

Resources

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1 Resources (References and Further Reading)

1.1 Quadrays and Synergetics (core starting points)

- **Quadray coordinates (intro and conversions):** [Urner - Quadray intro](#), [Urner - Quadrays and XYZ](#)
- **Synergetics background and IVM:** [Synergetics \(Fuller, overview\)](#)

1.2 4dsolutions (Kirby Urner) — repositories and key artifacts

- **Organization overview:** [4dsolutions \(GitHub org\)](#) — Python-centered explorations of Quadrays and synergetic geometry.
- **Math for Wisdom (m4w):** [m4w \(repo\)](#)
 - Quadray vectors and conversions: [qrays.py](#) (Qvector, SymPy-aware)
 - Synergetic tetravolumes and modules: [tetravolume.py](#) - Pdf/CM vs native IVM, BEAST
- **School_of_Tomorrow (notebooks/code):** [School_of_Tomorrow \(repo\)](#)
 - Tom Ace 5×5 determinant: [Qvolume.ipynb](#)
 - Bridging vs native tetravolumes: [VolumeTalk.ipynb](#)
- **Historical variants:** [qrays.py](#) also appears in [Python5 \(archive\)](#).

Context: These materials popularize the IVM/CCP/FCC framing of space, integer tetravolumes, and projective Quadray normalization. They inform the methods in this paper and complement the src/ implementations (see [quadray.py](#), [cayley_menger.py](#), [linalg_utils.py](#)).

1.3 Comprehensive index of 4dsolutions artifacts (selected)

1.3.1 Primary hub: School_of_Tomorrow (Python + notebooks)

- **Repository:** [School_of_Tomorrow](#)
- **Core modules:**
 - `grays.py`: Quadray implementation with normalization, conversions, and vector ops ([grays.py source — School_of_Tomorrow](#))
 - `quadcraft.py`: POV-Ray scenes for CCP/IVM arrangements, animations, and tutorials ([quadcraft.py source — School_of_Tomorrow](#))
 - `flextegrity.py`: Polyhedron framework, concentric hierarchy, POV-Ray export ([flextegrity.py source — School_of_Tomorrow](#))
 - Additional: `polyhedra.py`, `identities.py`, `smod_play.py` (synergetic modules)
- **Notebooks:**
 - `QuadCraft_Project.ipynb`: Interactive tutorials; CCP navigation and tetra demos ([QuadCraft_Project.ipynb — School_of_Tomorrow](#))
 - `Qvolume.ipynb`: Tom Ace 5×5 determinant; random-walk IVM volumes ([Qvolume.ipynb — School_of_Tomorrow](#))
 - `VolumeTalk.ipynb`: Bridging (CM/PdF) vs native (Ace/GdJ) tetravolumes ([VolumeTalk.ipynb — School_of_Tomorrow](#))
 - `TetraBook.ipynb`, `CascadianSynergetics.ipynb`, `Rendering_IVM.ipynb`, `SphereVolumes.ipynb` (visual and curricular materials)

1.3.2 Additional repositories

- **tetravolumes**: algorithms and pedagogy for tetra volumes
 - Repo: [tetravolumes](#)
 - Code: [tetravolume.py](#)
 - Notebooks: [Atoms R Us.ipynb](#), [Computing Volumes.ipynb](#)
- **rusty_rays**: Rust port highlighting cross-language consistency
 - Repo: [rusty_rays](#)
 - Sources: [Rust library implementation](#), [Rust command-line interface](#)
- **synmods**: Clojure/functional approach to Quadrays and synergetic modules
 - Repo: [synmods](#)
 - Sources: [grays.clj](#), [ramping_up.clj](#)
- **BookCovers**: VPython for interactive educational animations
 - Repo: [BookCovers](#)
 - Examples: [bookdemo.py](#), [stickworks.py](#), [tetravolumes.py](#)

1.3.3 Additional educational resources

- **Oregon Curriculum Network (OCN):** [OCN portal](#)
- **Python for Everyone:** [pymath page](#)
- **Python5 notebooks:** [Polyhedrons 101.ipynb](#)

1.3.4 Media and publications

- **YouTube demonstrations:** [Synergetics talk 1](#), [Synergetics talk 2](#), [Additional](#)
- **Academia profile:** [Kirby Urner at Academia.edu](#)
- **Fuller Institute:** [BFI — Big Ideas: Synergetics](#)

1.3.5 Background and community materials

- **RW Gray projects — Synergetics text:** [rwgrayprojects.com](#) (synergetics)
- **Fuller FAQ:** [C. J. Fearnley's Fuller FAQ](#)
- **Synergetics resource list:** [C. J. Fearnley's resource page](#)
- **Wikieducator:** [Synergetics hub](#)
- **Quadray animation:** [Quadray.gif](#) (Wikimedia Commons)

1.4 Geometry and volumes (Coxeter.4D context)

- **Regular polytopes (Euclidean E^4):** H. S. M. Coxeter, Regular Polytopes (Dover ed.), p. 119 clarifies Euclidean 4D vs spacetime.
- **Sphere packings and lattices:** J. H. Conway & N. J. A. Sloane, [Sphere Packings, Lattices and Groups \(Springer\)](#)
- **Cayley-Menger determinant:** [Cayley-Menger determinant \(reference\)](#)
- **Tetrahedron — volume:** [Tetrahedron: volume \(reference\)](#)
- **Bareiss algorithm (exact determinants):** [Bareiss algorithm \(reference\)](#)

1.5 Optimization and information geometry

- **Nelder-Mead method:** [Nelder-Mead \(reference\)](#)
- **Fisher information:** [Fisher information \(reference\)](#) — see also Eq. (??)
- **Natural gradient:** [Natural gradient \(reference\)](#) — see Eq. (??)

1.6 Active Inference

- **Free energy principle:** [Free energy principle \(reference\)](#)
- **Comprehensive review:** [Active Inference — recent review \(UCL Discovery, 2023\)](#)

1.7 Community discussions and context

- **Math4Wisdom:** [IVM \$\leftrightarrow\$ XYZ conversions \(curated page\)](#)
- **synergeo (groups.io):** [Synergetics discussion archive](#)
- **GeodesicHelp:** [Geodesic computations archive \(Google Groups\)](#)

1.8 Related projects and applications

- **QuadCraft:** [Tetrahedral voxel engine using Quadrays](#)
- **Flextegrity:** [Generating the Flextegrity Lattice \(academia.edu\)](#)

1.9 Tooling

- **GCC libquadmath (binary128):** [Official GCC libquadmath documentation](#)

1.10 Cross-language and cross-platform validation

- **Rust (rusty_rays)** and **Clojure (synmods)** mirror the Python algorithms for vector ops and tetravolumes, serving as independent checks on correctness and performance comparisons.
- **POV-Ray (quadcraft.py)** and **VPython (BookCovers)** demonstrate rendering pipelines for CCP/IVM scenes and educational animations.