

Superpixel Segmentation with Fully Convolutional Networks

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Abstract

In computer vision, superpixels have been widely used as an effective way to reduce the number of image primitives for subsequent processing. But only a few attempts have been made to incorporate them into deep neural networks. One main reason is that the standard convolution operation is defined on regular grids and becomes inefficient when applied to superpixels. Inspired by an initialization strategy commonly adopted by traditional superpixel algorithms, we present a novel method that employs a simple fully convolutional network to predict superpixels on a regular image grid. Experimental results on benchmark datasets show that our method achieves state-of-the-art superpixel segmentation performance while running at about 50fps. Based on the predicted superpixels, we further develop a downsampling/upsampling scheme for deep networks with the goal of generating high-resolution outputs for dense prediction tasks. Specifically, we modify a popular network architecture for stereo matching to simultaneously predict superpixels and disparities. We show that improved disparity estimation accuracy can be obtained on public datasets.

1. Introduction

In recent years, deep neural networks (DNNs) have achieved great success in a wide range of computer vision applications. The advance of novel neural architecture design and training schemes, however, often comes a greater demand for computational resources in terms of both memory and time. Consider the stereo matching task as an example. It has been empirically shown that, compared to traditional 2D convolution, 3D convolution on a 4D volume (height \times width \times disparity \times feature channels) [17] can better capture context information and learn representations for each disparity level, resulting in superior disparity estimation results. But due to the extra feature dimension, 3D convolution is typically operating on spatial resolutions that are lower than the original input image size for the time and memory concern. For example, CSPN [8], the top-1 method on the KITTI 2015 benchmark, conducts 3D

convolution at 1/4 of the input size and uses bilinear interpolation to upsample the predicted disparity volume for final disparity regression. To handle high resolution images (e.g., 2000 \times 3000), HSM [42], the top-1 method on the Middlebury-v3 benchmark, uses a multi-scale approach to compute disparity volume at 1/8, 1/16, and 1/32 of the input size. Bilinear upsampling is again applied to generate disparity maps at the full resolution. In both cases, object boundaries and fine details are often not well preserved in final disparity maps due to the upsampling operation.

In computer vision, superpixels provide a compact representation of image data by grouping perceptually similar pixels together. As a way to effectively reduce the number of image primitives for subsequent processing, superpixels have been widely adopted in vision problems such as saliency detection [41], object detection [32], tracking [37], and semantic segmentation [12]. However, superpixels are yet to be widely adopted in the DNNs for dimension reduction. One main reason is that, the standard convolution operation in the convolutional neural networks (CNNs) is defined on a regular image grid. While a few attempts have been made to modify deep architectures to incorporate superpixels [14, 11, 20, 34], performing convolution over an irregular superpixel grid remains challenging.

To overcome this difficulty, we propose a deep learning method to learn superpixels on the regular grid. Our key insight is that it is possible to associate each superpixel with a regular image grid cell, a strategy commonly used by traditional superpixel algorithms [22, 36, 10, 1, 23, 25, 2] as an initialization step (see Figure 2). Consequently, we cast superpixel segmentation as a task that aims to find association scores between image pixels and regular grid cells, and use a fully convolutional network (FCN) to directly predict such scores. Note that recent work [16] also proposes an end-to-end trainable network for this task, but this method uses a deep network to extract pixel features, which are then fed to a soft K-means clustering module to generate superpixels.

The key motivation for us to choose a standard FCN architecture is its simplicity as well as its ability to generate outputs on the regular grid. With the predicted superpixels, we further propose a general framework for down-

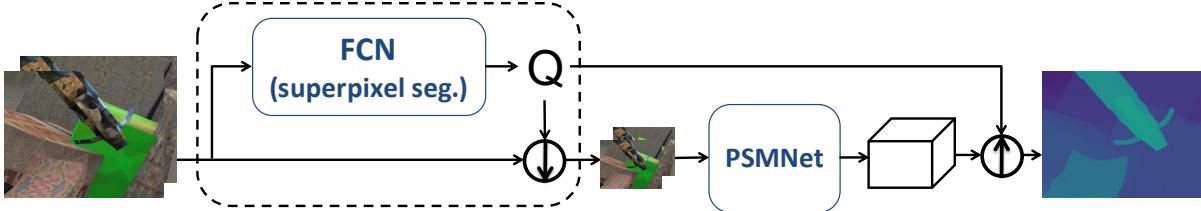


Figure 1. An illustration of our superpixel-based downsampling/upsampling scheme for deep networks. In this figure, we choose PSMNet [7] for stereo matching as our task network. The high-res input images are first downsampled using the superpixel association matrix Q predicted by our superpixel segmentation network. To generate a high-res disparity map, we use the same matrix Q to upsample the low-res disparity volume predicted by PSMNet for final disparity regression.

sampling/upsampling in DNNs. As illustrated in Figure 1, we replace the conventional operations for downsampling (*e.g.*, stride-2 convolutions) and upsampling (*e.g.*, bilinear upsampling) in the task network (PSMNet in the figure) with a superpixel-based downsampling/upsampling scheme to effectively preserve object boundaries and fine details. Further, the resulting network is end-to-end trainable. One advantage of our joint learning framework is that superpixel segmentation is now directly influenced by the downstream task, and that the two tasks can naturally benefit from each other. In this paper, we take stereo matching as an example and show how the popular network PSMNet [7], upon which many of the newest methods such as CSPN [8] and HSM [42] are built, can be adapted into our framework.

We have conducted extensive experiments to evaluate the proposed methods. For superpixel segmentation, experiment results on public benchmarks such as BSDS500 [3] and NYUv2 [28] demonstrate that our method is competitive with or better than the state-of-the-art w.r.t. a variety of metrics, and is also fast (running at about 50fps). For disparity estimation, our method outperforms the original PSMNet on SceneFlow [27] as well as high-res datasets HR-VS [42] and Middlebury-v3 [30], verifying the benefit of incorporating superpixels into downstream vision tasks.

In summary, the **main contributions** of the paper are: 1. We propose a simple fully convolutional network for superpixel segmentation, which achieves state-of-the-art performance on benchmark datasets. 2. We introduce a general superpixel-based downsampling/upsampling framework for DNNs. We demonstrate improved accuracy in disparity estimation by incorporating superpixels into a popular stereo matching network. To the best of our knowledge, we are the first to develop a learning-based method that simultaneously perform superpixel segmentation and dense prediction.

2. Related Work

Superpixel segmentation. There is a long line of research on superpixel segmentation, now a standard tool for many vision tasks. For a thorough survey on existing methods, we refer readers to the recent paper [33]. Here we focus on methods which use a regular grid in the initialization step.

Turbopixels [22] places initial seeds at regular intervals

based on the desired number of superpixels, and grows them into regions until superpixels are formed. [36] grows the superpixels by clustering pixels using a geodesic distance that embeds structure and compactness constraints. SEEDS [10] initializes the superpixels on a grid, and continuously refines the boundaries by exchanging pixels between neighboring superpixels.

The SLIC algorithm [1] employs K-means clustering to group nearby pixels into superpixels based on a 5-dimensional positional and CIELAB color features. Variants of SLIC include LSC [23] which maps each pixel into a 10-dimensional feature space and performs weighted K-means, Manifold SLIC [25] which maps the image to a 2-dimensional manifold to produce content-sensitive superpixels, and SNIC [2] which replaces the iterative K-means clustering with a non-iterative region growing scheme.

While the above methods rely on hand-crafted features, recent work [35] proposes to learn pixel affinity from large data using DNNs. In [16], the authors propose to learn pixel features which are then fed to a differentiable K-means clustering module for superpixel segmentation. The resulting method, SSN, is the first end-to-end trainable network for superpixel segmentation. Different from these methods, we train a deep neural network to directly predict the pixel-superpixel association map.

The use of superpixels in deep neural networks. Several methods propose to integrate superpixels into deep learning pipelines. These works typically use pre-computed superpixels to manipulate learnt features so that important image properties (*e.g.*, boundaries) can be better preserved. For example, [14] uses superpixels to convert 2D image patterns into 1D sequential representations, which allows a DNN to efficiently explore long-range context for saliency detection. [11] introduces a “bilateral inception” module which can be inserted into existing CNNs and perform bilateral filtering across superpixels, and [20, 34] employ superpixels to pool features for semantic segmentation. Instead, we use superpixels as an effective way to downsample/upsample. Further, none of these works has attempted to jointly learn superpixels with the downstream tasks.

Besides, our method is also similar to the deformable convolutional network (DCN) [9, 47] in that both can real-

ize adaptive respective field. However, DCN is mainly designed to better handle geometric transformation and capture contextual information for feature extraction. Thus, unlike superpixels, a deformable convolution layer does not constrain that every pixel has to contribute to (thus is represented by) the output features.

Stereo matching. Superpixel- or segmentation-based approach to stereo matching was first introduced in [4], and have since been widely used [15, 5, 19, 38, 6, 13]. These methods first segment the images into regions and fit a parametric model (typically a plane) to each region. In [39, 40], Yamaguchi *et al.* propose an optimization framework to jointly segments the reference image into superpixels and estimates the disparity map. [26] trains a CNN to predict initial pixel-wise disparities, which are refined using the slanted-plane MRF model. [21] develops an efficient algorithm which computes photoconsistency for only a random subset of pixels. Our work is fundamentally different from these optimization-based methods. Instead of fitting parametric models to the superpixels, we use superpixels to develop a new downsampling/upsampling scheme for DNNs.

In the past few years, deep networks [45, 31, 29, 44] taking advantage of large-scale annotated data have generated impressive stereo matching results. Recent methods [17, 7, 8] employing 3D convolution achieve the state-of-the-art performance on public benchmarks. However, due to the memory constraints, these methods typically compute disparity volumes at a lower resolution. [18] bilinearly upsamples the disparity to the output size and refine it using an edge-preserving refinement network. Recent work [42] has also explored efficient high-res processing, but its focus is on generating coarse-to-fine results to meet the need for anytime on-demand depth sensing in autonomous driving applications.

3. Superpixel Segmentation Method

In this section, we introduce our CNN-based superpixel segmentation method. We first present our idea of directly predicting pixel-superpixel association on a regular grid in Section 3.1, followed by a description of our network design and loss functions in Section 3.2. We further draw a connection between our superpixel learning regime with the recent convolutional spatial propagation (CSP) network [8] for learning pixel affinity in Section 3.3. Finally, in Section 3.4, we systematically evaluate our method on public benchmark datasets.

3.1. Learning Superpixels on a Regular Grid

In the literature, a common strategy adopted [22, 36, 10, 1, 23, 25, 2, 16] for superpixel segmentation is to first partition the $H \times W$ image using a regular grid of size $h \times w$ and consider each grid cell as an initial superpixel (i.e., a

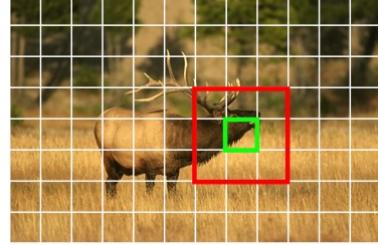


Figure 2. Illustration of \mathcal{N}_p . For each pixel p in the green box, we consider the 9 grid cells in the red box for assignment.

“seed”). Then, the final superpixel segmentation is obtained by finding a mapping which assigns each pixel $p = (u, v)$ to one of the seeds $s = (i, j)$. Mathematically, we can write the mapping as $g_s(p) = g_{i,j}(u, v) = 1$ if the (u, v) -th pixel belongs to the (i, j) -th superpixel, and 0 otherwise.

In practice, however, it is unnecessary and computationally expensive to compute $g_{i,j}(u, v)$ for all pixel-superpixel pairs. Instead, for a given pixel p , we constraint the search to the set of surrounding grid cells \mathcal{N}_p . This is illustrated in Figure 2. For each pixel p in the green box, we only consider the 9 grid cells in the red box for assignment. Consequently, we can write the mapping as a tensor $G \in \mathbb{Z}^{H \times W \times |\mathcal{N}_p|}$ where $|\mathcal{N}_p| = 9$.

While several approaches [22, 36, 10, 1, 23, 25, 2, 16] have been proposed to compute G , we take a different route in the paper. Specifically, we directly learn the mapping using a deep neural network. To make our objective function differentiable, we replace the hard assignment G with a soft association map $Q \in \mathbb{R}^{H \times W \times |\mathcal{N}_p|}$. Here, the entry $q_s(p)$ represents the probability that a pixel p is assigned to each $s \in \mathcal{N}_p$, such that $\sum_{s \in \mathcal{N}_p} q_s(p) = 1$. Finally, the superpixels are obtained by assigning each pixel to the grid cell with the highest probability: $s^* = \arg \max_s q_s(p)$.

Although it might seem a strong constraint that a pixel can only be associated to one of the 9 nearby cells, which leads to the difficulty to generate long/large superpixels, we want to emphasize the importance of the compactness. Superpixel is inherently an over-segmentation method. As one of the main purposes of our superpixel method is to perform the detail-preserved downsampling/upsampling to assist the downstream network, it is more important to capture spatial coherence in the local region. For the information goes beyond the 9-cell area, there is no problem to segment it into pieces and leave them for downstream network to aggregate with convolution operations.

Our method vs. SSN [16]. Recently, [16] proposes SSN, an end-to-end trainable deep network for superpixel segmentation. Similar to our method, SSN also computes a soft association map Q . However, unlike our method, SSN uses the CNN as a means to extract pixel features, which are then fed to a soft K-means clustering module to compute Q .

We illustrate the algorithmic schemes of the two methods

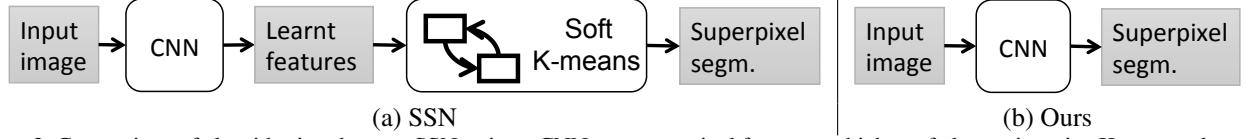


Figure 3. Comparison of algorithmic schemes. SSN trains a CNN to extract pixel features, which are fed to an iterative K-means clustering module for superpixel segmentation. We train a CNN to directly generate superpixels by predicting a pixel-superpixel association map.

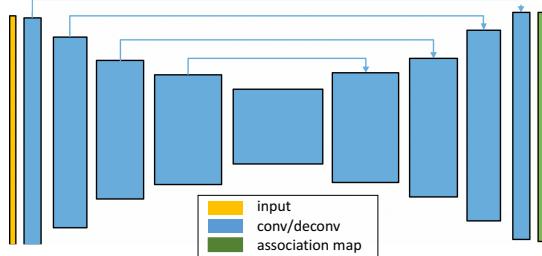


Figure 4. Our simple encoder-decoder architecture for superpixel segmentation. Please refer to the supplementary materials for detailed specifications.

in Figure 3. Both SSN and our method can take advantage of CNN to learn complex features using task-specific loss functions. But unlike SSN, we combine feature extraction and superpixel segmentation into a single step. As a result, our network runs faster and can be easily integrated into existing CNN frameworks for downstream tasks (Section 4).

3.2. Network Design and Loss Functions

As shown in Figure 4, we use a standard encoder-decoder design with skip connections to predict superpixel association map Q . The encoder takes a color image as input and produces high-level feature maps via a convolutional network. The decoder then gradually upsamples the feature maps via deconvolutional layers to make final prediction, taking into account also the features from corresponding encoder layers. We use leaky ReLU for all layers except for the prediction layer, where softmax is applied.

Similar to SSN [16], one of the main advantages of our end-to-end trainable superpixel network is its flexibility w.r.t. the loss functions. Recall that the idea of superpixels is to group similar pixels together. For different applications, one may wish to define similarity in different ways.

Generally, let $\mathbf{f}(\mathbf{p})$ be the pixel property we want the superpixels to preserve. Examples of $\mathbf{f}(\mathbf{p})$ include a 3-dimensional CIELAB color vector, and/or a N -dimensional one-hot encoding vector of semantic labels, where N is the number of classes, and many others. We further represent a pixel's position by its image coordinates $\mathbf{p} = [x, y]^T$.

Given the predicted association map Q , we can compute the center of any superpixel s , $\mathbf{c}_s = (\mathbf{u}_s, \mathbf{l}_s)$ where \mathbf{u}_s is the property vector and \mathbf{l}_s is the location vector, as follows:

$$\mathbf{u}_s = \frac{\sum_{\mathbf{p}:s \in \mathcal{N}_p} \mathbf{f}(\mathbf{p}) \cdot q_s(\mathbf{p})}{\sum_{\mathbf{p}:s \in \mathcal{N}_p} q_s(\mathbf{p})}, \quad \mathbf{l}_s = \frac{\sum_{\mathbf{p}:s \in \mathcal{N}_p} \mathbf{p} \cdot q_s(\mathbf{p})}{\sum_{\mathbf{p}:s \in \mathcal{N}_p} q_s(\mathbf{p})}. \quad (1)$$

Here, recall that \mathcal{N}_p is the set of surrounding superpixels of p , and $q_s(p)$ is the network predicted probability of p being associated with superpixel s . In Eq (1), each sum is taken over all the pixels with a possibility to be assigned to s .

Then, the reconstructed property and location of any pixel p are given by:

$$\mathbf{f}'(p) = \sum_{s \in \mathcal{N}_p} \mathbf{u}_s \cdot q_s(p), \quad p' = \sum_{s \in \mathcal{N}_p} \mathbf{l}_s \cdot q_s(p). \quad (2)$$

Finally, the general formulation of our loss function has two terms. The first term encourages the trained model to group pixels with similar property of interest, and the second term enforces the superpixels to be spatially compact:

$$L(Q) = \sum_p \text{dist}(\mathbf{f}(p), \mathbf{f}'(p)) + \frac{m}{S} \|\mathbf{p} - \mathbf{p}'\|_2, \quad (3)$$

where $\text{dist}(\cdot, \cdot)$ is the task specific distance metric depending on the pixel property $\mathbf{f}(p)$, S is the superpixel sampling interval, and m is a weight balancing the two terms.

In this paper, we consider two different choices of $\mathbf{f}(p)$. First, we choose the CIELAB color vector and use the ℓ_2 norm as the distance measure. This leads to an objective function similar to the original SLIC method [1]:

$$L_{SLIC}(Q) = \sum_p \|\mathbf{f}_{col}(p) - \mathbf{f}'_{col}(p)\|_2 + \frac{m}{S} \|\mathbf{p} - \mathbf{p}'\|_2. \quad (4)$$

Second, following [16], we choose the one-hot encoding vector of semantic labels and use cross-entropy $E(\cdot, \cdot)$ as the distance measure:

$$L_{sem}(Q) = \sum_p E(\mathbf{f}_{sem}(p), \mathbf{f}'_{sem}(p)) + \frac{m}{S} \|\mathbf{p} - \mathbf{p}'\|_2. \quad (5)$$

3.3. Connection to Spatial Propagation Network

Recently, [8] proposes the convolutional spatial propagation (CSP) network, which learns an affinity matrix to propagate information to nearby spatial locations. By integrating the CSP module into existing deep neural networks, [8] has demonstrated improved performance in affinity-based vision tasks such as depth completion and refinement. In this section, we show that the computation of superpixel centers using learnt association map Q can be written mathematically in the form of CSP, thus draw a connection between learning Q and learning the affinity matrix as in [8].

Given an input feature volume $X \in \mathbb{R}^{H \times W \times C}$, the convolutional spatial propagation (CSP) with a kernel size K and stride S can be written as:

$$\mathbf{y}_{i,j} = \sum_{a,b=-K/2+1}^{K/2} \kappa_{i,j}(a,b) \odot \mathbf{x}_{i \cdot S + a, j \cdot S + b}, \quad (6)$$

where $Y \in \mathbb{R}^{h \times w \times C}$ is an output volume such that $h = \frac{H}{S}$ and $w = \frac{W}{S}$, $\kappa_{i,j}$ is the output from an affinity network such that $\sum_{a,b=-K/2+1}^{K/2} \kappa_{i,j}(a,b) = 1$, and \odot is element-wise product.

In the meantime, as illustrated in Figure 2, to compute the superpixel center associated with the (i, j) -th grid cell, we consider all pixels in the surrounding $3S \times 3S$ region:

$$\mathbf{c}_{i,j} = \sum_{a,b=-3S/2+1}^{3S/2} \hat{q}_{i,j}(a,b) \odot \mathbf{x}_{i \cdot S + a, j \cdot S + b}, \quad (7)$$

where

$$\hat{q}_{i,j}(a,b) = \frac{q_{i,j}(u,v)}{\sum_{a,b=-3S/2+1}^{3S/2} q_{i,j}(u,v)}, \quad (8)$$

and $u = i \cdot S + a, v = j \cdot S + b$.

Comparing Eq. (6) with Eq. (7), we can see that computing the center of superpixel of size $S \times S$ is equivalent to performing CSP with a $3S \times 3S$ kernel derived from Q . Furthermore, both $\kappa_{i,j}(a,b)$ and $q_{i,j}(u,v)$ represent the learnt weight between the spatial location (u, v) in the input volume and (i, j) in the output volume. In this regard, predicting Q in our work can be viewed as learning an affinity matrix as in [8].

Nevertheless, we point out that, while the techniques presented in this work and [8] share the same mathematical form, they are developed for very different purposes. In [8], Eq. (6) is employed repeatedly (with $S = 1$) to propagate information to nearby locations, whereas in this work, we use Eq. (7) to compute superpixel centers (with $S > 1$).

3.4. Experiments

We train our model with segmentation labels on the standard benchmark BSDS500 [3] and compare it with state-of-the-art superpixel methods. To further evaluate the method generalizability, we also report its performances without fine-tuning on another benchmark dataset NYUv2 [28].

All evaluations are conducted using the protocols and codes provided by [33]¹. We run LSC [23], ERS [24], SNIC [2], SEAL [35], and SSN [16] with the original implementations from the authors, and run SLIC [1] and ETPS [43] with the codes provided in [33]. For LSC, ERS, SLIC and ETPS, we use the best parameters reported in [33], and for the rest, we use the default parameters recommended by the original authors.

¹<https://github.com/davidstutz/superpixel-benchmark>

Implementation details. Our model is implemented with PyTorch, and optimized using Adam with $\beta_1 = 0.9$ and $\beta_2 = 0.999$. We use L_{sem} in Eq. (5) for this experiment, with $m = 0.003$. During training, we randomly crop the images to size 208×208 as input, and perform horizontal/vertical flipping for data augmentation. The initial learning rate is set to 5×10^{-5} , and is reduced by half after 200k iterations. Convergence is reached at about 300k iterations.

For training, we use a grid with cell size 16×16 , which is equivalent to setting the desired number of superpixels to 169. At the test time, to generate varying number of superpixels, we simply resize the input image to the appropriate size. For example, by resizing the image to 480×320 , our network will generate about 600 superpixels. Furthermore, for fair comparison, most evaluation protocols expect superpixels to be spatially connected. To enforce that, we apply an off-the-shelf component connection algorithm to our output, which merges superpixels that are smaller than a certain threshold with the surrounding ones.²

Evaluation metrics. We evaluate the superpixel methods using the popular metrics including achievable segmentation accuracy (ASA), boundary recall and precision (BR-BP), and compactness (CO). ASA quantifies the achievable accuracy for segmentation using the superpixels as pre-processing step, BR and BP measure the boundary adherence of superpixels given the ground truth, whereas CO assesses the compactness of superpixels. The higher these scores are, the better the segmentation result is. As in [33], for BR and BP evaluation, we set the boundary tolerance as 0.0025 times the image diagonal rounded to the closest integer. We refer readers to [33] for the precise definitions.

Results on BSDS500. BSDS500 contains 200 training, 100 validation, and 200 test images. As multiple labels are available for each image, we follow [16, 35] and treat each annotation as an individual sample, which results in 1633 training/validation samples and 1063 testing samples. We train our model using both the training and validation samples.

Figure 5 reports the performance of all methods on BSDS500 test set. Our method outperforms all traditional methods on all evaluation metrics, except SLIC in term of CO. Comparing to the other deep learning-based methods, SEAL and SSN, our method achieves competitive or better results in terms of ASA and BR-BP, and significantly higher scores in term of CO. Figure 8 further shows example results of different methods. Note that, as discussed in [33], there is a well-known trade-off between boundary adherence and compactness. Although our method does not outperform existing methods on all the metrics, it appears to strike a better balance among them. It is also worth noting that by achieving higher CO score, our method is able to better capture spatially coherent information and avoids

²Code and models are available at https://github.com/fuy34/superpixel_fcn.

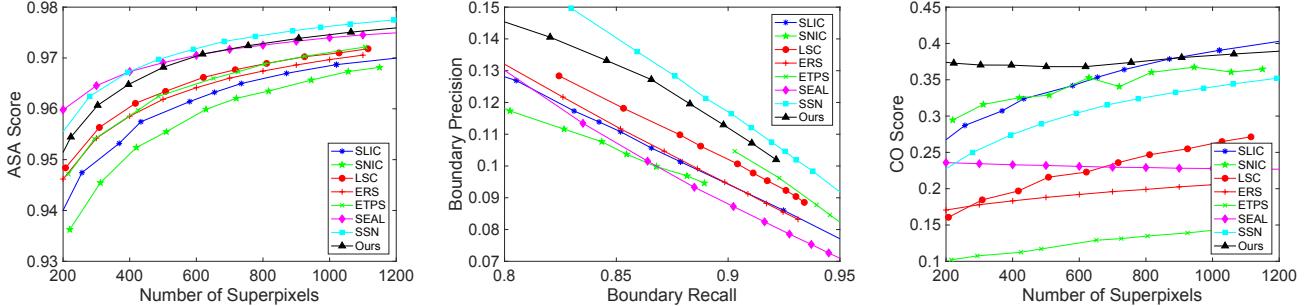


Figure 5. Superpixel segmentation results on BSDS500. **From left to right:** ASA, BR-BP, and CO.

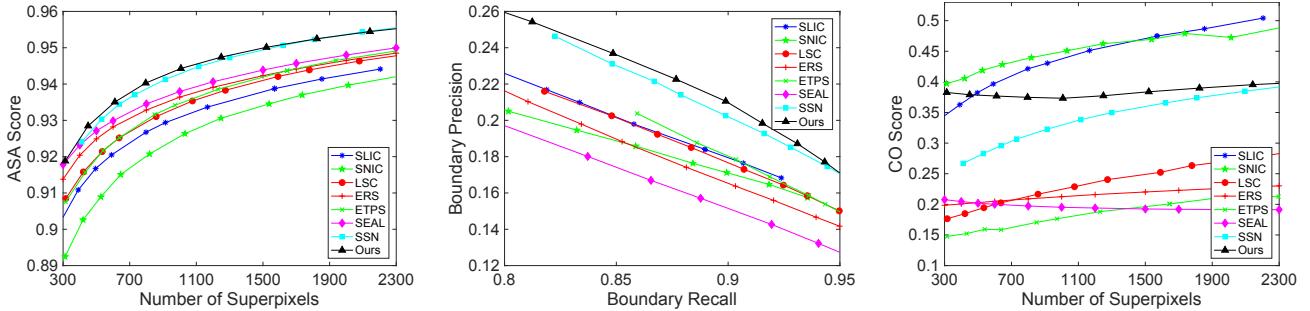


Figure 6. Superpixel segmentation results on NYUv2. **From left to right:** ASA, BR-BP, and CO.

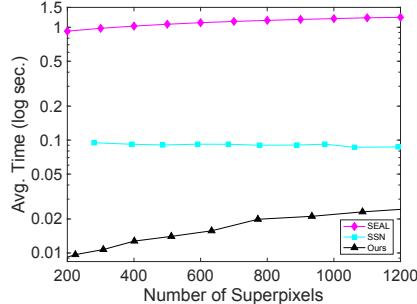


Figure 7. Average runtime of different DL methods w.r.t. number of superpixels. Note that y -axis is plotted in the logarithmic scale.

paying too much attention to image details and noises. This characteristic tends to lead to better generalizability, as shown in the NYUv2 experiment results.

We also compare the runtime difference among deep learning-based (DL) methods. Figure 7 reports the average runtime w.r.t. the number of generated superpixels on a NVIDIA GTX 1080Ti GPU device. Our method runs about 3 to 8 times faster than SSN and more than 50 times faster than SEAL. This is expected as our method uses a simple encoder-decoder network to directly generate superpixels, whereas SEAL and SSN first use deep networks to predict pixel affinity or features, and then apply traditional clustering methods (i.e., graph cuts or K-means) to get superpixels.

Results on NYUv2. NYUv2 is a RGB-D dataset originally proposed for indoor scene understanding tasks, which contains 1,449 images with object instance labels. By removing the unlabelled regions near the image boundary, [33] has developed a benchmark on a subset of 400 test images

with size 608×448 for superpixel evaluation. To test the generalizability of the learning-based methods, we directly apply the models of SEAL, SSN, and our method trained on BSDS500 to this dataset without any fine-tuning.

Figure 6 shows the performance of all methods on NYUv2. Generally, all deep learning-based methods perform well as they continue to achieve competitive or better performance against the traditional methods. Further, our method is shown to generalize better than SEAL and SSN, which is evident by comparing the corresponding curves in Figure 5 and 6. Specifically, our method outperforms SEAL and SSN in terms of BR-BP and CO, and is one of the best in terms of ASA. The visual results are shown in Figure 8.

4. Application to Stereo Matching

Stereo matching is a classic computer vision task which aims to find pixel correspondences between a pair of rectified images. Recent literature has shown that deep networks can boost the matching accuracy by building 4D cost volume (height \times width \times disparity \times feature channels) and aggregate the information using 3D convolution [7, 8, 46]. However, such a design consumes large amounts of memory because of the extra “disparity” dimension, limiting their ability to generate high-res outputs. A common remedy is to bilinearly upsample the predicted low-res disparity volumes for final disparity regression. As a result, object boundaries often become blur and fine details get lost.

In this section, we propose a downsampling/upsampling scheme based on the predicted superpixels and show how to integrate it into existing stereo matching pipelines to gener-

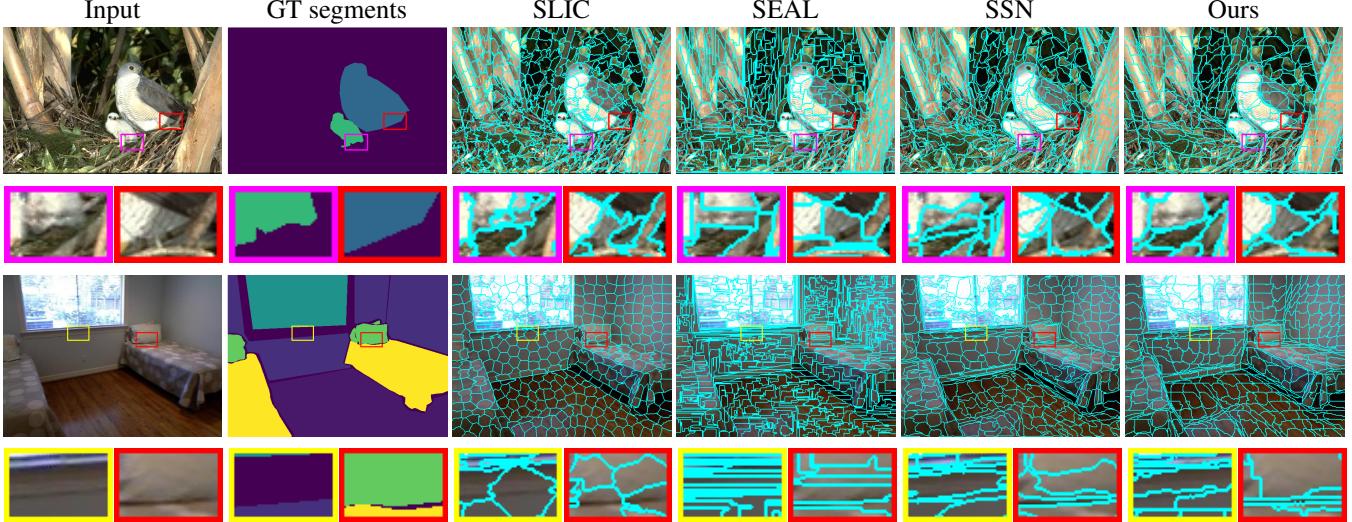


Figure 8. Example superpixel segmentation results. Compared to SEAL and SSN, our method is competitive or better in terms of object boundary adherence while generating more compact superpixels. **Top rows:** BSDS500. **Bottom rows:** NYUv2.

ate high-res outputs that better preserve the object boundaries and fine details.

4.1. Network Design and Loss Function

Figure 1 provides an overview of our method design. We choose PSMNet [7] as our task network. In order to incorporate our new downsampling/upsampling scheme, we change all the stride-2 convolutions in its feature extractor to stride-1, and remove the bilinear upsampling operations in the spatial dimensions. Given a pair of input images, we use our superpixel network to predict association maps Q_l , Q_r and compute the superpixel center maps using Eq. (1). The center maps (*i.e.*, downsampled images) are then fed into the modified PSMNet to get the low-res disparity volume. Next, the low-res volume is upsampled to original resolution with Q_l according to Eq. (2), and the final disparity is computed using disparity regression. We refer readers to the supplementary materials for detailed specification.

Same as PSMNet [7], we use the 3-stage smooth L_1 loss with the weights $\alpha_1 = 0.5$, $\alpha_2 = 0.7$, and $\alpha_3 = 1.0$ for disparity prediction. And we use the SLIC loss (Eq. (4)) for superpixel segmentation. The final loss function is:

$$L = \sum_{s=1}^3 \alpha_s \left(\frac{1}{N} \sum_{p=1}^N \text{smooth}_{L_1}(d_p - \hat{d}_p) \right) + \frac{\lambda}{N} L_{SLIC}(Q) \quad (9)$$

where N is the total number of pixels, and λ is a weight to balance the two terms. We set $\lambda = 0.1$ for all experiments.

4.2. Experiments

We have conducted experiments on three public datasets, SceneFlow [27], HR-VS [42], and Middlebury-v3 [30] to compare our model with PSMNet. To further verify the

benefit of joint learning for superpixels and disparity estimation, we trained two different models for our method. In the first model **Ours_fixed**, we fix the parameters in superpixel network and train the rest of the network (*i.e.*, the modified PSMNet) for disparity estimation. In the second model **Ours_joint**, we jointly train all networks in Figure 1. For both models, the superpixel network is pre-trained on SceneFlow using the SLIC loss. The experiments are conducted on 4 Nvidia TITAN Xp GPUs.

Results on SceneFlow. SceneFlow is a synthetic dataset contains 35,454 training and 4,370 test frames with dense ground truth disparity. Following [7], we exclude pixels with disparities greater than 192 in training and test time.

During training, we set $m = 30$ in the SLIC loss and randomly crop the input images into size 512×256 . To conduct 3D convolution at 1/4 of the input resolution as PSMNet does, we predict superpixels with grid cell size 4×4 to perform the $4 \times$ downsampling/upsampling. We train the model for 13 epochs with batch size 8. The initial learning rate is 1×10^{-3} , and is reduced to 5×10^{-4} and 1×10^{-4} after 11 and 12 epochs, respectively. For PSMNet, we use the authors’ implementation and train it with the same learning schedule as our methods.

We use the standard end-point-error (EPE) as the evaluation metric, which measures the mean pixel-wise Euclidean distance between the predicted disparity and the ground truth. As shown in Table 1, **Ours_joint** achieves the lowest EPE. Also note that **Ours_fixed** performs worse than the original PSMNet, which demonstrates the importance of joint training. Qualitative results are shown in Figure 9. One can see that both **Ours_fixed** and **Ours_joint** preserve fine details better than the original PSMNet.

Results on HR-VS. HR-VS is a synthetic dataset with ur-

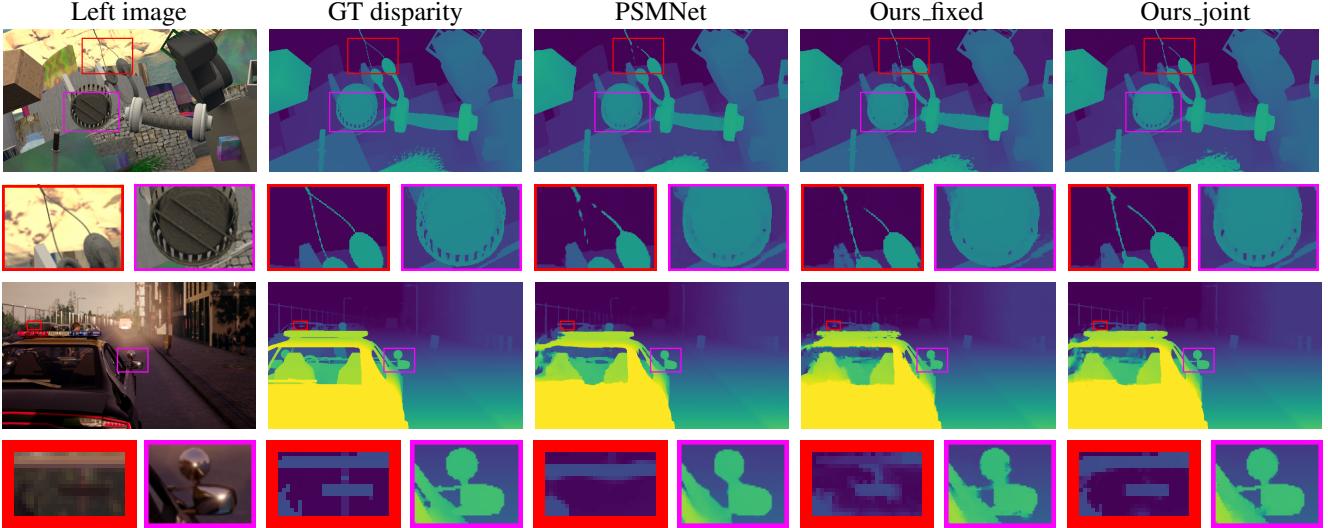


Figure 9. Qualitative results on SceneFlow and HR-VS. Our method is able to better preserve fine details, such as the wires and mirror frameworks in the highlighted regions. **Top rows:** SceneFlow. **Bottom rows:** HR-VS.

Table 1. End-point-error (EPE) on SceneFlow and HR-VS.

Dataset	PSMNet [7]	Ours_fixed	Ours.joint
SceneFlow	1.04	1.07	0.93
HR-VS	3.83	3.70	2.77

ban driving views. It contains 780 images at 2056×2464 resolution. The valid disparity range is $[9.66, 768]$. Because no test set is released, we randomly choose 680 frames for training, and use the rest for testing. Due to the relatively small data size, we fine-tune all three models trained on SceneFlow in the previous experiment on this dataset.

Because of the high resolution and large disparity, the original PSMNet cannot be directly applied to the full size images. We follow the common practice to downsample both the input images and disparity maps to $1/4$ size for training, and upsample the result to full resolution for evaluation. For our method, we predict superpixels with grid cell size 16×16 to perform $16\times$ downsampling/upsampling. During training, we set $m = 30$, and randomly crop the images into size 2048×1024 . We train all methods for 200 epochs with batch size 4. The initial learning rate is 1×10^{-3} and reduced to 1×10^{-4} after 150 epochs.

As shown in Table 1, our models outperform the original PSMNet. And a significantly lower EPE is achieved by joint training. Note that, comparing to SceneFlow, we observe a larger performance gain on this high-res dataset, as we perform $16\times$ upsampling on HR-VS but only $4\times$ upsampling on SceneFlow. Qualitative results are shown in Figure 9.

Results on Middlebury-v3. Middlebury-v3 is a high-res real-world dataset with 10 training frames, 13 validation frames³, and 15 test frames. We use both training and validation frames to tune the **Our.joint** model pre-trained on

SceneFlow with 16×16 superpixels. We set $m = 60$ and train the model for 30 epochs with batch size 4. The initial learning rate is 1×10^{-3} and divided by 10 after 20 epochs.

Note that, for the experiment, our goal is not to achieve the highest rank on the official Middlebury-v3 leaderboard. But instead, to verify the effectiveness of the proposed superpixel-based downsample/upsampling scheme. Based on the leaderboard, our model outperforms PSMNet across all metrics, some of which are presented in Table 2. The results again verify the benefit of the proposed superpixel-based downsample/upsampling scheme.

Table 2. Results on Middlebury-v3 benchmark.

Method	avgerr	rms	bad-4.0	A90
PSMNet_ROB [7]	8.78	23.3	29.2	22.8
Ours.joint	7.11	19.1	27.5	13.8

5. Conclusion

This paper has presented a simple fully convolutional network for superpixel segmentation. Experiments on benchmark datasets show that the proposed model is computationally efficient, and can consistently achieve the state-of-the-art performance with good generalizability. Further, we have demonstrated that higher disparity estimation accuracy can be obtained by using superpixels to preserve object boundaries and fine details in a popular stereo matching network. In the future, we plan to apply the proposed superpixel-based downsample/upsampling scheme to other dense prediction tasks, such as object segmentation and optical flow estimation, and explore different ways to use superpixels in these applications.

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³Named as additional dataset in the official website.

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Supplementary Materials for Superpixel Segmentation with Fully Convolutional Networks

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In Section 1 and Section 2, we provide the detailed architecture designs for the superpixel segmentation network and the stereo matching network, respectively. In Section 3, we report additional qualitative results for superpixel segmentation on BSDS500 and NYUv2, disparity estimation on Sceneflow, HR-VS, and Middlebury-v3, and superpixel segmentation on HR-VS.

1. Superpixel Segmentation Network

Table 1 shows the specific design of our superpixel segmentation network. We use a standard encoder-decoder design with skip connections to predict the superpixel association map Q . Batch normalization and leaky Relu with negative slope 0.1 are used for all the convolution layers, except for the association prediction layer (assoc) where softmax is applied.

Table 1. Specification of our superpixel segmentation network architecture.

Name	Kernel	Str.	Ch I/O	InpRes	OutRes	Input
cnn0a	3 × 3	1	3/16	208 × 208	208 × 208	image
cnn0b	3 × 3	1	16/16	208 × 208	208 × 208	cnn0a
cnn1a	3 × 3	2	16/32	208 × 208	104 × 104	cnn0b
cnn1b	3 × 3	1	32/32	104 × 104	104 × 104	cnn1a
cnn2a	3 × 3	2	32/64	104 × 104	52 × 52	cnn1b
cnn2b	3 × 3	1	64/64	52 × 52	52 × 52	cnn2a
cnn3a	3 × 3	2	64/128	52 × 52	26 × 26	cnn2b
cnn3b	3 × 3	1	128/128	26 × 26	26 × 26	cnn3a
cnn4a	3 × 3	2	128/256	26 × 26	13 × 13	cnn3b
cnn4b	3 × 3	1	256/256	13 × 13	13 × 13	cnn4a
upcnv3	4 × 4	2	256/128	13 × 13	26 × 26	cnn4b
icnv3	3 × 3	1	256/128	26 × 26	26 × 26	upcnv3+cnn3b
upcnv2	4 × 4	2	128/64	26 × 26	52 × 52	icnv3
icnv2	3 × 3	1	128/64	52 × 52	52 × 52	upcnv2+cnn2b
upcnv1	4 × 4	2	64/32	52 × 52	104 × 104	icnv2
icnv1	3 × 3	1	64/32	104 × 104	104 × 104	upcnv1+cnn1b
upcnv0	4 × 4	2	32/16	104 × 104	208 × 208	icnv1
icnv0	3 × 3	1	32/16	208 × 208	208 × 208	upcnv0+cnn0b
assoc	3 × 3	1	16/9	208 × 208	208 × 208	icnv0

2. Stereo Matching Network

Table 2 shows the architecture design of stereo matching network, in which we modify PSMNet [1] to perform superpixel-based downsampling/upsampling operations. We name it superpixel-based PSMNet (SPPSMNet).

Table 2. Specification of our stereo matching network (SPPSMNet) architecture.

Name	Kernel	Str.	Input	OutDim
Input				
Img_1/2				$H \times W \times 3$
Superpixel segmentation and superpixel-based wwnnsampling				
assoc_1/2	see Table 1		Img_1/2	$H \times W \times 9$
sImg_1/2	assoc_1/2	4	Img_1/2	$\frac{1}{4}H \times \frac{1}{4}W \times 3$
PSMNet feature extractor				
cnn0_1	$3 \times 3, 32$	1	sImg_1/2	$\frac{1}{4}H \times \frac{1}{4}W \times 32$
cnn0_2	3 × 3, 32	1	cnn0_1	$\frac{1}{4}H \times \frac{1}{4}W \times 32$
cnn0_3	3 × 3, 32	1	cnn0_2	$\frac{1}{4}H \times \frac{1}{4}W \times 32$
cnn1_x	$\begin{bmatrix} 3 \times 3, 32 \\ 3 \times 3, 32 \end{bmatrix} \times 3$	1	cnn0_3	$\frac{1}{4}H \times \frac{1}{4}W \times 32$
conv2_x	$\begin{bmatrix} 3 \times 3, 64 \\ 3 \times 3, 64 \end{bmatrix} \times 16$	1	cnn1_x	$\frac{1}{4}H \times \frac{1}{4}W \times 64$
cnn3_x	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 3$	1	cnn2_x	$\frac{1}{4}H \times \frac{1}{4}W \times 128$
cnn4_x	$\begin{bmatrix} 3 \times 3, 128 \\ 3 \times 3, 128 \end{bmatrix} \times 3, dila = 2$	1	cnn3_x	$\frac{1}{4}H \times \frac{1}{4}W \times 128$
PSMNet SPP module, cost volume, and 3D CNN				
output_1				$\frac{1}{4}H \times \frac{1}{4}W \times \frac{1}{4}D \times 1$
output_2			Please refer to [1] for details	$\frac{1}{4}H \times \frac{1}{4}W \times \frac{1}{4}D \times 1$
output_3				$\frac{1}{4}H \times \frac{1}{4}W \times \frac{1}{4}D \times 1$
Superpixel-based upsampling				
disp_prb1	bilinear upsampling assoc_1	N.A. 4	output_1	$\frac{1}{4}H \times \frac{1}{4}W \times D$ $H \times W \times D$
disp_prb2	bilinear upsampling assoc_1	N.A. 4	output_2	$\frac{1}{4}H \times \frac{1}{4}W \times D$ $H \times W \times D$
disp_prb3	bilinear upsampling assoc_1	N.A. 4	output_3	$\frac{1}{4}H \times \frac{1}{4}W \times D$ $H \times W \times D$
PSMNet disparity regression				
disp_1	disparity regression	N.A.	disp_prb1	$H \times W$
disp_2	disparity regression	N.A.	disp_prb2	$H \times W$
disp_3	disparity regression	N.A.	disp_prb3	$H \times W$

The layers which are different from the original PSMNet have been highlighted in bold face. In Table 2, we use input image size 256×512 with maximum disparity $D = 192$, which is the same as the original PSMNet, and we set superpixel grid cell size 4×4 to perform $4 \times$ downampling/upsampling.

For stereo matching tasks with high resolution images (*i.e.*, HR-VS and Middlebury-v3), we use input image size 1024×2048 with maximum disparity $D = 768$, and we set superpixel grid cell size 16×16 to perform $16 \times$ downsampling/upsampling. To further reduce the GPU memory usage, in the high-res stereo matching tasks, we reduce the

channel number of the layers “cnv4a” and “cnv4b” in the superpixel segmentation network from 256 to 128, remove the batch normalization operation in the superpixel segmentation network, and perform superpixel-based spatial upsampling after the disparity regression.

3. Additional Qualitative Results

3.1. Superpixel Segmentation

Figure 1 and Figure 2 show additional qualitative results for superpixel segmentation on BSDS500 and NYUv2. The three learning-based methods, SEAL, SSN, and ours, can recover more detailed boundaries than SLIC, such as the hub of the windmill in the second row of Figure 1 and the pillow on the right bed in the fourth row of Figure 2. Compared to SEAL and SSN, our method usually generate more compact superpixels.

3.2. Application to Stereo Matching

Figure 3, Figure 4, and Figure 6 show the disparity prediction results on SceneFlow, HR-VS and Middlebury-v3, respectively. Compared to PSMNet, our methods are able to better preserve the fine details, such as the headset wire (the seventh row of Figure 3), street lamp post (the first row of Figure 4) and the leaves (the fifth row of Figure 6). We also observe that our method can better handle textureless areas, such as the car back in the seventh row of Figure 4. It is probably because our method directly downsample the images 16 times before sending them to the modified PSMNet, while the original PSMNet only downsamples the image 4 times, and uses stride-2 convolution to perform another $4 \times$ downsampling later. The input receptive field (w.r.t. the original image) of our method is actually larger than that of original PSMNet, which enables our method to better leverage context information around the textureless area.

Figure 5 visualizes the superpixel segmentation results of **Ours.fixed** and **Ours.joint** methods on HR-VS dataset. In general, Superpixels generated by **Ours.joint** are more compact and pay more attentions to the disparity boundary. The color boundaries that are not aligned with the disparity boundary, such as the water pit on the road in the second row of Figure 5, are often ignored by **Ours.joint**. This phenomenon reflects the influence of disparity estimation on the superpixels in the joint training.

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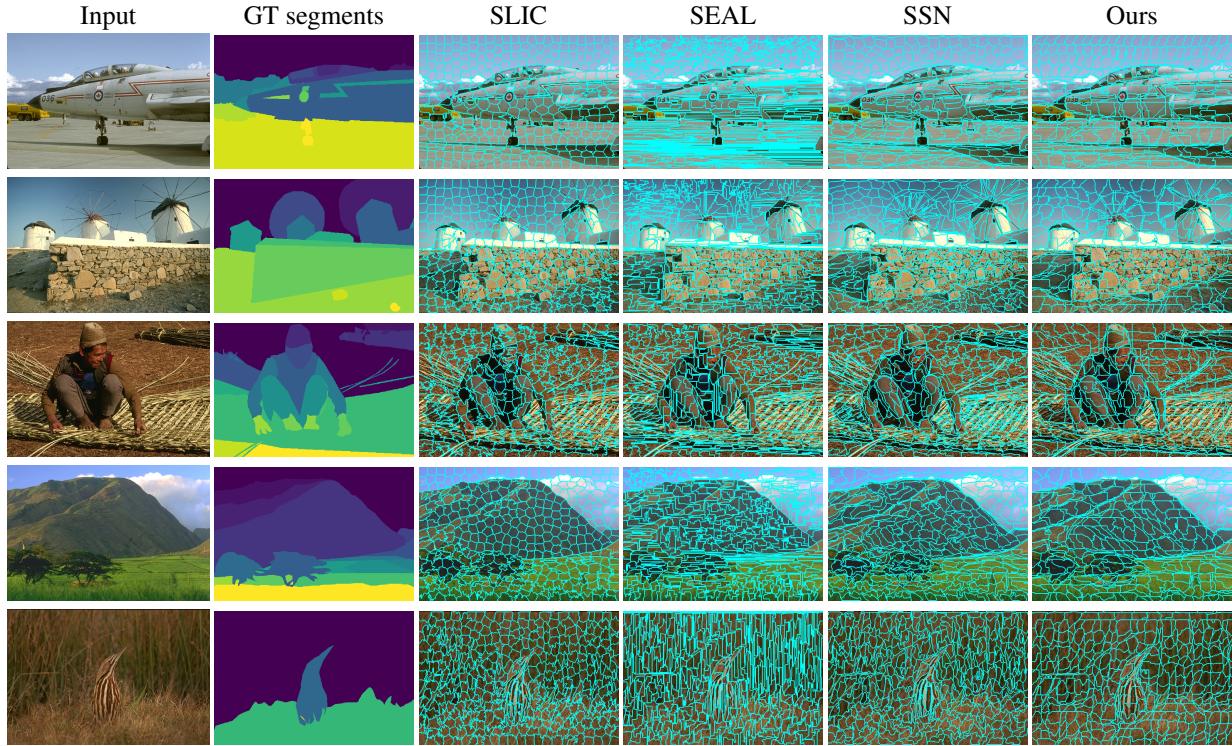


Figure 1. Additional superpixel segmentation results on BSDS500.

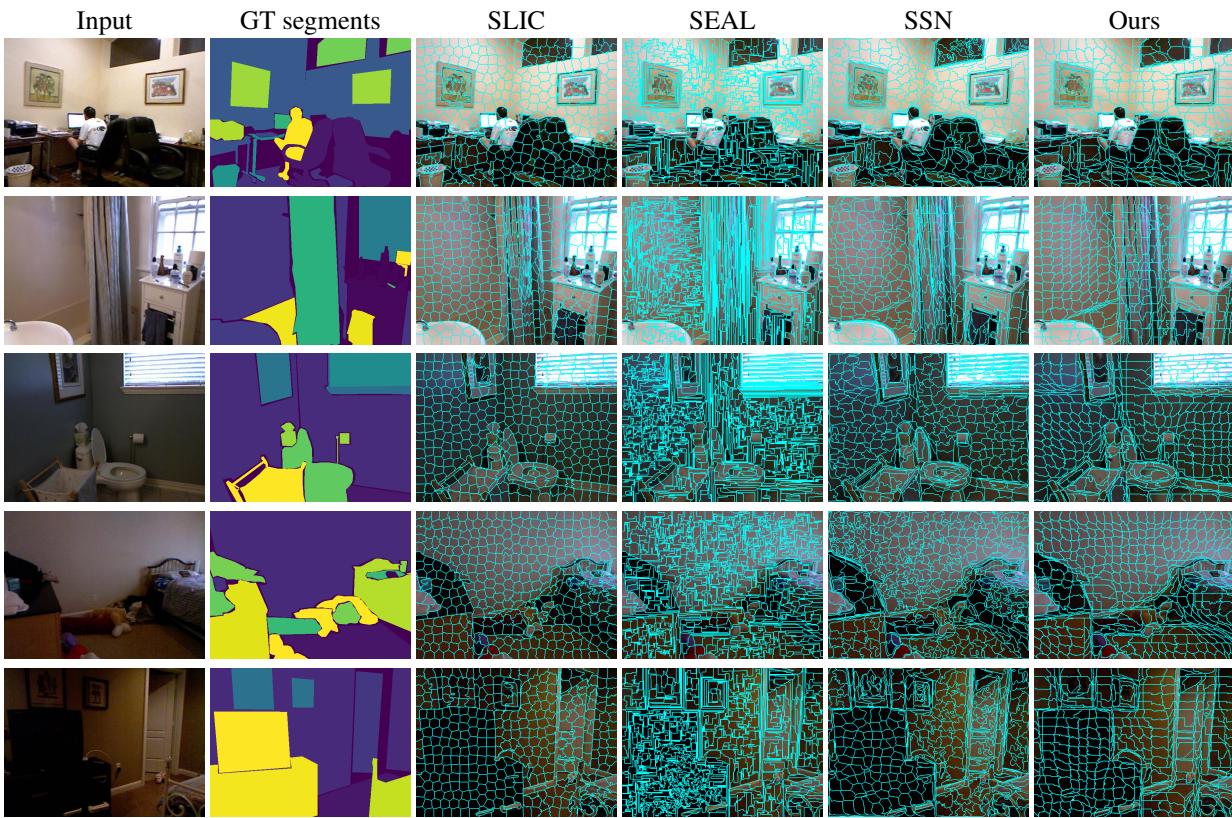


Figure 2. Additional superpixel segmentation results on NYUv2.

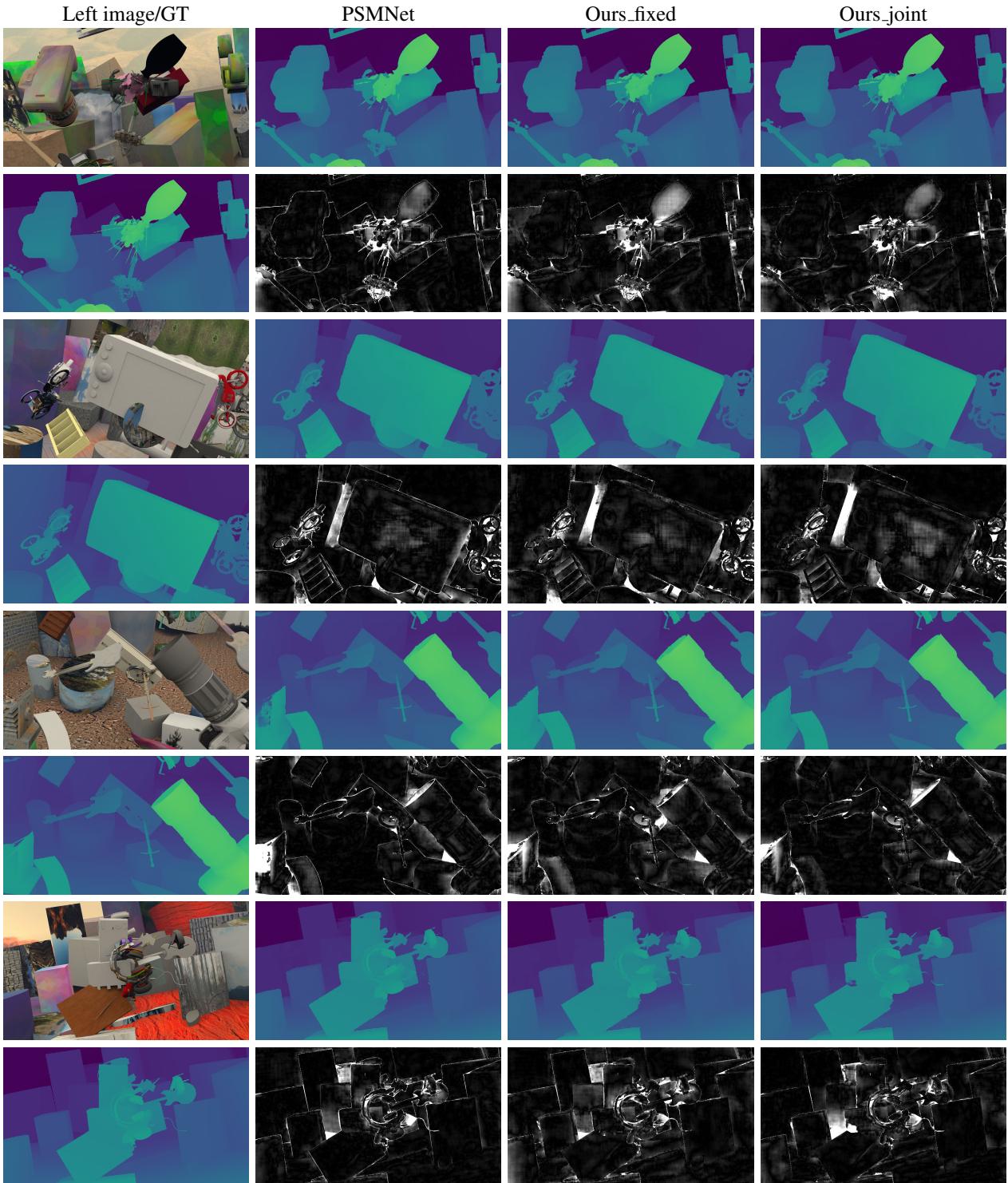


Figure 3. Disparity prediction results on SceneFlow. For each method, we show both the predicted disparity map (top) and the error map (bottom). For the error map, the darker the color, the lower the end point error (EPE).

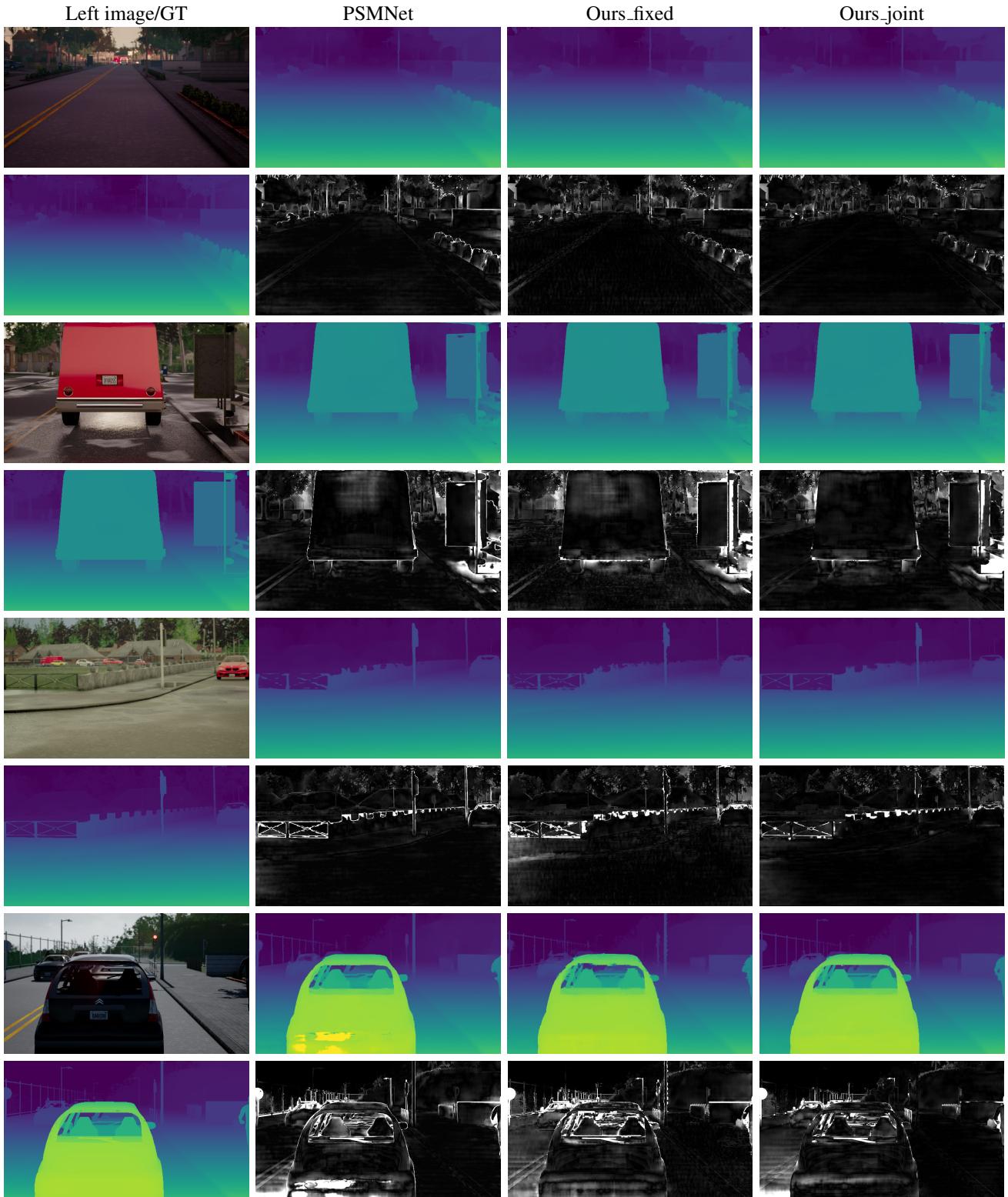


Figure 4. Disparity prediction results on HR-VS. For each method, we show both the predicted disparity map (top) and the error map (bottom). For the error map, the darker the color, the lower the end point error (EPE).

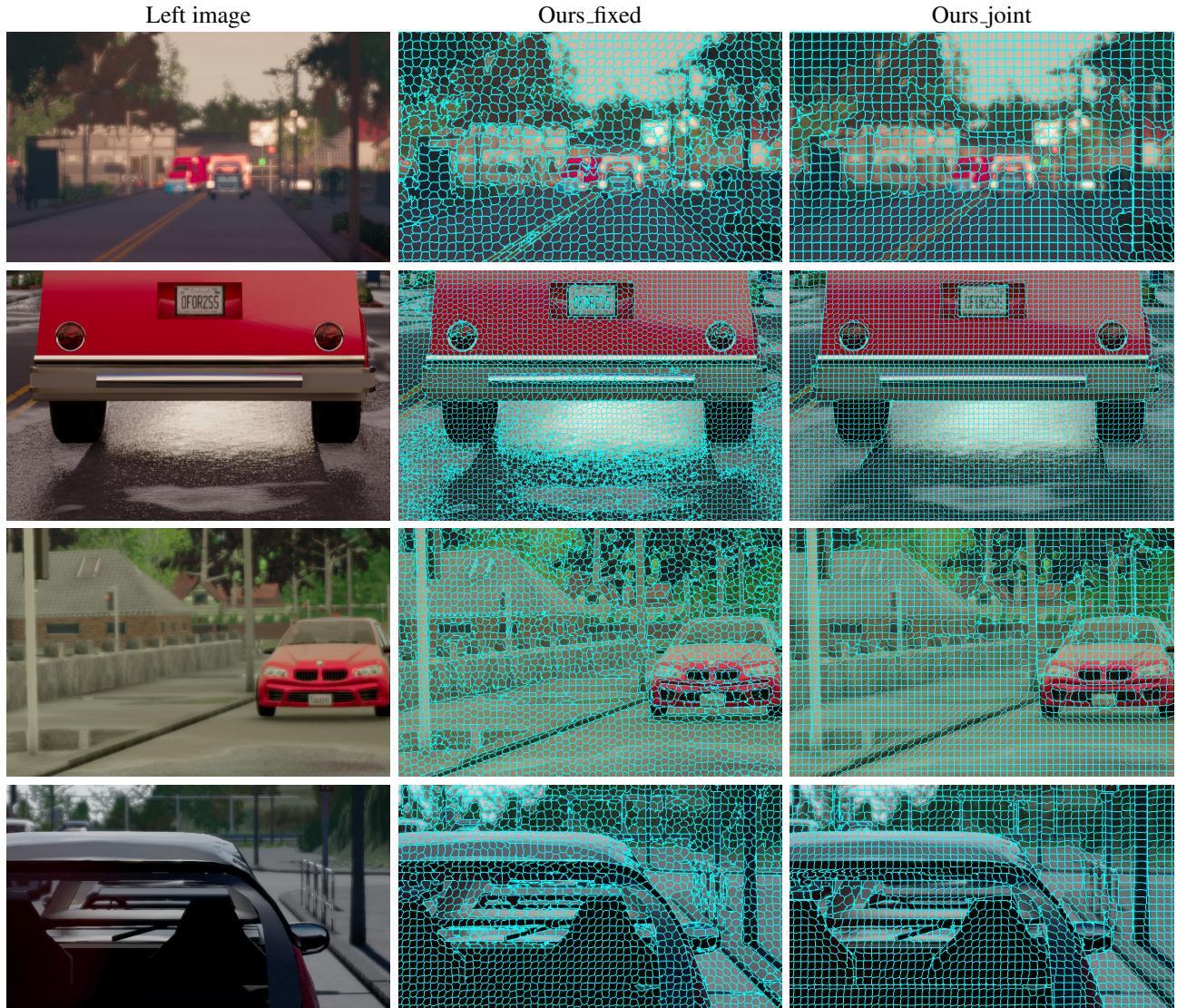


Figure 5. Comparsion of superpixel segmentation results on HR-VS. Note we do not enforce the superpixel connectivity here.

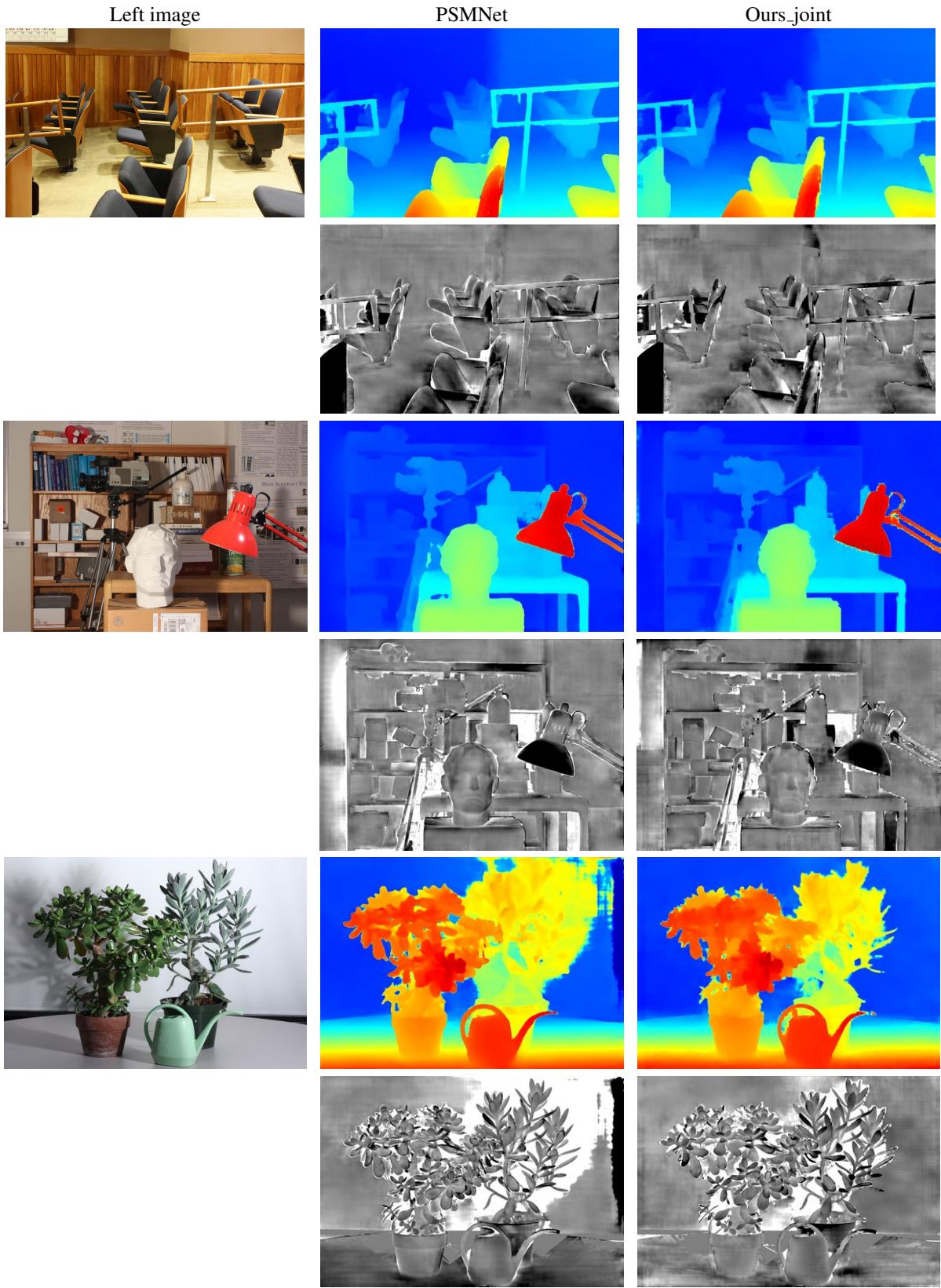


Figure 6. Disparity estimation results on Middlebury-v3. For each method, we show both the predicted disparity map (top) and the error map (bottom). For the error map, the darker the color, the lower the error. All the images are from Middlebury-v3 leaderboard.