Lectures on Al-driven Drug Discovery

Attention: Part II

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Topics

Part I

Preliminary topics:

Recurrent neural network

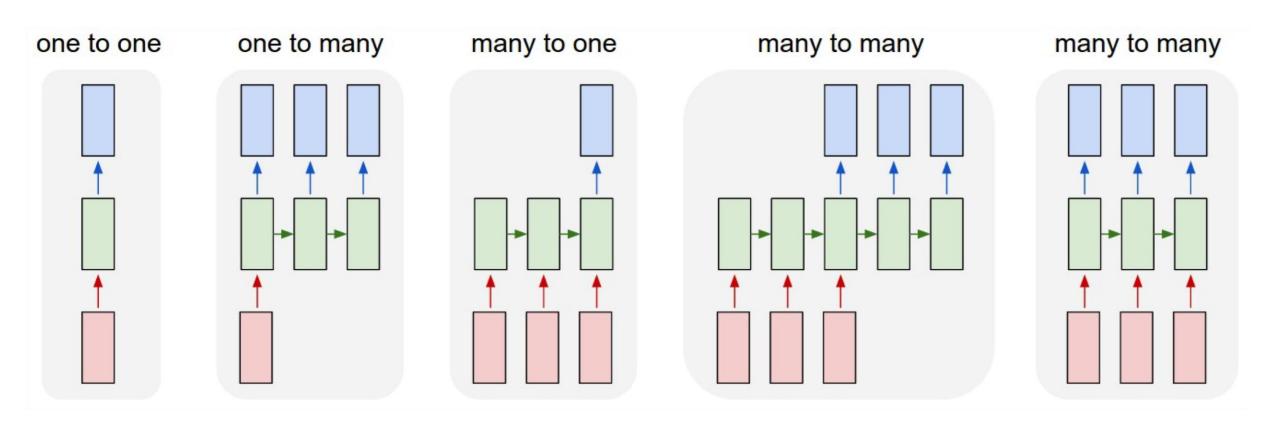
Sequence-to-Sequence with RNNs and Attention

Image Captioning with RNNs and Attention

Part II
Self-Attention Layer
The Transformer



Review: Recurrent Neural Networks



e.g. **Image Captioning** image -> sequence of words

e.g. **Machine Translation** seq of words -> seq of words



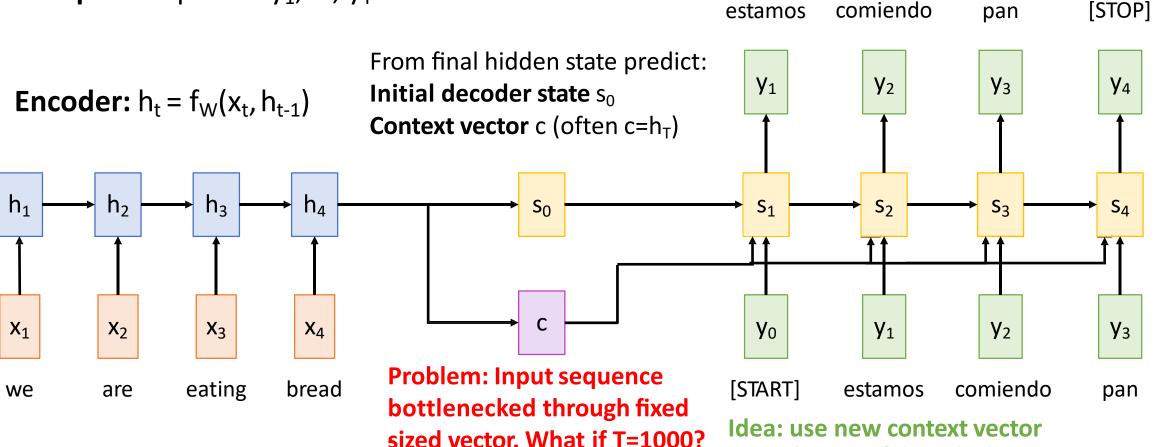
Review: Sequence-to-Sequence with RNNs

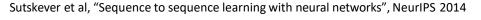
Input: Sequence $x_1, ... x_T$

Output: Sequence $y_1, ..., y_{T'}$

Decoder: $s_t = g_U(y_{t-1}, h_{t-1}, c)$

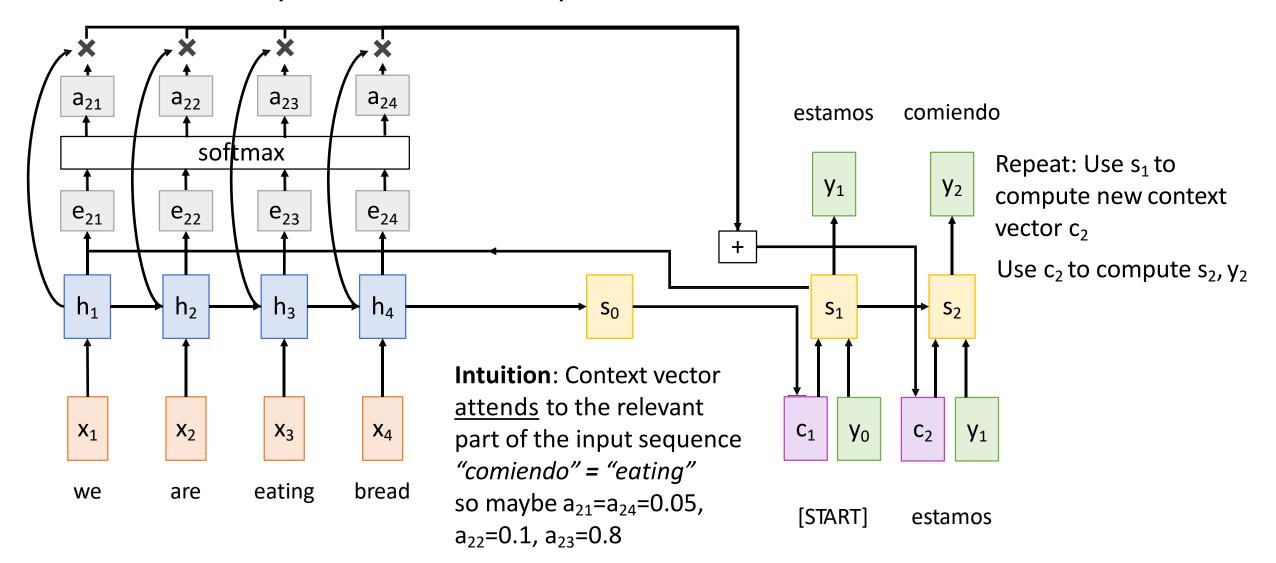
at each step of decoder!







Review: Sequence-to-Sequence with RNNs and Attention





Review: Image Captioning with RNNs and Attention

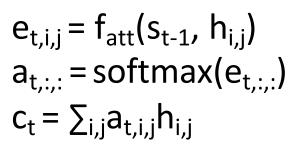
Each timestep of decoder uses a different context

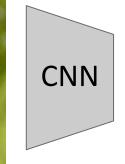
vector that looks at different parts of the image

sitting

cat

attention weights

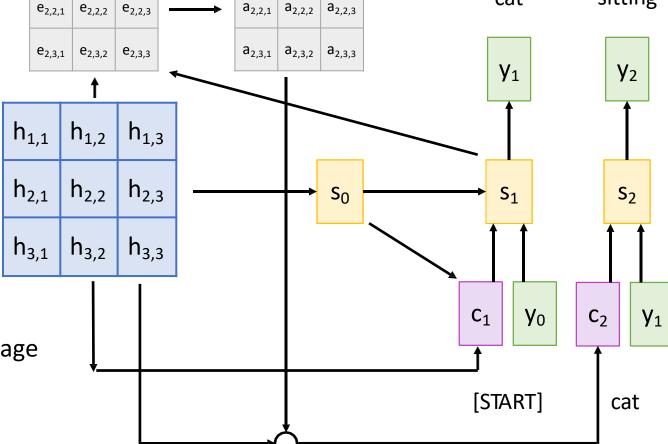




 $a_{2,1,1} \mid a_{2,1,2} \mid a_{2,1,3}$ $e_{2,1,2} \mid e_{2,1,3}$ softmax e_{2,2,2} $e_{2,2,3}$ $e_{2,3,1} \mid e_{2,3,2} \mid$ $e_{2,3,3}$ h_{1,2} $h_{1,3}$

Alignment scores

Use a CNN to compute a grid of features for an image



Xu et al, "Show, attend, and Tell: Neural Image Cap\$on Genera\$on with Visual attention", ICML 2015



Review: X, Attend, and Y

"Show, attend, and tell" (Xu et al, ICML 2015)
Look at image, attend to image regions, produce question

"Ask, attend, and answer" (Xu and Sattnko, ECCV 2016)
"Show, ask, attend, and answer" (Kazemi and Elqursh, 2017)
Read text of question, attend to image regions, produce answer

"Listen, attend, and spell" (Chan et al, ICASSP 2016)
Process raw audio, attend to audio regions while producing text

"Listen, attend, and walk" (Mei et al, AAAI 2016)
Process text, attend to text regions, output navigation commands

"Show, attend, and interact" (Qureshi et al, ICRA 2017)
Process image, attend to image regions, output robot control commands

"Show, attend, and read" (Li et al, AAAI 2019)
Process image, attend to image regions, output text



Inputs:

Query vector: **q** (Shape: D_Q)

Input vectors: X (Shape: $N_X \times D_X$)

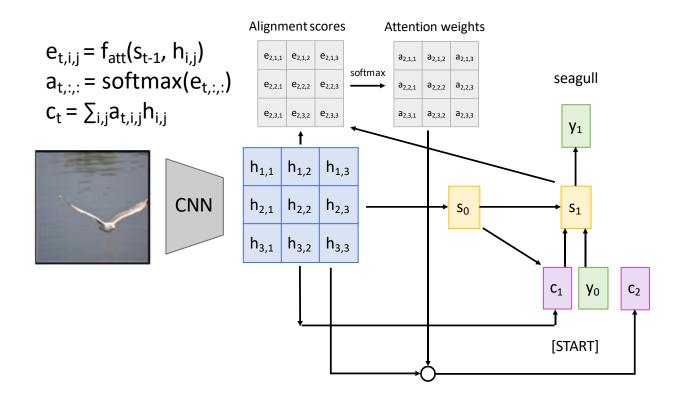
Similarity function: f_{att}

Computation:

Similarities: e (Shape: N_X) $e_i = f_{att}(q, X_i)$

attention weights: a = softmax(e) (Shape: N_x)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)





Inputs:

Query vector: **q** (Shape: D_Q)

Input vectors: X (Shape: $N_X \times D_X$)

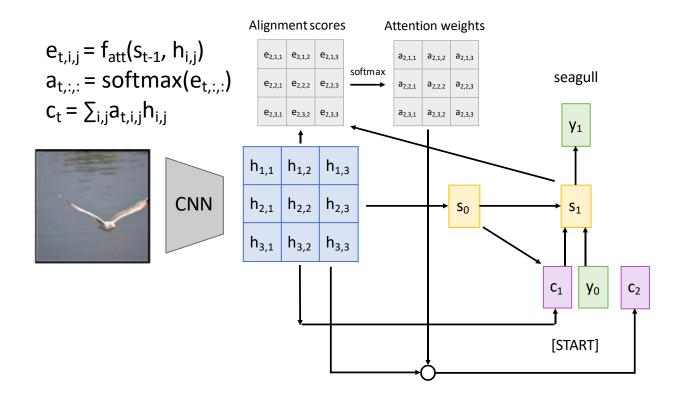
Similarity function: dot product

Computation:

Similarities: e (Shape: N_X) $e_i = \mathbf{q} \cdot \mathbf{X}_i$

attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)



Changes:

- Use dot product for similarity



Inputs:

Query vector: **q** (Shape: D_Q)

Input vectors: X (Shape: $N_X \times D_Q$)

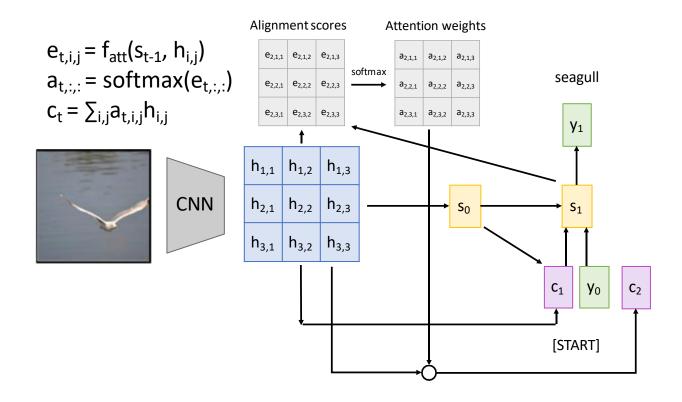
Similarity function: scaled dot product

Computation:

Similarities: e (Shape: N_X) $e_i = \mathbf{q} \cdot \mathbf{X}_i / \operatorname{sqrt}(D_Q)$

attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)



Changes:

- Use **scaled** dot product for similarity



Inputs:

Query vector: **q** (Shape: D_Q)

Input vectors: X (Shape: $N_X \times D_Q$)

Similarity function: scaled dot product

Large Similarities will cause softmax to saturate and give vanishing gradien ts Recall $a \cdot b = |a||b| \cos(angle)$

Suppose that a and b are constant vectors of dimension D

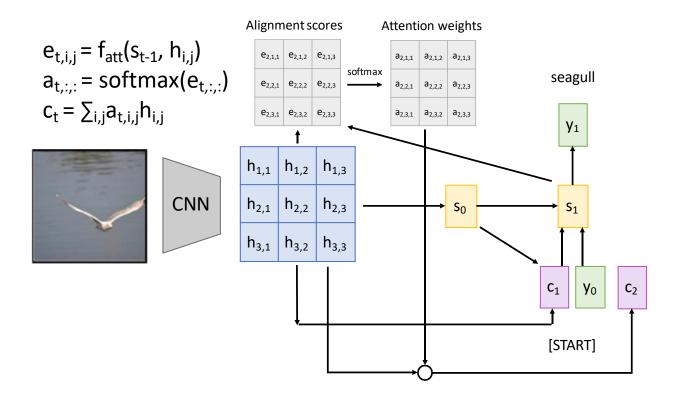
Then $|a| = (\sum_{i} a^{2})^{1/2} = a \operatorname{sqrt}(D)$

Computation:

Similarities: e (Shape: N_X) $e_i = \mathbf{q} \cdot \mathbf{X}_i / \operatorname{sqrt}(D_Q)$

attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)



Changes:

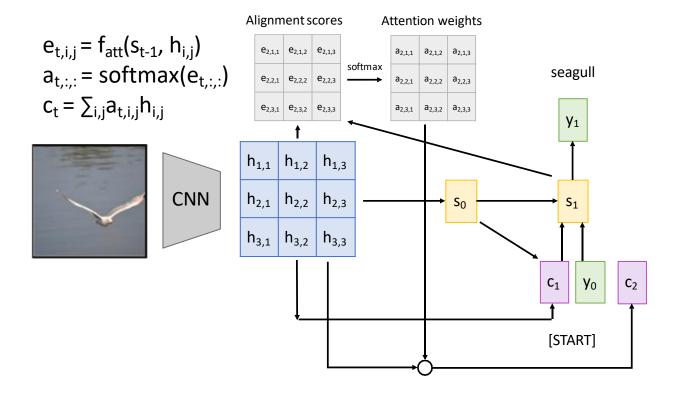
Use scaled dot product for similarity



Inputs:

Query vectors: \mathbf{Q} (Shape: $N_{\mathbf{Q}} \times D_{\mathbf{Q}}$)

Input vectors: \mathbf{X} (Shape: $N_X \times D_Q$)



Computation:

Similarities: $E = \mathbf{QX^T}$ (Shape: $N_Q \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{X}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AX (Shape: $N_Q \times D_X$) $Y_i = \sum_j A_{i,j} X_j$

Changes:

- Use dot product for similarity
- Multiple **query** vectors



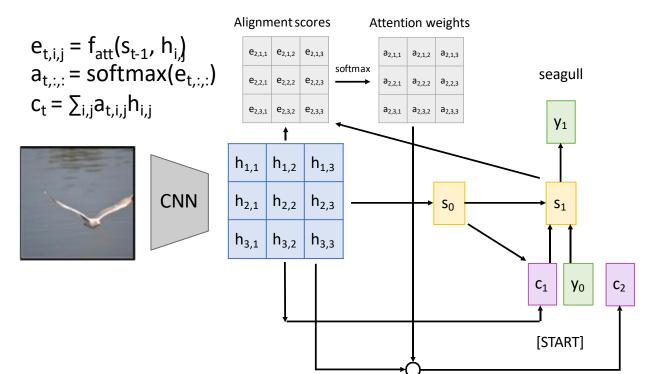
Inputs:

Query vectors: **Q** (Shape: $N_Q \times D_Q$)

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)



Computation:

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_Q \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

Changes:

- Use dot product for similarity
- Multiple query vectors
- Separate key and value



Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Computation:

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_{\mathsf{Q}} \times N_{\mathsf{X}}$) $E_{\mathsf{i},\mathsf{j}} = \mathbf{Q}_{\mathsf{i}} \cdot \mathbf{K}_{\mathsf{j}} / \operatorname{sqrt}(D_{\mathsf{Q}})$

attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

 X_1

 X_2

 X_3

 Q_1

 Q_2

 Q_3

 Q_4



Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$)

Computation:

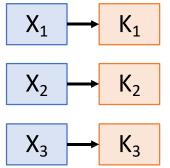
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Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



 Q_1

 Q_2

 Q_3

 Q_4



Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$)

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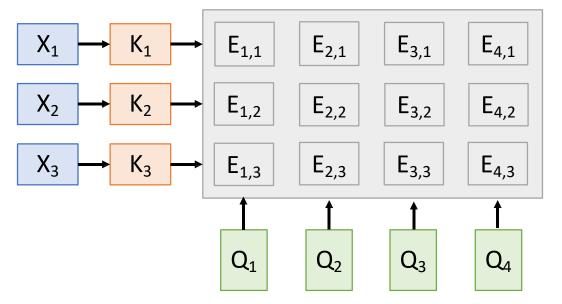
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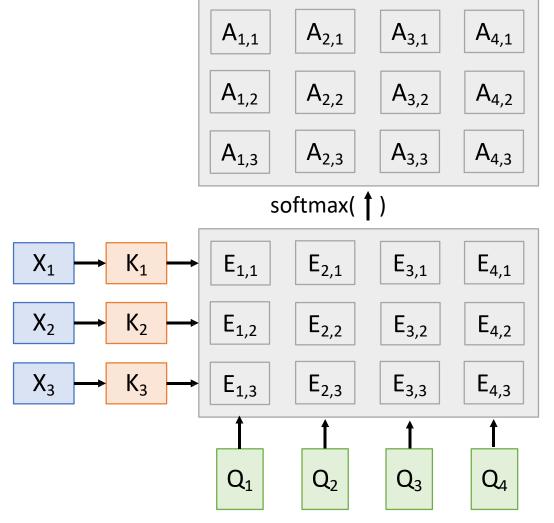
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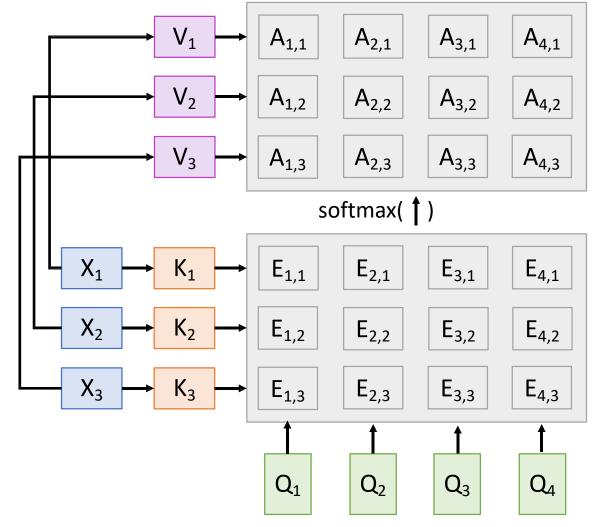
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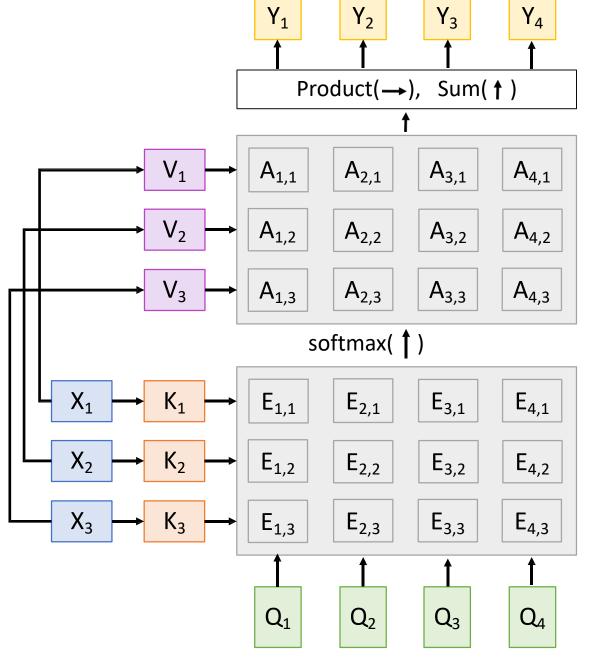
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attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)





One query per input vector

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_O$)

Computation:

Query vectors: Q = XW_Q

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_{\mathsf{X}} \times N_{\mathsf{X}}$) $E_{\mathsf{i},\mathsf{j}} = \mathbf{Q}_{\mathsf{i}} \cdot \mathbf{K}_{\mathsf{j}} / \operatorname{sqrt}(D_{\mathsf{Q}})$

attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

 $X_{\underline{1}}$ X_2 X_3



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Computation:

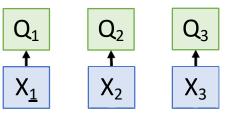
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attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)





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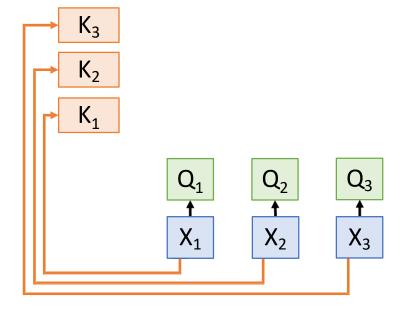
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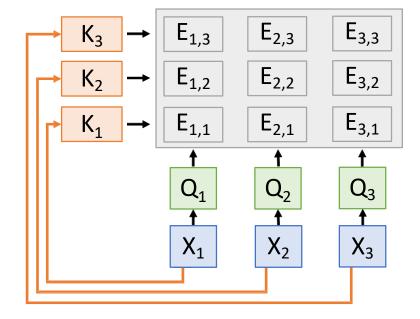
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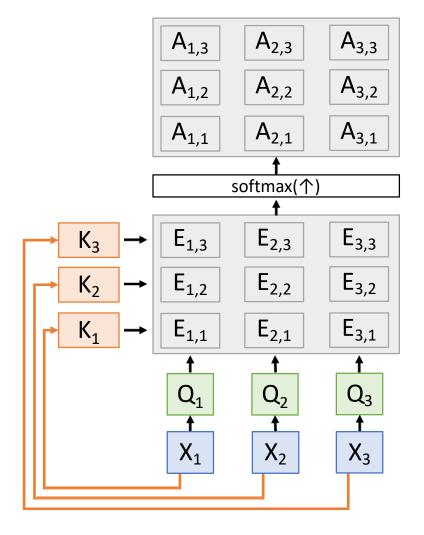
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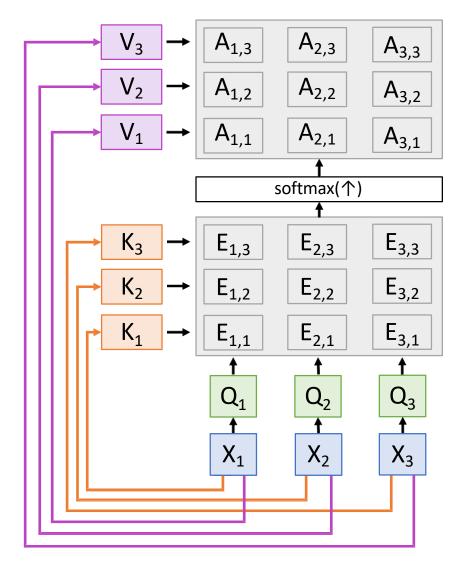
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Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_O$)

Computation:

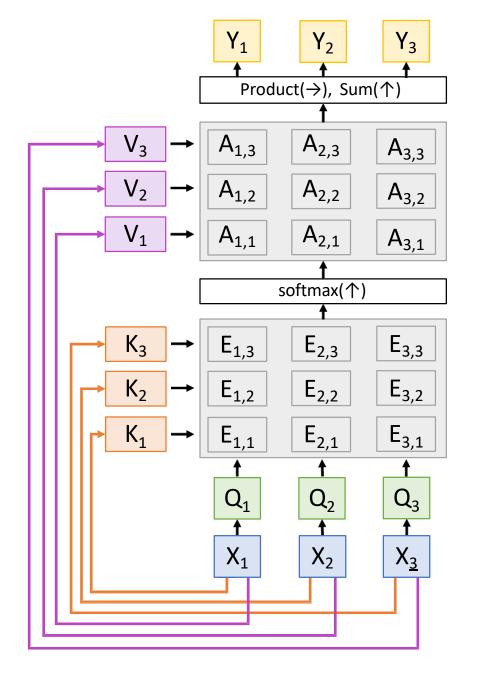
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attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)





Consider **permuting** the input vectors:

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_O$)

Computation:

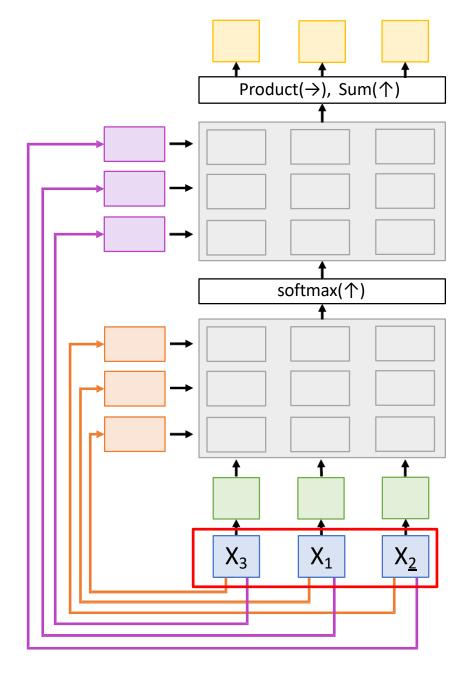
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)





Consider **permuting** the input vectors:

Inputs:

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Queries and Keys will be the same, but permuted

Computation:

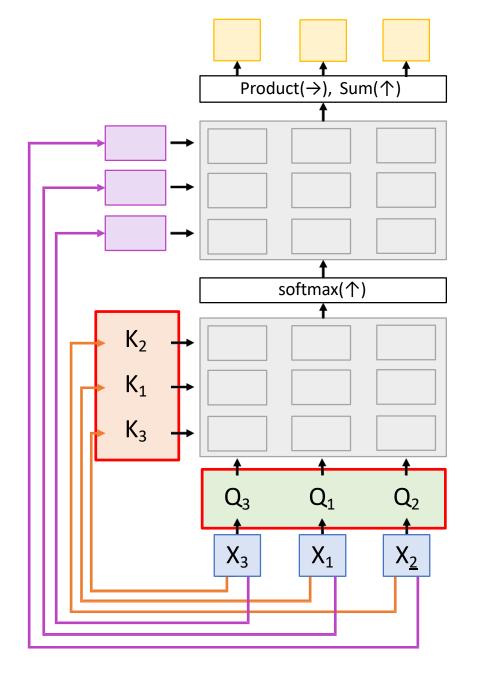
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)





Consider **permuting** the input vectors:

Inputs:

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Similarities will be the same, but permuted

Computation:

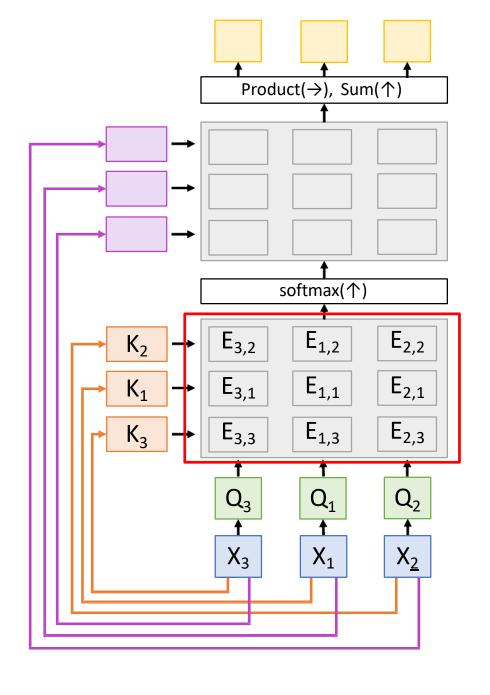
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Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)





Consider **permuting** the input vectors:

Inputs:

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

attention weights will

be the same, but

permuted

Computation:

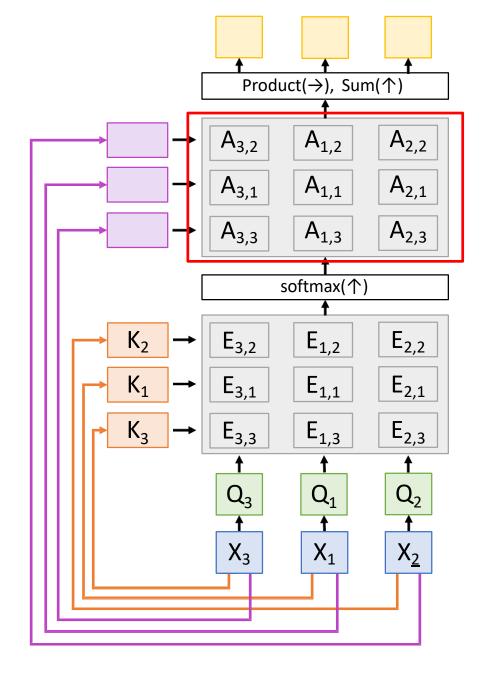
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_i / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)





Consider **permuting** the input vectors:

Inputs:

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Values will be the same, but permuted

Computation:

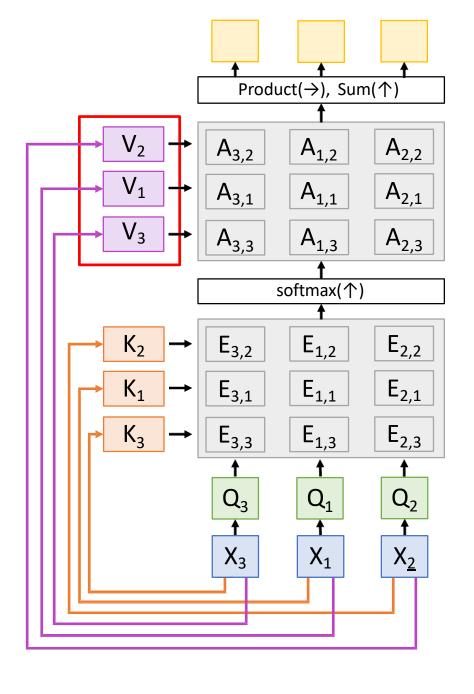
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_i / \operatorname{sqrt}(D_Q)$

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Input vectors: X (Shape: $N_X \times D_X$)

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Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Outputs will be the same, but permuted

Computation:

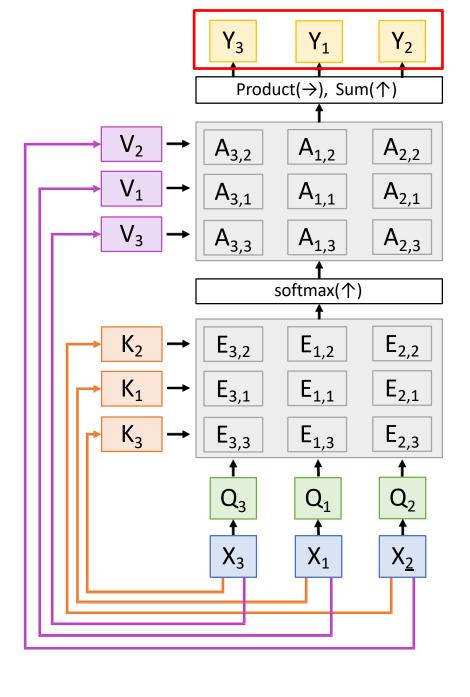
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)





Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_O$)

Computation:

Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{QK^T}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)

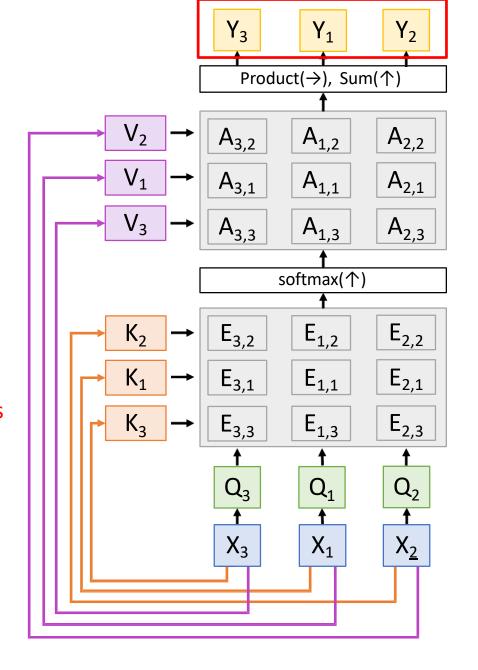
Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

Consider **permuting** the input vectors:

Outputs will be the same, but permuted

Self-attention layer is **Permutation Equivariant** f(s(x)) = s(f(x))

Self-attention layer works on **sets** of vectors





Self attention doesn't "know" the order of the vectors it is processing!

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_Q$)

Computation:

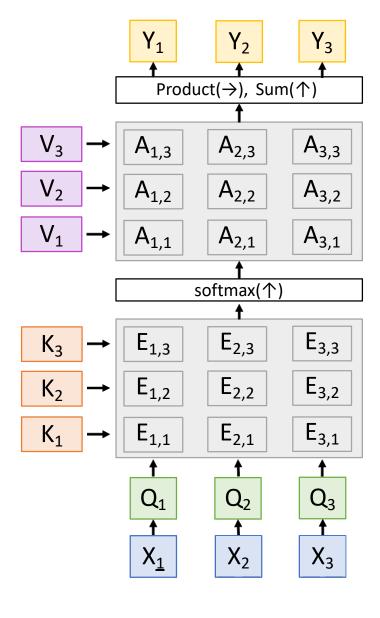
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)





Masked Self-Attention Layer

Don't let vectors "look ahead" in the sequence

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_O$)

Computation:

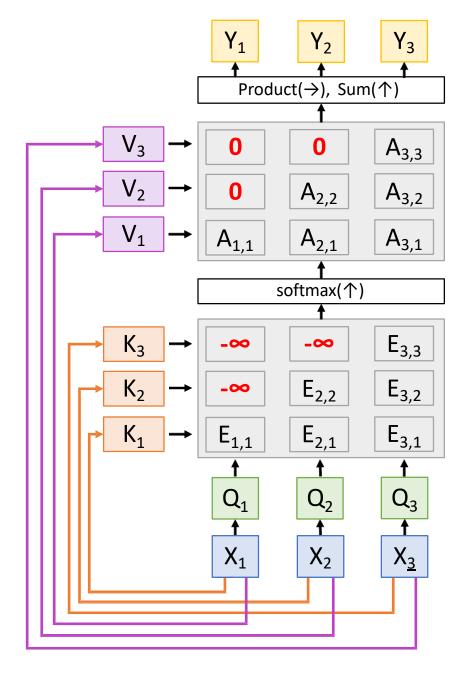
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_{\mathsf{X}} \times N_{\mathsf{X}}$) $E_{\mathsf{i},\mathsf{j}} = \mathbf{Q}_{\mathsf{i}} \cdot \mathbf{K}_{\mathsf{j}} / \operatorname{sqrt}(D_{\mathsf{Q}})$

attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)





Masked Self-Attention Layer

Don't let vectors "look ahead" in the sequence Used for language modeling (predict next word)

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_V (Shape: $D_X \times D_V$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Computation:

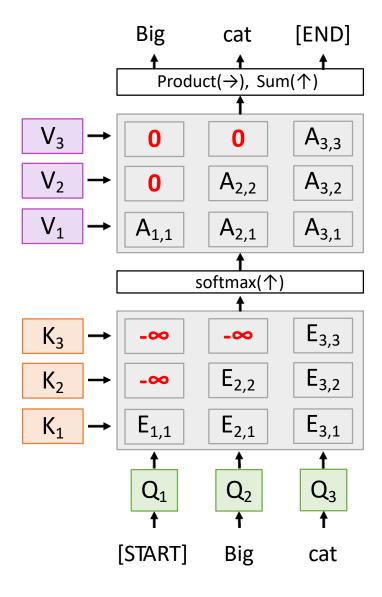
Query vectors: $Q = XW_Q$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

attention weights: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)





Multihead Self-Attention Layer

Use H independent "attention Heads" in parallel

Inputs:

Input vectors: X (Shape: $N_X \times D_X$)

Key matrix: W_K (Shape: $D_X \times D_Q$)

Value matrix: W_v (Shape: $D_x \times D_v$)

Query matrix: W_Q (Shape: $D_X \times D_Q$)

Hyperparameters:

Query dimension D_Q Number of heads H

Computation:

Query vectors: $Q = XW_Q$

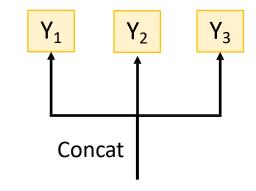
Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

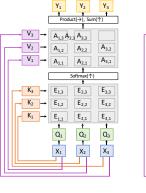
Value Vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

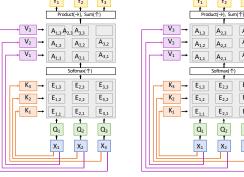
Similarities: $E = \mathbf{Q}\mathbf{K}^{\mathsf{T}}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$

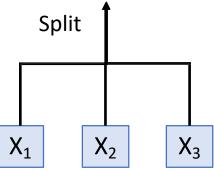
attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



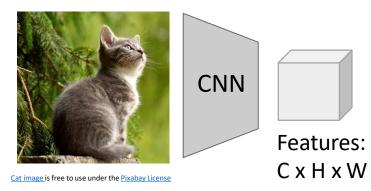






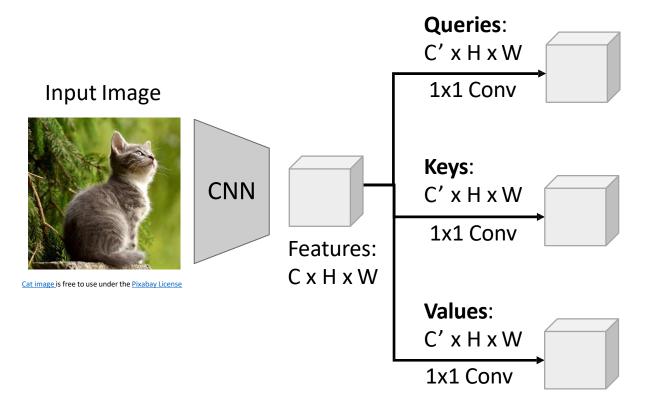


Input Image

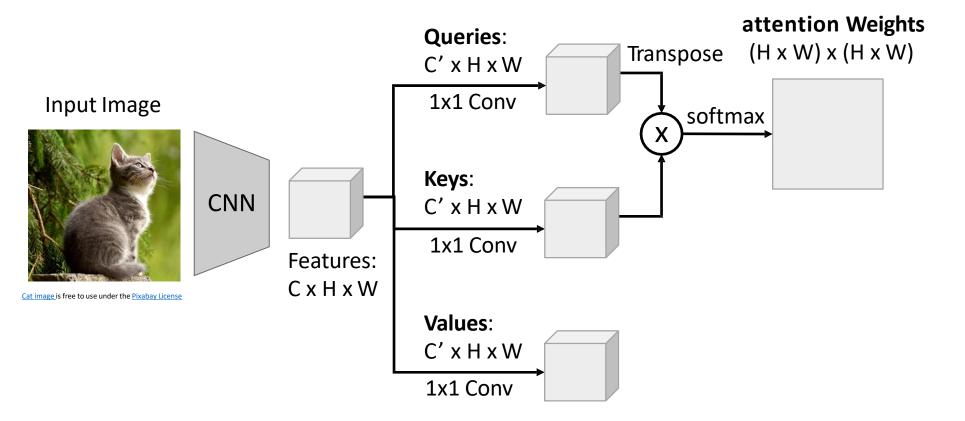




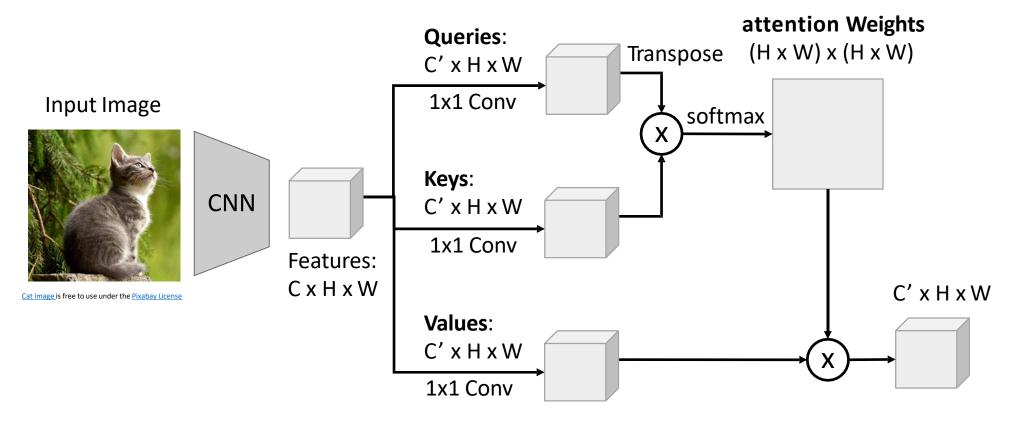




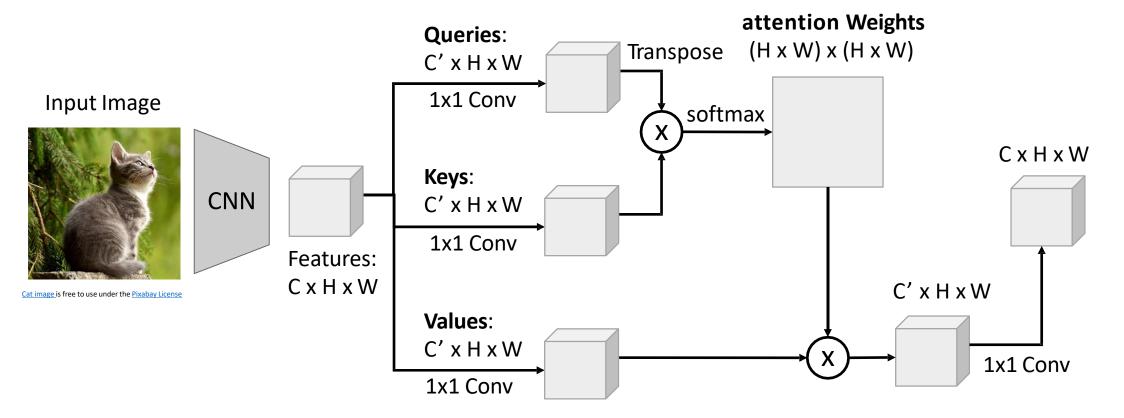




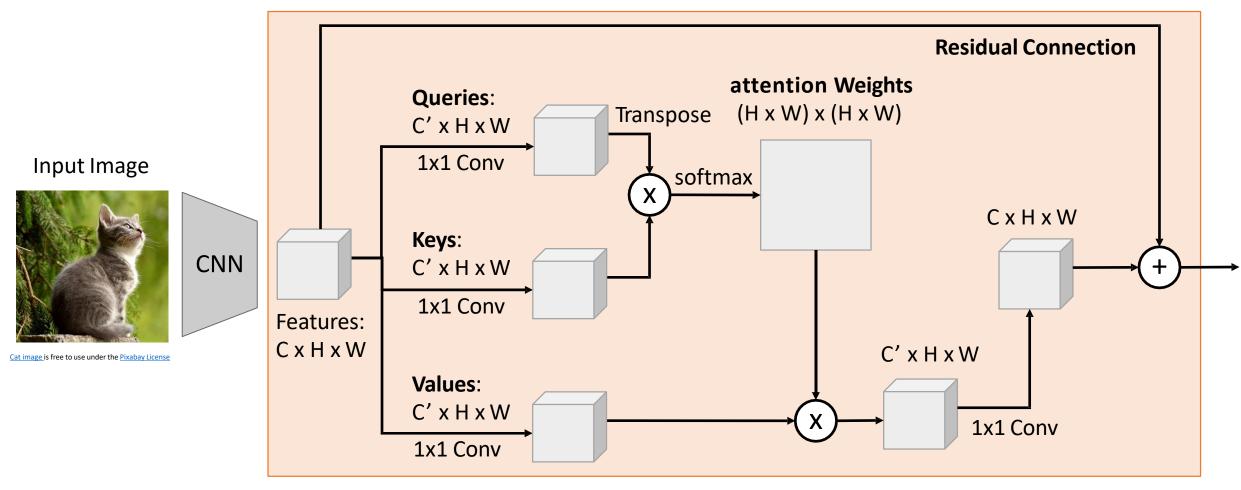








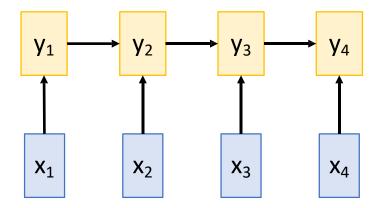




Self-attention Module



Recurrent Neural Network



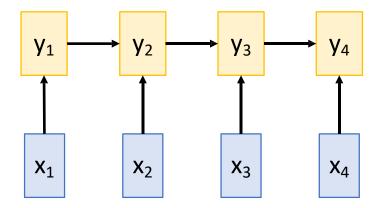
Works on **Ordered Sequences**

(+) Good at long sequences: Aher one RNN layer, h_T "sees" the whole sequence

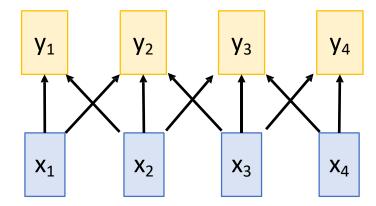
(-) Not parallelizable: need to compute hidden states sequentially



Recurrent Neural Network



1D Convolution



Works on **Ordered Sequences**

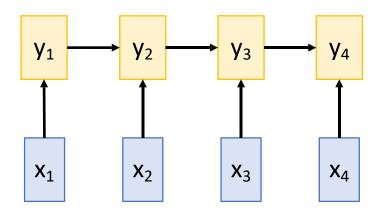
- (+) Good at long sequences: Aher one RNN layer, h_T "sees" the whole sequence
- (-) Not parallelizable: need to compute hidden states sequentially

Works on **Multidimensional Grids**

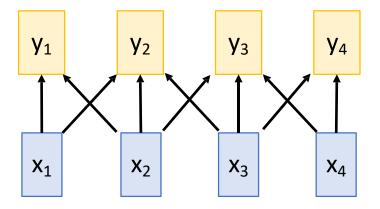
- (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
- (+) Highly parallel: Each output can be computed in parallel



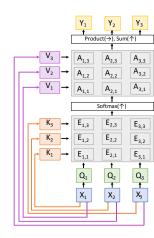
Recurrent Neural Network



1D Convolution



Self-attention



Works on **Ordered Sequences**

- (+) Good at long sequences: Aher one RNN layer, h_T "sees" the whole sequence
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Works on Multidimensional Grids

- (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
- (+) Highly parallel: Each output can be computed in parallel

Works on **Sets of Vectors**

- (-) Good at long sequences: after one self-attention layer, each output "sees" all inputs!
- (+) Highly parallel: Each output can be computed in parallel
- (-) Very memory intensive



Recurrent Neural Network

1D Convolution

Self-attention

attention is all you need

Vaswani et al, NeurIPS 2017

Works on **Ordered Sequences**

- (+) Good at long sequences: Aher one RNN layer, h_T "sees" the whole sequence
- (-) Not parallelizable: need to compute hidden states sequentially

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- (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
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Works on **Sets of Vectors**

- (-) Good at long sequences: after one self-attention layer, each output "sees" all inputs!
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 X_1

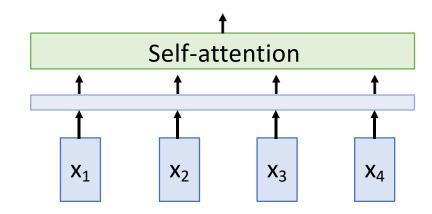
 X_2

 X_3

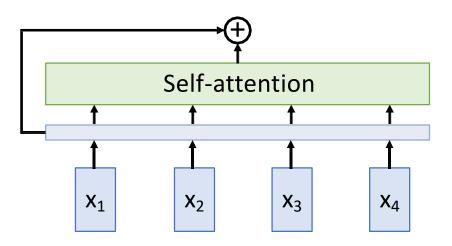
 X_4



All vectors interact with each other









Recall Layer Normalization:

Given $h_1, ..., h_N$ (Shape: D)

scale: γ (Shape: D)

shiD: β (Shape: D)

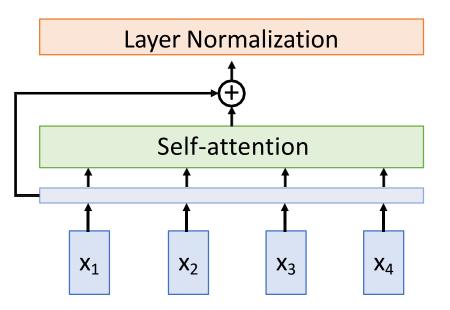
$$\mu_i = (1/D)\sum_i h_{i,i}$$
 (scalar)

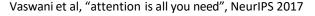
$$\sigma_{i} = (\sum_{i} (h_{i,i} - \mu_{i})^{2})^{1/2}$$
 (scalar)

$$z_i = (h_i - \mu_i) / \sigma_i$$

$$y_i = \gamma * z_i + \beta$$

Ba et al, 2016







Recall Layer Normalization:

Given h_1 , ..., h_N (Shape: D) scale: γ (Shape: D) shiD: β (Shape: D) $\mu_i = (1/D)\sum_j h_{i,j}$ (scalar)

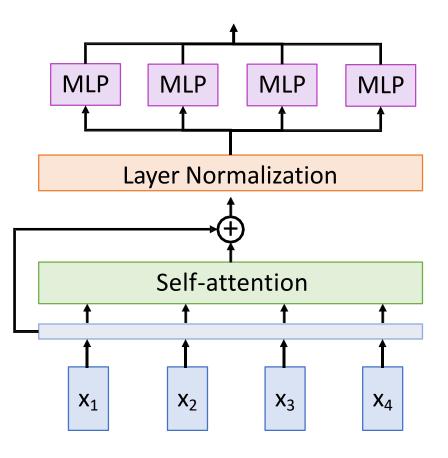
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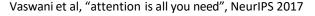
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Ba et al, 2016

MLP independently on each vector







Recall Layer Normalization:

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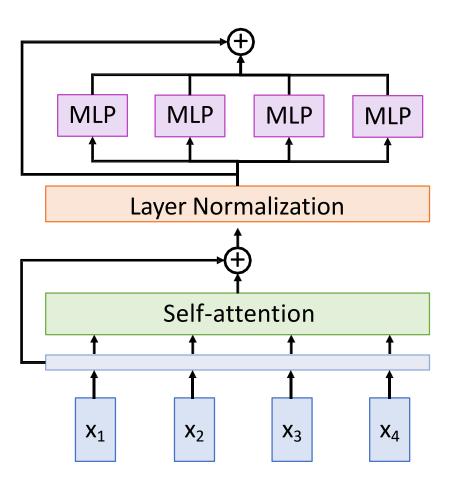
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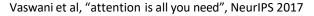
 $y_i = \gamma * z_i + \beta$

Ba et al, 2016

Residual connection

MLP independently on each vector







Recall Layer Normalization:

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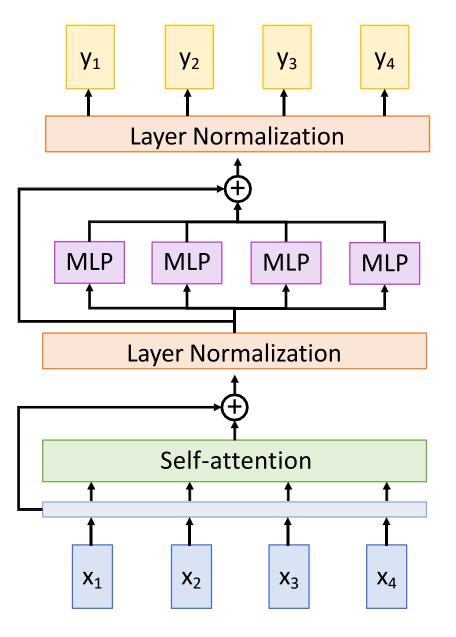
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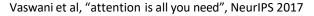
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Ba et al, 2016

Residual connection

MLP independently on each vector







Transformer Block:

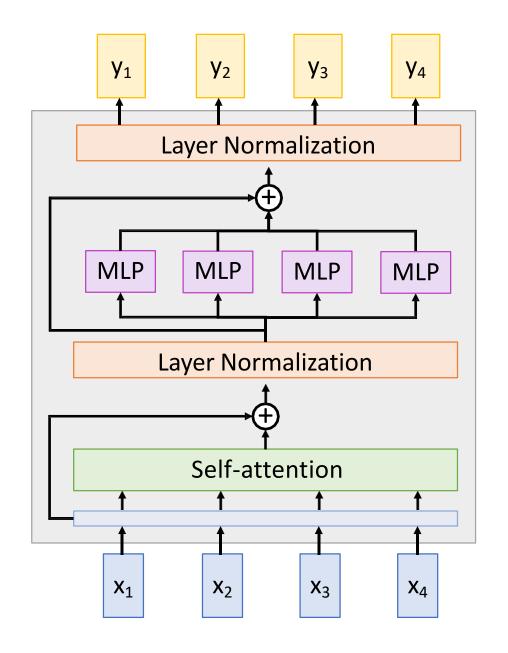
Input: Set of vectors x

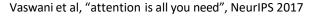
Output: Set of vectors y

Self-attention is the only interaction between vectors!

Layer norm and MLP work independently per vector

Highly scalable, highly parallelizable







Transformer Block:

Input: Set of vectors x

Output: Set of vectors y

Self-attention is the only interaction between vectors!

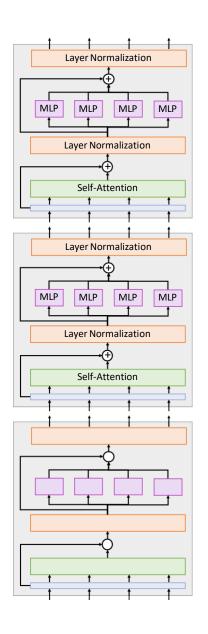
Layer norm and MLP work independently per vector

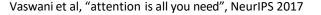
Highly scalable, highly parallelizable

A **Transformer** is a sequence of transformer blocks

Vaswani et al:

12 blocks, D_0 =512, 6 heads







The Transformer: Transfer Learning

"ImageNet Moment for Natural Language Processing"

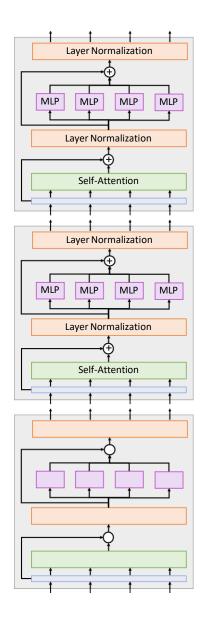
Pretraining:

Download a lot of text from the internet

Train a giant Transformer model for language modeling

Finetuning:

Fine-tune the Transformer on your own NLP task





Model	Layers	Width	Heads	Params	Data	Training
Transformer-Base	12	512	8	65M		8x P100 (12 hours)
Transformer-Large	12	1024	16	213M		8x P100 (3.5 days)



Model	Layers	Width	Heads	Params	Data	Training
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BERT-Base	12	768	12	110M	13 GB	
BERT-Large	24	1024	16	340M	13 GB	



Model	Layers	Width	Heads	Params	Data	Training
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BERT-Base	12	768	12	110M	13 GB	
BERT-Large	24	1024	16	340M	13 GB	
XLNet-Large	24	1024	16	~340M	126 GB	512x TPU-v3 (2.5 days)
RoBERTa	24	1024	16	355M	160 GB	1024x V100 GPU (1 day)



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RoBERTa	24	1024	16	355M	160 GB	1024x V100 GPU (1 day)
GPT-2	12	768	?	117M	40 GB	
GPT-2	24	1024	?	345M	40 GB	
GPT-2	36	1280	?	762M	40 GB	
GPT-2	48	1600	?	1.5B	40 GB	



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GPT-2	48	1600	?	1.5B	40 GB	
Megatron-LM	40	1536	16	1.2B	174 GB	64x V100 GPU
Megatron-LM	54	1920	20	2.5B	174 GB	128x V100 GPU
Megatron-LM	64	2304	24	4.2B	174 GB	256x V100 GPU (10 days)
Megatron-LM	72	3072	32	8.3B	174 GB	512x V100 GPU (9 days)

Shoeybi et al, "Megatron-LM: Training Multi-Billion Parameter Languge Models using Model Parallelism", 2019



~\$430,000 on Amazon AWS!

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Shoeybi et al, "Megatron-LM: Training Multi-Billion Parameter Languge Models using Model Parallelism", 2019



PROMPT (Human-written): In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.
OpenAI, "Better Language Models and their Implications", 2019, https://openai.com/blog/better-language-models/

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- Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.
- Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mount ains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a n atural fountain, surrounded by two peaks of rock and silver snow.
- Pérez and the others then ventured further into the valley. "By the time we reached the top of one peak, the water looked blue, with some crystals on top," said Pérez.
- Pérez and his friends were astonished to see the unicorn herd. These creatures could be seen from the air without having to move too much to see them they were so close they could touch their horns.
- While examining these bizarre creatures the scientists discovered that the creatures also spoke some fairly regular English. Pérez stated, "We can see, for example, that they have a common 'language,' something like a dialect or dialectic."
- Dr. Pérez believes that the unicorns may have originated in Argentina, where the animals were believed to be descendants of a lost race of people who lived there before the arrival of humans in those parts of South America.
- While their origins are still unclear, some believe that perhaps the creatures were created when a human and a unicorn met each other in a time before human civilization. According to Pérez, "In South America, such incidents seem to be quite common." How ever, Pérez also pointed out that it is likely that the only way of knowing for sure if unicorns are indeed the descendants of a lost alien race is through DNA. "But they seem to be able to communicate in English quite well, which I believe is a sign of evolution, or at least a change in social organization," said the scientist.

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Review

Part I

Preliminary topics:

Recurrent neural network

Sequence-to-Sequence with RNNs and Attention

Image Captioning with RNNs and Attention

Part II
Self-Attention Layer
The Transformer



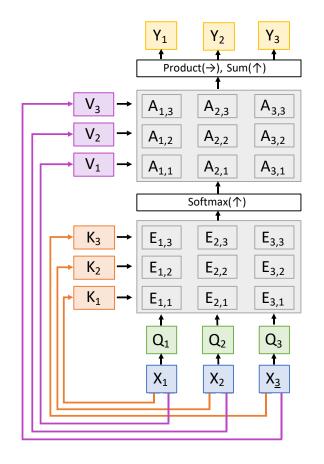
Summary

Adding **Attention** to RNN models lets them look at different parts of the input at each timestep



A dog is standing on a hardwood floor.

Generalized **Self-Attention** is new, powerful neural network primitive



Transformers are a new neural network model that only uses attention

