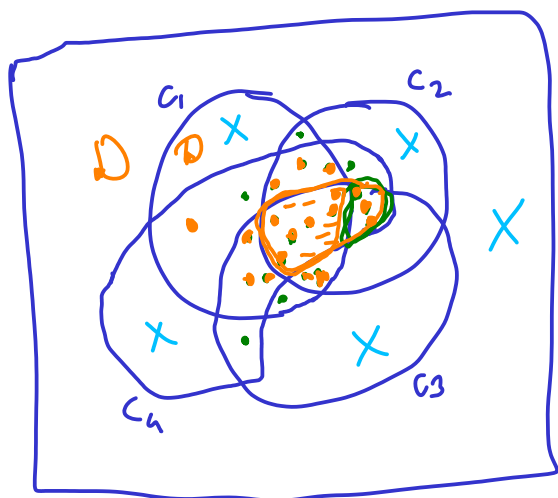


$\overline{m} \mid E. \Rightarrow \bar{N} = \text{none of the cond.}$

\Rightarrow exactly m cond.

$=$ at least m cond.

$$\bar{N} = S_0 - S_1 + S_2 - S_3 + \dots$$



$$E_2 = S_2 - \binom{3}{2} S_3 + \binom{4}{2} S_4$$

$c_2 \cap c_3 \cap c_4$

$N(c_1, c_2, c_3, c_4)$

$c_2 c_3$

$c_2 c_4$

$c_3 c_4$

$\binom{3}{2}$

$$S_2 = \sum_{i,j} N(c_i, c_j)$$

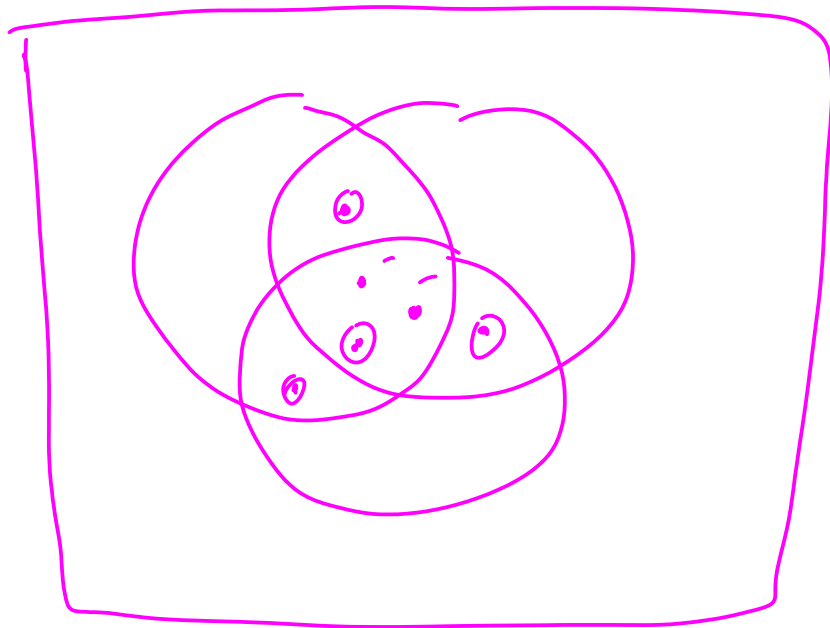
$$\binom{4}{2} - 4 \binom{3}{2} = \binom{4}{2}$$

$$6 - 12 = -6$$

$$= \underline{N(c_1, c_2) + N(c_1, c_3) + \dots}$$

$$S_3 = \sum N(c_i, c_j, c_k)$$

$$= \underline{N(c_1, c_2, c_3)} + \underline{N(c_1, c_2, c_4)} + \underline{N(c_1, c_3, c_4)} + \underline{N(c_2, c_3, c_4)}$$



$$L_2 = S_2 - \binom{2}{1} S_3$$



$$10 \times 4 = 40$$

$$E_2 = S_2 - \binom{3}{2} S_3 + \binom{4}{2} S_4 - \binom{5}{2} S_5$$

$$= \binom{5}{2} 2^{\binom{2}{2}} - \binom{3}{2} \binom{5}{3} 2^{\binom{2}{2}} + \binom{4}{2} \binom{5}{4} 1 - \binom{5}{2} \binom{5}{5} 1$$

$$= 10 \cdot 8 - 60 + 30 - 10 = 40 \checkmark$$

$$S_2 = \sum_{i,j} N(c_i c_j)$$



$$\begin{pmatrix} \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \end{pmatrix} \times \binom{5}{2} = 40$$

$\forall: 1 \leq i \leq 5$
 $C_i = V_i$ is isd.

t # of cond.

$$E_2 = S_2 - \binom{3}{2} S_3 + \binom{4}{2} S_4 - \binom{5}{2} S_5$$

$$= \binom{5}{2} 2^{\binom{2}{2}} - \binom{3}{2} \binom{5}{3} 2^{\binom{2}{2}} + \binom{4}{2} \binom{5}{4} 1 - \binom{5}{2} \binom{5}{5} 1$$

$$= 80 - 60 + 30 - 10$$

$$= 40$$



$$S_3 = N(c_1 c_2 c_3)$$

$$\binom{5}{3}$$

$$N(c_3 c_4 c_5)$$

$$N(c_1 c_3)$$

$$N(c_4 c_5)$$



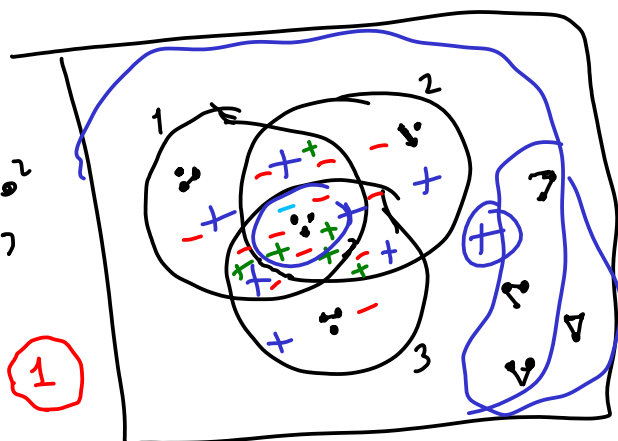
$$\begin{array}{c}
 \begin{array}{c} \bullet \\ \bullet \\ \bullet \\ \bullet \end{array} \quad \begin{array}{c} \bullet \\ \bullet \\ \bullet \end{array} \quad \dots \quad + \quad \begin{array}{c} \bullet \\ \bullet \\ \bullet \end{array} \quad + \quad \begin{array}{c} \bullet \\ \bullet \end{array} \\
 40 + 10 + 1 = 51
 \end{array}$$

$$\begin{aligned}
 L_2 &= S_2 - \binom{2}{1} S_3 + \binom{3}{1} S_4 - \binom{4}{1} S_5 \\
 &= \binom{5}{2} 2^{\binom{3}{2}} - \binom{2}{1} \binom{5}{3} 2^{\binom{2}{2}} + \binom{3}{1} \binom{5}{4} \cdot 1 - \binom{4}{1} \binom{5}{5} \cdot 1 \\
 &= 80 - 40 + 15 - 4 \\
 &= 40 + 11 = 51 //
 \end{aligned}$$

$$\bar{N} = S_0 - S_1 + S_2 - S_3$$

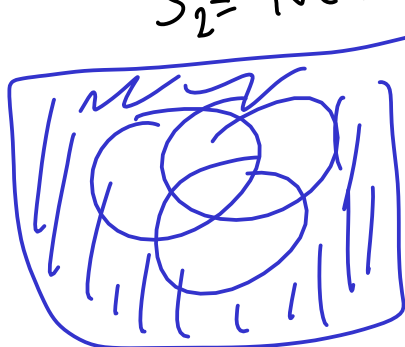
$$\begin{aligned}
 &= 2^3 - \binom{3}{1} 2^1 + \binom{3}{2} \boxed{1} - \binom{3}{3} \boxed{1} \\
 &= 8 - 6 + 3 - 1 = 4 //
 \end{aligned}$$

$$C_i: \begin{array}{c} 1 \quad 2 \\ \bullet \quad \bullet \\ \bullet \quad \bullet \end{array}$$

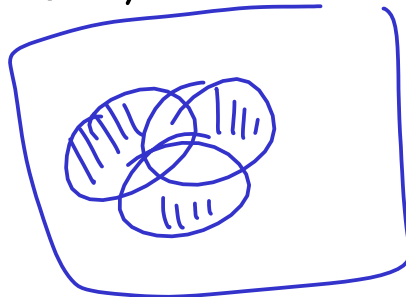


$$N(C_1 C_2 C_3)$$

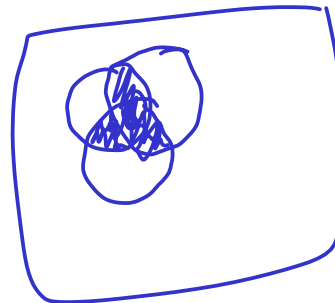
$$S_2 = N(C_1 C_2) + N(C_1 C_3) + N(C_2 C_3)$$



Ord. i.e



Exactly



At least

$$\text{At most } m = S_0 - L_{m+1}$$

M_m



at most 1

Derangement

C_i : pos i turns out to be wrong.

$$\text{round}\left(\frac{18!}{e}\right)$$

$$\bar{N}: S_0 - S_1 + S_2 - S_3 \dots + S_{18}$$

$$\frac{18!}{e} = \frac{1}{e}$$

$$\left(\frac{18!}{e}\right)$$

$$= 18! - \binom{18}{1} \cdot 17! + \binom{18}{2} 16! - \binom{18}{3} 15! \dots \frac{1}{2.718}$$

$$\frac{18.17}{2}$$

$$\binom{18}{18} 0!$$

$$= \frac{18!}{0!} - \frac{18!}{1!} + \frac{18!}{2!} - \frac{18!}{3!} + \frac{18!}{4!} \dots \frac{18!}{18!}$$

$$= 18! \left(\frac{1}{0!} - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} \dots \right)$$

$$\frac{1}{18!}$$

$$e^x = 1 + x + \frac{x^2}{2} + \frac{x^3}{3!} + \frac{x^4}{4!} \dots$$

$$\frac{d}{dx} e^x = 0 + 1 + x + \frac{x^2}{2} + \frac{x^3}{3!} \dots = e^x$$

$$e^{-1} = 1 - 1 + \frac{1}{2!} - \frac{1}{3!} \dots$$

$$\left(\frac{4!}{e}\right)$$

$$4! \left(1 - 1 + \frac{1}{2} - \frac{1}{6} + \frac{1}{24} \right)$$

$$24 - 24 + 12 - 4 + 1 = 9$$

$$\lim_{n \rightarrow \infty} \left(1 - \frac{1}{n}\right)^n = \frac{1}{e}$$

$$\left(\frac{3M - 1000}{3000}\right)^{3000}$$

