VILNIAUS UNIVERSITETAS
MATEMATIKOS IR INFORMATIKOS FAKULTETAS
PROGRAMŲ SISTEMŲ STUDIJŲ PROGRAMA

Faktų paieška pagal šabloną TLA+ įrodymų sistemoje

Fact search by pattern in the TLA+ proof system

Kursinis darbas

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Terminai

- ATP (Automated theorem proving) - TODO
- Proof construction – įrodymo rašymas (ranka), i.e.: dalis nuo `Proof` iki `Qed`.
- Proof search – ta dalis, kur ATP atlieka automatiškai.
- Proof synthesis – ???
- Proof script – viskas nuo `Theorem` iki `Qed`.
- Sequent – In mathematical logic, a sequent is a very general kind of conditional assertion. pvz.: $A_1, ..., A_m \vdash B_1, ..., B_n$. [DEFINITION STOLEN FROM WIKI]

Įvadas

Traciškai programų sistemų modeliai aprašomi tekstu ir vizualinėmis diagramomis (UML) - šie yra sunkiai patikrinami automatiniai įrankiais. **[TODO]**.

Formalūs metodai (angl. *formal methods*) yra programinės įrangos kūrimo metodai, kurie naudoja matematine logika pagrįstus modelius, tam kad būtų galima analizuoti ir įrodyti programinės įrangos modelio savybes.

TLA^+ yra formaliais metodais pagrįsta modeliavimo sistema, kuria galima patikrinti sistemų modelių savybęs, siekiant užtikrinti jų teisingumą.

Sėkmingi atvejai:

- (AWS) ... [New+15]
- Safety-crictical systems:
  - TAS [RP17]
  - A train status alert system [Sal+20]
  - Avation systems [Das+24]

Čia nežinau, gal per mažai faktiška: IDEs padidina prieinanumą ir gali padidini TLA+ naudojamumą. (Todėl verta/relevant tobulinti TLA+ LSP)

Search engines [probably irrelevant]:

- Isabelle [HK22],
- Loogle for theorems in Lean

Background

Basically, šitai: „In this section, we describe the fundamental technologies for this paper. We describe the proof assistant Coq, giving an overview of how it works, as well as describe Visual Studio Code (VS Code), the Language Server Protocol (LSP), and the concept of code completion.“ bet skirtą šitam darbui.

TLA+

Čia trumpai apie TLA+

- TLA in Isabelle: [Mer99], [GM11]
- TLA checksheet
- The TLA+ Toolbox [KLR19]
  - This paper by Kuppe et al presents the technical architecture of the toolbox
  - Nalabai paaiškina kaip vekia pats TLAMP.

TLAMP

paaiškinti kas yra ir kaip veikia TLAPM / TLAPS.

- TLA+ Proofs [Cou+12]
  - „We describe how to write TLA+ proofs and check them with TLAPS, the TLA+ Proof System.“

Encoding

- „Proof automation and type synthesis for set theory in the context of TLA+“ [Van14]
  - „Chapter 4 presents the generic integration framework for automated theorem provers in TLAPS and its main component, the translation to unsorted and many-sorted first-order logics.“
  - iš [Van14]:

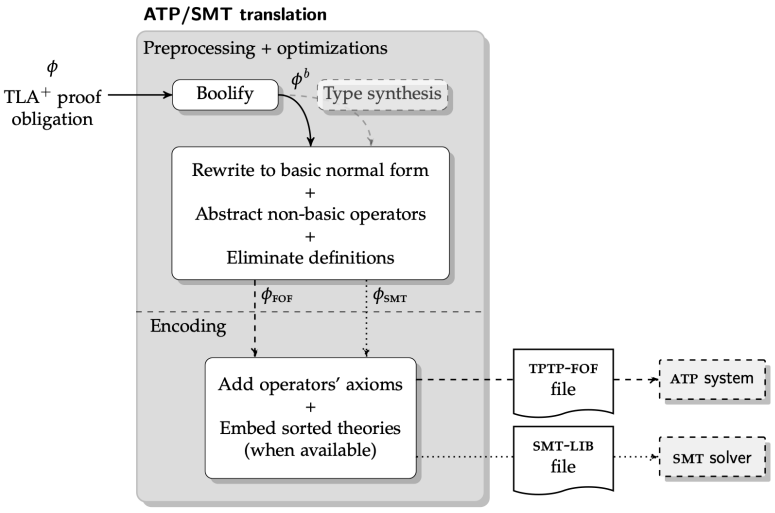

Figure 4.1: Schematic view of the translation from TLA$^+$ to the input languages of ATP and SMT solvers.

- „Encoding TLA$^+$'s Set Theory for Automated Theorem Provers“ [Def23]
  - Very lonk phd dissertation,
  - „In Chapter 4, we define a direct encoding of TLA+ into HOL. A higher-order logic is necessary to encode the second-order constructs of TLA+ and axiom schemas. For instance, set comprehension $\{x \in S : e\}$ is viewed as a second-order application setst(S, $\lambda x : e$), and the full schema of comprehension from ZF is encoded as a single axiom.“
- „Encoding TLA+ Proof Obligations Safely for SMT“ [Def25]
  - „To increase trust in TLAPS, we revisited the encoding of TLA+ for SMT, whose implementation had become too complex. Our approach is based on a first-order axiomatization with E-matching patterns. The new encoding is available with TLAPS and achieves performances similar to the previous version, despite its simpler design.“

Isabelle

The Isabelle/Isar Reference Manual

- TO READ: Automatic Proof and Disproof in Isabelle/HOL [BBN11]
- TO READ: Automatic verification of non-recursive algorithm of Hanoi Tower by using Isabelle Theorem Prover [XYX16]

Zenon

- Zenon: an Extensible Automated Theorem Prover Producing Checkable Proofs [BDD07]
  - „Zenon can directly generate Coq proofs (proof script or proof terms)“
  - „we present Zenon, an automated theorem prover for first or- der classical logic (with equality), based on the tableau method.“

Faktų paieška

Gal tinkami raktažodžiai: metaheuristic search, proof script synthesis, automated proof script synthesis

- Proof search engines:
  - TO READ: ProofCloud: A Proof Retrieval Engine for Verified Proofs in Higher Order Logic [Wan24]
  - `SErAPIS`

RocQ (Coq)

- 3110 Coq Tactics Cheatsheet

- „Expanding Coq With Type Aware Code Completion“ [DK23]
  - Kaip suprantu veikia tik su `rewrite` ir `apply` taktikomis: „For every file, at every location where the tactics apply and rewrite are used, request for a list of completion items.“
  - „Discovery is handled through the internal function that is also used by the Search command in Coq“
  - „For every file, at every location where the tactics `apply` and `rewrite` are used, request for a list of completion items.“
  - Realiai čia aprašo kaip geriausia sort'inti rezultatus, naudinga, bet čia pirma reikia turėti, ką sort'inti: „The only difference in how the algorithms are implemented is the sorting step.“
- TO READ: TacTok: semantics-aware proof synthesis [FBG20]
  - Machine learning

  - Gal turi gerų reference'ų: „Recent research has shown that the proof state can help predict the next step."
  - „In this paper, we present TacTok, the first technique that attempts to fully automate proof script synthesis by modeling proof scripts using both the partial proof script written thus far and the semantics of the proof state"
- TO READ: Coq search by type inhibition [Cza20a] [probably irrelevant]
- TO READ: PRoofster: Automated Formal Verification [Agr+23]
- TO READ: Coq `Search` komanda
- Hammer for Coq: Automation for dependent type theory [CK18]

  „This paper is the main reference for the hammer tactic."

  - „Practical proof search for Coq by type inhabitation" [Cza20b]

    „This paper is the main reference for the sauto tactic."

  - „A Shallow Embedding of Pure Type Systems into First-Order Logic" [Cza18]

    „This paper proves soundness of a core version of the translation used by the hammer tactic."
- Kiti Coq įrankiai:
  - CoqHammer
  - ASTactic [Irrelevant]
    – Machine learning based

      Jeigu kalbėsiu apie Rocq (dar žinomą kaip Coq) [Pau15]

Others

- Let AI/LLMs do it [Zho25] [outside the scope] Galimai naudinga:
  - „We present a novel approach to automated proof generation for the TLA+ Proof System (TLAPS) using Large Language Models (LLMs). Our method combines two key components: a sub-proof obligation generation phase that breaks down complex proof obligations into simpler sub-obligations, <...>"
- Isabelle/HOL `find_theorems`, `find_consts` komandos
- Pattern maching proofs in `Lean` & `Idris`.

Previous art/work

Dalykai, ant kurių galiu pagrįsti savo darbą.

Isabelle `find_theorems` ir `find_consts` komandos, kaip veikia Coq `Search` komanda. Kas ir kokie metodai iš kiekvieno buvo pasirinkti, paaiškinti kodėl pasirinkti.

Implementacija / kaip susijuniga su lsp ir TLAMP

Planas xuliganas:

vscode-lsp <-> tlamp_lsp <-> tlamp <-> Isabelle

Galutinis rezultatas, kaip veikia, kaip naudotis, kaip pritaikyti.

Pavyzdys

TLA+ pavyzdys, kuriame matosi kaip veikia faktų paieška.

Trūkumai

Rezultatai

Išvados

Notes

- **The E Theorem Prover (https://github.com/eprover/eprover/blob/master/DOC/E-3.1.html)**

  Kaip suprantu gan paprasta first-order logic theorem prover implementacija.

  1.2 versija turi ~157k C kodo eilučiu, tai tikriausiai ne tokia ir paprasta implementacija.

  Tikriausiai irrelevant

  - The CADE ATP System Competition (https://tptp.org/CASC/)
  - „E – a brainiac theorem prover“ [Sch02]

Šaltiniai

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Intelligence, and Reasoning, N. Dershowitz ir A. Voronkov, Sud., Berlin, Heidelberg: Springer Berlin Heidelberg, 2007, p. 151–165.

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