

#### DIPLOMATERVEZÉSI FELADAT

#### Danyi Dávid

Villamosmérnök hallgató részére

### Marker alapú helymeghatározás képfeldolgozással

Az információfeldolgozási kapacitás nagymértékű növekedésével párhuzamosan egyre szélesebb körben váltak alkalmazhatóvá (valós időben) képfeldolgozási, gépi látás alapú eljárások. Az ideálistól eltérően a valós képek feldolgozását számos hatás nehezíti, úgy mint zaj, optikai torzítások, megvilágítás- és színbeli különbségek, stb.

A feladat témája aktuális, az egyre gyakrabban alkalmazott mobil robotikai, kiterjesztett és virtuális valóság alkalmazásoknál minden esetben felmerül a "hol vagyok?" kérdés, azaz a nézponti paraméterek becslése, lokalizáció. A SLAM (Simultaneous Localization and Mapping) algoritmus számos szenzorforrás által biztosított információval alkalmazható, így kamerával is. Az általános megoldás tájékozódási pontok egymáshoz képesti elhelyezkedését becsli, a mérési bizonytalanságot folyamatosan csökkentve, valamint méri a tájékozódási pontokhoz képest a megfigyelő pozícióját.

Jelen munka is a fenti témához, kapcsolódik, cél megvizsgálni egy olyan mesterséges, passzív marker megvalósíthatóságát, ami bizonyos paraméterekben (azonosíthatósági tartomány, részleges láthatóság) jobbat kíván biztosítani, mint az elterjedt (ARtag, glyph, stb.) megoldások. A marker egy oldalukon nyitott különböző méretű és alakú négyszögeket tartalmaz. A diplomaterv célja megvizsgálni a javasolt marker jellemzőit és használhatóságát.

A hallgató feladatának a következőkre kell kiterjednie:

- Mutasson be pozícióbecslő algoritmusokat, röviden ismertesse ezek működését!
- Hasonlítson össze különböző nézőpontbecslési algoritmust síkban elhelyezkedő pontpárok alapján!
- Készítsen egy marker felismerő megoldást!
- Végezzen méréseket (ideális és valós képeken) a marker által meghatározott pozíció pontosságára vonatkozóan!
- Hasonlítsa össze és értékelje az eredményeket!

Tanszéki konzulens: Kovács Viktor, tanársegéd

Budapest, 2017. február 18.

Dr. Charaf Hassan egyetemi tanár tanszékvezető





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# Marker Based Localisation and Pose Estimation Using Image Processing

THESIS

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#### HALLGATÓI NYILATKOZAT

Alulírott *Dávid Danyi*, szigorló hallgató kijelentem, hogy ezt a szakdolgozatot meg nem engedett segítség nélkül, saját magam készítettem, csak a megadott forrásokat (szakirodalom, eszközök stb.) használtam fel. Minden olyan részt, melyet szó szerint, vagy azonos értelemben, de átfogalmazva más forrásból átvettem, egyértelműen, a forrás megadásával megjelöltem.

Hozzájárulok, hogy a jelen munkám alapadatait (szerző(k), cím, angol és magyar nyelvű tartalmi kivonat, készítés éve, konzulens(ek) neve) a BME VIK nyilvánosan hozzáférhető elektronikus formában, a munka teljes szövegét pedig az egyetem belső hálózatán keresztül (vagy autentikált felhasználók számára) közzétegye. Kijelentem, hogy a benyújtott munka és annak elektronikus verziója megegyezik. Dékáni engedéllyel titkosított diplomatervek esetén a dolgozat szövege csak 3 év eltelte után válik hozzáférhetővé.

Budapest, April 27, 2018	
	Dávid Danyi
	hallgató

### Kivonat

A képfeldolgozás nem újkeletű tudományterület, már évtizedek óta folynak kutatások ezen a téren. Sok, ma is használt algoritmust az 1960-as években fejlesztettek ki. Akkoriban főleg a tudósok körében használt, drága eszköznek számított a számítógépes képfeldolgozás. Műholdképek, orvosdiagnosztikai adatok elemzésére, optikai karakterfelismerésre használták. Az olcsó és nagy teljesítményű, általános felhasználású számítógépek terjedésével azonban új lehetőségek nyíltak meg ezen a területen. Lehetővé vált például a valósidejű képfeldolgozó algoritmusok futtatása. Ezen fejlődés nélkül lehetetlen lett volna a 3 dimenziós látórendszerek kifejlesztése. Ezek a rendszerek jóval számításigényesebbek a klasszikus képfeldolgozási problémáknál, de a mai technológiával már ezek a megoldások és elérhetőek az átlagos felhasználók számára. Ennek legfőbb jele a robot navigációs, virtuális- és kiterjesztett valóság alkalmazások széleskörű megjelenése.

Jelen munka a fiduciális markerek alapján történő nézőpont meghatározás alkalmazhatóságát vizsgálja. A nézőpont-meghatározás célja a kamera pozíciójának és orientációjának meghatározása egy ismert markerhez viszonyítva. Ez egy összetett feladat aminek a megoldása több képfeldolgozási- és optimalizációs feladat megoldását igényli. Ez a dolgozat be fogja mutatni a kép alapján történő nézőpont-meghatározás lépéseit.

A munka első részében ismertetésre kerül a nézőpont-meghatározási probléma. Először röviden össze lesz foglalva a P-n-P néven ismert probléma: a nézőpont meghatározás n pontpár alapján, aminek ismert a világkoordinátákban adott helyzete, valamint a képi helyzetük is. Ezt a problémát többen többféleképp megoldották, néhány ilyen megoldás alapvető gondolatmenete összefoglalásra kerül. Ennek a szakasznak a zárásaként összehasonlítom az eljárásokat és kiválasztom a tulajdonságaik alapján a projekt céljára a legideálisabbat.

A pozicionálás pontosságát és robusztusságát nagyban befolyásolhatja az alkalmazott fiduciális marker is. Vannak ugyan már elterjedt markertípusok (ARTag, glyph, stb...), de jelen munkában kísérletet teszek egy új marker tervezésére. Ez az új marker megpróbál jobb eredményt nyújtani bizonyos területek, mint a már elterjedt megoldások. Ezen marker alkalmazhatósága is vizsgálva lesz ebben a dolgozatban.

A dolgozat utolsó nagyobb része a markerek felismerésére használt képfeldolgozási eljárásokról fog szólni. A különböző algoritmusok rövid elméleti áttekintése után egy-egy implementációs javaslat is közlésre kerül. A felismerő eljárások hatékonysága is vizsgálat alá

kerül, ideális és zajos képeken egyaránt. A mérési eredmények alapján javasolni fogok egy, a projekt számára optimális markerfelismerő eljárást.

## Abstract

Image processing has been an intensively researched subject for decades. Many algorithms that are used today have been developed in the 1960s. At that time, it was a costly tool mainly used by scientists for satellite imagery, medical imaging, optical character recognition, etc... The advancement of cheap and powerful general purpose computers opened up new possibilities for research and application. Real time image processing became possible. An interesting and even more computationally expensive sub-field of computer vision is 3D reconstruction. With today's (consumer) technology it is possible to map the 3D world based on image processing solutions. Navigational, Augmented and Virtual Reality applications are spreading.

This paper will examine the use of fiducial markers for camera pose estimation using a single camera. The goal of pose estimation is to determine the position and orientation of the camera with respect to a known marker. This is a complex task, which involves multiple image processing steps, as well as solving optimization problems. This work will provide an overview of the steps necessary for estimating the camera pose based on picture of a fiducial marker.

A section of this work will be dedicated to the pose estimation problem. There will be a short summary of the problem of reconstructing the view point based on point pairs in the world coordinate system and image points. Then some algorithms will be summarised that solved that problem. This section will be closed by comparing the benefits and drawbacks of these algorithms and choosing the one that best suits the need of this project.

The choice of the marker also influences accuracy and robustness of the pose estimation solution. There are already some marker types available for use (ARTag, glyph, etc...). This paper also proposes a new marker type which tries to offer better performance than the aforementioned solutions. The applicability of the new marker will be examined in various conditions.

The last major part of this work is about the different possible methods for extracting the markers from the images. In that section there will be short theoretical summaries of the detection methods. After the theory is covered, implementations of the aforementioned methods will be recommended. The performance of the detection algorithms will also be benchmarked on optimal and noisy images. Based on the tests results an optimal method will be selected.

# Abbreviations

This is a complete list of the abbreviations used in this paper.

**DOF** Degrees of freedom

**RQIM** Random Quad Image Marker

 ${f SHT}$  Simple Hough Transformation

RHT Randomised Hough Transformation

**PPHT** Progressive Probabilistic Hough Transform

LSD Line Segment Detector

**LLA** Level-Line Angle

## Introduction

Computer vision, and image processing in general, is a computationally intensive area. In the past the use of these algorithms was severely limited by the lack of processing power. Image processing solutions were mostly used for scientific purposes, and the algorithms ran offline: real-time applications were not possible. Satellite photos were analysed, medical imaging solutions were developed at the time. Optical character recognition was also a popular topic for image processing research. A famous scientific example from that time gave the basis for the Hough transformation, which will also be discussed in this work. The transformation was developed to automatically analyse bubble chamber photographs.

With the developing technology, specifically semiconductor manufacturing, more and more possible uses for image processing began to appear. Around the 1970s cheaper computers and dedicated hardware solutions started spreading. This made it possible to create real time image processing applications for some use-cases. One such use-case was television standards conversion.

As general purpose computers became faster and cheaper, they replaced the specialised circuits in almost all areas of application. Nowadays image processing solution to common problems (localisation, mapping, measurement, etc...) is chosen as a solution because it became the cheapest and most versatile alternative. Furthermore, 3D computer vision applications became not only possible, but widespread. 3D scanners, range finders, virtual-and augmented reality solutions have spread from laboratories and research institutions to consumer electronics. Processing power is no longer a bottleneck for most computer vision applications.

# Chapter 1

# Pose estimation

- 1.1 Pose Estimation Algorithms
- 1.1.1 Fast and Globally convergent Pose Estimation
- 1.1.2 Linear Pose Estimation from Points or Lines
- 1.1.3 Robust Pose Estimation from a Planar Target
- 1.2 Comparison

### Chapter 2

## Markers

One of the goals of this project was to design a fiducial marker with advantageous properties for use in pose estimation. In a typical scenario the marker may be seen from largely varying viewpoints, therefore it has to have some level of scale invariability. If the observer is far from the marker, the smaller details may be lost due to the limited resolution of the camera. If the same observer moves closer to the marker, it may fill the whole field of view and some features may even slip off the image. This leads to another feature the marker needs to have: redundancy. If the observer gets too close to the marker or some obstacle partially blocks the view, the localisation still needs to provide usable results.

The intended use of the markers is spatial localisation and pose estimation. In other words: approximating the observers 3D coordinates (x, y, z) and orientation  $(\phi, \theta, \psi)$  with respect to the marker. It is supposed that the observer uses a single camera system for navigation (e.g. smartphone or robotic application with limited resources). This means the marker needs at least 6 degree of freedom.

To sum up the above discussed specifications, a suitable marker would have to:

- have at least 6 DOF
- be (to some degree) scale invariant
- have redundancy

In the following sections will be a recommendation for a marker conforming for the listed specifications. It is based on 3 connected line segments forming a quad with one missing side. The whole marker is built from quads with different side lengths and angles.

#### 2.1 Quad

A marker is put together from quads. Figure 2.1. shows two examples. One side of the quads is left out: they are put together from three joint line segments. The middle segment, with



Figure 2.1: Example for different quads

two adjoining lines, will be referred to as the 'base' of the quad. The outer segments are going to be called 'arms'.

A quad has 6 degrees of freedom. There are 3 independent distance parameters: the length of the base and the two arm segments. There are also 3 unrelated angle parameters: the angles between each arm and the base, and the orientation of the quad.



Figure 2.2: Quad parameters

Figure 2.2. shows the free parameters of a quad (the orientation is not shown on the image). The following notation is used:

a: The length of one arm

b: The length of the base

c : The length of the other arm

 $\alpha$ : The angle between one arm and the base

 $\beta$ : The angle between the other arm and the base

 $\gamma$ : The angle with which the whole quad is rotated

For the sake of simplicity, figure 2.2. does not show the rotation with  $\gamma$ . The quad would be rotated around the origin of it's coordinate system.

The values of the length parameters are given in pixels, although they can be expressed in any unit of distance. The angles can be given is degrees or radians (in the implementation degrees are used for easier human readability).

$$a \in (0, a_{max}] \tag{2.1}$$

$$b \in (0, b_{max}] \tag{2.2}$$

$$c \in (0, c_{max}] \tag{2.3}$$

$$\alpha \in (0, 180^{\circ}) \tag{2.4}$$

$$\beta \in (0, 180^\circ) \tag{2.5}$$

$$\gamma \in [0, 360^{\circ}) \tag{2.6}$$

Equations (2.1) through (2.6) specify the range of each parameter. The maximum of the distance parameters are set by the space left on the image for the given marker, there is no theoretical limit for them. There is also no constraint for the resolution of the parameters. From the applications point of view, there are quads with continuous<sup>1</sup> and discrete parameter spaces.

#### 2.1.1 Quad representation

There are several ways to represent quads, each with different advantageous properties. For this work multiple considerations were made in that regard. The most straightforward is to simply store the above mentioned parameters. This is simple and easy for human reading, which is great help in the development process.

A step forward from this is to norm the a, b and c parameter of the quad with the base segment's length. Then the following parameters are used:

s: marker size, the same as the base length

 $m_a$ : 'a' multiplier.  $m_a = a/b$ 

 $m_c$ : 'c' multiplier.  $m_c = c/b$ 

The  $\alpha, \beta, \gamma$  angle parameters are not changed. This gives a scale or size parameter for the quad, which is useful for marker generation. These two representations are good for development and marker generation, but not so much for calculations.

<sup>&</sup>lt;sup>1</sup>That is, only limited by the computational precision

A third option is to store the endpoints of the line segments. It requires the storage of 4 points: two endpoints  $(E_1, E_2)$  and two inner points  $(I_1, I_2)$ . Equations (2.7) through (2.10) define the points' coordinates before rotating with  $\gamma$ , using figure 2.2.'s notation.

$$I_1' = (-\frac{b}{2}, 0) \tag{2.7}$$

$$I_2' = (\frac{b}{2}, 0) \tag{2.8}$$

$$E_1' = \left(-\frac{b}{2} + b * \cos(\alpha), a * \sin(\alpha)\right) \tag{2.9}$$

$$E_2' = (\frac{b}{2} - c * \cos(\beta), c * \sin(\beta))$$

$$\tag{2.10}$$

$$Rot(\gamma) = \begin{pmatrix} cos(\gamma) & -sin(\gamma) \\ sin(\gamma) & cos(\gamma) \end{pmatrix}$$
 (2.11)

The point  $E_1, E_2, I_1, I_2$  can be obtained from  $E'_1, E'_2, I'_1, I'_2$  by a multiplication with the rotational matrix  $Rot(\gamma)$ .

That method is redundant for storage: it uses 8 parameters instead of 6. However this poses no practical problem in the scope of the project. The one outstanding benefit of this method is it's efficiency in calculations. Because it is based on points in a Euclidean space, linear algebraic methods (matrix multiplications) can be used for calculating the projective transformations.

In this project the second and the third options are used. The first, naive method is omitted because it has no considerable advantage over the other two. The second method, using the size, multiplier and angle parameters is used in marker generation. The third is used during the calculations and the recognition process.

#### 2.2 Marker

Quads are 6 DOF shapes: in theory it would be enough to use only one of them for localisation and pose estimation. However that method would have very low error tolerance and questionable accuracy even in a best case scenario. To comply with the specifications written in the beginning of this chapter, the markers are put together from multiple quads. By placing quads with different orientations and sizes the error tolerance and accuracy can be greatly improved.

An intrinsic positive quality of using multiple quads with varying sizes is the scale invariance. As mentioned, even a single quad is sufficient for the task at hand. If the smaller quads become unrecognisable because of the low resolution or too large distance, a successful measurement is still possible. The same is true on the other end of the spectrum: if the observer is too close to the marker and the larger ones leave the field of view, the position and orientation can be calculated from the smaller quads.

Figure 2.3. shows an example for a marker. It is generated with the simple algorithm described in the next section, and is not optimal in many ways. Nonetheless it is functional, even if only a fraction of the quads are registered for the measurement.



Figure 2.3: An example for a marker

The markers are going to be referred to as RQIM, which means Random Quad Image Marker. As the name suggests, the quads are randomly generated and placed on the markers.

Unless otherwise specified, RQIMs use quads with continuous parameter spaces. In this chapter there will also be a small introduction to discrete parameter markers and their potential applications.

#### 2.2.1 Marker generation

In the current state of the project, markers are randomly generated using a simple algorithm. The generator routine receives the number of quads to be used in the current RQIM. The core concept is to create the desired number of random quads and place them on the image.

Let the number of quads to generate be n. First, the quad sizes are picked. There is an upper and a lower limit for them, given in percent of the image size. The generated sizes

follow an exponential distribution:

$$s = e^{-x*f} (2.12)$$

Where s is the quad size, x is random number between 0 and 1 with uniform distribution, and f is a scale factor. Then the n sizes are ordered in descending order.

After the scale factors are picked, the whole quads are generated by the following method. A random quad is created with the first (the largest) scale and placed on the image. Then another quad is created with the next largest size. After every new quad a check is performed whether or not it can be placed on the marker. If it cannot, then a new quad is generated with the same scale factor until it can be placed or the algorithm reached the limit of retries.

With this simple logic n quads are placed on the RQIM and the creation process is finished. Below is the pseudo-code of the algorithm.

```
n_max = number of quads to create
f = scale factor for exponential distribution
lowlim = lower size limit
uplim = upper size limit
n = 0
while n < n_max
        size = exp(-rand() * f)
        if size > lowlim and size < uplim
                store size
                n = n+1
        endif
end
sort(sizes, descending)
n = 0
while n < n \max
        while quad placed or max tries
                quad = create_random_quad(sizes(n))
                if quad can be placed
                         place quad
                         n = n+1
                end
        end
end
return marker
```

This method is not optimal and is based on trial and error, but it gives usable markers for the development process.

#### 2.2.2 Discrete RQIM

There are experiments in progress with discrete parameter space quads. It may be advantageous to quantize the parameter space in order to decrease the error probability in the pose estimation process.

Quads with finite possible states can be stored using much less resources than their continuous counterpart. As an example let us take a look at the following quantisation.

**Angles:**  $15^{\circ}, 30^{\circ}, 45^{\circ}, 60^{\circ}, 75^{\circ}, 90^{\circ}, 105^{\circ}, 120^{\circ}$ 

Multipliers: 0.40, 0.60, 0.80, 1.0, 1.25, 1.50, 1.75, 2.0

Orientations:  $0^{\circ}, 22.5^{\circ}, 45^{\circ}, 67.5^{\circ} \dots 270^{\circ}, 292.5^{\circ}, 315^{\circ}, 337.5^{\circ}$ 

Sizes: 1, 0.8, 0.6, 0.5, 0.4, 0.3, 0.25, 0.2, 0.1, 0.08, 0.06, 0.05, 0.04, 0.03, 0.025, 0.02

In this example, there are 8 possible values for the angle parameters, also 8 for the multipliers, 16 for the orientation and also 16 for the sizes. If the possibilities are stored in a lookup table, it is enough for the quad to store the index at which the value is accessible. A quad is defined by two angle parameters, two multipliers, an orientation and a size. The angles (in this case) require at least 3 bits each, the multipliers also. The orientation and the size need 4 bits each. That gives a sum of 20 bits per quad, which is significantly less than the space required to store 6 floating point numbers per quad.

This 20 bit word is also usable as an ID for the quad. It may be possible to code information in these ID-s, so the marker could provide additional information. This information could be related to and used by the localisation process, or be totally unrelated, general data. These possibilities have not yet been extensively researched.

The discrete RQIMs are usually less dense than the continuous ones, due to the limited angle possibilities. This means fewer quads per marker, which leads to decreasing redundancy. An optimum must be found between the number of quads per RQIM and distance between quads in the parameter space.

### Chapter 3

# Quad detection

In this chapter there will be a summary of the image processing algorithms tried and used for the recognition of the fiducial markers. From a computer vision point of view the task is to detect joint line segments. This is a well researched task in image processing, there are many well tried algorithms for it.

In this chapter will be a short summary of the algorithms used for testing and performance comparison.

The general flow of processing is the same for every line fitting solution.

The process here diverges depending on which line fitting algorithm is used. They all need differently conditioned input images for optimal performance. The line fitter routines not necessarily have the same output format<sup>1</sup>, so conversion may be needed. This is the end of the marker recognition phase. This step of the process takes the raw input image and initiates quad structures based on the observed picture.

Three separate line fitting techniques and their variants were profiled in this experiment.

- Hough-transformation
- Corner detection
- Line Segment Detector[4]

The first one uses the Hough-transformation for line detection. There are many variants of the transformation: Standard Hough Transform, Probabilistic Hough Transform, Multiscale Hough Transform, etc... The 2 most commonly used are the standard- and the probabilistic variants. The OpenCV framework offers implementations for them, both were tested in the experiment.

The second detector is based on corner recognition. There are more variants of this method to try out, too. The corner metrics of a feature can be calculated differently with (Harris

<sup>&</sup>lt;sup>1</sup>Some return line segments defined by their endpoint, others use the polar representation of a line etc.

metric, eigenvalues, etc.) varying results. It is also needed for the solution to be scale invariant, which also can be achieved in a number of ways.

The third alternative is the Line Segment Detector algorithm described in [4]. It is a robust and fast algorithm for detecting line segments on an image. The OpenCV framework provides an implementation of it as well.

A typical marker shot with partial visibility is shown figure 3.1..



Figure 3.1: Partially visible marker (taken with commercial smartphone)

#### 3.1 Theoretical Overview

#### 3.1.1 Hough transformation

One of the most commonly used methods for line detection on images is the Hough transform. Over it's long history many publications have been made about it's applications, performance and improvements.

Originally it was developed by Paul Hough in 1959 and later patented in 1962[6]. It was intended to be used for machine analysis of bubble chamber photographs. In it's modern form (with the  $\theta - \rho$  parametrisation) was introduced in 1972 by Duda and Hart[3]. The transformation became popular in the image processing community after Ballard's article[1] about generalising the algorithm for detection of arbitrary shapes. There were many optimised and improved variants of the transformation, however the basic concept remained the same. In 1990 a publication[10] introduced the Randomized Hough Transform, which was a fundamentally new approach to the algorithm with notable merits. As opposed to

the one-to-many mapping of the simple Hough transform, the randomised version uses a convergent many-to-one mapping when creating the parameter space.

In this work the Standard Hough Transform and one of it's optimised versions, the Progressive Probabilistic Hough Transform will be used. The PPHT, although being probabilistic, doesn't belong to the class of randomised Hough transforms. It uses the same one-to-many mapping as the SHT. The OpenCV framework provides implementations for the SHT and the PPHT, which is one of the main reason why they were chosen for this project.

After this short historical overview the theory of the transformations will be discussed.

#### Standard Hough Transform

The transformation is used to find instances of a model on digital images. The models are usually simple geometric shapes like lines, circles or ellipses. The curves are described by their parameters, e.g. slope and intercept for a line, centre point and radius for a circle etc.. Every non-zero pixel<sup>2</sup> votes for the features it could be part of. The number of votes is stored for every possible parameter combination. Then a threshold is applied to the stored votes, and the remaining parameters are accepted as model instances.

At first Hough described the algorithm to lines, but later the method would be generalised to any analytic<sup>3</sup> curve or shape. This theoretical overview is based on the example of line detection. The process is the same for every analytic curve, the only difference is the parameter space's dimension. The original patent[6] used the slope-intercept representation of lines.

$$y = m * x + b \tag{3.1}$$

In this case, the parameter space is 2 dimensional and it's axes are m and b. Every point in the parameter space represent an image space line. With this representation every non-zero pixel in the image space transforms into a line in the parameter space. For a given  $(x_0, y_0)$  pair (3.2) gives the line in the parameter space.

$$b = -x_0 * m + y_0 \tag{3.2}$$

Collinear points in the image show up in the parameter space as intersecting lines. The more lines intersect in a given  $(m_0, b_0)$ , the more likely it is the image contains the  $y = m_0 * x + b_0$  line. The problem with this parametrisation is that the parameter space is unbounded along both axes. Both intersect and slope can have values in the range of  $(-\infty, \infty)$ . Duda and Hart[3] proposed an alternative parametrisation, which turned out to be better for application. They used the normal parametrisation of a line, shown in (3.3).

$$\rho = x * cos(\theta) + y * sin(\theta)$$
(3.3)

<sup>&</sup>lt;sup>2</sup>The transformation works on binary images

<sup>&</sup>lt;sup>3</sup>The Generalised Hough Transform even extends to arbitrary shapes

In (3.3)  $\rho$  means the distance of the line from the image plane's origin.  $\theta$  is angle of the normal vector of the line. If the normal parametrisation is used the parameter space

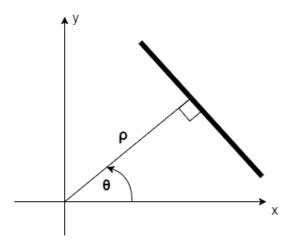


Figure 3.2: Normal line parameters

becomes finite in both dimensions.  $\theta$  is in the range of  $(0, 2\pi)$ ,  $\rho$  is bounded by the image size. In this case the image points define sinusoid curves in the parameter plane, and the line detection is done by searching for their intersections.

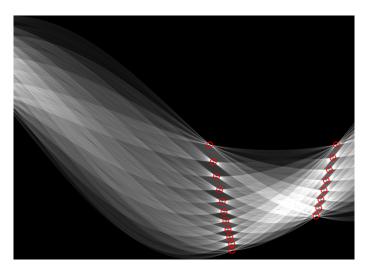


Figure 3.3: Hough-transform of a chessboard pattern

As mentioned before, the line detection is based on a voting scheme. The parameter space (in this case a 2 dimensional plane) is divided into bins.  $\rho$  and  $\theta$  are quantised in the desired resolution. The discrete  $(\rho, \theta)$  pairs define the bins. Every bin has accumulator. When a given  $(\rho_i, \theta_i)$  pair gets a vote it's corresponding accumulator is incremented by 1. The **SHT** (Standard Hough Transform) uses one-to-many divergent mapping. This means that every non-zero pixel votes for every possible parameter pair it could belong to. The above mentioned sinusoid is calculated with the desired resolution for the pixel, and the corresponding accumulators are updated.

When the accumulation phase is completed for the whole image, the local maxima of

the accumulators are found. Usually a threshold is applied in order to reduce noise and eliminate too short line segments. The radius of the non-maxima suppression also has impact on the results of the line fitting, it must be chosen carefully. After this step the parameters for the most likely line candidates are available.

As the **SHT** does not provide the endpoints of the line, they must be found by examining the original binary image. This can be done by simple checking every pixel along the line with the given parameters and deciding whether or not it is part of the feature. If it is desired, lines with gaps can also be accepted with this method. For more accurate fitting, a Least Squares approximation can also be applied to the pixels belonging to the line.

#### Progressive Probabilistic Hough Transform

The progressive probabilistic Hough transform is an optimised version of the SHT described in [8]. Probabilistic Hough transform variants were developed to overcome the comparatively high computational cost of the standard transform. The core concept is the same for most probabilistic versions of the Hough transform: not every none-zero point votes, only a randomly selected subset. These algorithms have to find a balance between minimising the proportion of image points that are used for voting while maintaining the accuracy of the detection process.

The original probabilistic Hough transform[7] solved this issue by introducing a tunable parameter p for the fraction of points to be used. First, a p fraction of the non-zero points are selected, than the SHT is performed on the selected subset. p can be low, the authors of [7] presented successful experiments with p = 2%. However, the results of the algorithm are greatly sensitive to the sampling rate. The authors analysed the problem on the special case of a single line immersed in noise and tried to formulate a solution for determining the p parameter. They succeeded, but the practical applicability is severely limited[8]: it requires a priori knowledge of the number of points belonging to the line. There was another approach to calculate the number of necessary votes[2]. It was shown that the probabilistic Hough transform can be formulated as the Monte Carlo approximation of the SHT, thus it is possible to deduce the desired error rate using the theory of Monte Carlo evaluation. Nevertheless, the core problem remained the same: a priori information was necessary for determining the sampling rate parameter. Usually there is only very limited information available, so conservative approximation is needed. This leads to the calculation of more votes then necessary, thus reducing the main advantage of the probabilistic method.

The progressive probabilistic Hough transform solves the above issue by "exploiting the difference in the fraction of votes needed to reliably detect lines (features) with different number of supporting points" [8]. This way for long lines only a small fraction of the line's points have to vote for the line to be registered. For shorter lines this proportion is of course higher. For lines with supporting points close to the votes generated by background noise a full transform must be performed.

The authors of [8] proposed the following algorithm to achieve the aforementioned goal. At each iteration a random non-zero image point is selected for voting to the possible model instances it could belong to. After each vote, the question "could the count be due to random noise?" [8] is evaluated. This requires a single comparison per bin update, with a threshold value changing by each vote cast. When a model instance (line) is detected, the supporting points retract their votes. The other points belonging to the same line are removed from the voting process. The pseudo-code representation below is directly quoted from [8].

```
    Check input image, if it is empty then finish
    Update the accumulator with a single pixel randomly selected from the input image
    Remove pixel from input image
    Check if the highest peak in the accumulator that was modified by the new pixel is higher than threshold 1. If not then goto 1.
    Look along a corridor specified by the peak in the accumulator, and find the longest segment of pixels either continuous or exhibiting a gap not exceeding a given threshold.
    Remove the pixels in the segment from the input image
    Unvote from the accumulator all the pixels from the line that have previously voted.
    If the line segment is longer than the minimum length add it into the output list.
    goto 1.
```

This algorithm has some considerable advantages of the standard and other, previous probabilistic variants of the Hough transform. It eliminates the need of *a priori* knowledge necessary for the tuning of probabilistic transforms while it remains much faster than the SHT. It should detect every instance of a model detectable by the SHT, at the latest when the voting finishes with the same number of voted pixels as for the standard transform. Another positive property of the algorithm is that features are detected as soon as the accumulator allows a decision: it is not necessary for all supporting points to vote. The algorithm can also be terminated at any time and still provide some useful output<sup>4</sup>.

Originally this transformation method was developed to speed up the Hough transform, while not being considerably more inaccurate. However, an unexpected result was observed by the authors. The PPHT outperformed the SHT in accuracy as well as speed. In sample images consisting of randomly positioned equal length lines, the PPHT produced less false negatives (missed line segments) and less false positives (incorrectly detected lines). This effect is due to the fact that PPHT clears out the votes of the detected lines as soon as they are found. This reduces the clutter in the accumulator, resulting in more accurate results, while also being more computationally efficient.

It also worth noting that the PPHT could, in theory, use every enhancement that were developed for the SHT. For example, the image gradient of the line segments could be used to reduce the number of pixels selected for voting. However, this aspect was not researched in the boundaries of this project.

<sup>&</sup>lt;sup>4</sup>However this aspect is not really important for this project

#### 3.1.2 Line Segment Detector

A fundamentally different approach to line detection was described in [4]. The algorithm is named **LSD** - for Line Segment Detector - by it's creators. It is which, unlike the SHT, detects line segments with subpixel accuracy by default. The runtime of the process is linear in the pixel count of the processed image. It also has fairly good noise suppression. Because of these advantageous properties was it considered for use in this project. The implementation used was provided by the OpenCV framework. In this section will be a short summary of the theory behind this algorithm.

The LSD takes as input a grayscale image and provides a list of line segments as output. The line detection is based on the image gradient. As a first step, a gradient field is generated from the input image. The gradient is taken using a 2x2 window, see (3.4).

$$g_x = \frac{i(x+1,y) + i(x+1,y+1) - i(x,y) - i(x,y+1)}{2},$$

$$g_y = \frac{i(x,y+1) + i(x+1,y+1) - i(x,y) - i(x+1,y)}{2}$$
(3.4)

Where i(x, y) is the intensity of the grayscale image at (x, y) point. The magnitude of the gradient is calculated by (3.5).

$$G(x,y) = \sqrt{g_x^2(x,y) + g_y^2(x,y)}$$
 (3.5)

The algorithm uses the angle of the gradient, which will be referred to as LLA (level-line angle), and is calculated by (3.6).

$$\arctan\left(\frac{g_x(x,y)}{-g_y(x,y)}\right) \tag{3.6}$$

The gradient obtained with (3.4) is the image gradient at the point (x + 0.5, y + 0.5). This half pixel offset is later added to the endpoints of the detected line segments.

Using the gradient information, a level-line field is constructed. Figure 3.4. shows an ex-

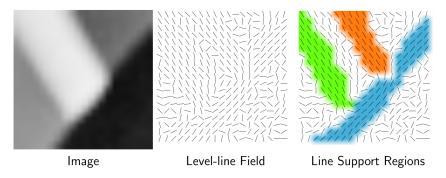


Figure 3.4: Illustration of the level-line field[4]

ample of the visualised level-line field. The next step of the algorithm is the segmentation of this field. It happens based on the level-line angle (the gradient angle defined in (3.6)).

The pixels that have the same LLA within a given threshold are grouped together. These segments are referred to as *line support regions*, see figure 3.4. for illustration. The segmentation is done with a region growing process.

Each line support region is a candidate for a line segment[4]. The line segments are represented with a rectangle. The main direction of the rectangle is determined by the principal inertial axis of the line support region. The size of the rectangle is chosen in a way to cover the whole line support region.

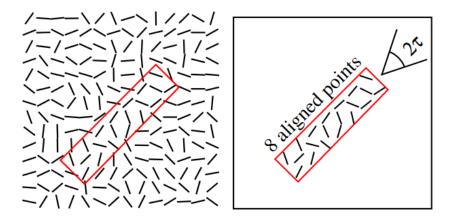


Figure 3.5: Illustration of the aligned points[4]

The pixels in the rectangle that have LLA close to the angle of the rectangle are called aligned points[4]. Figure 3.5. shows an example for the rectangular representation and the aligned points. The aligned points are used in the validation step of the algorithm.

The LSD algorithm uses an a contrario validation method. The idea behind that method is checking if it is probable that the current supporting points are caused by random noise. To achieve this, the authors of [4] created a noise model of the **level-line field**. A line segment becomes validated if the expected number of it's occurrences on the noise model is  $low^5$ .

#### 3.1.3 Corner Detection

Detecting quads not necessarily means the detection of line segments. Along with the above described methods based on line detection, a corner detecting algorithm was also benchmarked. The concept of this detection method is as follows. Detect the corners and end-points of a quad with some corner detection algorithm. Checks which detected pairs are connected with lines (or edges). Based on the connected pairs and their ordering, a quad can be reconstructed.

The OpenCV framework provides implementations for some popular corner detection algorithms. Specifically the Harris detector and the Shi-Thomas detector are covered. In

<sup>&</sup>lt;sup>5</sup>i.e. It is unlikely to be caused by random noise

this section will be a short theoretical summary of corner detection in general, and some specifics of the above mentioned solutions.

The basic idea of most corner detection algorithm is the following. Considering a local window on an image, corner regions show large change in average intensity if the window is shifted by a small amount in any direction. The mathematical formulation of the following idea is shown in (3.7).  $E_{x,y}$  is the change in intensity produced by shifting the window by (x,y).  $I_{u,v}$  is the intensity of the image at the point (u,v), and  $w_{u,v}$  specifies the image window. In the simplest case, the image window is rectangular and it is unity in a specified region and zero otherwise.

$$E_{x,y} = \sum_{u,v} w_{u,v} |I_{x+u,y+v} - I_{u,v}|^2$$
(3.7)

A naive approach of corner detection is to use (3.7) as it is. The local maxima of the minimum of (3.7) above a certain threshold can be used for a metric. With this method, three cases have to be considered:

- 1. **Flat region:** The windowed image region has almost constant intensity. In that case, all shifts will show small change.
- Edge region: The windowed image region has an edge in it. In that case shift in one direction will result in large change, but shifts in other directions will show low change in intensity.
- 3. Corner region: If the windowed region contains a corner, all shifts will show large change in the intensity.

The shifts can be chosen in a couple of ways: 90° shifts, 45° shifts in 8 or 4 directions, etc... Actually, this detection method is analysed in [5], and it is the base of the Harris detector.

However, the the above described corner detector suffers from a number of problems[5]. Firstly, it provides an anisotropic response, as only a discrete set of shifts are used. To address this issue, the Harris detector uses an analytic expansion of (3.7) around origin. See (3.8).

$$E_{x,y} = \sum_{u,v} w_{u,v} (I_{x+u,y+v} - I_{u,v})^2 = \sum_{u,v} w_{u,v} (x \frac{\partial I}{\partial x} + y \frac{\partial I}{\partial y} + O(x^2, y^2))^2$$
(3.8)

Another problem is that the above detection method's response is noisy[5] because of the rectangular and binary image window. The Harris detector resolves this issue by using a circular and smooth (for example Gaussian) window:

$$w_{u,v} = e^{-\frac{u^2 + v^2}{2\sigma^2}} \tag{3.9}$$

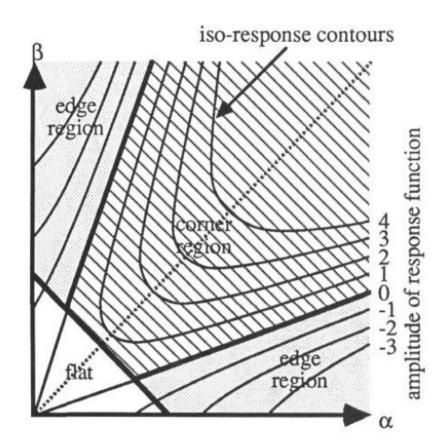


Figure 3.6: Image point classification based on Harris measure[5]

The third issue Harris found with the use of (3.7) as a corner metric is that it responds too readily t edges[5]. This is because only the minimum of E is taken into account when deciding whether a sampled window contains a corner or not. To address this issue, a reformulation of the corner measure was proposed that takes the variation of E with the direction of the change into consideration. For small changes, E, the average change in intensity generated by a shift with (x, y) can be written as:

$$E(x,y) = (x,y)M(x,y)^{T}$$
(3.10)

Where M is composed of the image gradients in the window. (3.12) shows M using the notation of (3.11)

$$I_x = \frac{\partial I}{\partial x}, I_y = \frac{\partial I}{\partial y} \tag{3.11}$$

$$\begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$
 (3.12)

Note that M describes the shape of the local autocorrelation function's shape at the origin. To describe E, [5] uses the eigenvalues of the matrix M, as it provides a rotationally invariant description. With this new method, the above mentioned cases (flat region, edge, corner) can be expressed as follows.

#### 1. Flat region: Both eigenvalues are small.

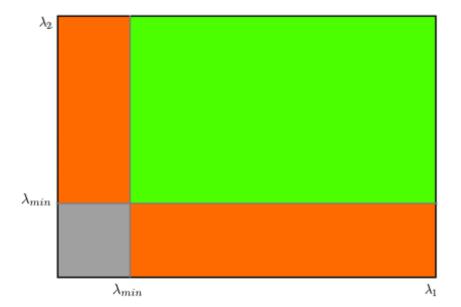


Figure 3.7: Image point classification based on Shi-Tomasi measure. Image source: OpenCV documentation

- 2. Edge region: One eigenvalue of M is small, the other is comparatively large.
- 3. Corner region: Both eigenvalues are large.

Figure 3.6. shows the above defined regions with respect to the eigenvalues ( $\alpha$  and  $\beta$  are the eigenvalues of M). The Harris detector also uses a metric for the "quality" of the detected edges or corners. This is noted with R and is defined below.

$$R = \det(M) - k(Trace(M))^2$$
(3.13)

k is a tunable parameter, its value is usually in the range of 0.01-0.05. The higher R is, the more likely that a corner is present in the sampled window. In figure 3.6. the curves mark the regions in the  $\alpha - \beta$  space that have the same R value.

This is the short theoretical summary of the Harris detector. A detailed mathematical derivation of the formulae can be found in [5].

The other corner detection method provided by the OpenCV framework is the Shi-Tomasi detector[9]. This detector uses the same concept as the Harris detector, however uses a different measure to classify features as corners. The scoring function is defined in (3.14).  $\lambda_1, \lambda_2$  is the same as  $\alpha, \beta$  for the Harris detector.

$$R = \min(\lambda_1, \lambda_2) \tag{3.14}$$

A feature is classified as a corner if R is greater than a threshold  $\lambda_{min}$ . Figure 3.7. shows this relation in the  $\lambda_1 - \lambda_2$  space. The Shi-Tomasi measure, while being simpler and requiring less computational power, shows better performance in images[9].

#### 3.2 Application for Quad Detection

#### 3.2.1 Conditioning

Before running the line detection algorithms some conditioning steps are done in order to improve their effectiveness. These processes are not uniform - every fitting method needs it's own.

The Hough transformation traditionally works best on thin lines. The easiest way is to generate an edge image with high-pass filtering. The OpenCV framework offers a wide variety of features for this task. The best result are obtained by using the Canny edge detector.

The skeletoning detector does not need a conditioning step, as it performs the band thinning on it's own.

The methods based on image gradients and corner detection both require some level of smoothing on the picture. In case of the corner detection the smoothing is useful for removing the false positive matches caused by the jagged edges, or in case os JPEG images the artefacts caused by the compression. The gradient detector simply gives a more spreadout and easier to analyse result on a smoothly changing gradient than it would on strict edge. The smoothing is also implemented using the OpenCV framework, which provides easy access to Gaussian filtering. The OpenCV implementation is based on convolution with a configurable Gaussian kernel. The kernel size and the deviation in x and y direction can be set. The Gaussian kernel and the convolution itself is handled in the framework.

## Chapter 4

# Marker Recognition

The preprocessing steps used for preparing the images for the line fitters (segmentation, thresholding, filtering etc.) will also be discussed.

The input is the raw image taken<sup>1</sup> by the observer. The first problem is finding the RQIM on the picture. When the marker area is located, it is necessary to discard the only partially visible and/or unrecognisable quads. At this point there is an image or set of images containing potentially good quads.

#### 4.1 Preprocessing

The preprocessing is done in two stages. The first is the segmentation, when quad-like blobs are found. The second step is the preparation of the aforementioned blobs for the line fitting algorithms' needs.

#### 4.2 Segmentation

The segmentation process is carried out on images roughly like the one shown in figure 3.1.. First the photos are converted to binary format by applying a threshold. The image is inverted in the process, because it makes more sense for the objects to be marked with non-zero elements than vice-versa. The threshold's value is determined using Otsu's method, which maximises the inter-class variance of the clusters<sup>2</sup>. The implementation is provided by the OpenCV framework.

Afterwards, the binary image is conditioned with a *close* morphology operator. The closing removes the gaps from the large connected areas (possible quads) and removes the *salt and pepper*-like noise. In the current implementation the kernel size of the morphology operator

<sup>&</sup>lt;sup>1</sup>In the development phase rendered pictures were used for better repeatability

<sup>&</sup>lt;sup>2</sup>Foreground and background

is constant, however it could be beneficial to calculate it from the global or local image parameters<sup>3</sup>.

The segmentation is based on finding continuous contours on the binary image. The OpenCV framework provides great functionality for this. The implementation is based on calculating the 8-neighbour chain code for the binary blobs on the image. The functions returns a list of list of points for the borders os each distinct contour.

The next step is the filtering of the found blobs. First the surely partial quads are discarded. This is done by calculating the bounding box of the contours, and if one of it's sides are touching the image border, the blob is marked as partial. With this approach it is possible that some fully visible quads that only touch the image border with one of their corner are lost. This problem can be easily fixed by checking the neighbourhood of the contact point, but this is not yet implemented.

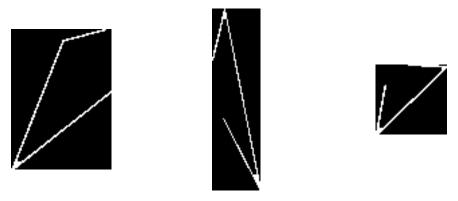


Figure 4.1: Quad candidates after segmentation

The next blob-filtering step is to filter out the false-positive contours. These false hits can be caused by the light conditions or the scene around the marker. For this purpose a simple metric is used to measure how likely a blob is to be a quad. This metric is the ratio of a blob's area and circumference. By experimentation this ratio for quads is found to be in the range of 10 and 50. The contours with ratios outside these limits are discarded.

The segmentation processes output is available as a single image with colour-coded<sup>4</sup> blobs or as a list of separate images each containing a quad candidate. Figure 4.1. shows an example for the output of the segmentation process.

<sup>&</sup>lt;sup>3</sup>e.g. image size, area of the connected region, etc.

<sup>&</sup>lt;sup>4</sup>Gray level, to be exact

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