Since the ultimate goal of affect detection is to sense naturalistic affective expressions, the modest 4.59% effect might represent a more accurate estimate of state-of-the-art multimodal affect detection improvement.

The question of whether this modest improvement in accuracy obtained by MM systems is worth their increased complexity is a question that is best addressed at the application level. It should also be noted that the present study only evaluated MM detectors from a single dimension, namely, performance improvements over UM detectors. However, MM detectors have additional advantages, such as providing higher fidelity models of affect expression and the ability to address missing data problems that can cripple UM detectors. Furthermore, the analysis that focused on assessing MM performance improvements over the second-best and worst UM classifier indicated that although combining modalities yields modest improvements in affect detection accuracies, considering multiple individual modalities can have a major impact on performance. This is because performance would be severely impacted if only one modality was modeled and in the worst case if it always happened to be the lower performing modality.

Turning back to MM1 effects, one reason for their relatively modest size, especially for the systems trained on more naturalistic data, is that there might be considerable redundancy among the different modalities. Strong correlations among the best UM, second-best UM, and MM accuracies provide some evidence to support this view. Evidence for redundancy among modalities can also be obtained by the fact that the best UM accuracies predicted 75.7% of the variance in MM accuracies and this finding generalizes to new studies. Impressive MM1 effects are not expected if the different modalities convey similar information, albeit in different ways. The analysis that found that MM accuracies increased when UM accuracies were more dissimilar provides some evidence in support of this claim.

The lower multimodal effects for natural emotional expressions compared to acted expressions might also be attributable to several differences among the two. In particular, some aspects of acted expressions that are conducive to multimodal effects include increased intensity (since they are usually exaggerated), decreased variability (since they are generated out of context), increased coordination between different modalities (since prototypical emotions are invoked), and increased specificity (since there is lower likelihood of multiple emotions being experienced) [Barrett 2006; Russell 2003].

Factors that Moderate MM Effects. We examined 10 system-level factors and identified three that moderated MM1 effects. We discovered that MM1 effects were positively impacted by acted data (vs. induced or natural data), number of affective states classified, and when model-level modality fusion methods were used (vs. feature or decision level). Two out of these four system-level factors (acted vs. nonacted data and model-level vs. non-model-level fusion) yielded a 3.6% improvement in predicting MM accuracy over best UM accuracy. Furthermore, fit of the final model with all three predictors was excellent (\mathbb{R}^2 of 0.832), and generalizes to new studies as verified with a 10-fold study-level cross-validation analysis.

The final model, specified in Equation (2), can be used by researchers to predict expected multimodal classification accuracy (proportion of cases correctly classified ranging from 0 to 1) prior to even constructing the classifiers. Best unimodal accuracy is the classification accuracy (as a proportion ranging from 0 to 1) of the best UM detector. Data type acted is an indicator variable set to 1 for acted data and 0 for induced data. Model-level fusion is also an indicator variable set to 1 for model-level fusion and 0 for feature- and decision-level fusion.

MM accuracy =
$$0.900 \times \text{Best unimodal accuracy} + 0.273 \times \text{Data type acted} + 0.312 \times \text{Model level fusion} - 0.253$$
 (2)

4.2. Theoretical Implications

The fact that combining MM accuracies yielded modest improvements has important implications for psychological theories of emotion. These theories in turn guide much of the affect detection models, so alignment of our findings with emotion theory has implications for next-generation affect detection systems.

The classical model of emotion, which was proposed by Tomkins [1962], Ekman [1992], and Izard [2007], and others, posits that discrete "affect programs" produce the physiological, behavioral, and subjective changes associated with a particular emotion. According to this theory of "basic emotions," there is a specialized circuit for each basic emotion in the brain. Upon activation, this circuit triggers a host of coordinated responses in the mind and body. In other words, an emotion is expressed via a sophisticated synchronized response that incorporates peripheral physiology, facial expression, speech, modulations of posture, affective speech, and instrumental action. This prediction is very relevant to affect detection because it suggests that MM affect detection should be more reliable due to this coordinated recruitment of response systems.

In contrast to this highly integrated, tightly coupled, central executive view of emotion, researchers have recently argued in favor of a disparate, loosely coupled, distributed perspective [Coan 2010; Lewis 2005]. According to this contemporary view, there is no central affect program that coordinates the various components of an emotional episode. Instead, these components are loosely coupled and the specific context and appraisals determine which bodily systems are activated. These models would accommodate the prediction that in most cases a combination of modalities might conceivably yield small improvements in classification accuracies. Hence, other than the rare cases of prototypical emotions, or in artificial experimental contexts involving

acted emotions, modest multimodal effects might be expected. Indeed, this is exactly what was observed in the present analysis.

4.3. Limitations and Future Work

There are five primary limitations to this work. The first pertains to the comprehensiveness of the studies that were analyzed. Our goal was to obtain a reasonably large sample of MM studies rather than attempting to analyze every single study in the literature. This is defendable because one does not need to study an entire population to estimate its parameters. Furthermore, almost all of the tests of statistical significance yielded significant results and we show evidence for model generalizability, thereby suggesting that our sample size of 90 studies was adequate to detect the relatively large effects in our data.

The second limitation was that there was some imbalance with respect to the modalities, data, evaluation metrics, and affective states classified. For example, a majority of the studies we analyzed focused on audio-visual affect recognition, so the results are somewhat biased toward these systems. It is important to note, however, that this imbalance in our study is linked to a similar imbalance in the current state of the art. Specifically, most studies focus on the audio and visual modalities, while central physiology, gaze, and content/context-based sensing are comparatively rare. Peripheral physiological-based affect sensing (i.e., biosignals) are quite common affect detection modalities, but these are not often combined with face, voice, text, and other modalities.

A third limitation that befalls all meta-analyses is the possibility of publication bias. This is because it is likely that the papers that report positive MM1 effects are more likely to be published, and subsequently included in this meta-analysis, than papers that report negligible or negative effects. We suspect that this might not be a severe issue in the present study, since approximately 15% of the studies reported negative or null (<1%) MM1 effects, but there is no clear way to assess publication bias with the present data.

A fourth limitation is that the present study is more consistent with an informal meta-analytic approach rather than a more formal meta-analysis procedure. This was due to a lack of available information needed to perform a formal meta-analysis. More specifically, one of the key steps in conducting a meta-analysis is to inversely weight the effect size with respect to its error, but error estimates on affect detection accuracies were never reported in the papers we analyzed. This also precluded the use of well-established techniques to identify and correct for publication bias like trim-and-fill procedures [Duval and Tweedie 2000].

Fifth, the somewhat large timespan (roughly 10 years) of the studies included in this analysis might also be of some concern since the newer classification and fusion methods were unavailable for some of the older studies. Although the selection procedure did bias newer studies in lieu of older ones, it is possible that the older studies might have yielded better multimodal accuracies if some of the latest multimodal fusion methods were used. However, this does not appear to be a major concern as publication date (normalized so that the earliest study in 2004 was coded as 0, 2005 as 1, and so on) was not correlated with MM1 (r(88) = 0.042, p = 0.696), MM2 (r(88) = 0.056, p = 0.600), or MMMin (r(88) = 0.102, p = 0.338) effects. Nevertheless, it would be informative to reanalyze some of the older datasets with newer methods to ascertain if the use of newer techniques results in performance improvements.

4.4. Recommendations for Future Systems

In this section we list some guidelines based on our analysis of the 90 multimodal detectors. These should be considered to be general recommendations since decisions should ultimately be guided by specific application contexts. Some of these suggestions

might seem obvious; however, they are noted here since some or all were ignored in more or less all of the studies.

First, there is a tradeoff between accuracy and authenticity in that highly accurate results are usually obtained in nonauthentic contexts, specifically building persondependent models to detect acted expressions recorded in ideal conditions. Lower accuracies obtained in more naturalistic contexts are of greater practical value. Second, excellent results without meaningful comparison conditions are of less importance than modest results with stringent comparisons. For example, if a new multimodal fusion technique is being proposed, then its improvement over simpler techniques (e.g., naïve feature-level fusion) should be reported. Similarly, classification accuracy (or recognition rate) is a meaningless metric without a baseline comparison when there is an uneven distribution of classes (more on this point follows). Third, only a small subset of the landscape encompassing modalities and affective states has been explored. In addition to refining systems that operate on already-explored areas of this landscape, systems that explore new areas could lead to exciting innovations and discoveries. One suggestion is to focus on different modalities in addition to or in lieu of the face and speech to detect nonbasic affective states that pervade human-computer interactions, such as confusion, frustration, and perhaps even boredom. Fourth, model-level fusion techniques that embrace, rather than ignore, time-varying relationships among different modalities showed significant promise, so it might be useful to channel research efforts into improving these techniques. Fifth, the standard procedure of collecting labeled data to train supervised classifiers is inherently limited due to the manual affect annotation process, thereby resulting in small datasets (in terms of number of unique individuals). It is unlikely that this approach will lead to models that generalize at large [Ocumpaugh et al. 2014]; hence, it might be useful to consider semisupervised learning approaches that only require a small subset of the training data to be annotated. Furthermore, crowd-sourcing techniques might be useful alternatives to current cumbersome annotation methods that simply do not scale to larger datasets [McDuff et al. 2012].

It would also be highly beneficial if there was a more or less standard approach to evaluating and reporting results of affect detectors. Some suggested evaluation criteria include (a) meaningful comparison conditions when new systems are being proposed (as noted previously), (b) using person-independent validation techniques, (c) testing promising affect detectors developed by other researchers on one's own datasets (this was very rare), (d) testing new techniques on multiple datasets (i.e., cross-corpus evaluations), and (e) studying generalizability to individuals of different demographics—also referred to as population validity.

Suggestions on how to report results include reporting of (a) accuracy metrics that correct for uneven distribution of classes, (b) error estimates on accuracy measures, (c) number of individuals and instances, and (d) other information noted in Table III. With respect to the first item in this list, Jeni et al. [2013] recently evaluated a number of classification accuracy metrics by performing simulations as well as analyzing real datasets with imbalanced class distributions (skewed data). Their findings indicated that several of the commonly used metrics, such as accuracy (recognition rate), kappa, F-score, Krippendorff's alpha, and area under the precision-recall curve, were adversely affected by data skew. Area under the Receiver Operating Characteristics (ROC) curve (AUC or A') was most robust to data skew, but tended to minimize poor performance when compared to precision-recall curves. They recommended reporting both original uncorrected performance metrics as well as skew-normalized versions of these metrics with the normalization conducted by up-sampling and down-sampling the *test* partitions (the paper also provides a link to software to compute the skew-normalized statistics).

4.5. Concluding Remarks

The phrase "consistent, but modest under natural conditions" succinctly captures performance of contemporary affect detectors. These MM detectors were consistently better than their UM counterparts, but the improvements were modest when the detectors were trained on naturalistic affect expressions. A fundamental question is whether these findings can be best explained by the method or by the data. In particular, were MM1 effects modest because the detectors are not sufficiently sophisticated to model the intricate nonlinear time-varied relationships between the different modalities? Or were they modest because the training data did not contain adequate expressions of coordination among modalities, thereby rendering even the most sophisticated detectors inept? The field of MM affect detection is too young to currently settle these issues, so an answer awaits further research.

However, there is another possibility beyond the method and the data. It may be the case that the expression of naturalistic emotions is inherently a diffuse phenomenon, which will yield modest effects irrespective of method or data. This suggests that in addition to considering different methods and data sources, it might be useful to consider alternate models of emotion beyond the classic view described in Section 4.2. Thus far, the emphasis has been on the method and the data, at the expense of examining the affective phenomenon itself (i.e., insufficient attention to recent development in emotion theories and alternate models). Perhaps a more balanced approach that combines better data sources and innovative algorithms with more diverse emotion models represents the most promising way forward.

Whatever the case may be, this review and analysis has shown that the field of multimodal affect detection has come a long way from the initial proof-of-concept systems of the past. Skeptics who thought that computers could never sense anything as elusive as affect have repeatedly been proven wrong. Even more significant is the fact that emerging systems go beyond detecting affect by dynamically responding to the sensed affect, thereby closing the so-called affective loop [Conati et al. 2005]. For example, the Affective AutoTutor is an intelligent tutoring system that improves learning gains for low domain-knowledge students by automatically sensing (via a MM analysis of contextual cues, facial features, and body movements) and responding to confusion, frustration, and boredom [D'Mello and Graesser 2012]. UNC-ITSPOKE is a speech-enabled intelligent tutoring system that automatically senses and responds to a learner's uncertainty by modeling acoustic-prosodic and lexical features of students' spoken responses [Forbes-Riley and Litman 2011]. Another example is the Affective Music Player, which strategically selects music to induce specific moods (positive, negative, neutral) on a personalized basis via a predictive psychophysiological model [van der Zwaag et al. 2013]. In general, systems that both sense and respond to affect are continually emerging as documented in a recent edited volume on affective computing [Calvo et al. 2014].

Despite impressive progress, one limitation of most (but not all of these systems) is that they have been tested in lab-based contexts (the Affective Music player is an exception). Hence, the challenge is now to repudiate critics who think that affective systems will forever be resigned to the confines of the lab and will never make it into real-world applications. This will require a concentrated effort to export affect detection out of the lab and into the wild, where one must contend with the dynamic nature and unpredictability of the real world. It is our hope that this will be reflected in the next review of multimodal affect detectors.

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Received June 2013; revised April 2014; accepted September 2014