

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 1

```
0001 !CAMB spherical and hypersphere
0002 !This version May 2006 - mino
0003 !Feb 2007: fixed for high l,
0004 !Feb 2009: minor fix for non-
0005 !Dec 2011: minor tweak to DoR
0006 !cccccccccccccccccccccccccccc
0007 !Flat bessel function module
0008
0009     module SpherBessels
0010         use Precision
0011         use ModelParams
0012         use Ranges
0013         implicit none
0014         private
0015
0016     !     Bessel functions and th
0017
0018         real(dl), dimension(:, :
0019
0020             integer num_xx, kmax
0021 !         parameters for working
0022 !         Both should increase if
0023 !             real(dl), parameter
0024 !             real(dl), parameter
0025
0026             Type(Regions):: BessR
0027
0028         public ajl, ajlpr, dd
0029         public USpherBesselWi
0030
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 1

```
0001 !CAMB spherical and hyper
0002 !This version May 2006 -
0003 !Feb 2007: fixed for high
0004 !Feb 2009: minor fix for
0005 !Dec 2011: minor tweak to
0006 !cccccccccccccccccccccccc
0007 !Flat bessel function mod
0008
0009     module SpherBessels
0010         use Precision
0011         use ModelParams
0012         use Ranges
0013         implicit none
0014         private
0015
0016     !     Bessel functions an
0017
0018         real(dl), dimension(:, :, :
0019
0020             integer num_xx, kmaxfile
0021 !         parameters for wor
0022 !         Both should increa
0023 !             real(dl), parame
0024 !             real(dl), parameter :: xl
0025
0026             Type(Regions):: BessRange
0027
0028         public ajl, ajlpr, ddajlp
0029         public USpherBesselWithDe
0030
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 31

```
0031 contains
0032
0033
0034 subroutine InitSpherBessel
0035 ! This subroutine reads t
0036 use lvalues
0037 implicit none
0038
0039 !See if already loaded
0040 if (allocated(ajl) .and.
0041 .and. (in
0042
0043 !Haven't made them before
0044 call GenerateBessels
0045
0046 if (DebugMsgs .and. Feedb
0047
0048 end subroutine InitSpherB
0049
0050 subroutine GenerateBessel
0051 use lvalues
0052 real(dl) x
0053 real(dl) xlim
0054 integer i,j
0055 integer max_ix
0056 real(dl), parameter :: be
0057
0058 if (DebugMsgs .and. Feedb
0059
0060
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 31

```
0031 contains
0032
0033
0034 subroutine InitSpherBesse
0035 ! This subroutine rea
0036 use lvalues
0037 implicit none
0038
0039 !See if already loaded wi
0040 if (allocated(ajl) .and.
0041 .and. (int(min(max_be
0042
0043 !Haven't made them before
0044 call GenerateBessels
0045
0046 if (DebugMsgs .and. Feedb
0047
0048 end subroutine InitSpherB
0049
0050 subroutine GenerateBessel
0051 use lvalues
0052 real(dl) x
0053 real(dl) xlim
0054 integer i,j
0055 integer max_ix
0056 real(dl), parameter :: be
0057
0058 if (DebugMsgs .and. Feedb
0059
0060
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 61

```
0061
0062      file_numl= lSamp%10
0063      file_l(1:lSamp%10) = kmaxfile = int(min(CP
0064      if (do_bispectrum) km
0065
0066
0067
0068      call Ranges_Init(Bess
0069
0070      call Ranges_Add_delta
0071      call Ranges_Add_delta
0072      call Ranges_Add_delta
0073      call Ranges_Add_delta
0074      call Ranges_Add_delta
0075
0076      call Ranges_GetArray(
0077      num_xx = BessRanges%n
0078
0079
0080      max_ix = min(max_besse
0081
0082      if (allocated(ajl)) de
0083      if (allocated(ajlpr))
0084      if (allocated(ddajlpr))
0085      Allocate(ajl(1:num_xx,
0086      Allocate(ajlpr(1:num_x
0087      Allocate(ddajlpr(1:num_
0088
0089      !$OMP PARALLEL DO DEFA
0090      do j=1,max_ix
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 61

```
0061
0062      file_numl= lSamp%10
0063      file_l(1:lSamp%10) = 1Sam
0064      kmaxfile = int(min(CP%Max
0065      if (do_bispectrum) kmaxfi
0066
0067
0068      call Ranges_Init(BessRang
0069
0070      call Ranges_Add_delta(Bes
0071      call Ranges_Add_delta(Bes
0072      call Ranges_Add_delta(Bes
0073      call Ranges_Add_delta(Bes
0074      call Ranges_Add_delta(Bes
0075
0076      call Ranges_GetArray(bess
0077      num_xx = BessRanges%npoi
0078
0079
0080      max_ix = min(max_bessels_
0081
0082      if (allocated(ajl)) deal
0083      if (allocated(ajlpr)) dea
0084      if (allocated(ddajlpr)) d
0085      Allocate(ajl(1:num_xx,1:m
0086      Allocate(ajlpr(1:num_xx,1
0087      Allocate(ddajlpr(1:num_xx
0088
0089      !$OMP PARALLEL DO DEFAULT
0090      do j=1,max_ix
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 91

```
0091      do i=1,num_xx  
0092          x=BessRanges%point  
0093          xlim=xlimfrac*1Sa  
0094          xlim=max(xlim,xli  
0095          xlim=lSamp%l(j)-x  
0096          if (x > xlim) the  
0097              if ((lSamp%l(j  
0098                  (ajl(i,j)=0  
0099                  else  
0100                      !if ( lSamp  
0101                          ! ajl(i,j)  
0102                          !else  
0103                              call bj1(l  
0104                              !end if  
0105                          end if  
0106                      end if  
0107                  else  
0108                      ajl(i,j)=0  
0109                  end if  
0110              end do  
0111      !      get the interpolation m  
0112          call spline(BessRange  
0113          call spline(BessRange  
0114          end do  
0115      !$OMP END PARALLEL DO  
0116      end subroutine GenerateB
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 91

```
0091      do i=1,num_xx  
0092          x=BessRanges%point  
0093          xlim=xlimfrac*1Sa  
0094          xlim=max(xlim,xli  
0095          xlim=lSamp%l(j)-x  
0096          if (x > xlim) the  
0097              if ((lSamp%l(j  
0098                  (1Samp%l(j  
0099                  ajl(i,j)=0  
0100                  else  
0101                      !if ( 1Sa  
0102                          ! ajl(i,j)  
0103                          !else  
0104                              call bj1(l  
0105                              !end if  
0106                          end if  
0107                      end if  
0108                  else  
0109                      ajl(i,j)=0  
0110                  end if  
0111              end do  
0112          !      get the interpo  
0113          call spline(BessRange  
0114          call spline(BessRange  
0115          end do  
0116      !$OMP END PARALLEL DO  
0117      end subroutine GenerateBe
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 121

```
0121  
0122 subroutine Bessels_Free  
0123  
0124 if (allocated(ajl)) de  
0125 if (allocated(ajlpr))  
0126 if (allocated(ddajlpr))  
0127 call Ranges_Free(BessR  
0128  
0129 end subroutine Bessels_  
0130  
0131  
0132 SUBROUTINE BJL(L,X,JL)  
0133 ! !== MODIFIED SUBROUTINE  
0134 ! !== CORRECTED THE SMALL  
0135 ! !== CORRECTED THE SIGN OF  
0136 ! !== WORKS FASTER AND MORE  
0137 ! !== zqhuang@astro.utoronto.ca  
0138 IMPLICIT NONE  
0139 INTEGER L  
0140 real(dl) X,JL  
0141 real(dl) AX,AX2  
0142 real(dl),PARAMETER::L  
0143 real(dl),PARAMETER::O  
0144 real(dl),PARAMETER::P  
0145 real(dl),PARAMETER::PID1  
0146 real(dl),parameter::R  
0147 real(dl),parameter::G  
0148 real(dl),parameter::G  
0149 real(dl),PARAMETER::P  
0150 real(dl) NU,NU2,BETA,
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 121

```
0121  
0122 subroutine Bessels_Free  
0123  
0124 if (allocated(ajl)) deallo  
0125 if (allocated(ajlpr)) deallo  
0126 if (allocated(ddajlpr)) d  
0127 call Ranges_Free(BessRang  
0128  
0129 end subroutine Bessels_F  
0130  
0131  
0132 SUBROUTINE BJL(L,X,JL)  
0133 ! !== MODIFIED SUBROUTINE  
0134 ! !== CORRECTED THE SMALL  
0135 ! !== CORRECTED THE SIGN OF  
0136 ! !== WORKS FASTER AND MORE  
0137 ! !== zqhuang@astro.utoronto.ca  
0138 IMPLICIT NONE  
0139 INTEGER L  
0140 real(dl) X,JL  
0141 real(dl) AX,AX2  
0142 real(dl),PARAMETER::LN2=0  
0143 real(dl),PARAMETER::ONEML  
0144 real(dl),PARAMETER::PID2=  
0145 real(dl),PARAMETER::PID4=  
0146 real(dl),parameter::ROOTP  
0147 real(dl),parameter::GAMMA  
0148 real(dl),parameter::GAMMA  
0149 real(dl),PARAMETER::PI=3.  
0150 real(dl) NU,NU2,BETA,BETA
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 151

```
0151      real(dl) sx,sx2
0152      real(dl) cotb,cot3b,c
0153      real(dl) trigarg,expt
0154
0155      IF(L.LT.0)THEN
0156          write(*,*) 'Can n
0157          STOP
0158      ENDIF
0159      AX=DABS(X)
0160      AX2=AX**2
0161      IF(L.LT.7)THEN
0162          IF(L.EQ.0)THEN
0163              IF(AX.LT.1.D-
0164                  JL=1.D0-A
0165          ELSE
0166              JL=DSIN(A
0167          ENDIF
0168
0169      ELSEIF(L.EQ.1)THE
0170          IF(AX.LT.2.D-
0171              JL=AX/3.D
0172          ELSE
0173              JL=(DSIN(
0174          ENDIF
0175      ELSEIF(L.EQ.2)THE
0176          IF(AX.LT.3.D-
0177              JL=AX2/15
0178          ELSE
0179              JL=(-3.0D
0180          ENDIF
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 151

```
0151      real(dl) sx,sx2
0152      real(dl) cotb,cot3b,cot6b
0153      real(dl) trigarg,expterm,
0154
0155      IF(L.LT.0)THEN
0156          error stop 'Can not e
0157      ENDIF
0158      AX=DABS(X)
0159      AX2=AX**2
0160      IF(L.LT.7)THEN
0161          IF(L.EQ.0)THEN
0162              IF(AX.LT.1.D-1)TH
0163                  JL=1.D0-AX2/6
0164          ELSE
0165              JL=DSIN(AX)/A
0166          ENDIF
0167
0168      ELSEIF(L.EQ.1)THEN
0169          IF(AX.LT.2.D-1)TH
0170              JL=AX/3.D0*(1
0171          ELSE
0172              JL=(DSIN(AX)/
0173          ENDIF
0174      ELSEIF(L.EQ.2)THEN
0175          IF(AX.LT.3.D-1)TH
0176              JL=AX2/15.D0*
0177          ELSE
0178              JL=(-3.0D0*DC
0179          ENDIF
```

/Users/lp1opa/Compare/camb_simdata/bess
els.f90, Top line: 181

```
0181      ELSEIF(L.EQ.3)THE  
0182          IF(AX.LT.4.D-  
0183              JL=AX*AX2  
0184          ELSE  
0185              JL=(DCOS(  
0186                  ENDIF  
0187          ELSEIF(L.EQ.4)THE  
0188              IF(AX.LT.6.D-  
0189                  JL=AX2**2  
0190          ELSE  
0191              JL=(DSIN(  
0192                  ENDIF  
0193          ELSEIF(L.EQ.5)THE  
0194              IF(AX.LT.1.DO  
0195                  JL=AX2**2  
0196          ELSE  
0197              JL=(DSIN(  
0198                  ENDIF  
0199          ELSE  
0200              IF(AX.LT.1.DO  
0201                  JL=AX2**3  
0202          ELSE  
0203              JL=(DSIN(  
0204                  DCOS(  
0205                  ENDIF  
0206          ENDIF  
0207      ELSE  
0208          NU=0.5DO+L  
0209          NU2=NU**2  
0210          IF(AX.LT.1.D-40)T
```

/Users/lp1opa/Compare/camb_des/bessels.
f90, Top line: 180

```
0180      ELSEIF(L.EQ.3)THEN  
0181          IF(AX.LT.4.D-1)TH  
0182              JL=AX*AX2/105  
0183          ELSE  
0184              JL=(DCOS(AX)*  
0185                  ENDIF  
0186          ELSEIF(L.EQ.4)THEN  
0187              IF(AX.LT.6.D-1)TH  
0188                  JL=AX2**2/945  
0189          ELSE  
0190              JL=(DSIN(AX)*  
0191                  ENDIF  
0192          ELSEIF(L.EQ.5)THEN  
0193              IF(AX.LT.1.DO)  
0194                  JL=AX2**2*AX/  
0195          ELSE  
0196              JL=(DSIN(AX)*  
0197                  ENDIF  
0198          ELSE  
0199          IF(AX.LT.1.DO)THE  
0200              JL=AX2**3/135  
0201          ELSE  
0202              JL=(DSIN(AX)*  
0203                  DCOS(AX)*  
0204                  ENDIF  
0205          ENDIF  
0206      ELSE  
0207          NU=0.5DO+L  
0208          NU2=NU**2  
0209          IF(AX.LT.1.D-40)THEN
```

/Users/lp1opa/Compare/camb_simdata/bess
els.f90, Top line: 211

```
0211          JL=0.D0
0212      ELSEIF((AX2/L).LT.
0213          JL=DEXP(L*DLO
0214              /NU*(1.D0-
0215      ELSEIF((real(L,d1
0216          BETA=AX-PID2*
0217          JL=(DCOS(BETA
0218              -DSIN(BETA
0219                  (NU2-2
0220      ELSE
0221          L3=NU**0.325
0222          IF(AX .LT. NU
0223              COSB=NU/A
0224              SX = DSQR
0225              COTB=NU/S
0226              SECB=AX/N
0227              BETA=DLOG
0228              COT3B=COT
0229              COT6B=COT
0230              SEC2B=SEC
0231              EXPTERM=( 
0232                  - ( (4
0233                  + ((16
0234                  + (32.
0235                      /NU)/N
0236          JL=DSQRT(
0237
0238          !
0239      ELSEIF (AX .G
0240
```

/Users/lp1opa/Compare/camb_des/bessels.
f90, Top line: 210

```
0210          JL=0.D0
0211      ELSEIF((AX2/L).LT.5.D
0212          JL=DEXP(L*DLOG(AX
0213              /NU*(1.D0-AX2
0214      ELSEIF((real(L,d1)**2
0215          BETA=AX-PID2*(L+1
0216          JL=(DCOS(BETA)*(1
0217              -DSIN(BETA)*((
0218                  (NU2-20.25)/8
0219      ELSE
0220          L3=NU**0.325
0221          IF(AX .LT. NU-1.3
0222              COSB=NU/AX
0223              SX = DSQRT(NU
0224              COTB=NU/SX
0225              SECB=AX/NU
0226              BETA=DLOG(COS
0227              COT3B=COTB**3
0228              COT6B=COT3B**2
0229              SEC2B=SECB**2
0230              EXPTERM=( (2.
0231                  - ( (4.D0
0232                  + ((16.D0
0233                  + (32.D0+
0234                      /NU)/NU
0235          JL=DSQRT(COTB
0236
0237
0238          !
0239      ELSEIF (AX .GT. N
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 241

```
0241  
0242  
0243  
0244  
0245  
0246  
0247  
0248  
0249  
0250  
0251  
0252  
0253  
0254  
0255  
0256  
0257  
0258  
0259  
0260  
0261  
0262  
0263  
0264  
0265  
0266  
0267  
0268  
0269  
0270
```

COSB=NU/A
SX=DSQRT(
COTB=NU/S
SECB=AX/N
BETA=DACO
COT3B=COT
COT6B=COT
SEC2B=SEC
TRIGARG=N
-()
+()
EXPTERM=(
-()
JL=DSQRT(

! /*

ELSE

BETA=AX-N
BETA2=BET
SX=6.D0/A
SX2=SX**2
SECB=SX**
SEC2B=SEC
JL=(GAMM
-(B
-()
+(()
+(()
-()
)

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 240

```
0240  
0241  
0242  
0243  
0244  
0245  
0246  
0247  
0248  
0249  
0250  
0251  
0252  
0253  
0254  
0255  
0256  
0257  
0258  
0259  
0260  
0261  
0262  
0263  
0264  
0265  
0266  
0267  
0268  
0269
```

COSB=NU/AX
SX=DSQRT(AX2-
COTB=NU/SX
SECB=AX/NU
BETA=DACOS(CO
COT3B=COTB**3
COT6B=COT3B**
SEC2B=SECB**2
TRIGARG=NU/CO
-((2.0+3.
+(16.D0-(
EXPTERM=((4.
-(32.D0+(
JL=DSQRT(COTB
!
/*

ELSE

BETA=AX-NU
BETA2=BETA**2
SX=6.D0/AX
SX2=SX**2
SECB=SX**0.33
SEC2B=SECB**2
JL=(GAMMA1*S
-(BETA2/1
-((BETA2-
+(((BETA2
+(((BETA2
-(((BETA

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 271

```
0271                                BE  
0272          ENDIF  
0273          ENDIF  
0274          ENDIF  
0275      IF(X.LT.0.AND.MOD(L,2  
0276      END SUBROUTINE BJL  
0277  
0278 !      end module SpherBessels  
0279  
0280  
0281  
0282  
0283 !cccccccccccccccccccccccccccc  
0284 !  
0285 ! Calculation of ultraspheric  
0286 ! Fortran version of the c pr  
0287 ! WKB approx described in ast  
0288 !  
0289 ! Modifications by Anthony Ch  
0290 ! Minor modifications to corr  
0291 ! the small chi approximation  
0292 ! the quadratic approximation  
0293 ! Bug fixed in downwards recu  
0294 !  
0295 ! The routine phi_recurs uses  
0296 ! the functions, which is acc  
0297 ! ***NOT STABLE FOR K=1 or  
0298 !  
0299 ! The routine phi_langer uses  
0300 ! uniform first-order asympto
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 270

```
0270                                BETA2+793  
0271          ENDIF  
0272          ENDIF  
0273          ENDIF  
0274      IF(X.LT.0.AND.MOD(L,2).NE  
0275      END SUBROUTINE BJL  
0276  
0277 !      end module SpherBess  
0278  
0279  
0280  
0281  
0282  
0283 !cccccccccccccccccccccccccccc  
0284 !  
0285 ! Calculation of ultrasph  
0286 ! Fortran version of the  
0287 ! WKB approx described in  
0288 !  
0289 ! Modifications by Anthon  
0290 ! Minor modifications to  
0291 ! the small chi approxima  
0292 ! the quadratic approxima  
0293 ! Bug fixed in downwards  
0294 !  
0295 ! The routine phi_recurs  
0296 ! the functions, which is  
0297 ! ***NOT STABLE FOR K=1  
0298 !  
0299 ! The routine phi_langer  
0300 ! uniform first-order asy
```

/Users/lplopa/Compare/camb_simdata/bessel.f90, Top line: 301

```
0301 ! and flat cases. This approx
0302 !
0303 ! The routine qintegral calcu
0304 ! to the eikonal integral use
0305 !
0306 ! The routine airy_ai returns
0307 ! passed. It employs a Pade-t
0308 ! a Taylor expansion around z
0309 !
0310 ! The routines polevl and ple
0311 ! evaluation routines used in
0312 !
0313 !cccccccccccccccccccccccccccccc
0314
0315
0316
0317 ! module USpherBessels
0318 ! use Precision
0319 ! implicit none
0320 ! private
0321
0322
0323 !public USpherBesselWithDeri
0324
0325
0326 ! contains
0327
0328     subroutine USpherBess
0329         !returns y1=ujl*sin
0330         !aim for accuracy >
```

/Users/lplopa/Compare/camb_des/bessels.f90, Top line: 300

```
0300 ! and flat cases. This ap
0301 !
0302 ! The routine qintegral c
0303 ! to the eikonal integral
0304 !
0305 ! The routine airy_ai ret
0306 ! passed. It employs a Pa
0307 ! a Taylor expansion arou
0308 !
0309 ! The routines polevl and
0310 ! evaluation routines use
0311 !
0312 !ccccccccccccccccccccccccccc
0313
0314
0315
0316
0317 ! module USpherBessels
0318 ! use Precision
0319 ! implicit none
0320 ! private
0321
0322
0323 !public USpherBesselWithD
0324
0325
0326
0327
0328     subroutine USpherBesselWi
0329         !returns y1=ujl*sinhChi a
0330         !aim for accuracy > 1% fo
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 331

```
0331      real(dl) Chi,beta,y1,  
0332      real(dl) sin_K, cot_K  
0333      integer l,K  
0334      logical, intent(IN) :  
0335      logical DoRecurs  
  
0337      if (closed) then  
0338          sin_K = sin(Chi)  
0339          cot_K= 1._dl/tan(  
0340              K=1  
0341      else  
0342          sin_K=sinh(Chi)  
0343          cot_K = 1._dl/tan  
0344              K=-1  
0345      end if  
  
0347      sinhChi = sin_K  
0348      cothChi = cot_K  
  
0350      DoRecurs = ((l<=45*Acc  
0351          .or.closed.and.(b  
  
0353 !Deep in the tails the closed  
0354 !Added July 2003 to prevent p  
0355      if (DoRecurs .and. clo  
0356          if (Chi < asin(sqrt(  
0357              if (phi_langer(l,K  
0358                  call phi_small_c  
0359                  return  
0360      end if
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 330

```
0330      real(dl) Chi,beta,y1,y2,s  
0331      real(dl) sin_K, cot_K  
0332      integer l,K  
0333      logical, intent(IN) :: cl  
0334      logical DoRecurs  
  
0336      if (closed) then  
0337          sin_K = sin(Chi)  
0338          cot_K= 1._dl/tan(Chi)  
0339              K=1  
0340      else  
0341          sin_K=sinh(Chi)  
0342          cot_K = 1._dl/tanh(Ch  
0343              K=-1  
0344      end if  
  
0346      sinhChi = sin_K  
0347      cothChi = cot_K  
  
0349      DoRecurs = ((l<=45*Accura  
0350          .or.closed.and.(beta*  
0351  
0352      !Deep in the tails the cl  
0353      !Added July 2003 to preve  
0354      if (DoRecurs .and. closed  
0355          if (Chi < asin(sqrt(  
0356              if (phi_langer(l,  
0357                  call phi_smal  
0358                  return  
0359      end if
```

/Users/lplopa/Compare/camb_simdata/bessels.f90, Top line: 361

```
0361      end if  
0362      end if  
0363  
0364      if (DoRecurs) then  
0365          !use recursive e  
0366          y1=phi_recur(1,K,be  
0367          y2=y1*(l+1)*cothChi  
0368          if (.not.closed.or.(  
0369              sqrt(beta**2-(K  
0370          !of course we could  
0371          !phi_recur to retu  
0372  
0373  
0374      else !WKB approx  
0375          y1=phi_langer(1,K,be  
0376          y2=y1*(l+1)*cothChi  
0377          if (.not.closed.or.(  
0378              sqrt(beta**2-(K  
0379  
0380      end if  
0381  
0382      end subroutine USpher  
0383  
0384  
0385  
0386      !Calculates y1,y2 (noramlized  
0387      !by integrating up the differ  
0388      !in the region in which phi_r  
0389      !This allows closed functions  
0390      subroutine phi_small_close
```

/Users/lplopa/Compare/camb_des/bessels.f90, Top line: 360

```
0360      end if  
0361      end if  
0362  
0363      if (DoRecurs) then  
0364          !use recursive evalua  
0365          y1=phi_recur(1,K,bet  
0366          y2=y1*(l+1)*cothChi  
0367          if (.not.closed.or.(l  
0368              sqrt(beta**2-(K*  
0369          !of course we could g  
0370          !phi_recur to return  
0371  
0372  
0373  
0374      else !WKB approx  
0375          y1=phi_langer(1,K,bet  
0376          y2=y1*(l+1)*cothChi  
0377          if (.not.closed.or.(l  
0378              sqrt(beta**2-(K*  
0379  
0380  
0381  
0382  
0383  
0384  
0385  
0386      !Calculates y1,y2 (noraml  
0387      !by integrating up the di  
0388      !in the region in which p  
0389      !This allows closed funct  
0390      subroutine phi_small_clos
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 391

```
0391      integer, intent(IN) :: l  
0392      real(dl), intent(IN) :: be  
0393      real(dl) y1,y2  
0394  
0395      integer nsteps,i  
0396  
0397      real(dl) ap1,nu2,dydchil,d  
0398      real(dl) x0, delchi,sh, h6  
0399      real(dl) y1_x,y2_x, tmp,xh  
0400  
0401      nsteps = 200  
0402      ap1 = 1*(l+1)  
0403      x0 = sqrt(ap1)/beta  
0404      nu2 = beta**2  
0405  
0406      if ((beta*chi)**2/l < 0.00  
0407      !Series solution  
0408  
0409      x = chi  
0410      sh = sin(x)  
0411      tmp=(ap1/sh**2 - nu2)  
0412      y1=1e-20  
0413      y2 = ((l+1)/x - (nu2-ap1  
0414      else  
0415  
0416      x = max(1d-7,chi - 50._dl/  
0417      y1=1e-20  
0418      y2 = (l+1)*y1/x  
0419  
0420      delchi = (chi-x)/nSteps
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 390

```
0390      integer, intent(IN) :: l  
0391      real(dl), intent(IN) :: b  
0392      real(dl) y1,y2  
0393  
0394      integer nsteps,i  
0395  
0396      real(dl) ap1,nu2,dydchil,  
0397      real(dl) x0, delchi,sh, h  
0398      real(dl) y1_x,y2_x, tmp,x  
0399  
0400      nsteps = 200  
0401      ap1 = 1*(l+1)  
0402      x0 = sqrt(ap1)/beta  
0403      nu2 = beta**2  
0404  
0405      if ((beta*chi)**2/l < 0.0  
0406      !Series solution  
0407  
0408      x = chi  
0409      sh = sin(x)  
0410      tmp=(ap1/sh**2 - nu2)  
0411      y1=1e-20  
0412      y2 = ((l+1)/x - (nu2-  
0413      else  
0414  
0415      x = max(1d-7,chi - 50  
0416      y1=1e-20  
0417      y2 = (l+1)*y1/x  
0418  
0419      delchi = (chi-x)/nSte
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 421

```
0421      h6=delchi/6
0422      hh=delchi/2
0423      sh = sin(x)
0424      tmp=(ap1/sh**2 - nu2)

0426      do i=1,nSteps
0427      ! One step in the ujl integra
0428      ! fourth-order Runge-Kutta me

0430      dydchi1=y2
0431      dydchi2=tmp*y1
0432      xh=x+hh
0433      yt1=y1+hh*dydchi1
0434      yt2=y2+hh*dydchi2
0435      dyt1=yt2
0436      tmp=(ap1/sin(xh))*
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 420

```
0420      h6=delchi/6
0421      hh=delchi/2
0422      sh = sin(x)
0423      tmp=(ap1/sh**2 - nu2)

0425      do i=1,nSteps
0426          ! One step in the
0427          ! fourth-order Ru

0429      dydchi1=y2
0430      dydchi2=tmp*y1
0431      xh=x+hh
0432      yt1=y1+hh*dydchi1
0433      yt2=y2+hh*dydchi2
0434      dyt1=yt2
0435      tmp=(ap1/sin(xh))*
```



```
0437      dyt2=tmp*yt1
0438
0439      yt1=y1+hh*dyt1
0440
0441      yt2=y2+hh*dyt2
0442
0443      dym1=yt2
0444      dym2=tmp*yt1
0445      yt1=y1+delchi*dym
0446      dym1=dyt1+dym1
0447      yt2=y2+delchi*dym
0448      dym2=dyt2+dym2
0449
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 451

```
0451          x=x+delchi      !e  
0452          sh=sin(x)  
0453          dyt1=yt2  
0454          tmp=(ap1/sh**2 -  
0455          dyt2=tmp*yt1  
0456          y1=y1+h6*(dydchi1  
0457          y2=y2+h6*(dydchi2  
0458          if (y1 > 1d10 .or.  
0459          [REDACTED]  
0460          y1=y1/1d10  
0461          y2=y2/1d10  
0462          [REDACTED]  
0463          end if  
0464          end do  
0465          [REDACTED]  
0466          end if [REDACTED]  
0467          [REDACTED]  
0468          y1_x = y1; y2_x = y2 [REDACTED]  
0469          [REDACTED]  
0470          delchi = (x0 - chi)/nS  
0471          h6=delchi/6  
0472          hh=delchi/2  
0473          [REDACTED]  
0474          do i=1,nSteps  
0475          ! One step in the ujl integra  
0476          ! fourth-order Runge-Kutta me  
0477          [REDACTED]  
0478          dydchi1=y2  
0479          dydchi2=tmp*y1  
0480          xh=x+hh
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 450

```
0450          x=x+delchi      !e  
0451          sh=sin(x)  
0452          dyt1=yt2  
0453          tmp=(ap1/sh**2 -  
0454          dyt2=tmp*yt1  
0455          y1=y1+h6*(dydchi1  
0456          y2=y2+h6*(dydchi2  
0457          if (y1 > 1d10 .or.  
0458          [REDACTED]  
0459          y1=y1/1d10  
0460          y2=y2/1d10  
0461          [REDACTED]  
0462          end if  
0463          end do  
0464          [REDACTED]  
0465          end if [REDACTED]  
0466          [REDACTED]  
0467          y1_x = y1; y2_x = y2 [REDACTED]  
0468          [REDACTED]  
0469          delchi = (x0 - chi)/nStep  
0470          h6=delchi/6  
0471          hh=delchi/2  
0472          [REDACTED]  
0473          do i=1,nSteps  
0474          ! One step in the ujl  
0475          ! fourth-order Runge-  
0476          [REDACTED]  
0477          dydchi1=y2  
0478          dydchi2=tmp*y1  
0479          xh=x+hh !mid
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 481

```
0481          yt1=y1+hh*dydchi1  
0482          yt2=y2+hh*dydchi2  
0483          dyt1=yt2  
0484          tmp=(ap1/sin(xh))*  
0485  
0486  
0487          dyt2=tmp*yt1  
0488  
0489          yt1=y1+hh*dyt1  
0490          yt2=y2+hh*dyt2  
0491  
0492          dym1=yt2  
0493          dym2=tmp*yt1  
0494          yt1=y1+delchi*dym  
0495          dym1=dyt1+dym1  
0496          yt2=y2+delchi*dym  
0497          dym2=dyt2+dym2  
0498  
0499          x=x+delchi      !e  
0500          sh=sin(x)  
0501          dyt1=yt2  
0502          tmp=(ap1/sh**2 -  
0503          dyt2=tmp*yt1  
0504          y1=y1+h6*(dydchi1  
0505          y2=y2+h6*(dydchi2  
0506          if (y1 > 1d10 .or.  
0507              y1=y1/1d10  
0508              y2=y2/1d10  
0509              y1_x = y1_x/1d1  
0510              y2_x = y2_x/1d1
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 480

```
0480          yt1=y1+hh*dydchi1    !y  
0481          yt2=y2+hh*dydchi2    !y  
0482          dyt1=yt2            !d  
0483          tmp=(ap1/sin(xh)**2 -  
0484  
0485  
0486          dyt2=tmp*yt1        !d  
0487  
0488          yt1=y1+hh*dyt1      !y  
0489          yt2=y2+hh*dyt2      !y  
0490  
0491          dym1=yt2            !d  
0492          dym2=tmp*yt1        !d  
0493          yt1=y1+delchi*dym1  !y  
0494          dym1=dyt1+dym1  
0495          yt2=y2+delchi*dym2  !y  
0496          dym2=dyt2+dym2  
0497  
0498          x=x+delchi      !end p  
0499          sh=sin(x)  
0500          dyt1=yt2            !d  
0501          tmp=(ap1/sh**2 - nu2)  
0502          dyt2=tmp*yt1        !d  
0503          y1=y1+h6*(dydchi1+dyt  
0504          y2=y2+h6*(dydchi2+dyt  
0505          if (y1 > 1d10 .or. y2  
0506              y1=y1/1d10  
0507              y2=y2/1d10  
0508              y1_x = y1_x/1d10  
0509              y2_x = y2_x/1d10
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 511

```
0511  
0512      end if  
0513    end do  
0514  
0515  
0516      tmp = phi_recur(1,1  
0517      y1 = y1_x * tmp  
0518      y2 = y2_x * tmp  
0519  
0520  
0521  end subroutine phi_small_c  
0522 !*****  
0523 !  
0524 ! Calculates Phi(l,beta,chi)  
0525 ! See Abbot and Schaefer, ApJ  
0526 ! recursion relations and clo  
0527 ! (Note: Their variable y is  
0528 !  
0529 ! When the flag direction is  
0530 ! must be used because the up  
0531 ! errors. The downwards recur  
0532 ! continues downwards to l=1,  
0533 ! using the closed form solut  
0534 ! Recipes of Bessel functions  
0535 !  
0536 !*****  
0537 function phi_recur(l, K, b  
0538 !doesn't like values which
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 510

```
0510  
0511      end if  
0512    end do  
0513  
0514  
0515      tmp = phi_recur(1,1,beta  
0516      y1 = y1_x * tmp  
0517      y2 = y2_x * tmp  
0518  
0519  
0520  end subroutine phi_small_c  
0521 !*****  
0522 !  
0523 ! Calculates Phi(l,beta,c)  
0524 ! See Abbot and Schaefer,  
0525 ! recursion relations and  
0526 ! (Note: Their variable y  
0527 !  
0528 ! When the flag direction  
0529 ! must be used because th  
0530 ! errors. The downwards r  
0531 ! continues downwards to  
0532 ! using the closed form s  
0533 ! Recipes of Bessel funct  
0534 !  
0535 !*****  
0536 function phi_recur(l, K,  
0537 !doesn't like values whic
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 541

```
0541      integer, intent(IN) :: l, K
0542      real(dl), intent(IN) :: bet
0543      real(dl) phi_recurs
0544      integer j, direction, lstar
0545      real(dl) ell, kay, arg, ans
0546      real(dl) root_K
0547      real(dl) phi0, phil, phi_pl
0548      real(dl), parameter :: ACC=
0549      real(dl) sin_K, cot_K
0550
0551      ell=dble(l)
0552
0553
0554      ! Test input values
0555
0556      if(l<0) then
0557          write(*,*) "Bessel funct"
0558          stop
0559      endif
0560      if(beta<0._dl) then
0561          write(*,*) "Wavenumber b"
0562          stop
0563      endif
0564      if ((abs(K)/=1).and.(K/=0))
0565          write(*,*) "K must be 1,"
0566          stop
0567      end if
0568
0569      if(K==1) then
0570          ibeta=nint(beta)
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 540

```
0540      integer, intent(IN) :: l,
0541      real(dl), intent(IN) :: b
0542      real(dl) phi_recurs
0543      integer j, direction, lst
0544      real(dl) ell, kay, arg, a
0545      real(dl) root_K
0546      real(dl) phi0, phil, phi_
0547      real(dl), parameter :: AC
0548      real(dl) sin_K, cot_K
0549
0550      ell=dble(l)
0551
0552
0553      ! Test input values
0554
0555      if(l<0) then
0556          call MPIStop("Bessel"
0557      endif
0558      if(beta<0._dl) then
0559          call MPIStop("Wavenum"
0560      endif
0561      if ((abs(K)/=1).and.(K/=0))
0562          call MPIStop("K must"
0563      end if
0564
0565      if(K==1) then
0566          ibeta=nint(beta)
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 571

```
0571      if(ibeta<3) then  
0572          write(*,*) "Wavenumber  
0573              stop  
0574      endif  
0575      if(ibeta<=1) then  
0576          write(*,*) "Wavenumber  
0577              stop  
0578      endif  
0579  endif  
0580  
0581  if (chi<1/BIG) then  
0582      phi_recurse=0  
0583      return  
0584  end if  
0585  
0586  kay = dble(K)  
0587  arg = beta * chi  
0588  beta2 = beta**2  
0589  
0590  if(K == 0) then  
0591      cot_K = 1._dl/chi  
0592      sin_K = chi  
0593      root_K = beta  
0594  else  
0595      root_K = sqrt(beta2 -kay*e  
0596  
0597      if(K == -1) then  
0598          cot_K = 1._dl/tanh(chi)  
0599          sin_K = sinh(chi)  
0600      else
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 567

```
0567      if(ibeta<3) then  
0568          call MPIStop("Wave  
0569      endif  
0570      if(ibeta<=1) then  
0571          call MPIStop("Wave  
0572      endif  
0573  endif  
0574  
0575  if (chi<1/BIG) then  
0576      phi_recurse=0  
0577      return  
0578  end if  
0579  
0580  kay = dble(K)  
0581  arg = beta * chi  
0582  beta2 = beta**2  
0583  
0584  if(K == 0) then  
0585      cot_K = 1._dl/chi  
0586      sin_K = chi  
0587      root_K = beta  
0588  else  
0589  
0590  
0591      if(K == -1) then  
0592          cot_K = 1._dl/tan  
0593          sin_K = sinh(chi)  
0594  else
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 601

```
0601      cot_K = 1._dl/tan(chi)
0602      sin_K = sin(chi)
0603      end if
0604
0605      endif
0606
0607
0608      ! Closed form solution for
0609
0610      if (abs(chi) < 1.d-4) then
0611          if (abs(arg)<1.d-4) then
0612              phi0 = 1._dl-chi**2*(bet
0613          else
0614              phi0=sin(arg)/arg
0615          end if
0616      else
0617          phi0 = sin(arg) / (beta
0618      end if
0619
0620      if (l==0) then
0621          phi_recurr=phi0
0622          return
0623      end if
0624
0625
0626      ! Closed form solution f
0627
0628      if((abs(chi) < 1.d-4).an
0629          if(arg < 1.d-4) then
0630              phil = chi*sqrt(be
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 595

```
0595      cot_K = 1._dl/tan
0596      sin_K = sin(chi)
0597      end if
0598
0599      endif
0600
0601
0602      ! Closed form solution fo
0603
0604      if (abs(chi) < 1.d-4) the
0605          if (abs(arg)<1.d-4) t
0606              phi0 = 1._dl-chi*
0607          else
0608              phi0=sin(arg)/arg
0609          end if
0610      else
0611          phi0 = sin(arg) / (be
0612      end if
0613
0614
0615
0616
0617
0618
0619
0620
0621
0622
0623
0624      ! Closed form solution fo
0625
0626      if((abs(chi) < 1.d-4).and
0627          if(arg < 1.d-4) then
0628              phil = chi*sqrt(b
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 631

```
0631      !beta2 * chi / (3.  
0632      else  
0633          phil = (sin(arg)/a  
0634              !(sin(arg)/arg -  
0635                  end if  
0636          elseif ((abs(arg) < 1.d-  
0637              phil = arg / 3._dl  
0638          else  
0639              if (K /= 0 ) then  
0640                  phil = sin(arg) *  
0641                      phil = phil/sqrt(b  
0642              else  
0643                  phil = (sin(arg)/a  
0644                  end if  
0645              end if  
0646          if(l==1) then  
0647              phi_recurr=phil  
0648              return  
0649          end if  
0650          ! Find recursion directi  
0651          ! direction = +1 for up  
0652  
0653          if(abs(cot_K) < root_K /  
0654              direction = 1  
0655          else  
0656              direction = -1  
0657          end if  
0658  
0659          ! For K=1, must do upwar  
0660          ! NOT STABLE for all val
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 625

```
0625      !beta2 * chi / (3  
0626      else  
0627          phil = (sin(arg)/  
0628              !(sin(arg)/arg -  
0629                  end if  
0630          elseif ((abs(arg) < 1.d-4  
0631              phil = arg / 3._dl  
0632          else  
0633              if (K /= 0 ) then  
0634                  phil = sin(arg) *  
0635                      phil = phil/sqrt(  
0636              else  
0637                  phil = (sin(arg)/  
0638                  end if  
0639              end if  
0640          if(l==1) then  
0641              phi_recurr=phil  
0642              return  
0643          end if  
0644          ! Find recursion directio  
0645          ! direction = +1 for upw  
0646  
0647          if(abs(cot_K) < root_K /  
0648              direction = 1  
0649          else  
0650              direction = -1  
0651          end if  
0652  
0653          ! For K=1, must do upward  
0654          ! NOT STABLE for all valu
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 661

```
0661  
0662      if(K==1) direction = 1  
0663  
0664      ! Do upwards recursion o  
0665  
0666  
0667      if(direction == 1)then  
0668          b_minus = sqrt(beta2  
0669          phi_minus = phi0  
0670          phi_zero = phil  
0671  
0672      do j=2,1  
0673  
0674          if(K == 0) then  
0675              phi_plus = ((2*  
0676          else  
0677              b_zero = sqrt(b  
0678              phi_plus = ((2*  
0679              b_minus = b_zer  
0680          end if  
0681          phi_minus = phi_ze  
0682          phi_zero = phi_plu  
0683      end do  
0684  
0685          phi_recurs=phi_plus  
0686  
0687  
0688          return  
0689  
0690
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 655

```
0655  
0656      if(K==1) direction = 1  
0657  
0658      ! Do upwards recursion on  
0659  
0660  
0661      if(direction == 1)then  
0662          b_minus = sqrt(beta2  
0663          phi_minus = phi0  
0664          phi_zero = phil  
0665  
0666  
0667  
0668          if(K == 0) then  
0669              phi_plus = ((  
0670          else  
0671              b_zero = sqrt  
0672              phi_plus = ((  
0673              b_minus = b_z  
0674          end if  
0675          phi_minus = phi_z  
0676          phi_zero = phi_pl  
0677      end do  
0678  
0679  
0680  
0681  
0682  
0683  
0684          phi_recurs=phi_plus  
0685  
0686  
0687          return  
0688
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 691

```
0691      ! Do downwards recurs
0692
0693      else
0694          lstart = 1 + 2 * int(
0695
0696          b_zero = sqrt(beta2 -
0697          phi_plus = 0._dl
0698          phi_zero = 1._dl
0699          answer = 0._dl
0700
0701          do j= lstart - 2,1,-1
0702
0703              if(K == 0) then
0704                  phi_minus = ((2
0705              else
0706                  b_minus = sqrt(
0707                  phi_minus = ((2
0708                  b_zero = b_minu
0709              end if
0710              phi_plus = phi_zer
0711              phi_zero = phi_min
0712
0713              if(j == 1) answer
0714              if((abs(phi_zero)
0715                  phi_plus = phi_
0716                  phi_zero = phi_
0717                  answer = answer
0718              end if
0719          end do
0720
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 685

```
0685      ! Do downwards recurs
0686
0687      else
0688          lstart = 1 + 2 * int(
0689
0690          b_zero = sqrt(beta2 -
0691          phi_plus = 0._dl
0692          phi_zero = 1._dl
0693          answer = 0._dl
0694
0695
0696
0697      if(K == 0) then
0698          phi_minus = (
0699      else
0700          b_minus = sqr(
0701          phi_minus = (
0702          b_zero = b_mi
0703      end if
0704      phi_plus = phi_ze
0705      phi_zero = phi_mi
0706
0707      if(j == 1) answer
0708      if((abs(phi_zero)
0709          phi_plus = ph_
0710          phi_zero = ph_
0711          answer = answ
0712      end if
0713
0714
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 721

```
0721      ! Normalize answer to
0722
0723      answer = answer*phil
0724      phi_recur=answer
0725
0726      end if
0727
0728      end function phi_recur
0729
0730
0731 !cccccccccccccccccccccccccccc
0732 !
0733 ! Calculates Phi(l,beta,chi)
0734 ! to the first-order WKB appr
0735 ! See C.M. Bender and S.A. Or
0736 ! Scientists and Engineers (M
0737 ! chapter 10.
0738 !
0739 ! Differential equation for n
0740 ! Schrodinger form \epsilon
0741 ! where \epsilon^2 = 1/l(l+1)
0742 ! alpha \equiv beta * epsilon
0743 !
0744 ! In the K= +1 case, the func
0745 ! determined by its value on
0746 ! conditions Phi(chi + pi) =
0747 !           Phi(pi - chi) =
0748 ! This interval contains one
0749 ! can be used.
0750 ! Note that the second condit
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 715

```
0715      ! Normalize answer to
0716
0717
0718
0719
0720      end if
0721
0722
0723
0724
0725 !cccccccccccccccccccccccccccc
0726 !
0727 ! Calculates Phi(l,beta,c
0728 ! to the first-order WKB
0729 ! See C.M. Bender and S.A.
0730 ! Scientists and Engineer
0731 ! chapter 10.
0732 !
0733 ! Differential equation f
0734 ! Schrodinger form \
0735 ! where \epsilon^2 = 1/l(
0736 ! alpha \equiv beta * eps
0737 !
0738 ! In the K= +1 case, the
0739 ! determined by its value
0740 ! conditions Phi(chi + pi)
0741 !           Phi(pi - chi)
0742 ! This interval contains
0743 ! can be used.
0744 ! Note that the second co
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 751

```
0751 ! condition on beta, which m
0752 ! eigenvalue(s), the region b
0753 ! enough for the asymptotic s
0754 ! have a small discontinuity
0755 ! this behavior is corrected
0756 ! series around the regular p
0757 ! The exact eigenvalue condit
0758 ! integer >= 3 with beta > 1.
0759 !
0760 !cccccccccccccccccccccccccccccc
0761
0762
0763
0764 function phi_langer(l,K
0765 integer l,K,ibeta,kay
0766 real(dl) phi_langer
0767 real(dl) ell,symm, anu,
0768 real(dl) beta,chi,eikon
0769 real(dl) epsilon, alpha
0770
0771 real(dl) cot_K, sin_K
0772 real(dl), parameter :: PI
0773
0774
0775 ell=dble(l)
0776 achi=chi
0777
0778 symm=1._dl
0779 !
0780 ! Test input values
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 745

```
0745 ! condition on beta, whic
0746 ! eigenvalue(s), the regi
0747 ! enough for the asymptot
0748 ! have a small discontinu
0749 ! this behavior is correc
0750 ! series around the regul
0751 ! The exact eigenvalue co
0752 ! integer >= 3 with beta
0753 !
0754 !ccccccccccccccccccccccccccc
0755
0756
0757
0758 function phi_langer(l,K,b
0759 integer l,K,ibeta,kay
0760 real(dl) phi_langer
0761 real(dl) ell,symm, anu, a
0762 real(dl) beta,chi,eikonal
0763 real(dl) epsilon, alpha,
0764
0765 real(dl) cot_K, sin_K
0766 real(dl), parameter :: PI
0767 PIOVER2=1.570796327d0
0768
0769
0770
0771
0772 ell=dble(l)
0773 achi=chi
0774
0775
0776 symm=1._dl
0777 !
0778 ! Test input values
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 781

```
0781 !  
0782     if(l<0) then  
0783         write(*,*) "Bessel f  
0784         stop  
0785     endif  
0786     if(beta<0._dl) then  
0787         write(*,*) "Wavenumb  
0788         stop  
0789     endif  
0790     if ((abs(K)/=1).and.(K/0775 !  
0791         write(*,*) "K must be 0776 call MPIStop("Bes  
0792         stop 0777 if(beta<0._dl) call MPISt  
0793     end if  
0794  
0795  
0796     if(K == 1) then 0778 if ((abs(K)/=1).and.(K/0  
0797         ibeta=nint(beta) 0779 call MPIStop("K must  
0798         if(ibeta<3) then 0780 end if  
0799             write(*,*) "Waven 0781  
0800             stop 0782  
0801         endif 0783 if(K == 1) then  
0802         if(ibeta<=1) then 0784 ibeta=nint(beta)  
0803             write(*,*) "Waven 0785 if(ibeta<3) call MPISt  
0804             stop 0786 if(ibeta<=1) call MPI  
0805         endif  
0806     endif  
0807  
0808     kay=K  
0809  
0810
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 775

```
0775 !  
0776     if(l<0) call MPIStop("Bes  
0777 if(beta<0._dl) call MPISt  
0778  
0779  
0780  
0781  
0782  
0783  
0784  
0785  
0786  
0787  
0788  
0789  
0790  
0791  
0792  
0793  
0794  
0795  
0796  
0797  
0798  
0799  
0800  
0801  
0802  
0803  
0804  
0805  
0806  
0807  
0808  
0809  
0810
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 811

```
0811 ! For closed case, find equiv
0812 !
0813     if(K==1) then
0814         achi=achi-2._dl*Pi*i
0815         if(achi>PI) then
0816             achi=2._dl*PI-ach
0817             if(2*(l/2).eq.1)
0818                 symm=symmm
0819             else
0820                 symm=-symmm
0821             endif
0822         endif
0823         if(achi>PI/2._dl) th
0824             achi=PI-achi
0825             if(2*((ibeta-1-1)
0826                 symm=symmm
0827             else
0828                 symm=-symmm
0829             endif
0830         endif
0831     endif
0832
0833 ! Definitions
0834     if(K == 0) then
0835         sin_K = achi
0836     else
0837         if(K == -1) then
0838             sin_K = sinh(a
0839             else
0840                 sin_K = sin(ac
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 792

```
0792 ! For closed case, find e
0793 !
0794     if(K==1) then
0795         achi=achi-2._dl*Pi*in
0796         if(achi>PI) then
0797             achi=2._dl*PI-ach
0798             if(2*(l/2).eq.1)
0799                 symm=symmm
0800             else
0801                 symm=-symmm
0802             endif
0803         endif
0804         if(achi>PI/2._dl) the
0805             achi=PI-achi
0806             if(2*((ibeta-1-1)
0807                 symm=symmm
0808             else
0809                 symm=-symmm
0810             endif
0811         endif
0812     endif
0813
0814 ! Definitions
0815     if(K == 0) then
0816         sin_K = achi
0817     else
0818         if(K == -1) then
0819             sin_K = sinh(achi
0820             else
0821                 sin_K = sin(achi)
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 841

```
0841      end if
0842    endif
0843
0844 ! Closed form solution for l=
0845 !
0846   if(l == 0) then
0847     arg=beta*achi
0848
0849     if((abs(achi)<1.d-4)
0850       if(abs(arg)<1.d-4
0851         wkb=1._dl-achi
0852       else
0853         wkb=sin(arg)/a
0854       endif
0855     else if((abs(arg)<1.
0856       wkb=1._dl-arg*arg
0857     else
0858       wkb=sin(arg)/(bet
0859     endif
0860     phi_langer=symm*wkb
0861     return
0862   endif
0863 !
0864 ! Closed form solution for l=
0865 !
0866   if(l==1) then
0867     arg=beta*achi
0868
0869     if((abs(achi)<1.d-4)
0870       if(abs(arg)<1.d-4
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 822

```
0822      end if
0823    endif
0824
0825 ! Closed form solution fo
0826 !
0827   if(l == 0) then
0828     arg=beta*achi
0829
0830   if((abs(achi)<1.d-4).
0831     if(abs(arg)<1.d-4
0832       wkb=1._dl-ach
0833     else
0834       wkb=sin(arg)/
0835     endif
0836   else if((abs(arg)<1.d
0837     wkb=1._dl-arg*arg
0838   else
0839     wkb=sin(arg)/(bet
0840   endif
0841   phi_langer=symm*wkb
0842   return
0843
0844 !
0845 ! Closed form solution fo
0846 !
0847   if(l==1) then
0848     arg=beta*achi
0849
0850   if((abs(achi)<1.d-4).
0851     if(abs(arg)<1.d-4
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 871

```
0871      wkb=achi*sqrt(  
0872      else  
0873          wkb=(sin(arg)/  
0874          endif  
0875      else if((abs(arg)<1.  
0876          wkb)arg/3._dl  
0877      else  
0878          if(K/=0) then  
0879              if(K==1) then  
0880                  cot_K=1._dl/ta  
0881              else  
0882                  cot_K=1._dl/ta  
0883              endif  
0884          wkb=sin(arg)*cot_  
0885          wkb=wkb/sqrt(beta  
0886      else  
0887          wkb=(sin(arg)/arg  
0888      endif  
0889      end if  
0890      phi_langer=symm*wkb  
0891      return  
0892  endif  
0893 !  
0894 ! Closed form solution for K=  
0895 !  
0896      if((K==1).and.(ibeta ==  
0897          wkb=(sin_K**ell)* &  
0898              sqrt(sqrt(2._dl  
0899          wkb=wkb*(1+0.1875d0/  
0900          phi_langer=symm*wkb
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 852

```
0852      wkb=achi*sqrt  
0853      else  
0854          wkb=(sin(arg)/  
0855          endif  
0856      else if((abs(arg)<1.d  
0857          wkb)arg/3._dl  
0858      else  
0859          if(K/=0) then  
0860              if(K==1) then  
0861                  cot_K=1._  
0862              else  
0863                  cot_K=1._  
0864              endif  
0865          wkb=sin(arg)*  
0866          wkb=wkb/sqrt(  
0867      else  
0868          wkb=(sin(arg)  
0869      endif  
0870      end if  
0871      phi_langer=symm*wkb  
0872      return  
0873  endif  
0874 !  
0875 ! Closed form solution fo  
0876 !  
0877      if((K==1).and.(ibeta == (   
0878          wkb=(sin_K**ell)* &  
0879              sqrt(sqrt(2._dl*p  
0880          wkb=wkb*(1+0.1875d0/e  
0881          phi_langer=symm*wkb
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 901

```
0901      return
0902      endif
0903
0904      ! Very close to 0, return 0 (
0905      !
0906      if(abs(achi)<1.d-8) then
0907          phi_langer=0._dl
0908          return
0909      endif
0910
0911
0912      ! For closed case, find corre
0913      !
0914      if(K==1) then
0915          anu=dble(ibeta)-1._d
0916      else
0917          anu=beta
0918      endif
0919      !
0920      ! Evaluate epsilon using asym
0921      !
0922      if(l<20) then
0923          epsilon=1._dl/sqrt(e)
0924      else
0925          epsilon=1._dl/ell-0.
0926      endif
0927
0928      alpha=epsilon*anu
0929      !
0930      ! Calculate the turning point
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 882

```
0882      return
0883      endif
0884
0885      ! Very close to 0, return
0886      !
0887      if(abs(achi)<1.d-8) then
0888          phi_langer=0._dl
0889          return
0890      endif
0891
0892
0893      ! For closed case, find c
0894      !
0895      if(K==1) then
0896          anu=dble(ibeta)-1._dl
0897      else
0898          anu=beta
0899      endif
0900      !
0901      ! Evaluate epsilon using
0902      !
0903      if(l<20) then
0904          epsilon=1._dl/sqrt(e)
0905      else
0906          epsilon=1._dl/ell-0.5
0907      endif
0908
0909      alpha=epsilon*anu
0910      !
0911      ! Calculate the turning p
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 931

```
0931 ! Function in question has on
0932 !
0933     if(K===-1) chi0=log((1._d)
0934     if(K==0) chi0=1._d1/alpha
0935     if(K==1) chi0=asin(1._d1)
0936
0937
0938 ! Very close to chi0, use usu
0939 !
0940     if(abs(achi-chi0)<1.d-5)
0941
0942 ! Calculate coefficients of 1
0943 ! in the neighborhood of the
0944 ! Q(chi)=a*(chi0-chi)+b*(chi0-
0945         alpha2=alpha*alpha
0946
0947         if(K===-1) then
0948             a=2._d1*alpha2*sq
0949             b=3._d1*alpha2**2
0950         endif
0951         if(K==0) then
0952             a=2._d1*alpha2*al
0953             b=3._d1*alpha2**2
0954         endif
0955         if(K==1) then
0956             a=2._d1*alpha2*sq
0957             b=3._d1*alpha2**2
0958         endif
0959
0960 ! Dependent variable x for wh
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 912

```
0912 ! Function in question ha
0913 !
0914     if(K===-1) chi0=log((1._d1)
0915     if(K==0) chi0=1._d1/alpha
0916     if(K==1) chi0=asin(1._d1/
0917
0918
0919 ! Very close to chi0, use
0920 !
0921     if(abs(achi-chi0)<1.d-5)
0922
0923 ! Calculate coefficie
0924 ! in the neighborhood
0925 ! Q(chi)=a*(chi0-chi)
0926         alpha2=alpha*alpha
0927
0928
0929
0930
0931
0932
0933
0934
0935
0936
0937
0938
0939
0940
0941 ! Dependent variable
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 961

```
0961 ! x>0 is the evanescent region
0962 !
0963     x=chi0-achi
0964 !
0965 ! Argument of Airy function
0966 !
0967     arg=(x+b*x*x/(5._dl*
0968 !
0969 ! Evaluate Airy function
0970 !
0971     wkb=airy_ai(arg)
0972 !
0973 ! Rest of functional dependen
0974 !
0975     wkb=wkb*(1._dl-b*x/
0976 ! Normalization factor:
0977
0978     wkb=wkb*symm*ROOTPI*
0979     phi_langer=wkb
0980
0981     return
0982 endif
0983
0984
0985 ! Langer approximation.
0986 !
0987 ! Transport factor:
0988 !
0989     tmp=sqrt(abs(1._dl/(sin_
0990
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 942

```
0942 ! x>0 is the evanesce
0943 !
0944     x=chi0-achi
0945 !
0946 ! Argument of Airy fu
0947 !
0948     arg=(x+b*x*x/(5._dl*a
0949 !
0950 ! Evaluate Airy funct
0951 !
0952     wkb=airy_ai(arg)
0953 !
0954 ! Rest of functional
0955 !
0956     wkb=wkb*(1._dl-b*x/(5.
0957 ! Normalization fact
0958
0959     wkb=wkb*symm*ROOTPI*(phi_langer=wkb
0960
0961
0962     return
0963 endif
0964
0965
0966 ! Langer approximation.
0967 !
0968 ! Transport factor:
0969 !
0970     tmp=sqrt(abs(1._dl/(sin_K
0971
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 991

```
0991 ! Eikonal factor
0992 !
0993     eikonal=qintegral(sin_K
0994
0995
0996
0997     arg=(1.5d0*eikonal/epsi
0998
0999     arg2=arg*arg
1000     if(achi>chi0) arg2=-arg
1001
1002 ! Multiply factors together
1003
1004     wkb=airy_ai(arg2)*symm*
1005     phi_langer=wkb
1006
1007 end function phi_langer
1008
1009 !cccccccccccccccccccccccccccc
1010 !
1011 ! Evaluates the exact solution
1012 ! eikonal solution, \int^x
1013 !
1014 ! In the open case, this inte
1015 ! and a log; its evaluation w
1016 ! of the Phi routine. An anal
1017 ! because the dependence on a
1018 ! region of the integrand con
1019 ! can only save the computati
1020 !
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 972

```
0972 ! Eikonal factor
0973 !
0974     eikonal=qintegral(sin_K,a
0975
0976
0977
0978     arg=(1.5d0*eikonal/epsi
0979
0980     arg2=arg*arg
0981     if(achi>chi0) arg2=-arg2
0982
0983 ! Multiply factors together
0984
0985     wkb=airy_ai(arg2)*symm*RO
0986     phi_langer=wkb
0987
0988 end function phi_langer
0989
0990 !ccccccccccccccccccccccccccc
0991 !
0992 ! Evaluates the exact sol
0993 ! eikonal solution, \in
0994 !
0995 ! In the open case, this
0996 ! and a log; its evaluati
0997 ! of the Phi routine. An
0998 ! because the dependence
0999 ! region of the integrand
1000 ! can only save the compu
1001 !
```

/Users/lplopa/Compare/camb_simdata/bessels.f90, Top line: 1021

```
1021 ! The integrals are very blan  
1022 ! be precomputed and cached t  
1023 ! on a relatively small numbe  
1024 !  
1025 ! Note that for the closed ca  
1026 ! and alpha; for arg > alpha,  
1027 ! integral to this case.  
1028 !  
1029 !ccccccccccccccccccccccccccc  
1030     function qintegral(sin_<br/>  
1031         implicit none  
1032         real(dl) qintegral, sin_<br/>  
1033         integer K  
1034         real(dl) alpha,exact,ar<br/>  
1035             real(dl), parameter ::<br/>  
1036                 PI=3.141592653589793d0<br/>  
1037             arg=alpha*sin_K<br/>  
1038             if(K==0) then<br/>  
1039                 if(arg>1._dl) then<br/>  
1040                     exact=sqrt(arg*ar<br/>  
1041                     qintegral=exact<br/>  
1042                     return<br/>  
1043                 else<br/>  
1044                     root1=sqrt(1._dl-<br/>  
1045                     exact=log((1._dl+<br/>  
1046                     qintegral=exact<br/>  
1047                     return<br/>  
1048<br/>  
1049<br/>  
1050
```

/Users/lplopa/Compare/camb_des/bessels.f90, Top line: 1002

```
1002 ! The integrals are very  
1003 ! be precomputed and cach  
1004 ! on a relatively small n  
1005 !  
1006 ! Note that for the close  
1007 ! and alpha; for arg > al  
1008 ! integral to this case.  
1009 !  
1010 !cccccccccccccccccccccccccc  
1011     function qintegral(sin_K,<br/>  
1012         implicit none  
1013         real(dl) qintegral, sin_K<br/>  
1014         integer K  
1015         real(dl) alpha,exact,arg,<br/>  
1016             real(dl), parameter :: PI=<br/>  
1017                 PIOVER2=1.570796327d0<br/>  
1018             arg=alpha*sin_K<br/>  
1019             if(K==0) then<br/>  
1020                 if(arg>1._dl) then<br/>  
1021                     exact=sqrt(arg*ar<br/>  
1022                     qintegral=exact<br/>  
1023                     return<br/>  
1024                 else<br/>  
1025                     root1=sqrt(1._dl-<br/>  
1026                     exact=log((1._dl+<br/>  
1027                     qintegral=exact<br/>  
1028                     return<br/>  
1029<br/>  
1030<br/>  
1031
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 1051

```
1051      endif
1052      else if(K===-1) then
1053          if(arg>1._dl) then
1054              root1=sqrt(arg*ar
1055              root2=sqrt(arg*ar
1056              exact=alpha/2._dl
1057                  2._dl*root1
1058                      (alpha*root
1059                      qintegral=exact
1060                      return
1061      else
1062          root1=sqrt((1._dl
1063          exact=alpha/2._dl
1064              1._dl))+0.5
1065              arg*arg*(1._
1066                  alpha*alpha
1067          if(2._dl*arg*arg+
1068              exact=exact-al
1069          endif
1070          qintegral=exact
1071          return
1072      endif
1073      else
1074          if(arg>1._dl) then
1075              root1=sqrt(arg*ar
1076              root2=sqrt(alpha*
1077              exact=alpha/2._dl
1078                  (2._dl*arg*arg
1079                      atan(-root2/(r
1080              if(2._dl*arg*arg-
```

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 1032

```
1032      endif
1033      else if(K===-1) then
1034          if(arg>1._dl) then
1035              root1=sqrt(arg*ar
1036              root2=sqrt(arg*ar
1037              exact=alpha/2._dl
1038                  2._dl*root1*r
1039                      (alpha*root1)
1040                      qintegral=exact
1041                      return
1042      else
1043          root1=sqrt((1._dl
1044          exact=alpha/2._dl
1045              1._dl))+0.5d0
1046              arg*arg*(1._d
1047                  alpha*alpha)
1048          if(2._dl*arg*arg+
1049              exact=exact-a
1050          endif
1051          qintegral=exact
1052          return
1053      endif
1054      else
1055          if(arg>1._dl) then
1056              root1=sqrt(arg*ar
1057              root2=sqrt(alpha*
1058              exact=alpha/2._dl
1059                  (2._dl*arg*ar
1060                      atan(-root2/(
1061              if(2._dl*arg*arg-
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 1081

```
1081      exact=exact+al
1082      endif
1083  else
1084      root1=sqrt((1._dl
1085      dummyarg=alpha*(1
1086      exact=0.5d0*log((
1087          alpha/2._dl*log(
1088              (alpha*alpha-1._
1089      endif
1090      qintegral=exact
1091      return
1092  endif
1093
1094 end function qintegral
1095
1096 !cccccccccccccccccccccccccccc
1097 !
1098 !      Airy function
1099 !
1100 ! Modified from original rout
1101 ! as part of the Cephes libra
1102 ! Modifications: eliminates c
1103 ! and translation to Fortran
1104 !
1105 !cccccccccccccccccccccccccccc
1106 !
1107 ! DESCRIPTION:
1108 !
1109 ! Solution of the differentia
1110 !
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 1062

```
1062      exact=exact+al
1063      endif
1064  else
1065      root1=sqrt((1._dl
1066      dummyarg=alpha*(1
1067      exact=0.5d0*log((
1068          alpha/2._dl*1
1069              (alpha*alpha-
1070      endif
1071      qintegral=exact
1072      return
1073  endif
1074
1075 end function qintegral
1076
1077 !cccccccccccccccccccccccccccc
1078 !
1079 !      Airy function
1080 !
1081 ! Modified from original
1082 ! as part of the Cephes 1
1083 ! Modifications: eliminat
1084 ! and translation to Fort
1085 !
1086 !cccccccccccccccccccccccccccc
1087 !
1088 ! DESCRIPTION:
1089 !
1090 ! Solution of the differe
1091 !
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 1111

```
1111 !      y''(x) = xy.  
1112 !  
1113 ! The function returns the two  
1114 ! and their first derivatives  
1115 !  
1116 ! Evaluation is by power series  
1117 ! by rational minimax approximation  
1118 !  
1119 !  
1120 !  
1121 ! ACCURACY:  
1122 ! Error criterion is absolute  
1123 ! when function > 1, except *  
1124 ! For large negative x, the accuracy is  
1125 ! For large positive x, the relative error is  
1126 !  
1127 ! Arithmetic domain   function  
1128 ! IEEE      -10, 0     Ai    1109  
1129 ! IEEE      0, 10     Ai    1110  
1130 ! IEEE      -10, 0     Ai'   1111  
1131 ! IEEE      0, 10     Ai'   1112  
1132 ! IEEE      -10, 10    Bi    1113  
1133 ! IEEE      -10, 10    Bi'   1114  
1134 ! DEC       -10, 0     Ai    1115  
1135 ! DEC       0, 10     Ai    1116  
1136 ! DEC       -10, 0     Ai'   1117  
1137 ! DEC       0, 10     Ai'   1118  
1138 ! DEC       -10, 10    Bi    1119  
1139 ! DEC       -10, 10    Bi'   1120  
1140 !
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 1092

```
1092 !      y''(x) = xy.  
1093 !  
1094 ! The function returns the two  
1095 ! and their first derivatives  
1096 !  
1097 ! Evaluation is by power series  
1098 ! by rational minimax approximation  
1099 !  
1100 !  
1101 !  
1102 ! ACCURACY:  
1103 ! Error criterion is absolute  
1104 ! when function > 1, except *  
1105 ! For large negative x, the accuracy is  
1106 ! For large positive x, the relative error is  
1107 !  
1108 ! Arithmetic domain   function  
1109 ! IEEE      -10, 0     Ai    1109  
1110 ! IEEE      0, 10     Ai    1110  
1111 ! IEEE      -10, 0     Ai'   1111  
1112 ! IEEE      0, 10     Ai'   1112  
1113 ! IEEE      -10, 10    Bi    1113  
1114 ! IEEE      -10, 10    Bi'   1114  
1115 ! DEC       -10, 0     Ai    1115  
1116 ! DEC       0, 10     Ai    1116  
1117 ! DEC       -10, 0     Ai'   1117  
1118 ! DEC       0, 10     Ai'   1118  
1119 ! DEC       -10, 10    Bi    1119  
1120 ! DEC       -10, 10    Bi'   1120  
1121 !
```

/Users/lplopa/Compare/camb_simdata/bessel.f90, Top line: 1141

```
1141 !  
1142 ! Cephes Math Library Release  
1143 ! Copyright 1984, 1987, 1989  
1144 ! Direct inquiries to 30 Fros  
1145 !  
1146  
1147     function airy_ai(x)  
1148     implicit none  
1149     real(dl) airy_ai  
1150     real(dl) x,z, zz, t, f,  
1151     real(dl) ak  
1152     real(dl) AN(8),AD(8),AF  
1153     real(dl), parameter ::  
1154     real(dl), parameter ::  
1155     real(dl), parameter ::  
1156  
1157  
1158     AN(1)=3.465381015256290  
1159     AN(2)=1.200759527396458  
1160     AN(3)=7.627960536152345  
1161     AN(4)=1.680892249346305  
1162     AN(5)=1.597563913501644  
1163     AN(6)=7.053609068404441  
1164     AN(7)=1.402646911633896  
1165     AN(8)=9.999999999999999  
1166  
1167     AD(1)=5.675945326387702  
1168     AD(2)=1.475625625848472  
1169     AD(3)=8.451389701414746  
1170     AD(4)=1.773180881454004
```

/Users/lplopa/Compare/camb_des/bessels.f90, Top line: 1122

```
1122 !  
1123 ! Cephes Math Library Rel  
1124 ! Copyright 1984, 1987, 1  
1125 ! Direct inquiries to 30  
1126 !  
1127  
1128     function airy_ai(x)  
1129     implicit none  
1130     real(dl) airy_ai  
1131     real(dl) x,z, zz, t, f, g  
1132     real(dl) ak  
1133     real(dl) AN(8),AD(8),AFN(  
1134     real(dl), parameter :: AM  
1135     real(dl), parameter :: c1  
1136     real(dl), parameter :: sq  
1137  
1138  
1139     AN(1)=3.46538101525629032  
1140     AN(2)=1.20075952739645805  
1141     AN(3)=7.62796053615234516  
1142     AN(4)=1.68089224934630576  
1143     AN(5)=1.59756391350164413  
1144     AN(6)=7.05360906840444183  
1145     AN(7)=1.40264691163389668  
1146     AN(8)=9.9999999999999995  
1147  
1148     AD(1)=5.67594532638770212  
1149     AD(2)=1.47562562584847203  
1150     AD(3)=8.45138970141474626  
1151     AD(4)=1.77318088145400459
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 1171

1171 AD(5)=1.642346928715297
1172 AD(6)=7.147784008255756
1173 AD(7)=1.409591356078340
1174 AD(8)=1.000000000000000
1175
1176 AFN(1)=-1.3169632341833
1177 AFN(2)=-6.2645654443191
1178 AFN(3)=-6.9315803603693
1179 AFN(4)=-2.7977998154511
1180 AFN(5)=-4.9190013260950
1181 AFN(6)=-4.0626592359488
1182 AFN(7)=-1.5927649623926
1183 AFN(8)=-2.7764910815523
1184 AFN(9)=-1.6778769848911
1185
1186 AFD(1)=1.33560420706553
1187 AFD(2)=3.26825032795224
1188 AFD(3)=2.67367040941499
1189 AFD(4)=9.18707402907259
1190 AFD(5)=1.47529146771666
1191 AFD(6)=1.15687173795188
1192 AFD(7)=4.40291641615211
1193 AFD(8)=7.54720348287414
1194 AFD(9)=4.51850092970580
1195
1196 AGN(1)=1.97339932091685
1197 AGN(2)=3.91103029615688
1198 AGN(3)=1.06579897599595
1199 AGN(4)=9.39169229816650
1200 AGN(5)=3.51465656105547

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 1152

1152 AD(5)=1.64234692871529701
1153 AD(6)=7.14778400825575695
1154 AD(7)=1.40959135607834029
1155 AD(8)=1.000000000000000
1156
1157 AFN(1)=-1.316963234183317
1158 AFN(2)=-6.264565444319123
1159 AFN(3)=-6.931580360369335
1160 AFN(4)=-2.797799815451191
1161 AFN(5)=-4.919001326095003
1162 AFN(6)=-4.062659235948854
1163 AFN(7)=-1.592764962392620
1164 AFN(8)=-2.776491081552329
1165 AFN(9)=-1.677876984891146
1166
1167 AFD(1)=1.3356042070655324
1168 AFD(2)=3.2682503279522461
1169 AFD(3)=2.6736704094149955
1170 AFD(4)=9.1870740290725962
1171 AFD(5)=1.4752914677166641
1172 AFD(6)=1.1568717379518804
1173 AFD(7)=4.4029164161521120
1174 AFD(8)=7.5472034828741429
1175 AFD(9)=4.5185009297058037
1176
1177 AGN(1)=1.9733993209168567
1178 AGN(2)=3.9110302961568827
1179 AGN(3)=1.0657989759959559
1180 AGN(4)=9.3916922981665023
1181 AGN(5)=3.5146565610554761

/Users/lp1opa/Compare/camb_simdata/bessel.f90, Top line: 1201

```
1201      AGN(6)=6.33888919628925  
1202      AGN(7)=5.85804113048388  
1203      AGN(8)=2.82851600836737  
1204      AGN(9)=6.98793669997260  
1205      AGN(10)=8.1178923955438  
1206      AGN(11)=3.4155178476592  
1207  
1208      AGD(1)=9.30892908077441  
1209      AGD(2)=1.98352928718312  
1210      AGD(3)=1.55646628932864  
1211      AGD(4)=5.47686069422975  
1212      AGD(5)=9.54293611618961  
1213      AGD(6)=8.64580826352392  
1214      AGD(7)=4.12656523824222  
1215      AGD(8)=1.01259085116509  
1216      AGD(9)=1.17166733214413  
1217      AGD(10)=4.91834570062930  
1218      !  
1219      ! Exponentially tiny for larg  
1220      !  
1221      if(x>AMAXAIRY) then  
1222          airy_ai=0._dl  
1223          return  
1224      endif  
1225      !  
1226      ! Pade fit for large negative  
1227      !  
1228      if(x<-2.09d0) then  
1229          t=sqrt(-x)  
1230          zeta=-2._dl*x*t/3._d
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 1182

```
1182      AGN(6)=6.3388891962892549  
1183      AGN(7)=5.8580411304838845  
1184      AGN(8)=2.8285160083673701  
1185      AGN(9)=6.9879366999726096  
1186      AGN(10)=8.117892395543892  
1187      AGN(11)=3.415517847659236  
1188  
1189      AGD(1)=9.3089290807744197  
1190      AGD(2)=1.9835292871831214  
1191      AGD(3)=1.5564662893286461  
1192      AGD(4)=5.4768606942297549  
1193      AGD(5)=9.5429361161896188  
1194      AGD(6)=8.6458082635239219  
1195      AGD(7)=4.1265652382422260  
1196      AGD(8)=1.0125908511650913  
1197      AGD(9)=1.1716673321441352  
1198      AGD(10)=4.918345700629300  
1199      !  
1200      ! Exponentially tiny for  
1201      !  
1202      if(x>AMAXAIRY) then  
1203          airy_ai=0._dl  
1204          return  
1205      endif  
1206      !  
1207      ! Pade fit for large nega  
1208      !  
1209      if(x<-2.09d0) then  
1210          t=sqrt(-x)  
1211          zeta=-2._dl*x*t/3._d
```

/Users/lplopa/Compare/camb_simdata/bessels.f90, Top line: 1231

```
1231      t=sqrt(t)
1232      ak=sqpii/t
1233      z=1._dl/zeta
1234      zz=z*z
1235      uf=1._dl+zz*polevl(z
1236      ug=z*polevl(zz,AGN,1
1237      theta=zeta+0.25d0*PI
1238      f=sin(theta)
1239      g=cos(theta)
1240      airy_ai=ak*(f*uf-g*u
1241      return
1242  endif
1243 !
1244 ! Pade fit for large positive
1245 !
1246 if(x>=2.09) then
1247     t=sqrt(x)
1248     zeta=2._dl*x*t/3._dl
1249     g=exp(zeta)
1250     t=sqrt(t)
1251     ak=2._dl*t*g
1252     z=1._dl/zeta
1253     f=polevl(z,AN,7)/pol
1254     airy_ai=sqpii*f/ak
1255     return
1256  endif
1257 !
1258 ! Taylor series for region ar
1259 !
1260
```

/Users/lplopa/Compare/camb_des/bessels.f90, Top line: 1212

```
1212      t=sqrt(t)
1213      ak=sqpii/t
1214      z=1._dl/zeta
1215      zz=z*z
1216      uf=1._dl+zz*polevl(zz
1217      ug=z*polevl(zz,AGN,10
1218      theta=zeta+0.25d0*PI
1219      f=sin(theta)
1220      g=cos(theta)
1221      airy_ai=ak*(f*uf-g*ug
1222      return
1223  endif
1224 !
1225 ! Pade fit for large posi
1226 !
1227 if(x>=2.09) then
1228     t=sqrt(x)
1229     zeta=2._dl*x*t/3._dl
1230     g=exp(zeta)
1231     t=sqrt(t)
1232     ak=2._dl*t*g
1233     z=1._dl/zeta
1234     f=polevl(z,AN,7)/pole
1235     airy_ai=sqpii*f/ak
1236     return
1237  endif
1238 !
1239 ! Taylor series for regio
1240 !
1241
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 1261

```
1261      f=1._dl
1262      g=x
1263      t=1._dl
1264      uf=1._dl
1265      ug=x
1266      ak=1._dl
1267      z=x*x*x
1268      do while (t>ACC)
1269          uf=uf*z
1270          ak=ak+1._dl
1271          uf=uf/ak
1272          ug=ug*z
1273          ak=ak+1._dl
1274          ug=ug/ak
1275          uf=uf/ak
1276          f=f+uf
1277          ak=ak+1._dl
1278          ug=ug/ak
1279          g=g+ug
1280          t=abs(uf/f)
1281      end do
1282
1283
1284      airy_ai=c1*f-c2*g
1285
1286      end function airy_ai
1287
1288 !cccccccccccccccccccccccccccccc
1289 ! Evaluate polynomial
1290 !cccccccccccccccccccccccccccccc
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 1242

```
1242      f=1._dl
1243      g=x
1244      t=1._dl
1245      uf=1._dl
1246      ug=x
1247      ak=1._dl
1248      z=x*x*x
1249      do while (t>ACC)
1250          uf=uf*z
1251          ak=ak+1._dl
1252          uf=uf/ak
1253          ug=ug*z
1254          ak=ak+1._dl
1255          ug=ug/ak
1256          uf=uf/ak
1257          f=f+uf
1258          ak=ak+1._dl
1259          ug=ug/ak
1260          g=g+ug
1261          t=abs(uf/f)
1262      end do
1263
1264
1265      airy_ai=c1*f-c2*g
1266
1267
1268
1269 !cccccccccccccccccccccccccc
1270 ! Evaluate polynomial
1271 !cccccccccccccccccccccccccc
```

/Users/lp1lopa/Compare/camb_simdata/bessel.f90, Top line: 1291

```
1291 ! DESCRIPTION:  
1292 !  
1293 ! Evaluates polynomial of deg  
1294 !  
1295 !  $y = C_0 + C_1 x + C_2 x^2 + \dots +$   
1296 !  
1297 !  
1298 !  
1299 ! Coefficients are stored in  
1300 !  
1301 !  $\text{coef}(1) = C_N, \dots, \text{coef}(N+1)$   
1302 !  
1303 !  
1304 ! The function plevl() assume  
1305 !  
1306 ! omitted from the array. It  
1307 ! otherwise the same as polev  
1308 !  
1309 !  
1310 ! SPEED:  
1311 !  
1312 ! In the interest of speed, t  
1313 ! of bounds arithmetic. This  
1314 ! the functions in the library  
1315 ! equipment features, the use  
1316 ! program in microcode or ass  
1317 !  
1318 ! Cephes Math Library Release  
1319 ! Copyright 1984, 1987, 1988  
1320 ! Direct inquiries to 30 Fros
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 1272

```
1272 ! DESCRIPTION:  
1273 !  
1274 ! Evaluates polynomial of  
1275 !  
1276 !  $y = C_0 + C_1 x + C_2 x^2 +$   
1277 !  
1278 !  
1279 !  
1280 ! Coefficients are stored  
1281 !  
1282 !  $\text{coef}(1) = C_N, \dots, \text{coef}(N+1)$   
1283 !  
1284 !  
1285 ! The function plevl() as  
1286 !  
1287 ! omitted from the array.  
1288 ! otherwise the same as p  
1289 !  
1290 !  
1291 ! SPEED:  
1292 !  
1293 ! In the interest of spee  
1294 ! of bounds arithmetic.  
1295 ! the functions in the li  
1296 ! equipment features, the  
1297 ! program in microcode or  
1298 !  
1299 ! Cephes Math Library Rel  
1300 ! Copyright 1984, 1987, 1  
1301 ! Direct inquiries to 30
```

/Users/lp1lopa/Compare/camb_simdata/bessels.f90, Top line: 1321

```
1321 !  
1322      function polevl(x,coef,  
1323      implicit none  
1324      real(dl) polevl  
1325      real(dl) x,ans  
1326      real(dl) coef  
1327      integer N,i  
1328  
1329      dimension coef(N+1)  
1330  
1331      ans=coef(1)  
1332      do i=2,N+1  
1333          ans=ans*x+coef(i)  
1334      end do  
1335      polevl=ans  
1336  
1337      end function polevl  
1338  
1339 !  
1340 !  
1341 ! Evaluate polynomial when co  
1342 ! Otherwise same as polevl.  
1343 !  
1344      function plevl(x,coef,N  
1345      implicit none  
1346      real(dl) plevl  
1347      real(dl) x,coef,ans  
1348      integer N,i  
1349      dimension coef(N)  
1350
```

/Users/lp1lopa/Compare/camb_des/bessels.f90, Top line: 1302

```
1302 !  
1303      function polevl(x,coef,N)  
1304      implicit none  
1305      real(dl) polevl  
1306      real(dl) x,ans  
1307      real(dl) coef  
1308      integer N,i  
1309  
1310  
1311  
1312      ans=coef(1)  
1313      do i=2,N+1  
1314          ans=ans*x+coef(i)  
1315      end do  
1316      polevl=ans  
1317  
1318      end function polevl  
1319  
1320 !  
1321 !  
1322 ! Evaluate polynomial whe  
1323 ! Otherwise same as polev  
1324 !  
1325      function plevl(x,coef,N)  
1326      implicit none  
1327      real(dl) plevl  
1328      real(dl) x,coef,ans  
1329      integer N,i  
1330      dimension coef(N)  
1331
```

/Users/lp1opa/Compare/camb_simdata/bessels.f90, Top line: 1351

```
1351      ans=x+coef(1)
1352      do i=2,N
1353          ans=ans*x+coef(i)
1354      end do
1355      plevl=ans
1356
1357      end function plevl
1358
1359
1360
1361      end module SpherBessels !US
1362
1363
1364
1365      SUBROUTINE BJL_EXTERN
1366      use SpherBessels
1367      use Precision
1368      !!== MODIFIED SUBROUT
1369      !!== CORRECTED THE SM
1370      !!== CORRECTED THE SI
1371      !!== WORKS FASTER AND
1372      !!== zqhuang@astro.ut
1373      IMPLICIT NONE
1374      INTEGER L
1375      real(dl) X,JL
1376
1377      call BJL(L,X,JL)
1378
1379      END SUBROUTINE BJL_EX
1380
```

/Users/lp1opa/Compare/camb_des/bessels.f90, Top line: 1332

```
1332      ans=x+coef(1)
1333      do i=2,N
1334          ans=ans*x+coef(i)
1335      end do
1336      plevl=ans
1337
1338      end function plevl
1339
1340
1341
1342      end module SpherBessels !
1343
1344
1345
1346      SUBROUTINE BJL_EXTERNAL(L
1347      use SpherBessels
1348      use Precision
1349      !!== MODIFIED SUBROUTINE
1350      !!== CORRECTED THE SMALL
1351      !!== CORRECTED THE SIGN O
1352      !!== WORKS FASTER AND MOR
1353      !!== zqhuang@astro.utoron
1354      IMPLICIT NONE
1355      INTEGER L
1356      real(dl) X,JL
1357
1358      call BJL(L,X,JL)
1359
1360      END SUBROUTINE BJL_EXTERN
1361
```

/Users/lp1lopa/Compare/camb_simdata/bess
els.f90, Top line: 1381

1381 |

/Users/lp1lopa/Compare/camb_des/bessels.
f90, Top line: 1362

1362 |