

Test I Study Sheet

Sept 8, 2022

Binary - base 2

- computers think & communicate in binary
- 0 = false/off, 1 = true/on

Decimal - base 10, digits 0-9

Hexadecimal - base 16

- 2 digits can represent values from 0-255
- same as 8 bits / 1 byte of binary

Bit - a single binary digit

Byte - 8 bits of data

- 256 different combinations *
- max val - 255, min val - 0

Binary → Decimal ~ each power of 2 on/off

eg. 0001 1110 → 16 + 8 + 4 + 2 = 30

1111 1111 → 255 (all are on & max is 255)

0010 0000 → 32 (one is on)

0011 1111 → 64 (everything on BEFORE 64)

Decimal → Binary ~ find largest power of 2 < decimal value

→ turn on corresponding pos, subtract & repeat

eg. 24 → 0001 1000

10 → 0000 1010

31 → 0001 1111

Adding Binary Nums

0 + 1 = 1

1 + 1 = 0 carry 1

1 + 1 + 1 = 1 carry 1

eg.
$$\begin{array}{r} 0001\ 0111 \\ + 0011\ 1110 \\ \hline 0101\ 0101 \end{array}$$

HEX table

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F

powers of 16

$4096 = 16^3$, $256 = 16^2$, $16 = 16^1$, $1 = 16^0$

Binary to Hex → binary → dec → hex or TRICK - split in half:

eg. 0001 | 0111 → 17₁₆ 0011 | 1010 → 3A

Or TRICK

FF \rightarrow 255

1111 1111

B2

1011 0010

HEX to Bin

or use

hex \rightarrow dec \rightarrow binary

Hex to Dec \rightarrow convert hex to numbers & mult by power of 16 & add tog

eg B2 $\rightarrow 11(16) + 2(1) = 178$

178₁₆ $\rightarrow 1(256) + 7(16) + 8 = 376$

FF \rightarrow 255

Dec to Hex \rightarrow determine how many digits of hex are by finding largest num $<$ decimal

4096 256 16 1

\rightarrow see how many of each power will

eg 2000 = 7 D 0
($256 \times 7 = 1792$) ($16 \times 3 = 104$)

44 = 2 C

4097₁₀ \rightarrow 100

ASCII - an 8-bit code

- used to represent a letter/number/sym

char \rightarrow ASCII code \rightarrow Binary

' ' \rightarrow 32 \rightarrow 0010 0000

Propositional Logic - tied to philosophy

- true (T) - 1, false (F) - 0

3 logical connectives: AND \wedge & &
OR \vee ||
NOT \neg - !

Truth tables - 2^n rows where n is # of variable
- cols - 1 for each var
- 1 for single not vars
- 1 for each operation (inside

eg. $(A \vee B) \wedge \bar{C}$ $2^3 = 8$ rows

A	B	C	\bar{C}	$(A \vee B)$	$(A \vee B) \wedge \bar{C}$	$\overline{(A \vee B) \wedge \bar{C}}$
1	1	1	0	1	0	1
1	1	0	1	1	1	0
1	0	1	0	1	0	1
1	0	0	1	1	1	0
0	1	1	0	1	0	1
0	1	0	1	1	1	0
0	0	1	0	0	0	1
0	0	0	1	0	0	1

Tautology - proposition that is always true

$$\neg p \vee \neg p$$

p	$\neg p$	$p \vee \neg p$
0	1	1

Contradiction - proposition that is always false

$$\neg p \wedge \neg p$$

p	$\neg p$	$p \wedge \neg p$
0	1	0

Eng \rightarrow Propositional Logic ~ English sentences can be converted to

* let statements

logical operators to determine truth value

* determine propositions

* determine logical operators

[e.g. the cat is not brown or the truck flies

let p represent "the cat is brown"

$$\neg p \vee q$$

\therefore trucks can't fly

let q represent "the truck flies"

\therefore true when cat is not brown.

Types of Operators - LOGICAL

\vee

(||)

OR

\wedge

(&&)

AND

\neg , -

(!)

NOT

ARITHMETIC

+

(+)

-

(-)

x

(*)

\div

(/)

R

(%)

ASSIGNMENT

=

(=)

RELATIONAL

\leq

(<=)

$>$ (>)

$<$

(<)

= (==)

\geq

(>=)

\neq (!=)

Logical Properties - DeMorgan's Law, Distributive, Commutative, Tautology, Contradiction, Associative, +

How to do a proof:

① Split into LS and RS

* don't skip steps & write which laws used

② Goals:

- work on one (or both) sides until they are equal

- Start with more complex side

③ Make conclusion (\therefore LS \approx RS \therefore ... \approx ...)