

# Representable functors

## Definition

Let  $\mathcal{C}$  be a category and **Set** the category of sets. For any object  $C \in \text{ob}(\mathcal{C})$ , one has a functor

$$h_C : \mathcal{C}^{\text{op}} \rightarrow \mathbf{Set}$$

sending  $A$  to  $\text{Mor}(A, C)$ .

A functor

$$F : \mathcal{C}^{\text{op}} \rightarrow \mathbf{Set}$$

is called representable if

$$F \xrightarrow{\sim} h_C$$

for some  $C$ .

## Question

Sending  $A$  to  $\text{Mor}(C, A)$ , we get another functor. What are its source and target?