# Project Summary

*The aim of researching the game of Go is to determine a winning position, where a capture occurs of a set of white stones surrounded by black stones. The game of Go is limited to two players, given a set position of pre-placed stones on the board. The project model being developed analyzes when all white stones are fully captured by black stones. The model will account for true or false cases that show a valid or invalid capture. The model will examine stones placed on a 5 by 5 grid.*

# Propositions

*List of the propositions used in the model, and their (English) interpretation.*

* Bi,j : This is **True** for position (i, j) if there is a black stone in it.
* Wi,j : This is **True** for position (i, j) if there is a white stone in it.
* Si,j : This is **True** for position (i, j) if there is a white stone at position (i, j) and if it is surrounded by 4 other stones in each cardinal direction.
* Oi,j : This is **True**for position (i, j) if the position is "out of bounds".
  + Out of bounds is defined as where **i or j** are not in the range **[0,n)**
* R:  **True** when all white stones can be taken, **False** when not all white stones can be taken

# Constraints

*List of constraint types used in the model and their (English) interpretation. You only need to provide one example for each constraint type: e.g., if you have constraints saying “cars have one colour assigned” in a car configuration setting, then you only need to show the constraints for a single car. Essentially, we want to see the pattern for all of the types of constraints, and not every constraint enumerated.*

Stones of two types cannot share the same position. A spot with a white stone cannot also have a black stone on it and vice versa.

Any position that is out of bounds we will consider to be a black stone. So, if a position is out of bounds there is a black stone on it.

For any position, a stone is surrounded if it is a white stone that is surrounded by either a white or black stone in all cardinal directions.

If there is a white stone that is not surrounded on all four sides by other stones, then all white stones are not captured in this position ().

# Model Exploration

## Automating Tests & Partial Assignments

We began by trying to implement a method of running tests in our Python script. We thought that this would speed up much of the experimentation when we could run and clearly see what cases passed or failed. However, in our journey, we encountered many roadblocks and finished with more knowledge of Bauhaus and Python decorators. Here are some brief points of the things we encountered as we built our automated tests.

We first tried to reset the state of our Encoding object, so we searched the Bauhaus documentation- which led us to purge\_propositions() clear\_constraints(). We tried implementing these by putting them in our Test.run() method at the top but ran into issues where the previous state would not be properly reset, such that the result of testcase1 would interfere with testcase2’s result, causing the rest of test cases beyond testcase1 to evaluate to False. We deduced this because when we ran each test as the first test in each list, it passed and gave predictable behaviour.

We were hesitant to abandon this approach, so a lot of time was spent debugging and trying to figure out why it wasn’t working. Eventually, we had a breakthrough when we put everything inside our Test.run() method, as fully resetting everything by creating a new Encoding object as well as reassigning new decorators solved the issue of test-to-test interference.

By instantiating brand new variables as well as classes for each test case, we were able to generate the following test cases and their visualizations- this way of testing was also our way of exploring specific partial assignments (board configurations).

A screen shot of a computer program

Description automatically generated

A screenshot of a computer

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A screenshot of a computer

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A black screen with white text

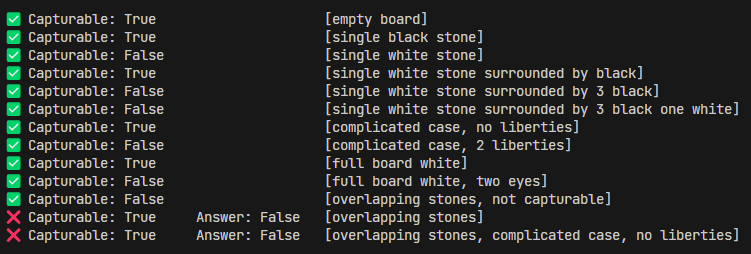
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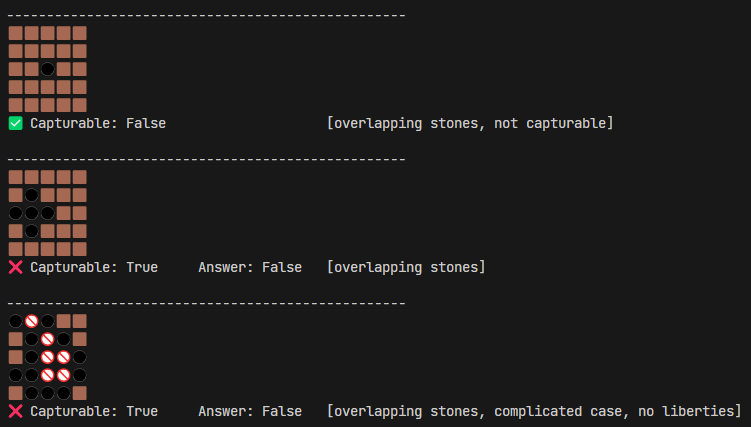
## Redundant Constraints

We discovered that none of our constraints were redundant. All are necessary for our model to run properly! However, along the way, we encountered bugs and fixed them by changing our implementation details. Here are some of the constraints we tried to remove:

### Removal of Overlapping Stones Constraint

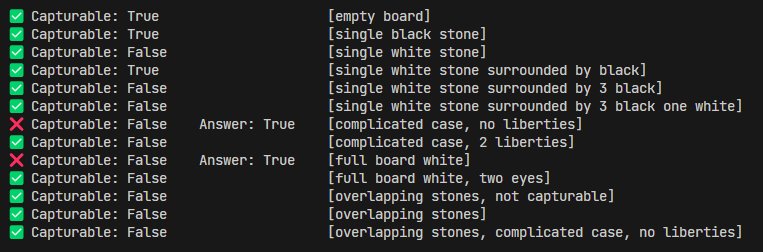
Just a detail of an obstacle we encountered on our journey: The first time around when we ran the tests, despite removing the constraint, it passed all cases. We later deduced that because of the way we implemented our surrounded(i,j) method- specifically, we returned early when finding a black stone, as we assumed that if at a position we found a black stone, there could be no white stone at that position. However, this early return led to us encoding the contrasting programmatically. When we removed this to reflect the True nature of our original logical statement- returning True if a white stone is surrounded, and False otherwise, the constraint we implemented in add\_constraints() for overlapping stones became necessary.





* Our last two test cases failed because we’d expect any invalid board state- such as one containing overlapping stones to evaluate to be False because it would be a contradiction. However, when the constraint is removed, we do not immediately evaluate to False from contradiction, as there is no constraint to create that contradiction. Instead, we pretend that there is no black stone when stones overlap- causing our last two cases where white stones normally are captured to evaluate to True.
* Note that in Image 1.2 above, where we show the board state of each test case, the overlapping stone displays as a black stone, and is positioned at (2,2), (1,2), and (1,3) respectively.

### Removal of Out-of-bounds is Black Stone Constraint





* When we removed this constraint, it led to white stones along the edges of the board to assume there were liberties instead of being blocked off.
* (Image 2 Case 2): the stone on (1,0) should be surrounded, but because one of its neighbours is the border, it lacks that proposition needed to deem it a surrounded stone- thereby failing the test case.
* (Image 2 Case 4): all the stones adjacent to the border are not seen as surrounded (notice the difference in emoji, surrounded stones are marked with a red slash and circle outline)

# Jape Proof Ideas

*List the ideas you have to build sequents & proofs that relate to your project.*

* For a single white stone that is surrounded by black stones, prove that it is surrounded.
* If there are no white stones, prove that all white stones are captured.
* If the board is all white stones, prove that all white stones are captured.
* If there exists a position that is out of bounds, then there exists a black stone.
* If a board has all white stone prove there are no black stones.
* For a single white stone surrounded by two black stones, prove it is not captured.
* Some mostly completed proofs can be found adjacent to this file.

# Requested Feedback

*Provide 2-3 questions you’d like the TA’s and other students to comment on.*

* What are some possible extensions that can be implemented to increase the complexity of the model? Do we need to increase the complexity of our model?
* Are our Jape proofs of the right level of complexity?
* Are there any additional constraints which may need to be implemented?
* What other ways of exploration do you see fits our problem/model?

# First-Order Extension

*Describe how you might extend your model to a predicate logic setting, including how both the propositions and constraints would be updated.* ***There is no need to implement this extension!***

## Propositions

* White (i,j): There is a white stone at position (i,j)
* Black(i,j): There is a black stone at position (i,j)
* Surround(i,j): The stone at location i,j is surrounded in all cardinal directions by other stones.
* Out(i,j): The position (i,j) is outside of the bounds of the board.
* Captured: True if all white stones can be taken and false otherwise.
* Equality: Allows us to set the state of a proposition directly.

## Constraints

* Stones of two types cannot share the same position.
* Any position that is out of bounds is considered a black stone.
* If a white stone is surrounded by white or black stones in each cardinal direction, then it is surrounded.
* If there is a white stone that is not surrounded, then not all stones can be captured.

# Useful Notation

*Feel free to copy/paste the symbols here and remove this section before submitting.*