

Tuesday 11/01/2022

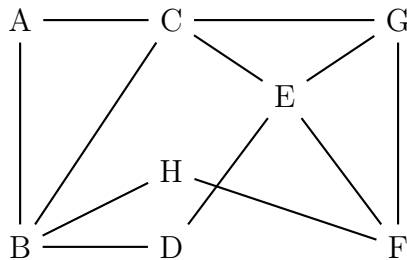
Final Exam

Duration: 90 minutes

Name:

Student No:

P1 [25 points] If exists in the graph, give an example of the following. If impossible, write impossible.
(Ex. If **path** was asked, a correct answer would be: A-C-E)



Eulerian trail:

Eulerian cycle:

Hamiltonian path:

P2 [10 points] Choose the correct option:

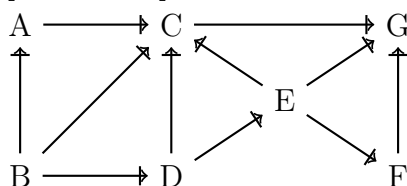
What is the chromatic number of $K_{3,4}$?

A) 2 B)3 C)4 D)6 E)12

What is the chromatic number of K_9 ?

A) 3 B)6 C)8 D)9 E)10

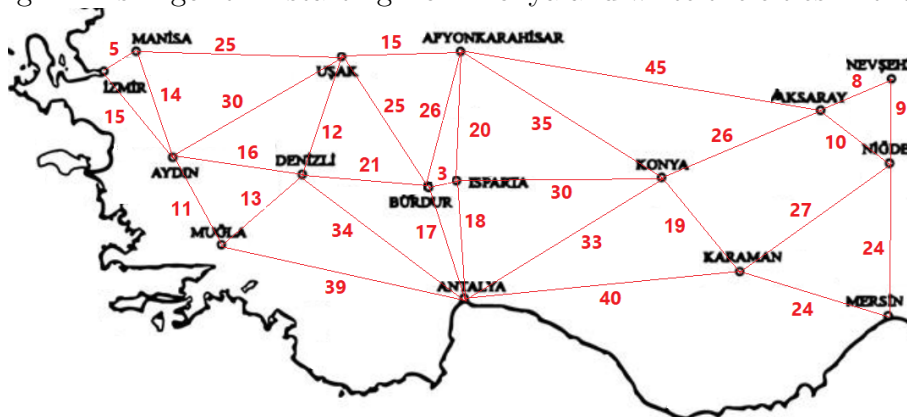
P3 [20 points] Topological Sort & Counting



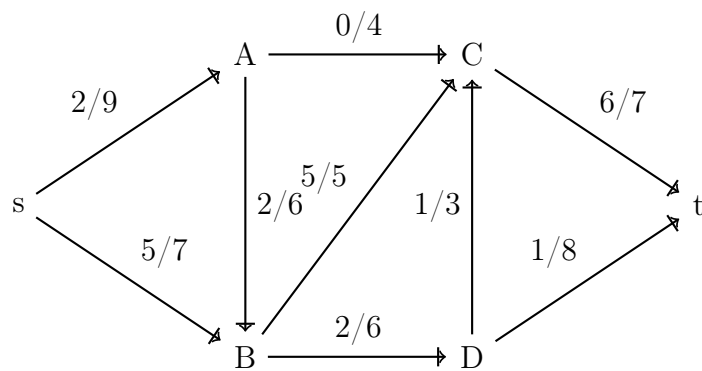
Give a topological order for the graph:

What is the number of possible topological orders?

P4 [15 points] Minimum Spanning Tree In the map below, draw a minimum spanning tree by using Prim's Algorithm starting from Konya and write the cities in the order you add them to the MST.



1	Konya	9	
2		10	
3		11	
4		12	
5		13	
6		14	
7		15	
8		16	

P5 [20 points] Network Flows

A network and a flow F on this network are given on the left.

1. According to the capacities, what is the maximum flow of this network?
2. Draw the residual graph.

P6 [15 points] Generating Functions & Combinations Solve this question using generating functions (Build the polynomial, determine the coefficient to look for, and calculate the final result) [Recall that $1/(1-x) = 1 + x + x^2 + x^3 + \dots$]

How many integer solutions are there to the equation $x_1 + x_2 + x_3 + x_4 + x_5 = 20$ with the restriction that all of $x_i \geq 1$ where two of them are odd and the remaining three are even integers?