

# Methodology

This section describes the implementation methodology and experimental setup used in the optimization project.

## Algorithm Implementation

### Gradient Descent Algorithm

The core algorithm implements the following iterative procedure:

**Input:** Initial point  $x_0$ , step size  $\alpha$ , tolerance  $\epsilon$ , maximum iterations  $N$

**Output:** Approximate solution  $x^*$

$k = 0$

while  $k < N$ :

$f = \text{compute\_gradient}(x_k)$

    if  $\|f\| < \epsilon$ :

        return  $x_k$  # Converged

$x_{k+1} = x_k - \alpha f$

$k = k + 1$

return  $x_k$  # Maximum iterations reached

Test Results: Convergence Metrics