

# Equivalence

## Definition

Let  $\mathcal{C}$  and  $\mathcal{D}$  be categories. If one has functors

$$F: \mathcal{C} \rightarrow \mathcal{D}$$

$$G: \mathcal{D} \rightarrow \mathcal{C}$$

together with natural transformations

$$F \circ G \xrightarrow{\sim} 1_{\mathcal{D}}$$

$$G \circ F \xrightarrow{\sim} 1_{\mathcal{C}},$$

then we say  $\mathcal{C}$  and  $\mathcal{D}$  are equivalent as categories.

## Question

In the definition of an equivalence between two categories, what happens if you replace natural transformations with equality?