



Chapter 4

Lists

Data Structures and Algorithms

Luong The Nhan, Tran Giang Son
Faculty of Computer Science and Engineering
University of Technology, VNU-HCM

- **L.O.2.1** - Depict the following concepts: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- **L.O.2.2** - Describe storage structures by using pseudocode for: (a) array list and linked list, including single link and double links, and multiple links; (b) stack; and (c) queue and circular queue.
- **L.O.2.3** - List necessary methods supplied for list, stack, and queue, and describe them using pseudocode.
- **L.O.2.4** - Implement list, stack, and queue using C/C++.



- **L.O.2.5** - Use list, stack, and queue for problems in real-life, and choose an appropriate implementation type (array vs. link).
- **L.O.2.6** - Analyze the complexity and develop experiment (program) to evaluate the efficiency of methods supplied for list, stack, and queue.
- **L.O.8.4** - Develop recursive implementations for methods supplied for the following structures: list, tree, heap, searching, and graphs.
- **L.O.1.2** - Analyze algorithms and use Big-O notation to characterize the computational complexity of algorithms composed by using the following control structures: sequence, branching, and iteration (not recursion).



Contents

- ➊ Linear list concepts
- ➋ Array implementation
- ➌ Singly linked list
- ➍ Other linked lists
- ➎ Comparison of implementations of list



Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list



Linear list concepts

Array
implementation

Singly linked list

Other linked lists

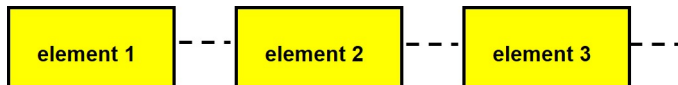
Comparison of
implementations of
list

Linear list concepts



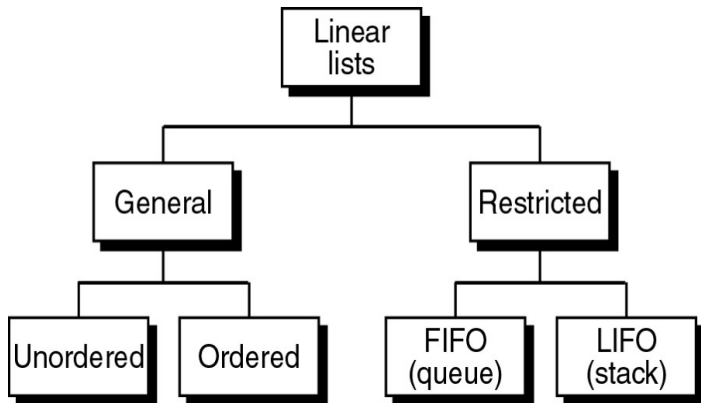
Definition

A linear list is a data structure in which each element has a unique successor.



Example

- Array
- Linked list





General list:

- No restrictions on which operation can be used on the list.
- No restrictions on where data can be inserted/deleted.
- **Unordered list** (random list): Data are not in particular order.
- **Ordered list**: data are arranged according to a key.

Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list



Restricted list:

- Only some operations can be used on the list.
- Data can be inserted/deleted only at the ends of the list.
- **Queue**: FIFO (First-In-First-Out).
- **Stack**: LIFO (Last-In-First-Out).

Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list

Definition

A list of elements of type T is a finite sequence of elements of T .

Basic operations:

- **Construct** a list, leaving it empty.
- **Insert** an element.
- **Remove** an element.
- **Search** an element.
- **Retrieve** an element.
- **Traverse** the list, performing a given operation on each element.





Extended operations:

- Determine whether the list is **empty** or not.
- Determine whether the list is **full** or not.
- Find the **size** of the list.
- **Clear** the list to make it empty.
- **Replace** an element with another element.
- **Merge** two ordered list.
- **Append** an unordered list to another.

Linear list concepts

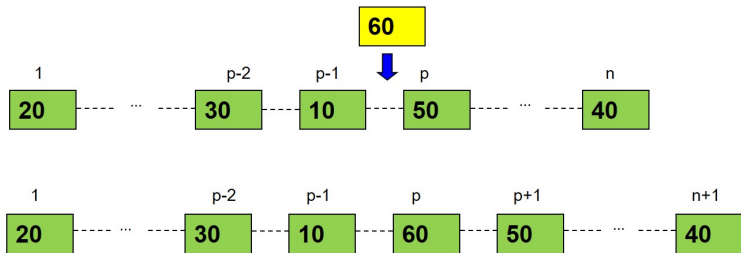
Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list

- Insert an element at a specified position p in the list
 - Only with *General Unordered List*.



Any element formerly at position p and all later have their position numbers increased by 1.

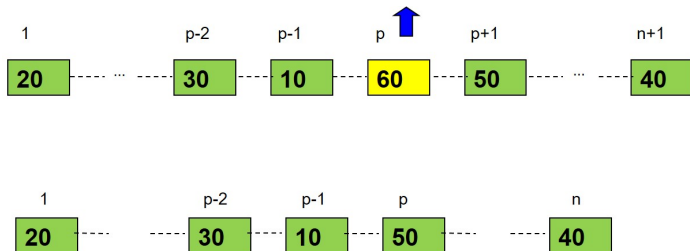




- **Insert an element with a given data**
 - With *General Unordered List*: can be made at any position in the list (at the beginning, in the middle, at the end).
 - With *General Ordered List*: data must be inserted so that the ordering of the list is maintained (searching appropriate position is needed).
 - With *Restricted List*: depend on it own definition (FIFO or LIFO).

Removal

- Remove an element at a specified position p in the list
 - With *General Unordered List* and *General Ordered List*.



The element at position p is removed from the list, and all subsequent elements have their position numbers decreased by 1.

- Retrieve an element at a specified position p in the list
 - With *General Unordered List* and *General Ordered List*.



retrieved data = 60

All elements remain unchanged.



- **Remove/ Retrieve an element with a given data**
 - With *General Unordered List* and *General Ordered List*: Searching is needed in order to locate the data being deleted/ retrieved.



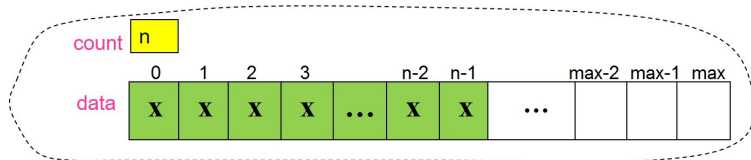
- **Insertion** is successful when the list is not full.
- **Removal, Retrieval** are successful when the list is not empty.





Array implementation

Automatically Allocated Array



Hình: Array with pre-defined maxsize and has n elements

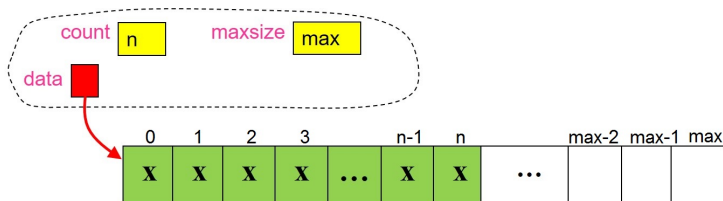
```
List // Contiguous Implementation of List
// number of used elements (mandatory)
count <integer>

// (Automatically Allocated Array)
data <array of <DataType> >

End List
```



Dynamically Allocated Array



```
List // Contiguous Implementation of List
// number of used elements (mandatory)
count <integer>

// (Dynamically Allocated Array)
data <dynamic array of <DataType> >

maxsize <integer>
End List
```



Dynamic Array: Implementation in C++

```
class DynamicArray {  
private:  
    int size;  
    int capacity;  
    int *storage;  
  
public:  
    DynamicArray() {  
        capacity = 10;  
        size = 0;  
        storage = new int[capacity];  
    }  
};
```



Dynamic Array: Implementation in C++

```
DynamicArray(int capacity) {  
    this->capacity = capacity;  
    size = 0;  
    storage = new int[capacity];  
}  
  
~DynamicArray() {  
    delete [] storage;  
}
```



Dynamic Array: Implementation in C++

```
void setCapacity(int );  
  
void rangeCheck(int );  
void set(int , int );  
int get(int );  
void removeAt(int );  
void insertAt(int , int );  
  
void print ();  
};
```



Dynamic Array: Implementation in C++

```
void DynamicArray::setCapacity(  
    int newCapacity) {  
    int *newStorage = new int[newCapacity];  
    memcpy(newStorage, storage,  
           sizeof(int) * size);  
    capacity = newCapacity;  
    delete[] storage;  
    storage = newStorage;  
}
```

```
void DynamicArray::ensureCapacity(int minCapacity) {  
    if (minCapacity > capacity) {  
        int newCapacity = (capacity * 3) / 2 + 1;  
        if (newCapacity < minCapacity)  
            newCapacity = minCapacity;  
        setCapacity(newCapacity);  
    }  
}
```



Dynamic Array: Implementation in C++

```
void DynamicArray::rangeCheck(int index) {  
    if (index < 0 || index >= size)  
        throw "Index out of bounds!";  
}  
  
void DynamicArray::set(int index ,  
                       int value) {  
    rangeCheck(index);  
    storage[index] = value;  
}  
  
int DynamicArray::get(int index) {  
    rangeCheck(index);  
    return storage[index];  
}
```



Dynamic Array: Implementation in C++

```
void DynamicArray::insertAt(int index ,
                           int value) {
    if (index < 0 || index > size)
        throw "Index out of bounds!";
    ensureCapacity(size + 1);

    int moveCount = size - index;
    if (moveCount != 0)
        memmove(storage + index + 1,
                storage + index ,
                sizeof(int) * moveCount);
    storage[index] = value;
    size++;
}
```



Dynamic Array: Implementation in C++

```
void DynamicArray::removeAt(int index) {  
    rangeCheck(index);  
    int moveCount = size - index - 1;  
    if (moveCount > 0)  
        memmove(storage + index ,  
                storage + (index + 1),  
                sizeof(int) * moveCount);  
    size --;  
}
```



Dynamic Array: Using

```
void DynamicArray::print() {  
    for (int i=0; i<this->size; i++) {  
        cout << storage[i] << " ";  
    }  
}  
  
int main() {  
    cout << "Dynamic Array" << endl;  
    DynamicArray* da = new DynamicArray(10);  
    da->insertAt(0, 55);  
    // ...  
    da->print();  
    return 0;  
}
```



Contiguous Implementation of List

In processing a contiguous list with n elements:

- **Insert** and **Remove** operate in time approximately proportional to n (**require physical shifting**).
- **Clear**, **Empty**, **Full**, **Size**, **Replace**, and **Retrieve** in constant time.





Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list

Singly linked list

Linked List

Definition

A **linked list** is an ordered collection of data in which each element contains the location of the next element.



Hình: Singly Linked List

```
list // Linked Implementation of List
  head <pointer>
  count <integer> // number of elements (optional)
end list
```



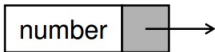
Nodes

The elements in a linked list are called **nodes**.

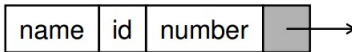
A **node** in a linked list is a structure that has at least two fields:

- the data,
- the address of the next node.

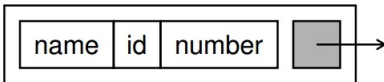
A node with
one data field

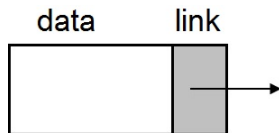


A node with
three data fields



A node with one
structured data field





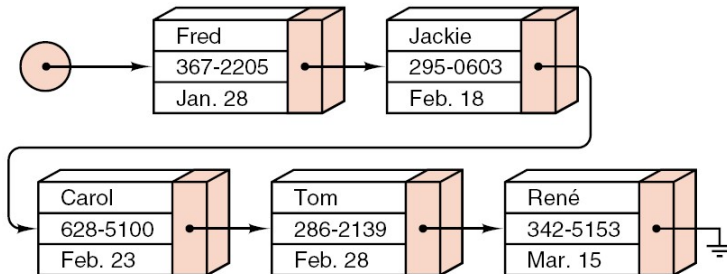
Hình: Linked list node structure

```
node
  data <dataType>
  link <pointer>
end node
```

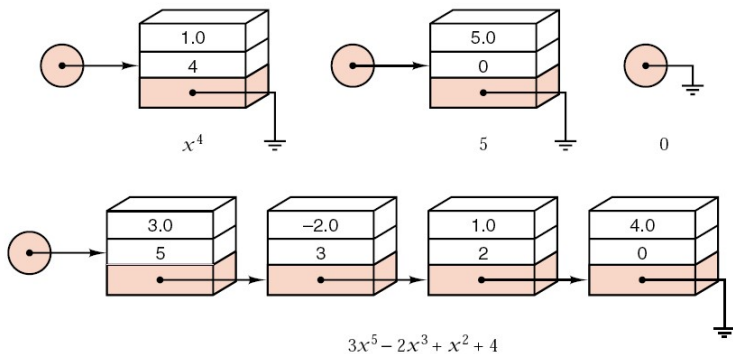
```
// General dataType:
dataType
  key <keyType>
  field1 <...>
  field2 <...>
  ...
  fieldn <...>
end dataType
```



Example



Example



Hình: List representing polynomial

Implementation in C++

Example

```
node
  data <dataType>
  link <pointer>
end node
```

```
struct Node {
    int data;
    Node *next;
};
```



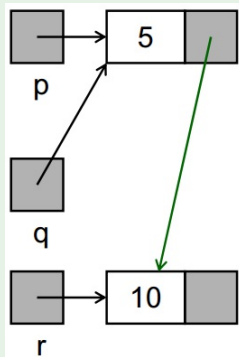
Implementation in C++

Example

```
#include <iostream>
using namespace std;

struct Node {
    int data;
    Node *next;
};

int main () {
    Node *p = new Node();
    p->data = 5;
    cout<< p->data << endl;
    Node *q = p;
    cout<< q->data << endl;
    Node *r = new Node();
    r->data = 10;
    q->next = r;
    cout<< p->next->data << endl;
}
```



Implementation in C++

Example

```
struct Node {  
    int data;  
    Node *next;  
};
```

```
struct Node {  
    float data;  
    Node *next;  
};
```

```
template <class ItemType>  
struct Node {  
    ItemType data;  
    Node<ItemType> *next;  
};
```



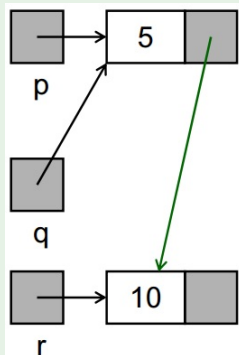
Implementation in C++

Example

```
#include <iostream>
using namespace std;

template <class ItemType>
struct Node {
    ItemType data;
    Node<ItemType> *next;
};

int main () {
    Node<int> *p = new Node<int>();
    p->data = 5;
    cout<< p->data << endl;
    Node<int> *q = p;
    cout<< q->data << endl;
    Node<int> *r = new Node<int>();
    r->data = 10;
    q->next = r;
    cout<< p->next->data << endl;
}
```



Node implementation in C++

```
template <class ItemType>
class Node {
    ItemType data;
    Node<ItemType> *next;

public:
    Node(){
        this->next = NULL;
    }

    Node(ItemType data){
        this->data = data;
        this->next = NULL;
    }
};
```



Linked list implementation in C++

```
template <class List_ItemType> list
class LinkedList {
    Node<List_ItemType> *head;
    int count;

public:
    LinkedList ();
    ~LinkedList ();
};
```



Linked list operations

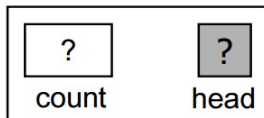
- Create an empty linked list
- Insert a node into a linked list
- Delete a node from a linked list
- Traverse a linked list
- Destroy a linked list



Create an empty linked list

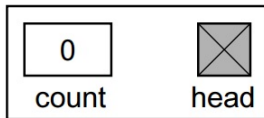


Before list



list.head = null
list.count = 0

After list



Create an empty linked list

Algorithm createList (ref list<metadata>)

Initializes metadata for a linked list

Pre: list is a metadata structure passed by reference

Post: metadata initialized

list.head = null

list.count = 0

return

End createList



Create an empty linked list

```
template <class List_ItemType>
class LinkedList {
    Node<List_ItemType> *head;
    int count;

public:
    LinkedList();
    ~LinkedList();
};

LinkedList<List_ItemType>::LinkedList(){
    this->head = NULL;
    this->count = 0;
}
```

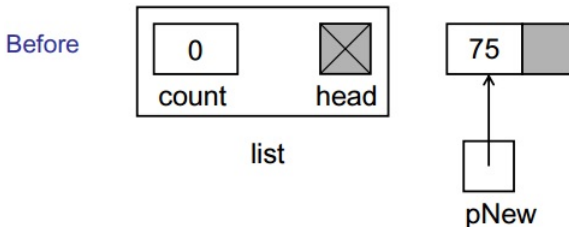


Insert a node into a linked list

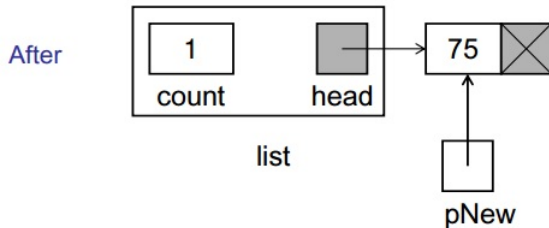
- 1 Allocate memory for the new node and set up data.
- 2 Locate the pointer `p` in the list, which will point to the new node:
 - If the new node becomes the first element in the List: `p is list.head`.
 - Otherwise: `p is pPre->link`, where `pPre` points to the predecessor of the new node.
- 3 Point the new node to its successor.
- 4 Point the pointer `p` to the new node.



Insert into an empty linked list

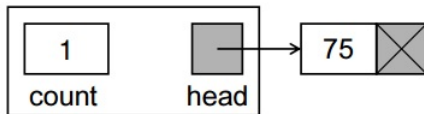


`pNew -> link = list.head`
`list.head = pNew`



Insert at the beginning

Before

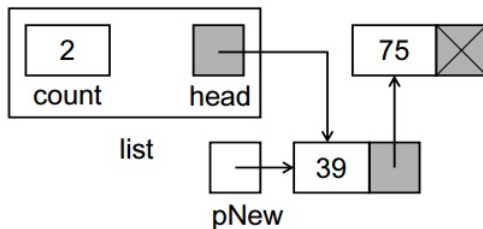


list

pNew

pNew -> link = list.head
list.head = pNew

After



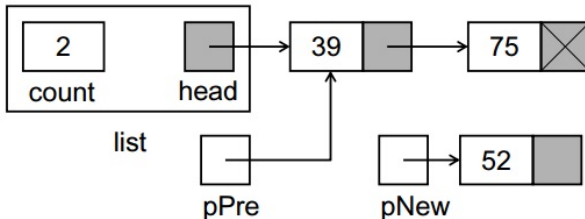
list

pNew



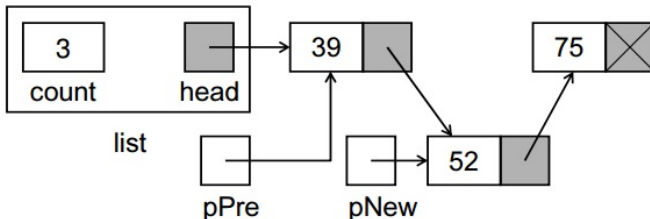
Insert in the middle

Before



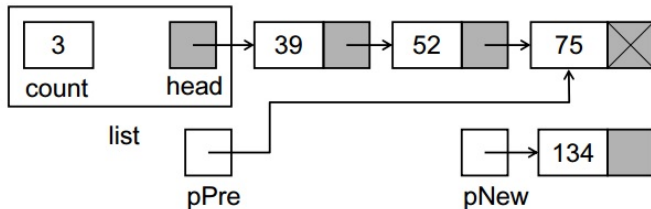
$$\begin{aligned} \text{pNew} \rightarrow \text{link} &= \text{pPre} \rightarrow \text{link} \\ \text{pPre} \rightarrow \text{link} &= \text{pNew} \end{aligned}$$

After



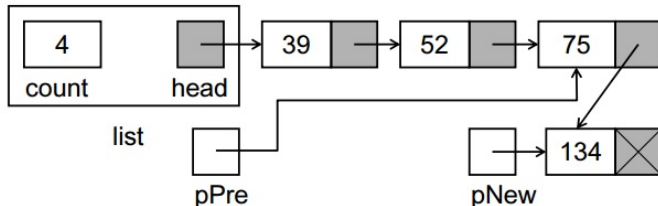
Insert at the end

Before



$pNew \rightarrow link = pPre \rightarrow link$
 $pPre \rightarrow link = pNew$

After



Insert a node into a linked list

- Insertion is successful when allocation memory for the new node is successful.
- There is **no difference** between insertion **at the beginning of the list** and insertion **into an empty list**.

```
pNew->link = list.head  
list.head = pNew
```

- There is **no difference** between insertion **in the middle** and insertion **at the end** of the list.

```
pNew->link = pPre->link  
pPre->link = pNew
```



Insert a node into a linked list

Algorithm insertNode(ref list<metadata>,
val pPre<node pointer>,
val dataIn<dataType>)

Inserts data into a new node in the linked list

Pre: list is metadata structure to a valid list
pPre is pointer data's logical predecessor
dataIn contains data to be inserted

Post: data have been inserted in sequence

Return true if successful, false if memory overflow



Insert a node into a linked list

```
allocate(pNew)
if memory overflow then
    | return false
end
pNew -> data = dataIn
if pPre = null then
    | // Adding at the beginning or into empty list
    | pNew -> link = list.head
    | list.head = pNew
else
    | // Adding in the middle or at the end
    | pNew -> link = pPre -> link
    | pPre -> link = pNew
end
list.count = list.count + 1
return true
End insertNode
```



Insert a node into a linked list

```
int LinkedList<List_ItemType>::InsertNode(  
    Node<List_ItemType> *pPre,  
    List_ItemType value) {  
    Node<List_ItemType> *pNew  
        = new Node<List_ItemType>();  
    if (pNew == NULL)  
        return 0;  
    pNew->data = value;  
    if (pPre == NULL) {  
        pNew->next = this->head;  
        this->head = pNew;  
    } else {  
        pNew->next = pPre->next;  
        pPre->next = pNew;  
    }  
    this->count++;  
    return 1;  
}
```



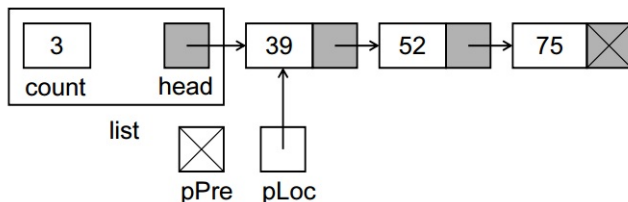
Delete a node from a linked list

- 1 Locate the pointer `p` in the list which points to the node to be deleted (`pDel` will hold the node to be deleted).
 - If that node is the first element in the List: `p is list.head`.
 - Otherwise: `p is pPre->link`, where `pPre` points to the predecessor of the node to be deleted.
- 2 `p` points to the successor of the node to be deleted.
- 3 Recycle the memory of the deleted node.



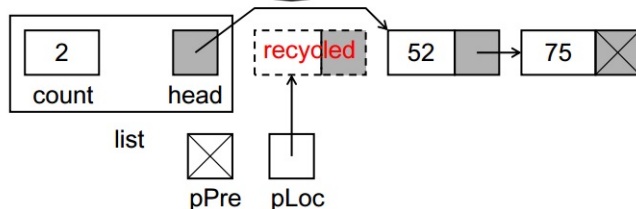
Delete first node

Before



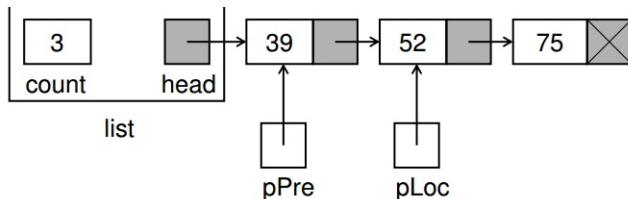
list.head = pLoc -> link
recycle(pLoc)

After



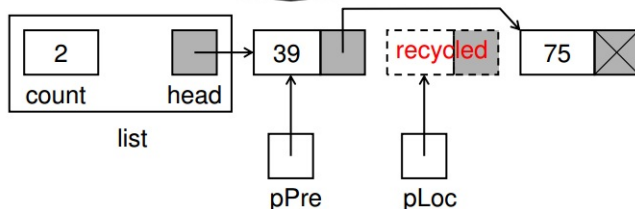
General deletion case

Before



$pPre \rightarrow \text{link} = pLoc \rightarrow \text{link}$
recycle (pLoc)

After



Delete a node from a linked list

- Removal is successful when the node to be deleted is found.
- There is **no difference** between removal the node **from the beginning** of the list and removal the **only-remained node** in the list.

```
list.head = pDel->link  
Recycle pDel
```

- There is **no difference** between removal a node **from the middle** and removal a node **from the end** of the list.

```
pPre->link = pDel->link  
Recycle pDel
```



Delete a node from a linked list

Algorithm deleteNode(ref list<metadata>,
val pPre<node pointer>,
val pLoc<node pointer>,
ref dataOut<dataType>)

Delete data from a linked list and returns it to calling module

Pre: list is metadata structure to a valid list
pPre is a pointer to predecessor node
pLoc is a pointer to node to be deleted
dataOut is variable to receive deleted data

Post: data have been deleted and returned to caller



Delete a node from a linked list

```
dataOut = pLoc -> data
if pPre = null then
    | // Delete first node
    | list.head = pLoc -> link
else
    | // Delete other nodes
    | pPre -> link = pLoc -> link
end
list.count = list.count - 1
recycle (pLoc)
return
End deleteNode
```



Delete a node from a linked list

```
List_ItemType LinkedList<List_ItemType>::DeleteNode(  
    Node<List_ItemType> *pPre,  
    Node<List_ItemType> *pLoc) {  
    List_ItemType result = pLoc->data;  
    if (pPre == NULL){  
        this->head = pLoc->next;  
    } else {  
        pPre->next = pLoc->next;  
    }  
    this->count--;  
    delete pLoc;  
    return result;  
}
```



Searching in a linked list

- **Sequence Search** has to be used for the linked list.
- List is ordered accordingly to the key field.

- Public method Search of List ADT:

```
<ErrorCode> Search (ref DataOut <DataType>)
```

Can not return a pointer to a node if found.

- Auxiliary function Search of List ADT:

```
<ErrorCode> Search (val target <KeyType>,  
                    ref pPre <pointer>, ref pLoc <pointer>)
```

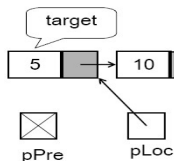
Searches a node and returns a pointer to it if found.



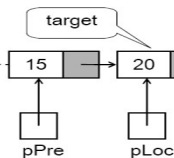


Successful Searches

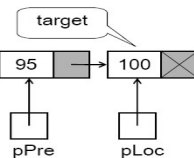
Located first



Located middle

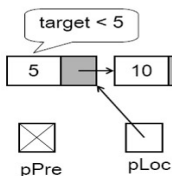


Located last

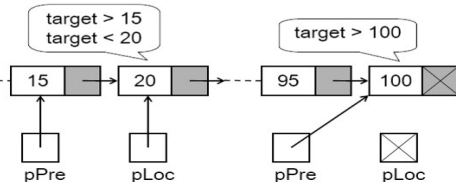


Unsuccessful Searches

Less than first



Greater than last



Searching in a linked list

Algorithm Search(val target <keyType>,
 ref pPre<node pointer>,
 ref pLoc<node pointer>)

Searches a node in a singly linked list and return a pointer to it if found.

Pre: target is the key need to be found

Post: pLoc points to the first node which is equal or greater than key, or is NULL if target is greater than key of the last node in the list.

pPre points to the largest node smaller than key, or is NULL if target is smaller than key of the first node.

Return found or notFound



Searching in a linked list

```
pPre = NULL
pLoc = head
while (pLoc is not NULL) AND (target > pLoc
->data.key) do
    |   pPre = pLoc
    |   pLoc = pLoc ->link
end
if pLoc is NULL then
    |   return notFound
else
    |   if target = pLoc ->data.key then
    |       |   return found
    |   else
    |       |   return notFound
    |   end
end
End Search
```



Searching in a linked list

```
int LinkedList<List_ItemType>::Search(  
    List_ItemType value ,  
    Node<List_ItemType>* &pPre ,  
    Node<List_ItemType>* &pLoc){  
    pPre = NULL;  
    pLoc = this->head;  
    while (pLoc != NULL && pLoc->data != value){  
        pPre = pLoc;  
        pLoc = pLoc->next;  
    }  
    return (pLoc != NULL);  
    // found: 1; notfound: 0  
}
```



Retrieve algorithm

- Using Search Algorithm to locate the node.
- Retrieving data from that node.



Retrieve algorithm

Algorithm Retrieve(val target <KeyType>, ref DataOut <DataType>)

Retrieves data from a singly linked list.

Pre: target is the key its data need to be retrieved

Post: if target is found, DataOut will receive data.

Return success or failed

```
errorCode = Search(target, pPre, pLoc)
```

```
if errorCode = notFound then
```

```
    |   return failed
```

```
else
```

```
    |   DataOut = pLoc->data
```

```
    |   return success
```

```
end
```

```
End Retrieve
```



Traverse a linked list

Traverse module controls the loop: calling a **user-supplied algorithm** to process data

Algorithm Traverse(ref <void> process (ref Data <DataType>))

Traverses the list, performing the given operation on each element.

Pre: process is user-supplied

Post: The action specified by process has been performed on every element in the list, beginning at the first element and doing each in turn.

pWalker = list.head

while *pWalker not null* **do**

process(pWalker -> data)

 pWalker = pWalker -> link

end

End Traverse



Traverse a linked list

```
void LinkedList<List_ItemType>::Traverse() {
    Node<List_ItemType> *p = head;
    while (p != NULL){
        p->data++; // process data here!!!
        p = p->next;
    }
}

void LinkedList<List_ItemType>::Traverse(void
    (*visit)(List_ItemType &)) {
    Node<List_ItemType> *p = head;
    while (p != NULL){
        (*visit)(p->data);
        p = p->next;
    }
}
```



Destroy a linked list

Algorithm destroyList (val list<metadata>)

Deletes all data in list.

Pre: list is metadata structure to a valid list

Post: all data deleted

while *list.head not null* **do**

 dltPtr = list.head

 list.head = this.head -> link

 recycle (dltPtr)

No data left in list. Reset metadata

end

list.count = 0

return

End destroyList



Destroy a linked list

```
void LinkedList<List_ItemType>::Clear(){
    Node<List_ItemType> *temp;
    while (this->head != NULL){
        temp = this->head;
        this->head = this->head->next;
        delete temp;
    }
    this->count = 0;
}

LinkedList<List_ItemType>::~~LinkedList(){
    this->Clear();
}
```



Linked list implementation in C++

```
template<class List_ItemType>

class LinkedList{

    Node<List_ItemType>* head;
    int count;

protected:
    int InsertNode(Node<List_ItemType>* pPre,
                  List_ItemType value);

    List_ItemType DeleteNode(Node<List_ItemType>* pPre,
                             Node<List_ItemType>* pLoc);

    int Search(List_ItemType value,
               Node<List_ItemType>* &pPre,
               Node<List_ItemType>* &pLoc);

    void Traverse();
};
```



Linked list implementation in C++

```
template<class List_ItemType>
class LinkedList{

protected:
    // ...

public:
    LinkedList();
    ~LinkedList();

    void InsertFirst(List_ItemType value);
    void InsertLast(List_ItemType value);
    int InsertItem(List_ItemType value, int position);
    List_ItemType DeleteFirst();
    List_ItemType DeleteLast();
    int DeleteItem(int position);
    int GetItem(int position, List_ItemType &dataOut);
    void Print2Console();
    void Clear();

    // Augment your methods for linked list here!!!
    LinkedList<List_ItemType>* Clone();
};
```



Linked list implementation in C++

How to use Linked List data structure?

```
int main(int argc, char* argv[]) {  
    LinkedList<int>* myList =  
        new LinkedList<int>();  
    myList->InsertFirst(15);  
    myList->InsertFirst(10);  
    myList->InsertFirst(5);  
    myList->InsertItem(18,3);  
    myList->InsertLast(25);  
    myList->InsertItem(20,3);  
    myList->DeleteItem(2);  
    printf("List_1:\n");  
    myList->Print2Console();  
}
```



Linked list implementation in C++

How to use Linked List data structure?

```
// ...  
  
int value;  
LinkedList<int>* myList2 = myList->Clone();  
printf("\nList_2:\n");  
myList2->Print2Console();  
myList2->GetItem(1, value);  
printf("Value_at_position_1:_%d", value);  
  
delete myList;  
delete myList2;  
return 1;  
}
```



Sample Solution: Insert

```
template <class List_ItemType>
int LinkedList<List_ItemType>::InsertItem (
    List_ItemType value, int position) {

    if (position < 0 || position > this->count)
        return 0;

    Node<List_ItemType> *newPtr, *pPre;
    newPtr = new Node<List_ItemType>();
    if (newPtr == NULL)
        return 0;

    newPtr->data = value;

    if (head == NULL) {
        head = newPtr;
        newPtr->next = NULL;
    }
    else if (position == 0) {
        newPtr->next = head;
        head = newPtr;
    }
}
```



Sample Solution: Insert

```
else {  
    // Find the position of pPre  
    pPre = this->head;  
  
    for (int i = 0; i < position - 1; i++)  
        pPre = pPre->next;  
  
    // Insert new node  
    newPtr->next = pPre->next;  
    pPre->next = newPtr;  
}  
  
this->count++;  
return 1;  
}
```



Sample Solution: Delete

```
template <class List_ItemType>
int LinkedList<List_ItemType>::Deleteltem(int position){
    if (position < 0 || position > this->count)
        return 0;

    Node<List_ItemType> *dltPtr , *pPre;

    if (position == 0) {
        dltPtr = head;
        head = head->next;
    } else {
        pPre= this->head;
        for (int i = 0; i < position -1; i++)
            pPre = pPre->next;
        dltPtr = pPre->next;
        pPre->next = dltPtr->next;
    }

    delete dltPtr;
    this->count--;
    return 1;
}
```



Sample Solution: Clone

```
template <class List_ItemType>
LinkedList<List_ItemType>*
    LinkedList<List_ItemType>::Clone(){
    LinkedList<List_ItemType>* result =
        new LinkedList<List_ItemType>();

    Node<List_ItemType>* p = this->head;

    while (p != NULL) {
        result->InsertLast(p->data);
        p = p->next;
    }

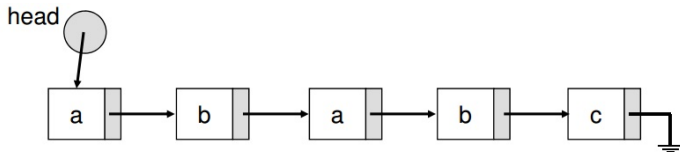
    result->count = this->count;
    return result;
}
```



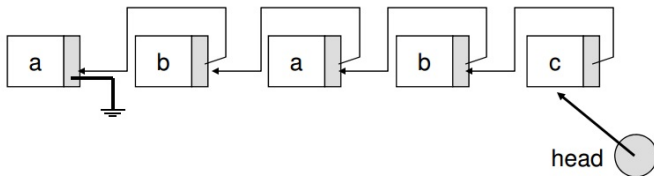
Reverse a linked list

Exercise

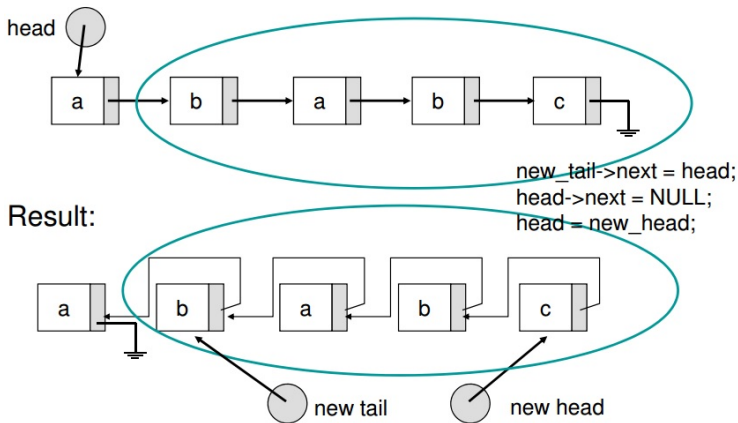
```
template <class List_ItemType>
void LinkedList<List_ItemType>::Reverse(){
    // ...
}
```



Result:



Reverse a linked list



Hình: Hint



Linear list concepts

Array
implementation

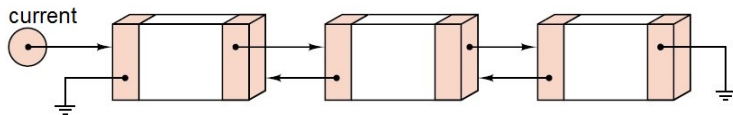
Singly linked list

Other linked lists

Comparison of
implementations of
list

Other linked lists

Doubly Linked List



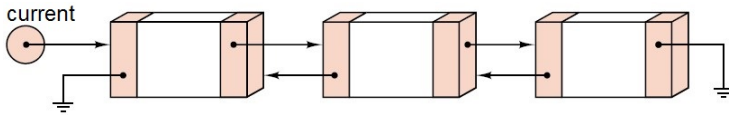
Hình: Doubly Linked List allows going forward and backward.

```
node
  data <dataType>
  next <pointer>
  previous <pointer>
end node
```

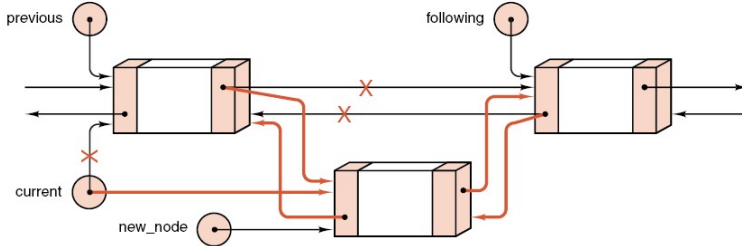
```
list
  current <pointer>
end list
```



Doubly Linked List

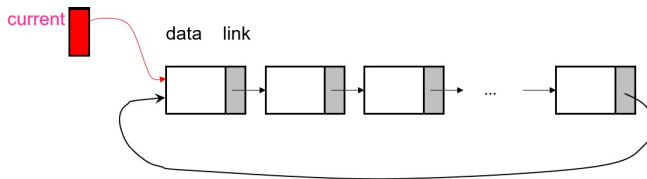


Hình: Doubly Linked List allows going forward and backward.



Hình: Insert an element in Doubly Linked List.

Circularly Linked List

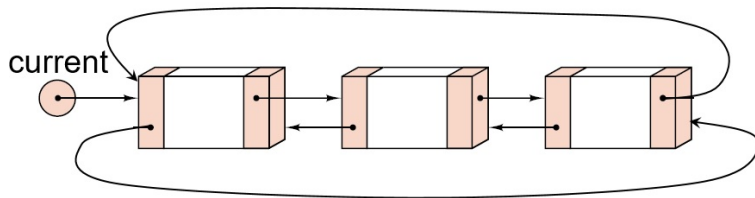


```
node
  data <dataType>
  link <pointer>
end node
```

```
list
  current <pointer>
end list
```



Double circularly Linked List

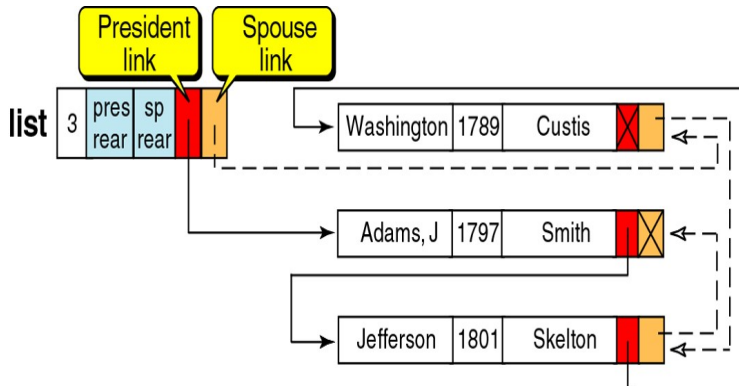


```
node
  data <dataType>
  next <pointer>
  previous <pointer>
end node
```

```
list
  current <pointer>
end list
```

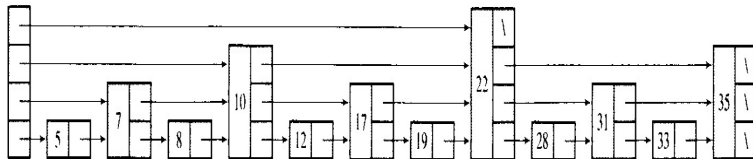


Multilinked List



Hình: Multilinked List allows traversing in different order.

Skip List



Hình: Skip List improves sequential searching.



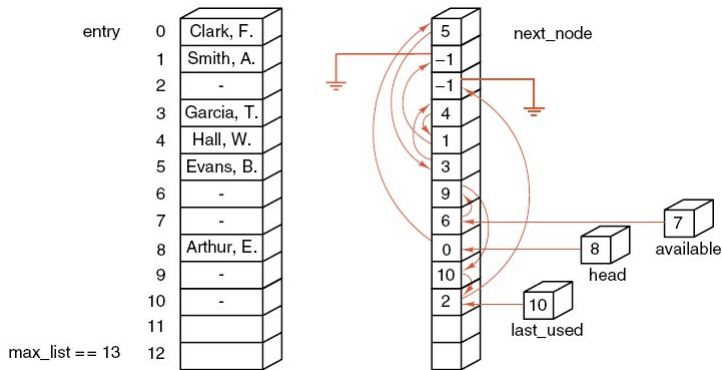
Choice of variants of Linked List

To choose among linked Implementations of List, consider:

- Which of the operations will actually be performed on the list and which of these are the most important?
- Is there locality of reference? That is, if one entry is accessed, is it likely that it will next be accessed again?
- Are the entries processed in sequential order? If so, then it may be worthwhile to maintain the last-used position as part of list.
- Is it necessary to move both directions through the list? If so, then doubly linked lists may prove advantageous.



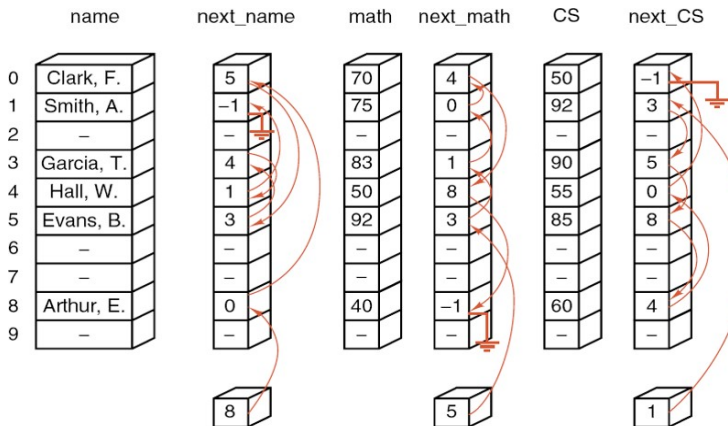
Linked List In Array



There are two linked lists in array:

- One (**head**) manages used entries.
- Another (**available**) manages empty entries (have been used or not yet)

Multilinked List In Array



Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list

Sparse Matrice

students

1 2 8,000

courses

| | | | | | | | | | | | | |
|-----|---|--|---|---|--|---|--|---|---|---|--|--|
| 1 | | | | A | | | | C | | | | |
| 2 | A | | B | | | | | | | B | | |
| | | | | | | A | | | | | | |
| | | | C | | | | | | A | | | |
| | B | | | B | | C | | | | | | |
| | | | | | | | | | | | | |
| 300 | | | A | | | | | | | | | |



Linear list concepts

Array
implementation

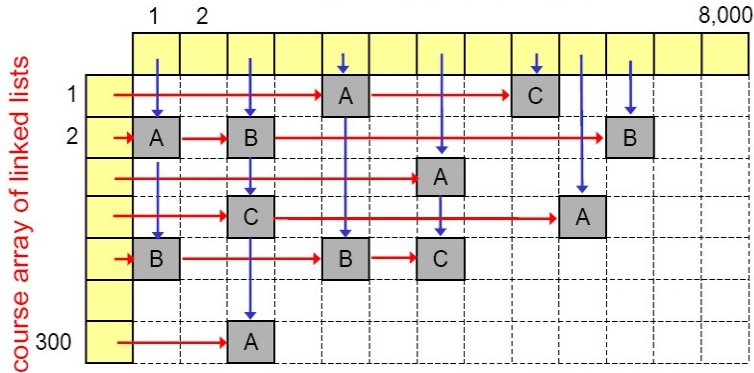
Singly linked list

Other linked lists

Comparison of
implementations of
list



student array of linked list



Hình: Two one-dimensional arrays of Linked List are used



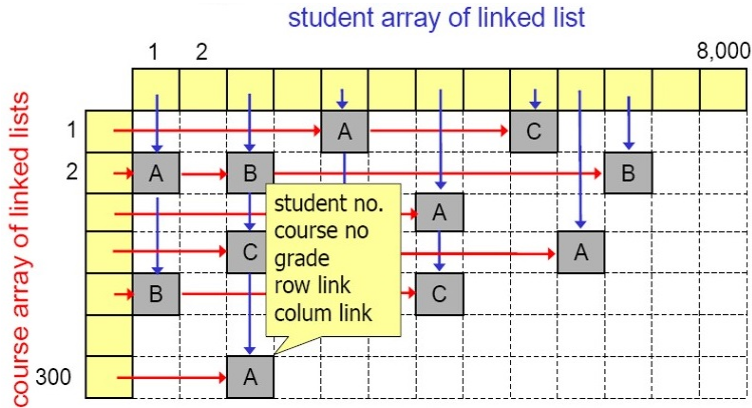
Linear list concepts

Array implementation

Singly linked list

Other linked lists

Comparison of implementations of list



- Why **two** arrays of linked lists?
- How about **two linked lists** of linked lists?
- How about **3-D** sparse matrices?





Linear list concepts

Array
implementation

Singly linked list

Other linked lists

Comparison of
implementations of
list

Comparison of implementations of list

- **Pros:**
 - Access to an array element is fast since we can compute its location quickly.
- **Cons:**
 - If we want to insert or delete an element, we have to shift subsequent elements which slows our computation down.
 - We need a large enough block of memory to hold our array.



- **Pros:**
 - Inserting and deleting data does not require us to move/shift subsequent data elements.
- **Cons:**
 - If we want to access a specific element, we need to traverse the list from the head of the list to find it which can take longer than an array access.
 - Linked lists require more memory



Comparison of implementations of list

- **Contiguous storage is generally preferable when:**
 - the entries are individually very small;
 - the size of the list is known when the program is written;
 - few insertions or deletions need to be made except at the end of the list; and
 - random access is important.
- **Linked storage proves superior when:**
 - the entries are large;
 - the size of the list is not known in advance; and
 - flexibility is needed in inserting, deleting, and rearranging the entries.

