

## Review .

Binomial Process :

$$p = \lambda \cdot \Delta .$$

$$E(T) = \frac{1}{\lambda}$$

$$\text{Var}(T) = \frac{1-p}{\lambda^2}$$

deviation of time between request .

Poisson Process :

$$E(T) = \frac{1}{\lambda} , \text{Var}(T) = \frac{1}{\lambda^2} , \sigma = \frac{1}{\lambda}$$

$$E(T_k) = \frac{k}{\lambda} , \text{Var}(T) = \frac{k}{\lambda^2} , \sigma = \frac{\sqrt{k}}{\lambda}$$

$$P\{X(t) = x\} = e^{-\lambda t} \cdot \frac{(\lambda t)^x}{x!}$$

$$P\{T \leq t\} = 1 - e^{-\lambda t}$$

$$P\{T > t\} = e^{-\lambda t}$$

# Final Review.

## Chapter 6.

$$(a^x)' = a^x \cdot \ln a$$

$$p = \lambda \cdot \Delta, n = \frac{t}{\Delta}$$

1. Binomial Process:

Expect time between request.

$$P(x) = C(n, x) \cdot p^x \cdot (1-p)^{n-x}$$

$$E(T) = \frac{1}{\lambda} \quad \text{Var}(T) = \frac{1-p}{\lambda^2} \quad \text{for inter}$$

When  $n \geq 30, 0.05 \leq p \leq 0.95,$

i). Binomial  $(n, p) \approx \text{Normal}(u = np, \sigma = \sqrt{npq})$

ii). Continuity correction.

$$P\{x(t) < \bar{x}\} = P\{-0.5 < x(t) < \underbrace{\bar{x} + 0.5}_x\} = P\left\{\frac{-0.5 - u}{\sigma} < Z < \frac{x - u}{\sigma}\right\}$$

2. Poisson Process:

$$P\{x(t) = x\} = e^{-\lambda t} \cdot \frac{(\lambda t)^x}{x!}$$

$$P\{T \leq t\} = 1 - e^{-\lambda t}$$

$$P\{T > t\} = e^{-\lambda t}$$

$$\left\{ \begin{array}{l} P\{T_k > t\} = P\{x(t) < k\} \\ P\{T_k < t\} = P\{x(t) \geq k\} \end{array} \right\} \Rightarrow \text{Then Apply } P\{x(t) = k\} = e^{-\lambda t} \cdot \frac{(\lambda t)^k}{k!}$$

## Chapter 7.

In a unlimited BSSQP system, if currently there are  $x$  jobs in the system, and in a course of  $n$  frames, then the number can change by  $n$  at most.

Therefore, we only need to deal with  $0 \sim x+n$

## Chapter 8.9.

1.  $\delta(\bar{x}) = \frac{\delta}{\sqrt{n}} \rightarrow \sqrt{p(1-p)}$ , if Bernoulli.

2. Method of moments:

$u_1 = E(x) = \int x \cdot f(x) dx$  to find the relationship between  $E(\bar{x})$  and  $\theta$ .

For Binomial:  $E(x) = n \cdot p$       Exponential:  $\lambda$

Poisson:  $E(x) = \lambda$

Geometric:  $E(x) = \frac{1}{p}$