#### Hash

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#### Basic concepts

## Hash functions

Direct Hashing Modulo division Digit extraction Mid-square Mid-square

Folding Rotation

Pseudo-random

Collision resolution

Open addressing Linked list resolution

Bucket hashing

## Chapter 9 Hash

Data Structures and Algorithms

**Luong The Nhan, Tran Giang Son** Faculty of Computer Science and Engineering University of Technology, VNU-HCM



#### Hash functions Direct Hashing

Modulo division Digit extraction Mid-square Mid-square Folding Rotation

## Pseudo-random

Open addressing Linked list resolution

Bucket hashing

## Collision resolution

- **L.O.5.1** Depict the following concepts: hashing table, key, collision, and collision resolution.
- L.O.5.2 Describe hashing functions using pseudocode and give examples to show their algorithms.
- L.O.5.3 Describe collision resolution methods using pseudocode and give examples to show their algorithms.
- **L.O.5.4** Implement hashing tables using C/C++.
- L.O.5.5 Analyze the complexity and develop experiment (program) to evaluate methods supplied for hashing tables.
- L.O.1.2 Analyze algorithms and use Big-O notation to characterize the computational complexity of algorithms composed by using the following control structures: sequence, branching, and iteration (not recursion).

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## Collision resolution

- Sequential search: O(n)
- Binary search:  $O(\log_2 n)$

→ Requiring several key comparisons before the target is found.

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## Search complexity:

	1		
Size	Binary	Sequential	Sequential
		(Average)	(Worst Case)
16	4	8	16
50	6	25	50
256	8	128	256
1,000	10	500	1,000
10,000	14	5,000	10,000
100,000	17	50,000	100,000
1,000,000	20	500,000	1,000,000



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Is there a search algorithm whose complexity is O(1)?

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Is there a search algorithm whose complexity is O(1)? YES



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keys

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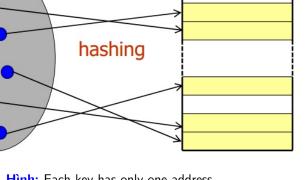
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## Collision resolution

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memory addresses

Hình: Each key has only one address

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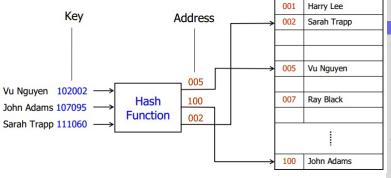
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## Collision resolution

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- Home address: address produced by a hash function.
- Prime area: memory that contains all the home addresses.

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## Collision resolution

- Home address: address produced by a hash function.
- Prime area: memory that contains all the home addresses.
- Synonyms: a set of keys that hash to the same location.
- Collision: the location of the data to be inserted is already occupied by the synonym data.

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- Home address: address produced by a hash function.
- Prime area: memory that contains all the home addresses.
- Synonyms: a set of keys that hash to the same location.
- Collision: the location of the data to be inserted is already occupied by the synonym data.
- Ideal hashing:
  - No location collision
  - Compact address space

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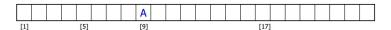
## Collision resolution

Insert A, B, C

hash(A) = 9

hash(B) = 9

hash(C) = 17



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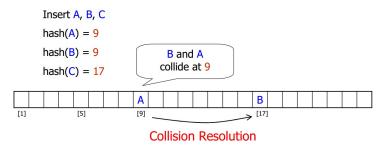
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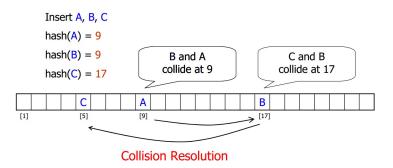
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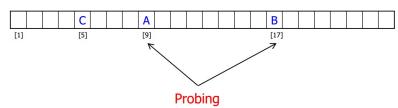
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Searh for B

hash(A) = 9

hash(B) = 9

hash(C) = 17



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## Hash functions

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## **Direct Hashing**

The address is the key itself:

hash(Key) = Key

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## **Direct Hashing**

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## Collision resolution

- Advantage: there is no collision.
- Disadvantage: the address space (storage size) is as large as the key space.

## Modulo division

## $Address = Key \ mod \ listSize$

- Fewer collisions if listSize is a prime number
- Example: Numbering system to handle 1,000,000 employees Data space to store up to 300 employees

 $hash(121267) = 121267 \mod 307 = 2$ 

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## Collision resolution

## **Digit extraction**

## Address = selected digits from Key

## Example:

 $379452 \rightarrow 394$ 

 $121267 \rightarrow 112$ 

 $378845 \rightarrow 388$ 

 $160252 \rightarrow 102$ 

 $045128 \rightarrow 051$ 

#### Hash

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## Collision resolution

## Mid-square

## $Address = middle \ digits \ of \ Key^2$

## Example:

 $9452 * 9452 = 89340304 \rightarrow 3403$ 

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## Collision resolution

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- Disadvantage: the size of the  $Key^2$  is too large.
- Variations: use only a portion of the key.
   Example:

 $379452: 379 * 379 = 143641 \rightarrow 364$ 

121267: 121 \* 121 =  $014641 \rightarrow 464$ 

 $045128: 045 * 045 = 002025 \rightarrow 202$ 

## **Folding**

The key is divided into parts whose size matches the address size.

## Example:

Key = 
$$123|456|789$$
  
fold shift  
 $123 + 456 + 789 = 1368$   
 $\rightarrow 368$ 

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## Collision resolution

## **Folding**

The key is divided into parts whose size matches the address size.

## Example:

Key = 
$$123|456|789$$
  
fold shift  
 $123 + 456 + 789 = 1368$   
 $\rightarrow 368$ 

# fold boundary 321 + 456 + 987 = 1764 $\rightarrow$ 764

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## Collision resolution

## **Rotation**

- Hashing keys that are identical except for the last character may create synonyms.
- The key is rotated before hashing.

original key	rotated key	
60010 <mark>1</mark>	<b>1</b> 60010	
60010 <mark>2</mark>	<b>2</b> 60010	
60010 <mark>3</mark>	<b>3</b> 60010	
60010 <mark>4</mark>	<b>4</b> 60010	
60010 <mark>5</mark>	<b>5</b> 60010	

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## Pseudo-random

## Collision resolution

## **Rotation**

Used in combination with fold shift.

```
original key rotated key 600101 \rightarrow 62 \quad 160010 \rightarrow 26 600102 \rightarrow 63 \quad 260010 \rightarrow 36 600103 \rightarrow 64 \quad 360010 \rightarrow 46 600104 \rightarrow 65 \quad 460010 \rightarrow 56 600105 \rightarrow 66 \quad 560010 \rightarrow 66
```

Spreading the data more evenly across the address space.

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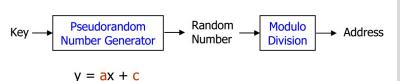
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## Pseudo-random

## Collision resolution

## Pseudo-random



For maximum efficiency,  $\boldsymbol{a}$  and  $\boldsymbol{c}$  should be prime numbers.

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## Collision resolution

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# Example:

$$Key = 121267$$

$$a = 17$$

$$c = 7$$

$$listSize = 307$$

$$Address = ((17*121267 + 7) \mod 307)$$

$$= (2061539 + 7) \mod 307$$

$$= 2061546 \mod 307$$

$$= 41$$

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**Collision resolution** 

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- Except for the direct hashing, none of the others are one-to-one mapping
  - → Requiring collision resolution methods
- Each collision resolution method can be used independently with each hash function

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## ollision resolutio

 A rule of thumb: a hashed list should not be allowed to become more than 75% full.

## Load factor:

$$\alpha = (k/n) \times 100$$

n = list size

k = number of filled elements

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## collision resolutio

- As data are added and collisions are resolved, hashing tends to cause data to group within the list.
  - → Clustering: data are unevenly distributed across the list.
- High degree of clustering increases the number of probes to locate an element.
  - → Minimize clustering.

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## ollision resolutio

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 Primary clustering: data become clustered around a home address.

Insert A<sub>9</sub>, B<sub>9</sub>, C<sub>9</sub>, D<sub>11</sub>, E<sub>12</sub>



[9] [10] [11] [12] [13]

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• Secondary clustering: data become grouped along a collision path throughout a list.

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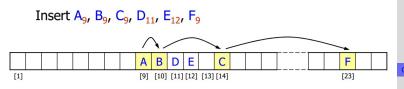
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### Collision resolution

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- Open addressing
- Linked list resolution
- Bucket hashing

When a collision occurs, an unoccupied element is searched for placing the new element in.

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Collision resolution

### collision resolution

## Open addressing

# Hash function:

$$h: U \to \{0, 1, 2, ..., m-1\}$$

set of keys

addresses

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#### Collision resolution

### Open addressing

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## Hash and probe function:

$$hp: U {\times} \{0,1,2,...,m{-}1\} \to \{0,1,2,...,m{-}1\}$$

set of keys probe numbers

addresses

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### Collision resolution

### Open addressing

**Algorithm** hashInsert(ref T <array>, val k <key>) Inserts key k into table T.

```
 \begin{split} \mathbf{i} &= 0 \\ \mathbf{while} \ i < m \ \mathbf{do} \\ & \quad \mathbf{j} = \mathsf{hp}(\mathsf{k}, \ \mathsf{i}) \\ & \quad \mathbf{if} \ T[j] = \mathit{nil} \ \mathbf{then} \\ & \quad | \ T[j] = \mathsf{k} \\ & \quad | \ \mathsf{return} \ \mathsf{j} \\ & \quad \mathsf{else} \\ & \quad | \ \mathbf{i} = \mathsf{i} + 1 \\ & \quad \mathsf{end} \end{split}
```

end

return error: "hash table overflow"

End hashInsert

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#### Open addressing

**Algorithm** hashSearch(val T <array>, val k <key>) Searches for key k in table T.

```
 \begin{aligned} \mathbf{i} &= \mathbf{0} \\ \mathbf{while} \ i &< m \ \mathbf{do} \\ &\mid \mathbf{j} &= \mathrm{hp}(\mathbf{k}, \ \mathbf{i}) \\ &\quad \mathbf{if} \ T[j] &= k \ \mathbf{then} \\ &\mid \ \mathrm{return} \ \mathbf{j} \\ &\quad \mathbf{else} \ \mathbf{if} \ T[j] &= \mathit{nil} \ \mathbf{then} \\ &\mid \ \mathrm{return} \ \mathrm{nil} \\ &\quad \mathbf{else} \\ &\mid \ \mathbf{i} &= \mathbf{i} + 1 \\ &\quad \mathbf{end} \end{aligned}
```

end
return nil
End hashSearch

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## There are different methods:

- Linear probing
- Quadratic probing
- Double hashing
- Key offset

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### Collision resolution

### Open addressing

• When a home address is occupied, go to the next address (the current address + 1):  $hp(k,i) = (h(k) + i) \mod m$ 

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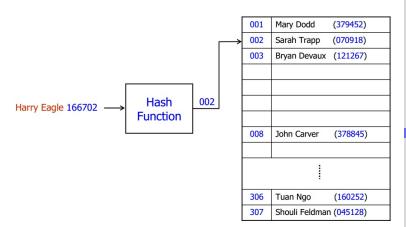
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### Collision resolution

### Open addressing

 When a home address is occupied, go to the next address (the current address + 1):  $hp(k,i) = (h(k) + i) \mod m$ 



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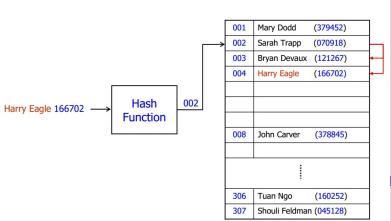
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#### Collision resolution

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## Advantages:

- quite simple to implement
- data tend to remain near their home address (significant for disk addresses)
- Disadvantages:
  - produces primary clustering

## **Quadratic Probing**

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# The address increment is the collision probe number squared:

$$hp(k,i) = (h(k) + i^2) \mod m$$

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## **Quadratic Probing**

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## Advantages:

works much better than linear probing

## • Disadvantages:

- time required to square numbers
- produces secondary clustering

$$h(k_1) = h(k_2) \to hp(k_1, i) = hp(k_2, i)$$

## **Double Hashing**

# • Using two hash functions:

$$hp(k,i) = (h_1(k) + ih_2(k)) \mod m$$

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### Collision resolution

### Open addressing

### **Key Offset**

 The new address is a function of the collision address and the key.

$$offset = [key/listSize]$$
  
 $newAddress =$   
 $(collisionAddress + offset) \ mod \ listSize$ 



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----

## Collision resolution

### Open addressing

## **Key Offset**

 The new address is a function of the collision address and the key.

$$\begin{split} offset &= [key/listSize] \\ newAddress &= \\ (collisionAddress + offset) \; mod \; listSize \end{split}$$

$$hp(k,i) = (hp(k,i-1) + [k/m]) \mod m$$

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### Collision resolution

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## Hash and probe function:

$$hp: U \times \{0, 1, 2, ..., m-1\} \rightarrow \{0, 1, 2, ..., m-1\}$$

set of keys probe numbers

addresses

 $\{hp(k,0),hp(k,1),\ldots,hp(k,m-1)\}$  is a permutation of  $\{0,1,\ldots,m-1\}$ 

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#### Collision resolution

### Open addressing

### Linked List Resolution

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- Major disadvantage of Open Addressing: each collision resolution increases the probability for future collisions.
  - → use linked lists to store synonyms

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### Linked list resolution

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Bucket hashing

001	Mary Dodd	(379452)	$\triangleright$			
002	Sarah Trapp	(070918)	-	$\rightarrow$	Harry Eagle	(166702)
003	Bryan Devaux	(121267)	$\rightarrow$	1		
			$\rightarrow$		Chris Walljas	sper (572556)
			$\rightarrow$			$\hat{1}$
			$\rightarrow$	1		
			$\rightarrow$		ove	rflow area
800	John Carver	(378845)	$\rangle$	1		
			$\rightarrow$	1	C prin	ne area
306	Tuan Ngo	(160252)	$\rightarrow$			
307	Shouli Feldmar	n (045128)	$\rightarrow$			

### **Bucket hashing**

# Hash

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### Collision resolution

Open addressing Linked list resolution

Bucket hashing

# Hashing data to buckets that can hold multiple pieces of data.

 Each bucket has an address and collisions are postponed until the bucket is full.

## **Bucket hashing**

1600 65 (6.5	Mary Dodd	(379452)			
001					
199555	Sarah Trapp	(070918)			
002	Harry Eagle	(166702)			
	Ann Georgis	(367173)			
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#### Basic concepts

#### Hash functions

Direct Hashing
Modulo division
Digit extraction
Mid-square
Mid-square
Folding

Rotation Pseudo-random

### Collision resolution

Open addressing Linked list resolution

Bucket hashing