Dr JanV's c++ header-library

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## **Chapter 1**

# **Namespace Documentation**

## 1.1 drjanv Namespace Reference

## **Functions**

- double Legendre (int N, double x)
- double dLegendredx (int N, double x)
- double d2Legendredx2 (int N, double x)
- std::vector< double > LegendreRoots (unsigned int N, unsigned int max\_iters=1000, double tol=1.0e-12)
- std::pair< std::vector< double >, std::vector< double >> GaussLegendreQuadrature (unsigned int N, bool verbose=false, unsigned int max\_iters=1000, double tol=1.0e-12)
- template<typename T, typename D = int>
   std::vector< T > Range (T start, T end, D delta=1)

#### 1.1.1 Function Documentation

## 1.1.1.1 Legendre()

Provides the function evaluation of the Legendre polynomial  $P_N$  at value  ${\bf x}.$ 

#### **Parameters**

|   | int Order of the Legendre polynomial. |
|---|---------------------------------------|
| X | double The evaluation point.          |

## 1.1.1.2 dLegendredx()

Provides the function evaluation of the derivative of the Legendre polynomial  $\frac{dP_N}{dx}$  at value x.

#### **Parameters**

| Ν | int Order of the Legendre polynomial. |
|---|---------------------------------------|
| Х | double The evaluation point.          |

## 1.1.1.3 d2Legendredx2()

```
double drjanv::d2Legendredx2 (
          int N,
           double x )
```

Provides the function evaluation of the second derivative of the Legendre polynomial  $\frac{d^2P_N}{dx^2}$  at value x.

#### **Parameters**

| Ν | int Order of the Legendre polynomial. |  |
|---|---------------------------------------|--|
| Х | double The evaluation point.          |  |

## 1.1.1.4 LegendreRoots()

```
std::vector< double > drjanv::LegendreRoots (
    unsigned int N,
    unsigned int max_iters = 1000,
    double tol = 1.0e-12 )
```

Finds the roots of the Legendre polynomial.

The algorithm is that depicted in:

[1] Barrera-Figueroa, et al., "Multiple root finder algorithm for Legendre and Chebyshev polynomials via Newton's method", Annales Mathematicae et Informaticae, 33 (2006) pp. 3-13.

## **Parameters**

| Ν         | Is the order of the polynomial.   |
|-----------|---|
| roots     | Is a reference to the roots.  |
| max_iters | Maximum newton iterations to perform for each root. Default: 1000.            |
| tol       | Tolerance at which the newton iteration will be terminated. Default: 1.0e-12. |

#### Returns

A std::vector<double> containg a sorted list of roots in the interval [-1,1].

#### **Author**

Jan

## 1.1.1.5 GaussLegendreQuadrature()

```
std::pair< std::vector< double >, std::vector< double > > drjanv::GaussLegendreQuadrature (
    unsigned int N,
    bool verbose = false,
    unsigned int max_iters = 1000,
    double tol = 1.0e-12 )
```

Populates the abscissae and weights for a Gauss-Legendre quadrature given the number of desired quadrature points.

#### **Parameters**

| Ν         | Is the number of quadrature points.   |
|-----------|---|
| roots     | Is a reference to the roots.  |
| max_iters | Maximum newton iterations to perform for each root. Default: 1000.            |
| tol       | Tolerance at which the newton iteration will be terminated. Default: 1.0e-12. |

## Returns

A pair with each part of type std::vector<double> and equal in size. The first part is a vector of quadrature points and the second part is a vector of weights.

## Author

Jan

## 1.1.1.6 Range()

Returns a range of number according to the logic of the parameters.

## **Parameters**

| start | First number in the sequence.   |
|-------|---|
| end   | Termination criteria. If the delta is positive then the sequence will terminate if i>=end, otherwise if the delta is negative the sequence will terminate if i<=end |
| delta | Cannot be 0. Default 1. Can be negative.  |

## Returns

A  $\operatorname{\mathtt{std}}$ : vector of template type T containing the range according to the logic.

## Example:

```
auto iorder = drjanv::Range<int>(0, 10); // 0,1,...,9
auto iorder = drjanv::Range<int>(9,-1,-1); //9,8,...,0
```

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