Efficient Data Structures Used in Our Implementation