Overview an Installation of Sage

Basic usag

Interactive shell and scripting

Arithmetic and built-in functions

Applications i various

domains

Number Theo Calculus

Graph plotting

Sage and LTE

More applications and further

Contributing

Questions

## An Introduction to Sage

#### Arvind S Raj

Department of Cybersecurity Systems and Networks Amrita University, India

1 February 2014 / FOSDEM

Overview and Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various

Algebra Number Theory

Graph plotting
Matrix algebra
Sage and LTEX

More applications and further reading

Contributing to Sagemath

Questions'

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains
- 4 More applications and further reading
- 5 Contributing to Sagemath
- 6 Questions?

Overview an Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications i various

Number Theor Calculus Graph plotting Matrix algebra

More application and further

Contributing to Sagemat

Ougetions

- Graduate CS student at Amrita University, India.
- Passionate about computer security and Python.
- Use Sage in Cryptography labs, Mathematics courses and CTF contests.

Overview and Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various

Algebra Number Theory

Graph plotting
Matrix algebra
Sage and LTEX

More applications and further reading

Contributing to Sagemath

Questions'

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains
- 4 More applications and further reading
- **5** Contributing to Sagemath
- 6 Questions?

Overview and Installation of Sage

Basic usage Interactive shell and scripting Arithmetic and built-in functions

Applications invarious domains
Algebra
Number Theory
Calculus
Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions?

#### Installation

- Pre-built binaries for most OS.
- PPA for Ubuntu.
- Packaging efforts underway for Debian and Fedora.
- GPL licensed mathematics software.
- Unified interface to about 90 popular Python libraries.
- Two modes: command(like Python shell) and notebook(web interface).
- Power of IPython shell and Python programming language.
- "sagerc" file: \$HOME/.sage/init.sage or \$SAGE STARTUP FILE.

Overview an Installation of Sage

Basic usage Interactive shell a

Interactive shell ar scripting Arithmetic and built-in functions

Applications i various domains <sup>Algebra</sup>

Calculus
Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions<sup>1</sup>

- 1 Overview and Installation of Sage
- 2 Basic usage
  Interactive shell and scripting
  Arithmetic and built-in functions
- 3 Applications in various domains
- 4 More applications and further reading
- **5** Contributing to Sagemath
- 6 Questions?

Installation of Sage

Interactive shell and scripting

Arithmetic and built-in functions

Applications i

domains
Algebra
Number Theory

Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions?

- Overview and Installation of Sage
- 2 Basic usage Interactive shell and scripting Arithmetic and built-in functions
- 3 Applications in various domains
- 4 More applications and further reading
- **5** Contributing to Sagemath
- 6 Questions?

Overview an Installation o

Basic usage Interactive shell and scripting Arithmetic and

Applications various

Algebra
Number Theory
Calculus
Graph plotting

Matrix algebra
Sage and LaTEX

applications and further reading

Contributing to Sagemat

Questions

- Sage interpreter: IPython shell.
- Sage scripts
  - Similar to Python scripts; .sage extension.
  - import names from sage.all
  - Run as sage <filename> <arguments> like Python.
  - Other possibilities: profiling, compiling sage files(Cython), access C functions directly.

Overview and Installation of Sage

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications i various domains

Calculus
Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions'

- 1 Overview and Installation of Sage
- 2 Basic usage Interactive shell and scripting Arithmetic and built-in functions
- 3 Applications in various domains
- 4 More applications and further reading
- 5 Contributing to Sagemath
- 6 Questions?

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications i various domains

Algebra Number Theory Calculus

Matrix algebra
Sage and LTEX

More applications and further reading

Contributing

Questions?

- General arithmetic supported by an (I)Python shell.
  - ^ is exponent and ^^ is XOR.
  - For integers, / reduces to lowest fraction and // performs integer division.
- Support mathematical functions and constants with arbitrary precision.
  - pi.n(digits=20) = 3.1415926535897932385
  - e.n(digits=25) = 2.718281828459045235360287
  - golden\_ratio.n(prec=60) = 1.6180339887498948
  - $n(\sin(pi/3), prec=60) = 0.86602540378443865$
  - sqrt (263) .n (digits=20) = 16.217274740226854774
  - n(cos(5\*pi/4), prec=60) = -0.70710678118654752

Overview and Installation of Sage

Basic usage Interactive shell ar scripting Arithmetic and built-in functions

Applications in various domains

domai Algebra

Number Theo

Graph plottir Matrix algeb

Sage and LTE

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains

Algebra

Number Theory

Calculus

Graph plotting

Matrix algebra

Sage and LATEX

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview and Installation of Sage

Basic usage Interactive shell as scripting Arithmetic and built-in functions

Applications various domains

Algebra

Number The

Graph plottir Matrix algeb

Sage and LATE

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains Algebra

Number Theory Calculus Graph plotting Matrix algebra Sage and l⁴T⊨X

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview an Installation o Sage

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications i various domains

domains Algebra

Calculus
Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions?

· Factorizing polynomials.

• 
$$factor(x^4 - 15x^3 + 84x^2 - 208x + 192) = (x - 3)(x - 4)^3$$

• 
$$factor(x^3 - 6x^2 + 11x - 6) = (x - 1)(x - 2)(x - 3)$$

- Solving polynomial equations.
  - $solve([x^2 4x + 2 == -1], x) = [x = 3, x = 1]$
  - Solutions to  $x^2 + 3xy + y^2 = 0$  and x y = 4 = [[1.1055728, -2.8944272], [2.8944272, -1.1055728]]
- Use find\_root where solve does not work. Also useful to find solutions in a particular interval.
  - solve(cos(t) == sin(t), t) = [sin(t) = cos(t)]
  - $find\_root(cos(t) == sin(t), 0, pi) = 0.785398163397$

Overview and Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various domains

Number Theory

Matrix algebra

More
applications

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
  - 2 Basic usage
- 3 Applications in various domains

Algebra

**Number Theory** 

Calculus

Graph plotting

Matrix algebra

Sage and LATEX

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview and Installation of Sage

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications various domains <sup>Algebra</sup> Number Theory

Graph plotting Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions

- Modulus: mod(27, 12) = 3 and power\_mod(27, 2, 12) =
- Primality test: *is\_prime*(13) = True, *is\_prime*(15) = False
- prime\_range(1,35) = [2,3,5,7,11,13,17,19,23,29,31].
  - Generator version: primes(1,35)
- primes\_first\_n(11) = [2,3,5,7,11,13,17,19,23,29,31]
- next\_prime(29) = 31 and previous\_prime = 23
- factorial(20) = 2432902008176640000, factor(20) = 2<sup>2</sup> · 5, divisors(20) = [1, 2, 4, 5, 10, 20]
- gcd(10, 15) = 5, lcm(10, 15) = 30

Overview and Installation of Sage

Basic usage Interactive shell as scripting Arithmetic and built-in functions

Applications i various domains

Algebra Number The

Calculus

Graph plotting Matrix algebra

Sage and Ell

applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains

Algebra

Number Theory

Calculus

Graph plotting Matrix algebra Sage and LATEX

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview an Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

domains

Algebra

Number Theo
Calculus

Graph plotting
Matrix algebra
Sage and LTE

More applications and further reading

Contributing to Sagement

Questions<sup>4</sup>

#### Differentiation

- diff(sin(x) + cos(x) = cos(x) sin(x)
- $diff((sin(x^2)^3)) = 6 x cos(x^2) sin(x^2)^2$
- Integration
  - integral(cos(x) sin(x)) = cos(x) + sin(x)
  - $integral(6 * x * cos(x^2) * sin(x^2)^2, x) = sin(x^2)^3$
- Partial differential and solving differential equations also possible!

Overview and Installation of Sage

Basic usage
Interactive shell ar
scripting
Arithmetic and
built-in functions

Applications various domains

Algebra Number Theor

Graph plotting Matrix algebra

Sage and LTE

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains

Algebra

Number Theory

Calculus

Graph plotting

Matrix algebra

Sage and LATEX

- 4 More applications and further reading
  - **5** Contributing to Sagemath



Overview and Installation of

Basic usage
Interactive shell and scripting
Arithmetic and

Applications i

Algebra
Number Theo

Graph plotting Matrix algebra

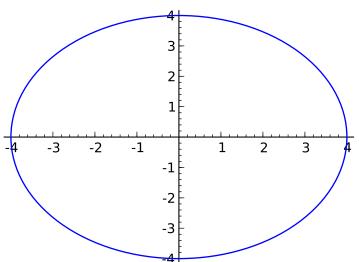
Sage and LTE

applications and further reading

Contributing to Sagement

Questions

Circle of radius 4 centered at (0, 0): c = circle((0, 0), 4)



Overview and Installation of

Basic usage
Interactive shell and scripting
Arithmetic and built in functions

Applications i various domains

Number The

Graph plotting

Sage and P

More

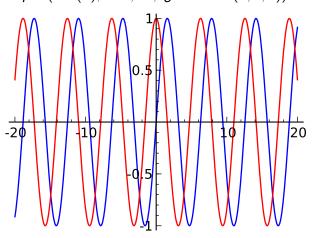
applications and further reading

Contributing to Sagemat

Questions

Multiple functions in same plot.

$$plot(sin(x), -20, 20, rgbcolor = (0, 0, 1)) + plot(cos(x), -20, 20, rgbcolor = (1, 0, 0))$$



# Graph Plotting(cont.)

Arvin

Overview an Installation o

Basic usa

Interactive shell an scripting
Arithmetic and built-in functions

Applications i

Algebra

Number The

Graph plotting

Matrix algebr

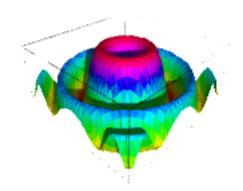
Sage and LTE

application and further reading

Contributing to Sagemat

Questions'

$$f = \frac{\sin(y*y+x*x)}{\sqrt{(x*x+y*y+.0001)}}: plot3d(f, (-3,3), (-3,3))$$



Overview and Installation of Sage

Basic usage
Interactive shell ar
scripting
Arithmetic and
built-in functions

Applications various domains

Algebra Number Theory

Graph plotting Matrix algebra

More applications and further

Contributing to Sagement

Questions?

- 1 Overview and Installation of Sage
  - 2 Basic usage
- 3 Applications in various domains

Algebra Number Theory

Calculus

Graph plotting

Matrix algebra

Sage and LATEX

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview an Installation o Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

various domains Algebra

Algebra
Number Theory

Graph plotting
Matrix algebra

More application and further

Contributing to Sagemath

Questions?

### • Creating matrices: m = Matrix([[1, 2], [3, 4], [5, 6]])

Arithmetic operations

• 
$$P = Matrix([[1,2],[3,4]]), Q = Matrix([[7,8],[5,6]])$$

• 
$$P + Q = \begin{pmatrix} 8 & 10 \\ 8 & 10 \end{pmatrix}$$
,  $P - Q = \begin{pmatrix} -6 & -6 \\ -2 & -2 \end{pmatrix}$ 

• 
$$P * Q = \begin{pmatrix} 17 & 20 \\ 41 & 48 \end{pmatrix}$$
,  $4 * P = \begin{pmatrix} 4 & 8 \\ 12 & 16 \end{pmatrix}$ 

• 
$$P^3 = \begin{pmatrix} 37 & 54 \\ 81 & 118 \end{pmatrix}$$
,  $P^{-1} = \begin{pmatrix} -2 & 1 \\ \frac{3}{2} & -\frac{1}{2} \end{pmatrix}$ ,  $|P| = -2$ 

 More functions: is\_singular, is\_symmetric, is skew symmetric, is invertible, is square

Overview an Installation o Sage

Basic usage
Interactive shell ar
scripting
Arithmetic and
built-in functions

Applications various domains

Algebra Number Theory

Graph plotting

Sage and LATEX

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains

Algebra Number Theory Calculus

Graph plotting

Matrix algebra

Sage and LATEX

- 4 More applications and further reading
- **5** Contributing to Sagemath



Overview an Installation of Sage

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications various domains

Algebra Number Theor

Graph plotting
Matrix algebra

Sage and LITEX

applications and further reading

Contributing to Sagemath

Questions'

LATEXrepresentation: latex(P)

```
\left(\begin{array}{rr}
1 & 2 \\
3 & 4
\end{array}\right)
```

- view(P): Display PDF(pdflatex)/HTML(MathJAX) depending on mode.
- SageT<sub>E</sub>X: Call Sage commands from L<sup>A</sup>T<sub>E</sub>X.
  - Regular statement: \sage{pow\_mod(27, 2, 12)}
  - Plots: \sageplot{plot(sin(x) + cos(x), -20, 20)}
  - \sageblock and \sagesilent: Embedding Sage code

Overview an Installation o Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various

Algebra Number Theory Calculus

Matrix algebra
Sage and LTEX

More applications and further reading

Contributing to Sagemath

Questions

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains
- 4 More applications and further reading
- 5 Contributing to Sagemath
- 6 Questions?

Overview an Installation of Sage

Basic usage
Interactive shell and scripting
Arithmetic and built-in functions

Applications ir various domains

Algebra Number Theor

Graph plotting
Matrix algebra

More applications and further reading

Contributing to Sagemath

Questions'

- Interfacing with other algebra systems(GP/PARI, Singular, Maxima)
- Polynomials
- Combinatorics
- Graph and group theory
- Linear algebra
- Elliptic curves
- Advanced portions of everything discussed

# References and further reading

Arvin

Overview an Installation o

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications i various domains

Number Theory Calculus Graph plotting Matrix algebra

More applications and further reading

Contributing to Sagemat

Questions

- Sage tutorial: http://www.sagemath.org/doc/tutorial/index.html
- Thematic tutorials: http://www.sagemath.org/doc/thematic\_tutorials/index.html
- Tutorials for those with some mathematics background: http://www.sagemath.org/doc/prep/index.html

Overview and Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various

Algebra
Number Theory

Graph plotting Matrix algebra Sage and LaTEX

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains
- 4 More applications and further reading
- 5 Contributing to Sagemath
- 6 Questions?

Overview an Installation of Sage

Basic usage Interactive shell an scripting Arithmetic and built-in functions

Applications in various domains

Algebra

Number Theory Calculus Graph plotting Matrix algebra Sage and LaTEX

More applications and further reading

Contributing to Sagemath

Questions

- · Packaging for Linux distros.
- Improve startup time.
- UI enhancements: Notebook and 2D plots.
- Mobile applications: Android, iOS.
- Mathematicians help with specific libraries.
- Visit http://www.sagemath.org/development.html for more information on getting involved.

Overview and Installation of Sage

Basic usage
Interactive shell an scripting
Arithmetic and built-in functions

Applications various

Algebra
Number Theory

Graph plotting Matrix algebra Sage and LTEX

More applications and further reading

Contributing to Sagemath

Questions?

- 1 Overview and Installation of Sage
- 2 Basic usage
- 3 Applications in various domains
- 4 More applications and further reading
- 5 Contributing to Sagemath
- 6 Questions?

Overview and Installation of Sage

Basic usage

scripting

Arithmetic and
built-in functions

various

domains

Algebra

Calculus

Graph plottin

Matrix algebra

Sage and E

More applications and further

Contributing to Sagemat

Questions?

# Questions?

Overview and Installation of Sage

#### Basic usage

scripting

Arithmetic and built-in functions

various

Algebra

Algebra

Calculus

Graph plotting

Matrix algebra

Sage and 🔄

More applications and further

Contributing

Questions?

# Thank you!