

principal rings

## Definition

Let  $A$  be a ring. A left ideal  $\mathfrak{a} \subset A$  is called principal if

$$\mathfrak{a} = Aa$$

for some  $a \in A$ .

## Definition

Let  $A$  be a non-zero commutative ring. It is called a principal ring if every ideal is principal.

## Question

Let  $k$  be a field and consider  $A = M_2(k)$ , the ring of all square matrices of size 2 with entries in  $k$ . Let  $\alpha \subset A$  be the right ideal consisting of matrices whose first row is zero. Is  $\alpha$  principal?