

UNIVERSIDAD DE CÓRDOBA

Facultad de Ciencias

Grado de Física

Trabajo Fin de Grado

Baryon acoustic oscillations in a non-flat universe

Código del TFG: **FS22-17-FSC**

Tipo de TFG: **Trabajo teórico-práctico**

Autor: Santiago Sanz Wuhl



Fecha de entrega

Agradecimientos

Incluir los agradecimientos, si procede.

Contents

Índice general	2
List of figures	3
List of tables	4
Resumen. Palabras clave	5
Abstract. Keywords	6
1 Introduction	7
1.1 The Hot Big Bang model	7
1.2 Cosmic Microwave Background	8
1.3 Baryon Acoustic Oscillations	9
1.4 Curvature, dark matter and the expansion of the universe	12
1.5 A Cold Dark Matter model	14
2 Objectives	17
3 Methods and materials.	18
4 Results	25
Conclusiones	28
Conclusions	29
Bibliografía	30
Anexo: Example of data visualisation code with python & matplotlib	31

List of figures

1.1	The all-sky map of CMB anisotropies as seen by space-based Observatory Planck	8
1.2	Different stages of the Baryon Acoustic Oscillations.	10
1.3	The first observations of the Baryon Acoustic Oscillations phenomenon, observed independently by the Sloan Digital Sky Survey (SDSS) [4] as seen in the left panel and the 2dF collaboration [5] in the right panel. These were the main tools that finally determined the existence of the BAO. The SDSS result shows the measured correlation function $\xi(s)$. This function represents the distribution of the distance in between galaxies. Note the similarity between this graph and the frozen BAO from the figure 1.2. The local maximum at $s \approx 100 \text{ h}^{-1} \text{ Mpc}$ corresponds to the BAO peak. The 2dF result, seen in the rightmost panel is the measured power spectrum $P(k)$ (here called $W(k)$, which is the Fourier transform of the $\xi(r)$ function.	11
3.1	The power spectrum $P(k)$ of the LRG eBOSS [8] catalogue as calculated by RUSTICO assuming a flat universe ($\Omega_k = 0.00$)	21
3.2	Graphic representation of the power spectrum $P(k)$ as calculated by CLASS (left panel), the smoothed power spectrum $P_{smooth}(k)$ (middle panel) and the oscillations $O_{lin}(k)$ (right panel) for a flat universe $\Omega_k = 0.00$	21
3.3	The BAO analysis pipeline schematic	24
4.1	Calculation of the cosmological observables for different fiducial cosmologies.	27

List of Tables

1.1	Fiducial cosmological parameter values used in the BAO analysis and values for the ‘derived’ values r_d , D_H/r_d , D_M/r_d	15
4.1	Results of the measurement of the cosmological observables we were interested in. This table shows the same data as the figure 4.1.	26

Resumen

En este trabajo de fin de grado se hace uso de herramientas de computación de alto rendimiento y análisis de datos para estudiar los efectos de ligeras variaciones en el modelo cosmológico estándar, el modelo Λ *Cold Dark Matter* (Λ CDM). Si bien este modelo asume un universo espacialmente plano, se observa que las variaciones de hasta un 20% en el parámetro de curvatura del universo Ω_k no tienen consecuencias significativas en los observables que nos interesan.

Este trabajo se basa en las oscilaciones acústicas de bariones, un fenómeno que nos permite estudiar el comportamiento del universo en sus etapas más tempranas (los primeros 380.000 años de sus 13.800 millones de años de vida, ¡un 0,03% de la vida del universo!). Estas oscilaciones dan forma a la estructura a gran escala del universo y, lo que es más importante, establecen una "regla cósmica" r_d con respecto a la cual se miden las distancias cosmológicas, como la distancia de Hubble D_H y la distancia del diámetro angular D_M .

Después de analizar el catálogo de galaxias de la encuesta espectroscópica de oscilaciones acústicas de bariones extendida, se obtuvieron los siguientes resultados: $D_H/r_d = 18.66 \pm 0.72$ y $D_M/r_d = 18.28 \pm 0.53$ para un universo plano, en concordancia con los resultados para todos los valores del parámetro Ω_k indicados, y lo que es más importante, con resultados anteriores en el campo.

Palabras clave: Cosmología; Astrofísica; Oscilaciones Acústicas de Bariones; Análisis de datos.

Abstract

In this Bachelor's Thesis we make use of high performance computing and data analysis tools to study the effects of slight variations in the Standard Cosmological model, the Λ Cold Dark Matter (Λ CDM) model. While this model assumes a spatially flat universe, we observe that variations of around 20% in the curvature parameter of the universe Ω_k have no significant consequences in the observables that interest us.

This work is based off the Baryon Acoustic Oscillations, a phenomenon that allows us to study the behaviour of the universe in its earliest stages (the first 380.000 of its 13.8 billion years of lifetime – a 0.03% of the Universe's lifetime!). These oscillations shape the large scale structure of the universe, and more importantly, set a 'cosmic ruler' r_d with respect to which is used to measure cosmological distances, such as the Hubble distance D_H and angular diameter distance D_M .

After analyzing the extended Baryon Oscillation Spectroscopic Survey galaxy catalogue, we achieve the following results: $D_H/r_d = 18.66 \pm 0.72$ y $D_M/r_d = 18.28 \pm 0.53$ for a flat universe, in concordance to the results for all the stated Ω_k parameter values, and more importantly with previous results in the field.

Keywords: Cosmology; Astrophysics; Baryon Acoustic Oscillations; Data Analysis.

CHAPTER 1

Introduction

1.1. THE HOT BIG BANG MODEL

The most accepted model for the origin of the universe is the Big Bang model, that models the beginning of the universe as a hot dense state. The Big Bang surprisingly to some conveys no "bang", but the sudden existence of all the matter in the universe, in the shortest of times, in the smallest of spaces, about 13.8 billion years ago. After an unthinkable small interval of time, the universe began a short period of rapid expansion known as *cosmic inflation*, in which the universe grew by a factor 10^{27} in a mere 10^{-33} seconds. This inflation is thought to be due to the inflaton, a quantum scalar field. It is theorized that it is the inflaton's vacuum energy what caused the universe to expand as greatly.

As any quantum field¹ the inflaton presents fluctuations. This means, even in the vacuum state² there is constant creation and annihilation of particles. These fluctuations are what cause anisotropies in the matter distribution of the universe, fact that will be important later in this work.

After the inflation phase, the universe cooled enough for what is known as the Quark-Gluon plasma to form. In this state, temperatures were high enough as to consider relativistic the random motion of the particles in it. After some cooling due to cosmic expansion, the combination between quarks to form hadrons was allowed, leading to what is known as the hadronic epoch. However, due to the short mean free path of the photons, the universe is still opaque to electromagnetic radiation.

As the universe kept expanding the densities decreased and the temperatures cooled,

¹Quantum fields are a tool used by Quantum Field Theory (QFT) to more accurately describe particles and their interactions, at high enough energies.

²To define vacuum in QFT is not as easy a task as it was in classical mechanics (or even non-relativistic quantum mechanics). These details go beyond the scope of this work, and thus will not be dealt with.

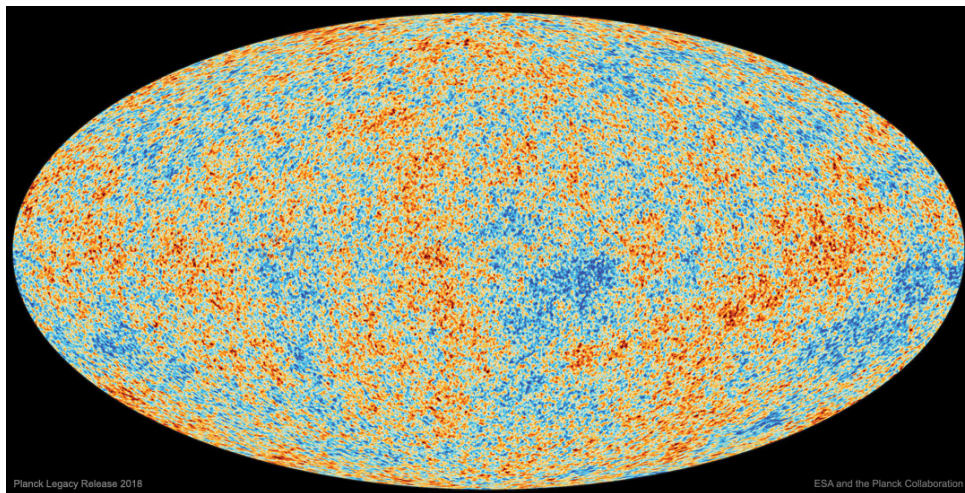


Figure 1.1: The all-sky map of CMB anisotropies as seen by Space-based Observatory Planck [1]. The colors in this map represent the fluctuations around the mean $T = 2.7\text{ K}$ with fluctuations of 10^{-5} with respect to the average temperature. Red means higher temperature than the average, whilst blue means lower temperature than the average.

the existence of atoms was starting to be allowed, the He and H atoms. This period would finish at the universe age of 380,000 years, moment known as recombination. Recombination is thought of as the time at which the Thomson Scattering mechanisms stop being effective (the scattering cross section of this process becomes negligible and thus the photon mean free path grows considerably). As soon as recombination ends, the thermally activated photons which are no longer energetic enough to interact with the electrons now travel freely through space. This emission is known as the Cosmic Microwave Background (CMB) and is the oldest direct observation using electromagnetic radiation we can take of the universe.

Though the name ‘recombination’ implies the fact that the universe used to be ‘combined’ and then ceased to be so, it just comes from the fact that recombination was theorized before the Big Bang theory was thought of.

1.2. COSMIC MICROWAVE BACKGROUND

We see in the figure 1.1 the CMB as observed by the Planck collaboration [1]. The radiation we observe is the photons that were emitted about 13.8 billion years ago. Since the CMB appears as a result of the thermal photons emitted by the electrons in the primordial plasma, it offers great insight into what the plasma looked like, and the way it behaved.

The Cosmic Microwave Background was discovered in 1965 as a serendipity by Penzias and Wilson [2]. They observed a noise signal, uniformly distributed³ from every direction, day or night, summer or winter, almost as if it came directly from the origin of the

³It will we later discovered that it was not actually uniformly distributed.

universe. This discovery was considered to be solid evidence for the Big Bang model and more importantly, the beginning of the modern cosmology. All of this became the reason Penzias and Wilson received a Nobel prize 13 years later, in 1978.

Since what is being measured are the photons left from recombination, which corresponds to a thermal radiation curve, we may use Wien's displacement law

$$T = \frac{b}{\lambda} \quad (1.1)$$

with $b \approx 2.897$ mm K Wien's constant, T the black body radiation and λ the wavelength at which the spectral radiation intensity is maximum to calculate the corresponding temperature to the measured wavelength. Using Planck's law, the measured temperature is 2.7 K which corresponds to a measured wavelength of 1.06 mm (microwave radiation, as the name Cosmic *Microwave* implies).

In 1991 anisotropies in the CMB were first discovered, by the COBE satellite[3] later earning Smoot and Mather a nobel prize. As of 2023 the most precise measurements correspond to the Planck experiment in 2018 [1] by the European Space Agency. These anisotropies can be seen in the figure 1.1.

Of course, 2.7 K was not the temperature of the plasma at recombination, as it was approximately hotter by a factor $z = 1090$, or ≈ 3000 K. The reason we measure such smaller temperatures is because of the expansion of the universe. If today ($t = t_0$) some radiation of wavelength λ_o were observed, that somehow is known to have been traveling for some time Δt will have stretched due to the expansion of the universe. In other words, the wavelength λ_e of the emitted radiation was smaller by a factor⁴ $a(t')^{-1}$, with $t' = t_0 - \Delta t$ being the earlier time at which the radiation was emitted, and $a(t_0) = 1$ by definition. By Wien's displacement law (1.1), this corresponds to a higher temperature by a factor $a(t')$.

Thus, the CMB becomes crucial in explaining the large scale structure of the universe, since the photons that decoupled from the plasma at recombination wasted more energy leaving denser regions behind losing thermal energy in the process. Appearing at a slightly lower temperature (gravitational redshift). On the contrary, those in void regions will appear hotter, being blueshifted. Therefore, temperature fluctuations in the CMB correspond to density fluctuations in the early universe.

1.3. BARYON ACOUSTIC OSCILLATIONS

Before recombination, both matter and photons were coupled into the same fluid which we have called the primordial plasma. The particles in the plasma interacted primarily with one another through gravity and the electromagnetic field, depending on the type of

⁴The factor $a(t)$ is known as the scale factor of the universe, and will be explained with further detail later in the work.

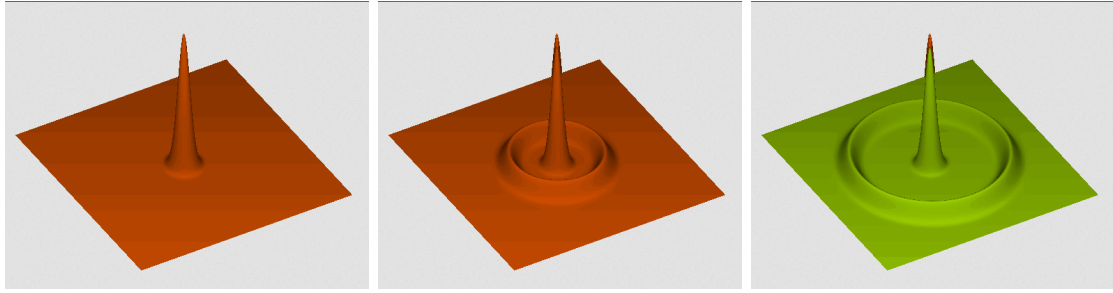


Figure 1.2: Different stages of the Baryon Acoustic Oscillations, as an evolution with time. At first, in the leftmost panel the origin of the oscillations are shown. This is, baryon matter clumped together with dark matter. As the thermal photons from the black body radiation push matter through space, the formed wavefront propagates through space, as seen in the middle pannel. After recombination, when the wavelength of the radiation gets sufficiently stretched due to cosmic inflation, the photons do not have enough energy for Thomson Scattering to be effective and thus the oscillations freeze; or to be more precise, the wavefronts freeze. This stage is shown in the rightmost panel. Courtesy of the diagram: <https://lweb.cfa.harvard.edu/~deisenst/acousticpeak/anim.gif>.

matter considered.

As already mentioned, matter was not distributed homogenously. This means that at any point in time before recombination, one could find ‘lumps’ of dark and baryonic (standard) matter. Combining the restoring force of the gravitational attraction between dark and baryonic matter with itself and with one another, and the repulsion caused by the radiation pressure due to the Thomson Effect between baryons and photons, the results are pure acoustic waves propagating through the plasma, with the dark matter lumps being in the center of these waves. Since the baryonic matter is dragged by these sound waves, they are called Baryon Acoustic Oscillations (BAO), and a simplistic explanation of their mechanism is shown in the figure 1.2

The waves would propagate throughout the plasma as long as the baryon-photon interaction was strong enough i.e. up to recombination, at which point they froze in time leaving higher density regions. Higher density means higher gravitational intensity, which in turn means higher galaxy proliferation in spherical distributions. These spherical distributions (which can be measured in the CMB) are what is known as the large scale structure of the universe.

At big enough distances, the radii (r_d) of these spheres, also called the sound horizon is used as a ‘cosmic ruler’. Big scale measurements are calculated in terms of r_d , which is measured from the CMB. This means it needs to be calibrated from external information. r_d has been measured from the CMB to be around 150 Mpc or 500 million lightyears. To give an idea of the size of r_d , the radius of the observable universe is around 100 times r_d .

Given the large dimensions of this cosmic ruler and the homogeneity of the universe on large scales, this ruler is only affected by cosmological expansion rather than late-time

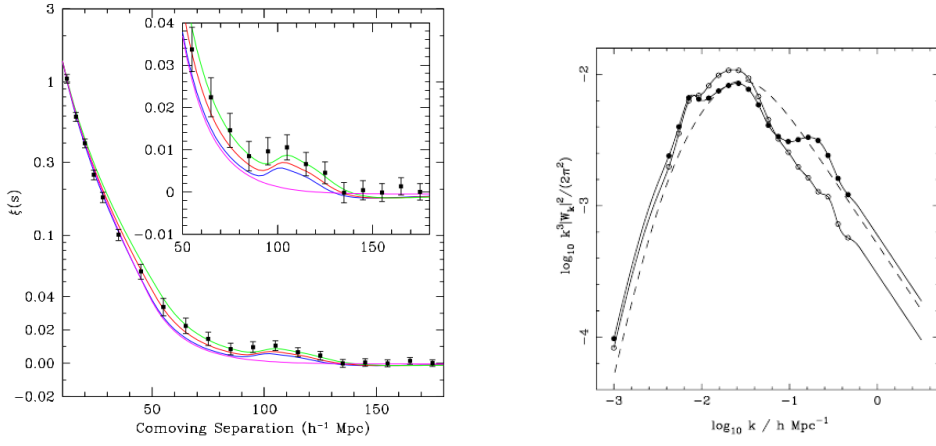


Figure 1.3: The first observations of the Baryon Acoustic Oscillations phenomenon, observed independently by the Sloan Digital Sky Survey (SDSS) [4] as seen in the left panel and the 2dF collaboration [5] in the right panel. These were the main tools that finally determined the existence of the BAO. The SDSS result shows the measured correlation function $\xi(s)$. This function represents the distribution of the distance in between galaxies. Note the similarity between this graph and the frozen BAO from the figure 1.2. The local maximum at $s \approx 100 \text{ h}^{-1} \text{ Mpc}$ corresponds to the BAO peak. The 2dF result, seen in the rightmost panel is the measured power spectrum $P(k)$ (here called $W(k)$, which is the Fourier transform of the $\xi(r)$ function.

gravitational effects. Therefore, it has a constant comoving⁵ size throughout the universe.

These structures were observed for the first time in 2005 simultaneously both by the 2dF Galaxy Redshift Survey[5] and the Sloan Digital Sky Survey[4], the results of which can be seen in the figure 1.3. In these pictures one sees the correlation function $\xi(s)$ and the power spectrum $P(k)$ (though in the figure 1.3 it is called W_k). The correlation function $\xi(r)$, with r being a distance variable measures the frequency of the separation distance between any two galaxies. If the BAO hypothesis is true, then one would find a local maximum at r_d , the radius of the frozen spherical waves, which can be seen. These will be the main tools for the study of the BAO, and will be more precisely explained in the chapter 3.

The other tool for studying the BAO is the power spectrum seen in the right panel of the figure 1.3. It is, without need of more detail, the Fourier transform of the $\xi(s)$ function. Indeed, since there is a repeating pattern of wavelength r_d , one would find local maxima in the spectrum at integer multiples of $k = 2\pi/r_d$.

⁵‘Comoving’ meaning the distance one would measure had the expansion of the universe not existed

1.4. CURVATURE, DARK MATTER AND THE EXPANSION OF THE UNIVERSE

After Hubble discovered the expansion of the universe through Hubble's Law[6]

$$v = H_0 d \quad (1.2)$$

With v the recession speed (the speed at which some point in space is receding only considering the expansion of the universe), $H_0 = 100h \text{ km s}^{-1} \text{ Mpc}^{-1}$ Hubble's constant, h a factor that parametrizes our ignorance on the true value of H_0 (estimated to be around 0.67), and d the distance of said point, a great deal of studies concerning the expansion of the universe started. The most relevant result of those for this report are Friedmann's equations

$$H^2(t) := \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G\rho}{3} + \frac{\Lambda c^2}{3} - k\frac{c^2}{a^2} \quad (1.3)$$

$$3\frac{\ddot{a}}{a} = \Lambda c^2 - 4\pi G \left(\rho + \frac{3p}{c^2}\right) \quad (1.4)$$

In these equations we see many new parameters: $H(t)$ is a generalization of H_0 , H_0 being the value of $H(t)$ at $t = t_0$ where t_0 is the age of the universe; $a(t)$ is the scale factor of the universe, meaning that if a certain length measurement Δx was taken at time t_1 , then that same measurement would be $\frac{a(t_2)}{a(t_1)}\Delta x$ at t_2 ; G is the Newton's gravitational constant, ρ the density of the universe (including baryonic, dark matter, radiation and neutrinos)⁶, Λ is the cosmological constant which contains information about Dark Energy. Finally we see k , which is the spatial (Gaussian) curvature of the universe. This is, asymptotical curvature.

These equations are a result of the Friedmann–Lemaître–Robertson–Walker metric

$$ds^2 = -c^2 dt^2 + a^2(t) \left(\frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right) \quad (1.5)$$

which are a direct result of solutions to Einstein's field equations of General Relativity, which will not be covered in this work. In (1.5) one sees the usual components in a flat space Minkowskian metric

$$ds^2 = -c^2 dt^2 + dr^2 + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \quad (1.6)$$

and some new terms, $a(t)$ and k . $a(t)$ is the aforementioned scale factor, and k a measure of the curvature of the universe. It is easier now to see that $a(t)$ is crucial in the way lengths are measured, being an overall factor in the spatial part that is homogenous but time-dependent. One can also notice how having different types of universe affects differently to the metric. For example $k = 0$ yields (as one would expect from a curvature parameter) a flat universe. $k > 0$ corresponds to a universe with spherical geometry and $k < 0$ to a universe of hyperbolical geometry.

⁶In this work, we will only be worried about baryonic and dark matter.

If one managed to solve the differential equations in (1.3), the result would be $a(t)$, a description of the history of the expansion of the universe. Moreover, it is also important to notice the relationship between the expansion of the universe and the distribution of matter in the universe.

From (1.3) we define the density parameter Ω_m as $\frac{\rho}{\rho_c}$, with the critical density $\rho_c = \frac{3H_0^2}{8\pi G}$, which represents the transition point (for a universe without cosmological constant) between an ever expanding universe with negative curvature (open universe) and a collapsing universe with positive curvature (closed universe). Similarly from the rest of the terms in the equation (1.3)

$$\Omega_\Lambda = \frac{\Lambda c^2}{3H^2}, \Omega_k = -\frac{kc^2}{H^2 a^2} \quad (1.7)$$

Ω_Λ corresponds to the density of dark energy in the universe, while Ω_k is not a density *per se*, but is related to the total energy content of the universe, determining its curvature. These parameters are what define the certain cosmology we are using, and obey the cosmic sum rule

$$1 = \Omega_m + \Omega_\Lambda + \Omega_k \quad (1.8)$$

Which is just a result of dividing (1.3) evaluated at present time, by H_0^2 .

Historically, the concept of cosmological expansion appeared when Hubble observed that the radiation of the nearby galaxies was all shifted towards the red end of the spectrum. Of course, since the universe is expanding and the distance between two points increases with time, the wave length of a certain radiation would also be affected by this expansion. This stretching of the wave length is what is known as *redshift*

$$z = \frac{\lambda_o - \lambda_e}{\lambda_e} = \frac{\lambda_o}{\lambda_e} - 1 \quad (1.9)$$

Being λ_o the observed wavelength and λ_e the emitted wavelength of the considered radiation. z is a measure of how much the universe stretched while the radiation travelled, and it can be related to $a(t)$ through

$$\frac{\lambda_o}{\lambda_e} = 1 + z = \frac{a(t_o)}{a(t_e)} \quad (1.10)$$

Which means that z is an (adimensional) temporal variable that admits an interpretation as a temporal variable.

However, this redshift z should not be confused with the redshift caused by the Doppler Effect of objects moving away. The processes are different in origin, since cosmological redshift does not need relative movement to shift the radiation towards red wavelengths, it is the expansion of the universe what stretches the wavelength. On the contrary, the Doppler Effect appears when pulses emitted at regular time are emitted further away due to the movement of the wave source.

We thus define the comoving distance $\Delta x'$ of a measurement Δx as

$$\Delta x' = \frac{\Delta x}{a(t)} = (1 + z)\Delta x \quad (1.11)$$

i.e. the distance one would have measured had the expansion of the universe not existed.

With these definitions we can define the observables we are interested in calculating/measuring. Firstly, through (1.3) we calculate $H(z)$ as

$$H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_k(1+z)^2 + \Omega_\Lambda} \quad (1.12)$$

We also define the function of z $D_H(z)$ known as the Hubble distance

$$D_H(z) = \frac{c}{H(z)} \quad (1.13)$$

Note that for $z = 0$ D_H gives us an idea of the distance at which the recession speed is greater than the speed of light in the vacuum, which is a direct consequence of (1.2). D_H can also be used to estimate the order of magnitude of the observable universe.

Through the Hubble distance we define the comoving distance

$$D_C(z) = \frac{c}{H_0} \int_0^z \frac{dz'}{\sqrt{\Omega_m(1+z')^3 + \Omega_k(1+z')^2 + \Omega_\Lambda}} \quad (1.14)$$

From this expression one defines the angular diameter distance for some redshift z

$$D_M(z) = \begin{cases} \frac{D_H}{\sqrt{\Omega_k}} \sinh \left[\sqrt{\Omega_k} D_C / D_H \right] & \Omega_k > 0 \\ D_C & \Omega_k = 0 \\ \frac{D_H}{\sqrt{|\Omega_k|}} \sin \left[\sqrt{|\Omega_k|} D_C / D_H \right] & \Omega_k < 0 \end{cases} \quad (1.15)$$

And for completeness, the comoving angular diameter distance $D_A(z) = \frac{D_M(z)}{1+z}$.

1.5. Λ COLD DARK MATTER MODEL

In the definitions in (1.7) the parameters Ω were introduced. This definitions, plus the definition of the density parameter Ω_m are part of the set of parameters that form the Λ Cold Dark Matter (Λ CDM) model.

This model is the simplest available way of explaining the current state of the universe, with six different constants. The name is derived from two of the biggest components of the universe, Λ (the cosmological constant, related to Dark Energy) and Cold Dark Matter, which is thought to be

- **Cold:** Non relativistic ($v \ll c$)
- **Non baryonic:** Made up of non baryonic matter i.e. anything other than protons and neutrons (and by convention, electrons).
- **Disipationless:** Since Dark Matter does not interact with the electromagnetic field, it can not dissipate temperature through photon emission.
- **Collisionless:** Dark matter particles can only interact through gravity and possibly, the weak force and so they do not collide with one another.

Parameter	Fiducial Value
Ω_b	0.0481
Ω_c	0.2604
H_0	67.6 km s ⁻¹ Mpc ⁻¹
τ_{reio}	0.09
A_s	$2.04031526769 \times 10^{-9}$
n_s	0.97
Ω_k	[-0.20 , +0.20]
r_d	147.784 Mpc
D_H/r_d	18.7
D_M/r_d	18.3
Ω_Λ	[0.49, 0.89]

Table 1.1: Fiducial cosmological parameter values used in the BAO analysis and values for the ‘derived’ values r_d , D_H/r_d , D_M/r_d .

The information on this cold dark matter is inside Ω_m , since the density ρ in

$$\Omega_m = \frac{\rho}{\rho_c} = \frac{\rho_b + \rho_{\text{CDM}}}{\rho_c} \quad (1.16)$$

Allowing us to define two new adimensional density parameters $\Omega_b = \frac{\rho_b}{\rho_c}$ and $\Omega_c = \frac{\rho_{\text{CDM}}}{\rho_c}$, which are part of the six free parameters that define a certain cosmology. These are Ω_b , Ω_c , H_0 , the optical density of reionization τ_{reio} , the amplitude of the primordial power spectrum A_s , the spectral index of the primordial power spectrum n_s . Note there is no special choice of parameters, these are just the free parameters chosen for this work. The values for the chosen free parameters are seen in the table 1.1

In this work, an extension of the Λ CDM model is considered. Though the standard cosmological model considers a flat universe, the curvature parameter will not be fixed to 0 and is therefore allowed to be a free parameter, adding a new degree of freedom to the standard model (not to be confused with the standard model in particle physics). This model can be further extended by considering the mass of the neutrinos, the quintaessential force (dark energy)...

The fiducial (starting) values of these parameters that will be used in this work are And Ω_k that will vary between -0.2 and 0.2 . From these free parameters, one derives some parameters. Of those, the main interest is in Ω_Λ , r_d , D_H , and D_A . Ω_Λ changes with Ω_k for a fixed Ω_m by the cosmic sum rule (1.8)

$$\Omega_\Lambda = 1 - \Omega_m - \Omega_k \quad (1.17)$$

Thus Ω_Λ varies between 0.49 and 0.89.

Finally, we define two more parameters α_\parallel and α_\perp . These parameters measure the distortion of the measurements in two different directions. α_\parallel is related to the distortion

parallel to the line of sight, and α_{\perp} , perpendicular to the line of sight. They are defined by

$$\alpha_{\parallel} = \frac{[D_H(z)/r_d]}{[D_H(z)/r_d]^{\text{fid}}}, \alpha_{\perp} = \frac{[D_A(z)/r_d]}{[D_A(z)/r_d]^{\text{fid}}} \quad (1.18)$$

With z being the redshift at which the measurements were taken.

CHAPTER 2

Objectives

The general objective of this final degree work is to study the behavior of baryon acoustic oscillation (BAO) observables, namely the sound horizon distance r_s , the Hubble parameter distance D_H , and the angular diameter distance D_A , as a function of the curvature parameter Ω_k . To achieve this objective, the following specific objectives are proposed:

1. Review the theoretical background of BAO observables, including their physical origin and mathematical formulation, and become familiar with the software tools Rustico, BRASS, and Python for data analysis and visualization.
2. Learn to use these software tools for data preprocessing, analysis, and visualization of BAO-related cosmological data sets, particularly those related to the curvature parameter Ω_k .
3. Investigate the impact of different values of Ω_k on the behavior of BAO observables.
4. Analyze the most recent observational data on BAO observables, obtained from experiments such as SDSS, BOSS, and eBOSS, and compare the results with theoretical predictions for different values of Ω_k .
5. Make use of high performance computing to solve Physics problems.
6. Specific data analysis software development.
7. Learn to control computer clusters via SSH(Secure Shell).

Together, these objectives will provide a comprehensive understanding of the behavior of BAO observables for different values of Ω_k , and their role in constraining the curvature parameter and other cosmological parameters.

CHAPTER 3

Methods and materials.

For this work, many different tools were used, which will be categorized in hardware, software and mathematical tools.

In terms of hardware, the author was granted access to the computer facilities of the *FQM-378* research group of the Universidad de Córdoba. Access to these clusters was crucial for the calculations done throughout the work, reducing the time needed for each calculation in several orders of magnitude. Besides the clusters, the author also needed his own personal computer, mainly to remotely access the clusters and also for other types of calculations that could not have been done from the clusters. These calculations include among other things, plotting of figures.

The main mathematical tool for this work was the Fourier Transform [7]. The Fourier Transform is a consequence of Fourier's Theorem. This theorem states that for every 'nice'¹ periodic function $f(x)$ of period L one can find a unique linear combination of sine and cosine functions such that

$$f(x) = C + \sum_{n \text{ odd}} a_n \sin\left(\frac{nx}{L}\right) + \sum_{n \text{ even}} b_n \cos\left(\frac{nx}{L}\right) \quad (3.1)$$

With C , a_n , b_n given by²

$$\begin{cases} C &= \frac{1}{L} \int_L f(x) dx \\ a_n &= \frac{1}{L} \int_L f(x) \sin\left(2\pi \frac{nx}{L}\right) dx, \text{ n odd} \\ b_n &= \frac{1}{L} \int_L f(x) \cos\left(2\pi \frac{nx}{L}\right) dx, \text{ n even} \end{cases} \quad (3.2)$$

¹The conditions for which this theorem does not apply are beyond the scope of this work, and so the 'niceness' of a function need not be defined

²The subscript in \int_L only implies the integration over the length L , since it can be proven that any periodic function $f(x)$ with period L verifies $\int_0^L f(x) dx = \int_a^{L+a} f(x) dx$ for any value of a . This is, the point at which the integral begins makes no difference, as long as the integration is done over a whole period.

This was the original Fourier's result. However this theorem can be expanded to the complex realm as

$$f(x) = \sum_{n=0}^{\infty} c_n e^{i2\pi \frac{nx}{L}}, \text{ with } c_n = \frac{1}{L} \int_L f(x) e^{-i2\pi \frac{nx}{L}} dx \quad (3.3)$$

For each mode n one can define a new variable $k = 2\pi n/L$, leading to the actual definition of the Fourier Transform

$$\tilde{f}(k) = \frac{1}{2\pi} \int_L f(x) e^{-ikx} dx \quad (3.4)$$

In this work, the power spectrum $P(\mathbf{k})$ is considered, which is the Fourier Transform of the correlation function $\xi(\mathbf{r})$. This function, as was already mentioned in section 1.3 is the distribution of the distances at which galaxies are found to be distant of one another. Since the amount of galaxies present is finite, the data set must then be discrete. This motivates us towards the definition of the Discrete Fourier Transform of a certain data set $\{(x_i, \xi(x_i))\}_{i=1}^N$

$$P(k_j) = \frac{1}{2\pi} \sum_{i=1}^N e^{-ik_j x_i} \xi(x_i) \quad (3.5)$$

Though one must think that the periodic function hypothesis is being broken, since of course the universe is not made of repeating blocks of the galaxies that surround us. That the universe is infinitely big and repeating is an assumption that needs to be done in order to calculate this Fourier Transform. In other words, these calculations assume periodic boundary conditions.

Another thing to be noted is the fast growing complexity of the algorithm described by (3.5), which grows as N^2 , with N the number of points used for the calculation. To solve this one would use the Fast Fourier Transform (FFT) [7], instead of the Discrete Fourier Transform. This algorithm is based in the decomposition of the space considered with $N = N_1 N_2$ data points, into two smaller spaces with N_1 and N_2 data points. It then factorizes each problem into smaller problems, and recursively breaks the configuration down into even smaller problems, thus greatly reducing the complexity of the algorithm from N^2 to $N \log N$.

The $P(\mathbf{k})$ has been until now only been vaguely defined. Let $\rho(\mathbf{x})$ determine the density of galaxies at a given point and $\bar{\rho}$ the average density throughout the universe. As the interest lays in the fluctuations around the density, it is only natural to be interested in the overdensity $\delta(\mathbf{x})$ at some position \mathbf{x}

$$\delta(\mathbf{x}) = \frac{\rho(\mathbf{x}) - \bar{\rho}}{\bar{\rho}} \quad (3.6)$$

From this magnitude one calculates the aforementioned correlation function $\xi(\mathbf{r})$ as³

$$\xi(\mathbf{r}) = \langle \delta(\mathbf{x}) \delta(\mathbf{x}') \rangle = \frac{1}{V} \int_V d^3 \mathbf{x} \delta(\mathbf{x}) \delta(\mathbf{x} - \mathbf{r}) \quad (3.7)$$

³Note only the dependency on $r = \|\mathbf{r}\|$ remains, since the universe is (assumed to be) homogenous and isotropic

with $\mathbf{r} = \mathbf{x} - \mathbf{x}'$. And the power spectrum is then defined as its three dimensional Fourier Transform.

To calculate $P(\mathbf{k})$ one then needs three coordinates for each galaxy (as would be expected from a three dimensional universe). These coordinates will be 2 angular coordinates (the astronomical coordinates declination δ and right ascension α) and a radial coordinate r which must be calculated from z . For this it is necessary to assume a cosmology, since it is what dictates the conversion from redshift to distance through Hubble's law (1.2). For this transformation, the redshift is interpreted as a Doppler shift. At low enough velocities, $z \approx v/c$ and so (1.2) can be approximated to

$$cz = H_0 r \quad (3.8)$$

The last step to calculate the power spectrum is to interpolate in between each galaxy, similar to how one would build a heatmap. This way the catalogue is continuous and no longer discrete. Now, with a continuous density function $\rho(\mathbf{x})$ all necessities for the power spectrum are met and it can be finally calculated.

All these magnitudes are related to what is called the second moment of the overdensity. In general, the n th moment μ_n of some magnitude x with a probability distribution $P(x)$ is defined as

$$\mu_n = \int_{-\infty}^{\infty} x^n P(x) dx \quad (3.9)$$

Though this is done only in one dimension, the definition of the n th moment of a magnitude x is easily extended to more dimensions. It should be natural to ask why is only the second moment of the overdensity δ considered.⁴ It has been measured in the CMB that the universe is a gaussian field, and these kinds of fields have the property that any moment μ_n with $n \geq 3$ will be 0. These moments (e.g. $\langle \delta(\mathbf{x})\delta(\mathbf{y})\delta(\mathbf{z}) \rangle$) have been shown to all be compatible with 0. This is predicted by the inflation theory, but the strongest reason to believe this is the experimental data.

All these calculations are performed by Rapid foUrier STatIstics COde⁵(RUSTICO). This software needs the specific galaxy catalogue to be used, and the statement of the cosmology that is going to be used, in a similar fashion as was done in 1.5. The catalogue to be used in this work is the Luminous Red Galaxy sample from the extended Baryon Oscillation Spectroscopic Survey (LRG eBOSS [8]). With this information it then takes the mentioned steps: Transforms each redshift z to a radial distance r , assigns each galaxy to a point \mathbf{x} , calculates through interpolation the galaxy density at each point $\rho(\mathbf{x})$, the overdensity at each point $\delta(\mathbf{x})$, the correlation function $\xi(\mathbf{r})$ and finally its FFT to obtain the power spectrum $P(\mathbf{k})$, as seen in the figure 3.1.

Having the data, it is then necessary to have a model that explains it. The Cosmic Linear Anisotropy Solving System⁶(CLASS) library allows the user to calculate the theoretical curve $P(k)$ should have for each cosmology. This software takes the corresponding cosmology as an input and returns the power spectrum seen in the leftmost panel of the

⁴The dependency on \mathbf{x} was dropped since δ can be both spoken of in configuration space and momentum (Fourier) space. These representations correspond to the $\xi(\mathbf{r})$ and $P(\mathbf{k})$ functions, respectively.

⁵Gil-Marín, H. <https://github.com/hectorgil/rustico>

⁶Lesgourgues, J., Tram, T., & Schoenenberg, N. https://github.com/lesgourg/class_public

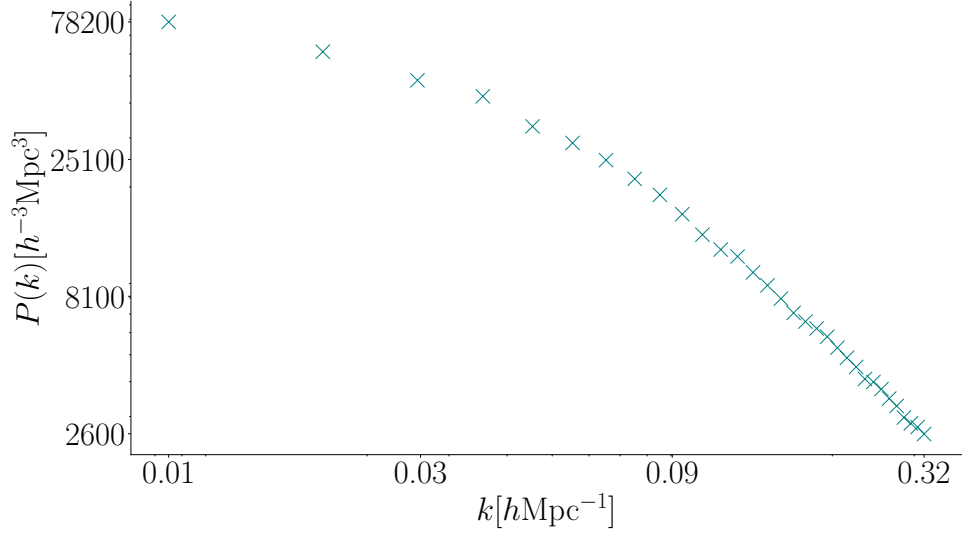


Figure 3.1: The power spectrum $P(k)$ of the LRG eBOSS [8] catalogue as calculated by RUSTICO assuming a flat universe ($\Omega_k = 0.00$)

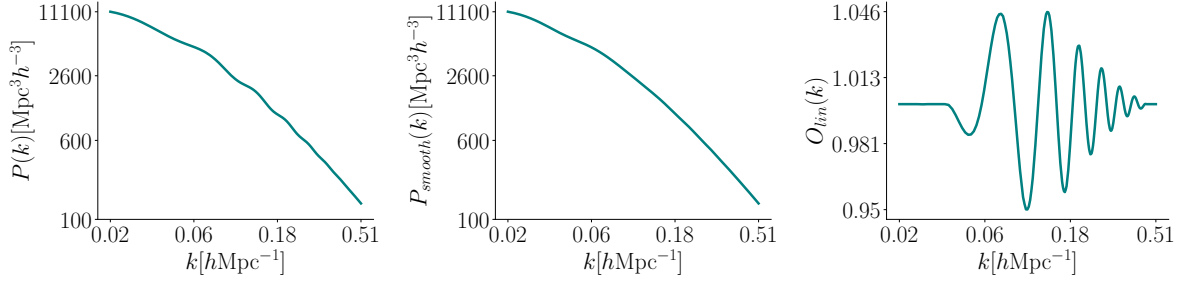


Figure 3.2: Graphic representation of the power spectrum $P(k)$ as calculated by CLASS (left panel), the smoothed power spectrum $P_{smooth}(k)$ (middle panel) and the oscillations $O_{lin}(k)$ (right panel) for a flat universe $\Omega_k = 0.00$.

figure 3.2. Note that this curve looks like a decreasing function which will be named $P_{smooth}(k)$, modulated by an oscillating curve, named $O_{lin}(k)$. These two functions are seen in the middle and rightmost panels respectively, of the figure 3.2, and verify

$$P(k) = P_{smooth}(k)O_{lin}(k) \quad (3.10)$$

To split the power spectrum $P(k)$ into these two functions, the routine `remove_bao` from the Montepython project ⁷ has been used. This routine takes as input the power spectrum $P(k)$ as an array of points. It then computes the geometrical curvature of the curve and interpolates in between the points at which the calculated curvature results in 0. The output of this function is the smoothed power spectrum $P_{smooth}(k)$. By the definition (3.10), the pure BAO $O_{lin}(k)$ are calculated through

$$O_{lin}(k) = \frac{P(k)}{P_{smooth}(k)} \quad (3.11)$$

⁷Brinckmann T. https://github.com/brinckmann/montepython_public

The relationship between the data and the model is analyzed through the Bao and RSD Algorithm for Spectroscopy Surveys ⁸(BRASS). This software allows for the calculation of the α parameters, as defined by (1.18). BRASS takes as input the calculated power spectrum (given by RUSTICO) for some fiducial cosmology, and the theoretic power spectrum for some other fiducial cosmology. It returns, among many other fit parameters, the α_{\parallel} and α_{\perp} parameters along with their standard deviations that will allow the calculation of the observables D_H/r_s and D_A/r_s . A graphic scheme of the procedure followed throughout this work can be seen in the figure 3.3 and it can be summarized as follows:

1. Starting from a certain galaxy catalogue (in this case, the extended Baryon Oscillation Spectroscopic Survey (eBOSS)). This catalogue consists on the astronomical coordinates declination δ and right ascension α of each galaxy and their measured redshift z .
2. To transform each z into a radial distance assume a fiducial cosmology $(\Omega_m, \Omega_{\Lambda}, \Omega_k) = (0.31, 0.69 - \Omega_k, \Omega_k)$. This assumption automatically sets the fiducial values

$$\left[\frac{D_H}{r_d} \right]^{\text{fid}}, \left[\frac{D_M}{r_d} \right]^{\text{fid}} \quad (3.12)$$

Through the definitions (1.13) and (1.15).

3. Having the distance from Earth to the galaxies r , and their angular coordinates (δ, α) , their position can be calculated. Knowing the positions we now have a discrete distribution $\rho(\mathbf{x})$ of galaxies. This distribution is then smoothed out, and its overdensity $(??)$ calculated.
4. Knowing $\delta(\mathbf{x})$, calculate the correlation function $\xi(\mathbf{r})$ using (3.7).
5. From $\xi(\mathbf{r})$ calculate the power spectrum $P(\mathbf{k})$ through its FFT. The steps 3 to 5 are done by RUSTICO.
6. Generate a fiducial template using CLASS assuming a certain cosmology. In this case, a flat cosmology $(\Omega_m, \Omega_{\Lambda}, \Omega_k) = (0.31, 0.69, 0.00)$ that will stay constant for every iteration. Split it into its main components, $P_{\text{smooth}}(k)$ and $O_{\text{lin}}(k)$ using the *remove_bao* routine from montepython.
7. With the outputs from RUSTICO and CLASS, fit the CLASS template to the RUSTICO data using BRASS, obtaining the best-fit parameters α_{\parallel} and α_{\perp} and their corresponding standard deviations.
8. This allows us to obtain the measured observables

$$\frac{D_H}{r_d} = \alpha_{\parallel} \left[\frac{D_H}{r_d} \right]^{\text{fid}} \quad (3.13)$$

$$\frac{D_M}{r_d} = \alpha_{\perp} \left[\frac{D_M}{r_d} \right]^{\text{fid}} \quad (3.14)$$

$$(3.15)$$

And their corresponding standard deviations.

⁸Gil-Marín H. <https://github.com/hectorgil/brass>

All of these calculations were done thanks to the clusters to which I was granted access to in the *FQM-378* research group in the Universidad de Córdoba, which had the following specifications:

- 1 node, named Pauli,
- 40 threads for this node, *Intel(R) Xeon(R) Silver 4210R CPU @ 2.40GHz*,
- 64Gb of memory,
- The following Linux version: Ubuntu 22.04.2 LTS, release 22.04 with codename jammy.

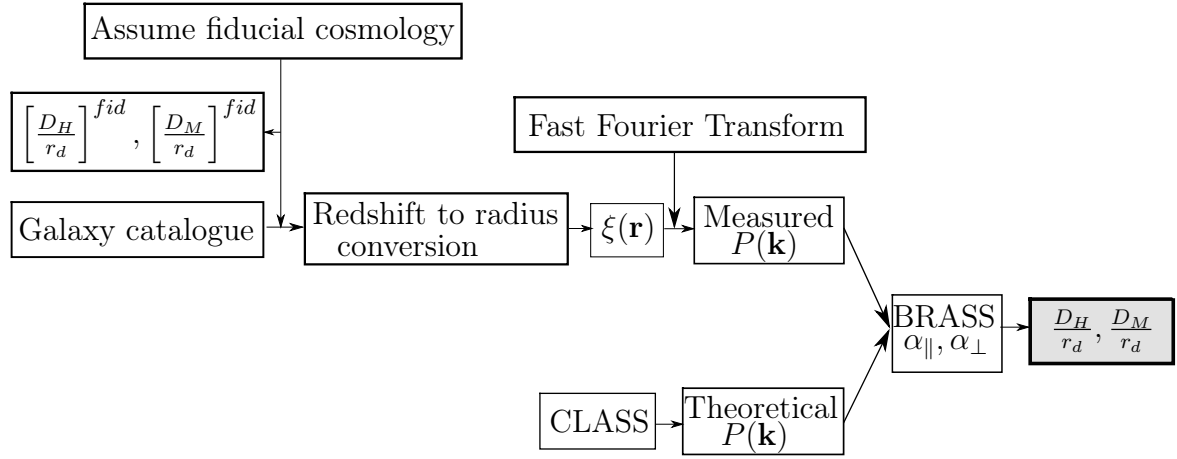


Figure 3.3: The BAO analysis pipeline scheme that was followed throughout this work, that was described along this chapter.

CHAPTER 4

Results

Using the tools mentioned in chapter 3, we obtain the data seen in the table 4.1. Firstly, a template power spectrum $P(k)$ was generated using CLASS. This template stays fixed throughout the calculations, to that of the standard cosmological model. This is, with the six parameters stated in 1.5 and $\Omega_k = 0.00$. Having the template, the BAO are removed using the *remove_bao* routine from montepython, to obtain exactly the plots seen in 3.2.

For this fixed template, nine different power spectrums were calculated using RUSTICO. We again use the Λ CDM, but this time not assuming a flat universe. Each power spectrum is generated with Ω_k varying from -0.20 to 0.20, in steps of 0.05, thus yielding the mentioned 9 different power spectrums.

For each one of these Ω_k , the software BRASS was used to calculate each corresponding best fitting parameter in the line-of-sight (α_{\parallel}) and the transverse (α_{\perp}) directions, and its standard deviation. With the α values calculated, we now know the relation between the fiducial cosmological observables (this is, our initial guess) and the measured value of these observables. In other words, $\alpha = 1$ would correspond to the case in which the fiducial cosmology corresponded to the cosmology that better fit the data.

These α values can be seen in the figure 4.1, which presents the α_{\parallel} and α_{\perp} on the first row, the fiducial D_H/r_d , D_M/r_d on the second row and the measured D_H/r_d , D_M/r_d for each fiducial cosmology.

The BRASS calculations were done in an iterative way, which means the output from the software was used as the initial condition for the next iteration. To assure better results three iterations were made for each cosmology. Each iteration for each data point lasted about two hours, which means each data point needed approximately six hours and the whole data set needed a whole forty five hours of computation time.

Both the table 4.1 and the figure 4.1 show the results of the calculation of the different observables for different fiducial curvature parameters Ω_k . While the table allows us to grasp on the exact values for each measurement, the figure shows the very important tendency of the measurements. Note that the growing tendency of the α (both parallel and perpendicular) cancels the decreasing tendency of the $[D/r_d]$ and thus the measured

Ω_k	D_H/r_d	D_M/r_d
-0.20	19.57 ± 0.85	17.85 ± 0.51
-0.15	19.25 ± 0.84	17.85 ± 0.54
-0.10	19.00 ± 0.80	17.96 ± 0.59
-0.05	18.82 ± 0.77	18.13 ± 0.59
0.00	18.66 ± 0.72	18.28 ± 0.53
0.05	18.61 ± 0.65	18.25 ± 0.47
0.10	18.57 ± 0.61	18.24 ± 0.43
0.15	18.50 ± 0.56	18.23 ± 0.41
0.20	18.36 ± 0.53	18.34 ± 0.39

Table 4.1: Results of the measurement of the cosmological observables we were interested in. This table shows the same data as the figure [4.1](#).

observables stay approximately constant with changes in Ω_k . The most important result from these representations is that every measured observable stays within one standard deviation from one another, resulting in compatible results for changes of Ω_k in the range $[-0.20, 0.20]$.

The observable values corresponding to our universe, $D_H/r_d = 18.68 \pm 0.72$ and $D_M/r_d = 18.13 \pm 0.58$ must be compared to previous experiments. We see these results are compatible with the bibliography [9]. The measurements ($D_H/r_d = 19.77 \pm 0.47$ and $D_M/r_d = 17.65 \pm 0.30$) in the mentioned article are done through different methods, and represent the most precise measurements for the redshift range of the SDSS surveys as of 2020.

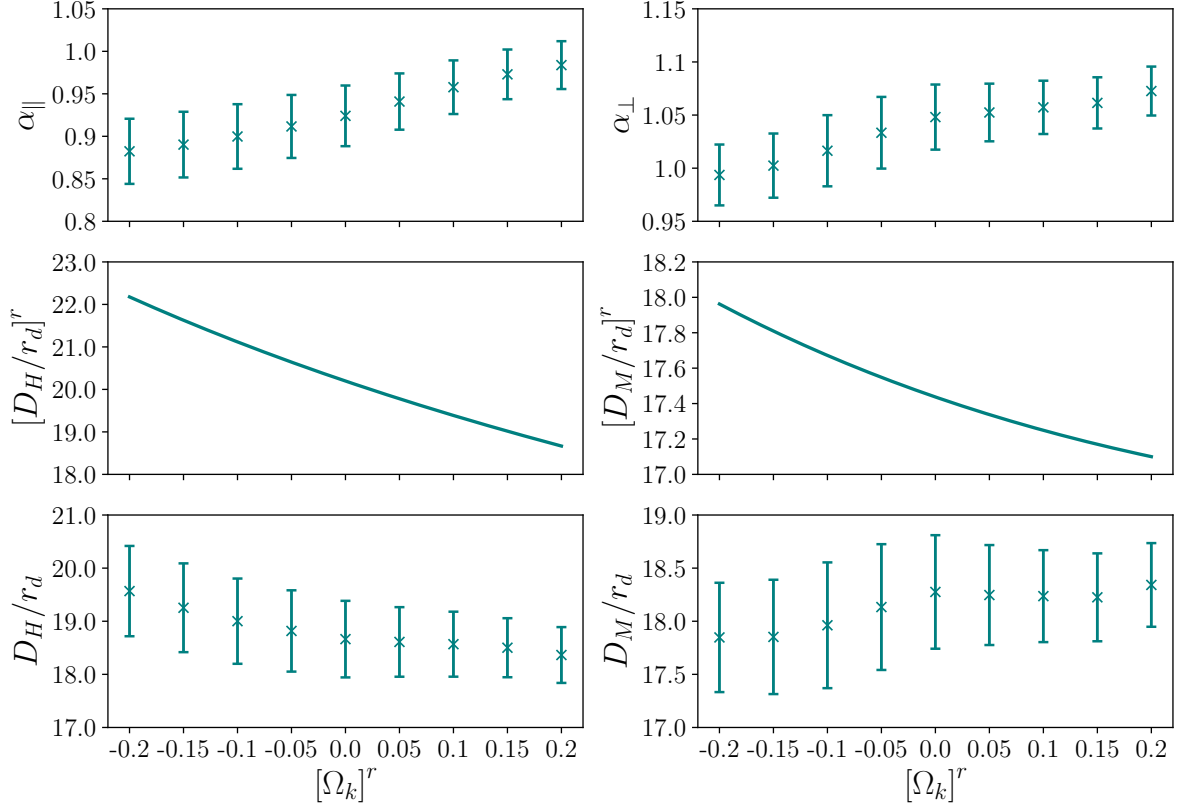


Figure 4.1: Results of the application of the BAO technique to eBOSS galaxies. Top panel: Best fit values and uncertainties on the shifts of the BAO feature in the distribution of galaxies along the line of sight (α_{\parallel}) and perpendicular to that direction (α_{\perp}) for different values of Ω_k . Middle panel: the fiducial distances (Hubble distance and angular diameter distance) as a function of Ω_k (with the matter parameter $\Omega_m = 0.31$, and the dark energy parameter $\Omega_{\Lambda} = 1 - \Omega_m - \Omega_k$, using the equations (1.13) and (1.15)) evaluated at the redshift of eBOSS galaxies. Bottom panel: Best fit values and uncertainties for the Hubble distance and angular diameter distance to eBOSS galaxies for different assumptions on the value of the curvature parameter Ω_k , computed as the product of the above two panels. The inferred distances for different values of Ω_k are consistent with each other within $1\text{-}\sigma$.

Conclusiones

En relación a los objetivos establecidos en el capítulo 2, y considerando los resultados obtenidos en el capítulo 4, se pueden extraer las siguientes conclusiones de este trabajo:

1. Hemos revisado e implementado la metodología de Oscilaciones Acústicas de Bariones (BAO, por sus siglas en inglés) para medir distancias cosmológicas en el Universo, y la hemos aplicado a una muestra de galaxias del Extended Baryon Oscillation Spectroscopic Survey (eBOSS).
2. Hemos utilizado software de cosmología avanzada como CLASS, RUSTICO y BRASS para desarrollar un pipeline que obtiene mediciones de distancia cosmológica de un catálogo de galaxias utilizando la técnica BAO.
3. Además, hemos desarrollado código utilizando la librería Matplotlib escrita en Python para generar visualizaciones de alta calidad de nuestros resultados.
4. Los ordenadores de alto rendimiento del grupo de investigación FQM-378 de la Universidad de Córdoba se han utilizado para calcular la Transformada Rápida de Fourier de la función de correlación de 2 puntos de las galaxias de eBOSS, y para determinar las posiciones de las características de BAO en el espectro de potencia, junto con sus incertidumbres.
5. Suponiendo un modelo cosmológico plano, nuestras mediciones de distancia inferidas a las galaxias de eBOSS (normalizadas a la escala del horizonte de sonido) son: $D_H/r_d = 18.68 \pm 0.72$ y $D_M/r_d = 18.13 \pm 0.58$ para la distancia angular, consistentes con trabajos previos [9].
6. Nuestro resultado principal es que no hay dependencia significativa de estas observables con respecto a cambios en el valor asumido del parámetro Ω_k en el rango de estudio.

Por lo tanto, concluimos que la suposición de un valor particular de Ω_k en la conversión de corrimiento al rojo a distancia no tiene ningún efecto significativo (al menos en el rango $\Omega_k \in [-0.20, +0.20]$) en las distancias cosmológicas inferidas a las galaxias de eBOSS utilizando la metodología BAO.

Conclusions

Relative to the objectives stated in the chapter 2, and seeing the results obtained in the chapter 4, the following conclusions can be made from this work.

1. We have reviewed and implemented the Baryon Acoustic Oscillation (BAO) methodology to measure cosmological distances in the Universe, and we have applied it to a sample of galaxies from the extended Baryon Oscillation Spectroscopic Survey (eBOSS)
2. We have used advanced cosmology software such as CLASS, RUSTICO and BRASS to develop a pipeline that obtains cosmological distance measurements of a galaxy catalogue using the BAO technique.
3. In addition, we have developed code using the Matplotlib library written in Python to generate quality level visualization of our results.
4. The high performance computers of the University of Cordoba FQM-378 research group have been used to calculate the Fast Fourier Transform of the 2-point correlation function of eBOSS galaxies, and to determine the positions of the BAO features in the power spectrum, together with their uncertainties.
5. Assuming a flat cosmological model, our inferred distance measurements to eBOSS galaxies (normalized to the sound horizon scale) are: $D_H/r_d = 18.68 \pm 0.72$ and $D_M/r_d = 18.13 \pm 0.58$ for the angular diameter distance, consistent with previous works [9].
6. Our main result is that there is no significant dependence of these observables with respect to changes in the assumed value of the Ω_k parameter in the range of study.

Therefore, we conclude that the assumption of a particular Ω_k value in the redshift-to-distance conversion does not have any significant effect (at least in the range $\Omega_k \in [-0, 20, +0, 20]$) on the inferred cosmological distances to eBOSS galaxies using the BAO methodology.

Bibliography

- [1] Planck Collaboration. (2018). Planck 2018 results. VI. Cosmological parameters. *Astronomy & Astrophysics*, 641, A6. <https://doi.org/10.1051/0004-6361/201833910>
- [2] Penzias, A. A., & Wilson, R. W. (1965). A Measurement of Excess Antenna Temperature at 4080 Mc/s. *The Astrophysical Journal*, 142, 419. <https://doi.org/10.1086/148307>
- [3] Smoot, G. F., & Mather, J. C. (1992). Structure in the COBE differential microwave radiometer first-year maps. *The Astrophysical Journal*, 396, L1-L5. <https://doi.org/10.1086/186504>
- [4] Eisenstein, D. J., et al. (The SDSS Collaboration) (2005). Detection of the Baryon Acoustic Peak in the Large-Scale Correlation Function of SDSS Luminous Red Galaxies. *The Astrophysical Journal*, 633, 560-574. <https://doi.org/10.1086/466512>
- [5] Cole, S., et al. (The 2dFGRS Collaboration) (2005). The 2dF Galaxy Redshift Survey: power-spectrum analysis of the final dataset and cosmological implications. *Monthly Notices of the Royal Astronomical Society*, 362, 505-534. <https://doi.org/10.1111/j.1365-2966.2005.09318.x>
- [6] Hubble, E. (1929). A relation between distance and radial velocity among extragalactic nebulae. *Proceedings of the National Academy of Sciences*, 15(3), 168-173. <https://doi.org/10.1073/pnas.15.3.168>
- [7] D. H. Bailey and P. N. Swarztrauber, “A Fast Method for the Numerical Evaluation of Continuous Fourier and Laplace Transforms,” *SIAM Journal on Scientific Computing*, vol. 15, no. 5, pp. 1105-1110, 1994. <https://doi.org/10.1137/0915067>
- [8] S. Alam *et al.* [eBOSS], Phys. Rev. D **103**, no.8, 083533 (2021) doi:10.1103/PhysRevD.103.083533 [arXiv:2007.08991 [astro-ph.CO]].
- [9] Héctor Gil-Marín, et al. The Completed SDSS-IV extended Baryon Oscillation Spectroscopic Survey: measurement of the BAO and growth rate of structure of the luminous red galaxy sample from the anisotropic power spectrum between redshifts 0.6 and 1.0. *Monthly Notices of the Royal Astronomical Society*, 498(2):2492–2531, Aug. 2020. URL: <https://arxiv.org/abs/2007.08994>

Anexo: Example of data visualisation code with python & matplotlib

```
1 import matplotlib.pyplot as plt
2 import numpy as np
3 from pathfix import Path
4
5
6 #CLASS output that was spaced linearly and with the BAO removed.
7 #The power spectrum. *pk*069* is a regex to identify the data
8 #we are interested in.
9 pklin = Path('../linospace_class').glob('*pk*069*')
10 #The smoothed power spectrum
11 psmooth = Path('../linospace_class').glob('*psm*069*')
12 #The pure BAO
13 Olin = Path('../linospace_class').glob('*Olin*069*')
14
15
16 #Routine to read the data files used throughout this work
17 pklin, params = util_tools.many_files(list(pklin))
18 psmooth, params = util_tools.many_files(list(psmooth))
19 Olin, params = util_tools.many_files(list(Olin))
20
21 #Our k-region of interest
22 kmin, kmax = 0.02, 0.51
23
24 fontsize = 28 #Text fontsize
25
26 #Using for loop since there is code common to the three data sets
27 for i, data in enumerate([pklin[0], psmooth[0], Olin[0]]):
28     fig, ax = plt.subplots()
29     ax.spines['top'].set_visible(False)
30     ax.spines['right'].set_visible(False)
31     ax.set_xscale('log'), ax.set_yscale('log')
32     x, y = np.array(data[0]), np.array(data[1])
33     idx = np.where(np.logical_and(x<=kmax, x>=kmin))
34     x = x[idx]
35     y = y[idx]
36
37     ax.plot(x, y, color='teal', linewidth=3)
38
```



```

39 logx = np.log10(x)
40 logy = np.log10(y)
41 xticks = np.logspace(min(logx), max(logx), 4, base=10)
42 yticks = np.logspace(min(logy), max(logy), 4, base=10)
43
44 if i==0:
45     yticks = [int(x) for x in np.round(yticks, -2)]
46     ylabel = r'$ P(k) [Mpc$^3 h^{-3}]$'
47     name = 'Pklin' #The filename
48     print('First plot done!')
49 elif i==1:
50     yticks = [int(x) for x in np.round(yticks, -2)]
51     ylabel = r'$ P_{smooth}(k) [Mpc$^3 h^{-3}]$'
52     name = 'Psm'
53     print('Second plot done!')
54 elif i==2:
55     yticks = [x for x in np.round(yticks, 3)]
56     ylabel = r'$ O_{lin}(k)$'
57     name = 'Olin'
58     print('Third plot done!')
59
60 ax.set_xticks([], minor=True)
61 ax.set_xticks(xticks)
62 ax.set_xticklabels(np.round(xticks, 2), fontsize=fontsize)
63
64 ax.set_yticks([], minor=True)
65 ax.set_yticks(yticks)
66 ax.set_yticklabels(yticks, fontsize=fontsize)
67
68 ax.set_xlabel(r'$k [h Mpc$^{-1}] $', fontsize=fontsize)
69 ax.set_ylabel(ylabel, fontsize=fontsize)
70
71 fig.set_tight_layout(True)
72 plt.savefig(f'../figs/{name}.pdf')
73
74 plt.show()

```