

# Table of Laplace Transforms

| $f(t)$                             | $\mathcal{L}[f(t)] = F(s)$                        |      | $f(t)$  | $\mathcal{L}[f(t)] = F(s)$        |      |
|------------------------------------|---|------|---|-----------------------------------|------|
| 1                                  | $\frac{1}{s}$                                     | (1)  | $\frac{ae^{at} - be^{bt}}{a - b}$                     | $\frac{s}{(s - a)(s - b)}$        | (19) |
| $e^{at}f(t)$                       | $F(s - a)$  | (2)  | $te^{at}$   | $\frac{1}{(s - a)^2}$             | (20) |
| $\mathcal{U}(t - a)$               | $\frac{e^{-as}}{s}$                               | (3)  | $t^n e^{at}$  | $\frac{n!}{(s - a)^{n+1}}$        | (21) |
| $f(t - a)\mathcal{U}(t - a)$       | $e^{-as}F(s)$                                     | (4)  | $e^{at} \sin kt$                                      | $\frac{k}{(s - a)^2 + k^2}$       | (22) |
| $\delta(t)$                        | 1   | (5)  | $e^{at} \cos kt$                                      | $\frac{s - a}{(s - a)^2 + k^2}$   | (23) |
| $\delta(t - t_0)$                  | $e^{-st_0}$                                       | (6)  | $e^{at} \sinh kt$                                     | $\frac{k}{(s - a)^2 - k^2}$       | (24) |
| $t^n f(t)$                         | $(-1)^n \frac{d^n F(s)}{ds^n}$                    | (7)  | $e^{at} \cosh kt$                                     | $\frac{s - a}{(s - a)^2 - k^2}$   | (25) |
| $f'(t)$                            | $sF(s) - f(0)$                                    | (8)  | $t \sin kt$   | $\frac{2ks}{(s^2 + k^2)^2}$       | (26) |
| $f^n(t)$                           | $s^n F(s) - s^{(n-1)}f(0) - \dots - f^{(n-1)}(0)$ | (9)  | $t \cos kt$   | $\frac{s^2 - k^2}{(s^2 + k^2)^2}$ | (27) |
| $\int_0^t f(x)g(t - x)dx$          | $F(s)G(s)$  | (10) | $t \sinh kt$  | $\frac{2ks}{(s^2 - k^2)^2}$       | (28) |
| $t^n \ (n = 0, 1, 2, \dots)$       | $\frac{n!}{s^{n+1}}$                              | (11) | $t \cosh kt$  | $\frac{s^2 - k^2}{(s^2 - k^2)^2}$ | (29) |
| $t^x \ (x \geq -1 \in \mathbb{R})$ | $\frac{\Gamma(x + 1)}{s^{x+1}}$                   | (12) | $\frac{\sin at}{t}$                                   | $\arctan \frac{a}{s}$             | (30) |
| $\sin kt$                          | $\frac{k}{s^2 + k^2}$                             | (13) | $\frac{1}{\sqrt{\pi t}} e^{-a^2/4t}$                  | $\frac{e^{-a\sqrt{s}}}{\sqrt{s}}$ | (31) |
| $\cos kt$                          | $\frac{s}{s^2 + k^2}$                             | (14) | $\frac{a}{2\sqrt{\pi t^3}} e^{-a^2/4t}$               | $e^{-a\sqrt{s}}$                  | (32) |
| $e^{at}$                           | $\frac{1}{s - a}$                                 | (15) | $\operatorname{erfc}\left(\frac{a}{2\sqrt{t}}\right)$ | $\frac{e^{-a\sqrt{s}}}{s}$        | (33) |
| $\sinh kt$                         | $\frac{k}{s^2 - k^2}$                             | (16) |   |                                   |      |
| $\cosh kt$                         | $\frac{s}{s^2 - k^2}$                             | (17) |   |                                   |      |
| $\frac{e^{at} - e^{bt}}{a - b}$    | $\frac{1}{(s - a)(s - b)}$                        | (18) |   |                                   |      |