



班级

姓名

编号

科目

第

T<sub>2</sub> 构造  $f: [0, 1] \rightarrow [a, b]$ ,  $f(x) = a + (b-a) \cdot x$

T<sub>4</sub> ①:  $A_1 = \{x \mid (\exists n) (n \in \mathbb{N} \wedge x = n^2)\}$

②:  $A_2 = \{x \mid (\exists n) (n \in \mathbb{N} \wedge x = n^3)\}$

③:  $A_3 = \{x \mid (\exists n) (n \in \mathbb{N} \wedge x = n^4)\}$

T<sub>7</sub> (1) ~~100~~  $2^m \leq k^m \leq m^m \leq 2^m \Rightarrow k^m = 2^m$

(2)  $2^m \leq l^m \leq m^m \leq 2^m \Rightarrow l^m = 2^m = k^m$

T<sub>9</sub> 将点按  $|x| + |y|$  的值划分为下面的点集

$$A_0 = \{(0, 0)\} \quad A_1 = \{(-1, 0), (0, -1), (0, 1), (1, 0)\}$$

$$A_2 = \{(-2, 0), (-1, -1), (0, -2), (2, 0), (1, 1), (0, 2), (1, -1), (-1, 1)\}$$

$\vdots$

构造  $f: \mathbb{N} \rightarrow$  整点的集合

$$f(0) = (0, 0), f(1) = (-1, 0), f(2) = (0, -1), \dots$$

$f$  为单射且  $f$  为满射  $\Rightarrow$  所有整点构成的集合为可数集

T<sub>10</sub>

$$(1) 3 \quad (2) \aleph_0 \quad (3) \aleph_0 \quad (4) \{x \mid (\exists n)(n \in \mathbb{N} \wedge x = n^0)\} = \aleph_0$$

$$(5) \aleph_0 \leq \text{card}(B \cup D) \leq \text{card}(B) + \text{card}(D) = \aleph_0 + \aleph_0 = \aleph_0 \quad \therefore \aleph_0$$

$$(6) = |\mathbb{N}|^{|\mathbb{N}|} = \aleph_0^{\aleph_0} = 2^{\aleph_0} = \aleph_1$$

$$(7) = |\mathbb{R}|^{|\mathbb{R}|} = 2^{\aleph_1}$$