

VILNIAUS UNIVERSITETAS  
MATEMATIKOS IR INFORMATIKOS FAKULTETAS  
PROGRAMŲ SISTEMŲ STUDIJŲ PROGRAMA

**Hibridinio genetinio paieškos algoritmo transporto  
maršrutų optimizavimo uždaviniams spręsti  
lygiagretinimas**

**Parallelization of Hybrid Genetic Search Algorithm for Solving  
Vehicle Routing Problem**

Kursinis darbas

Atliko: 4 kurso 1 grupės studentas

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# Terminai

## Ivadas

paragrafas apie VRP relevance

### Plačiau apie VRP constraints

Galimi constraints, kuriuos galima uždėti ant VRP problemų:

- kiekviena transporto priemonė gali turėti (skirtingą) maršruto pradžios laiką
- kiekviena transporto priemonė gali turėti (skirtingą) maksimalų atstumą, kurį gali nukeliauti
- kiekviena transporto priemonė gali turėti (skirtingą) maksimalią talpą
- kiekvienos transporto priemonės vairuotojas gali turėti (skirtingą) tvarkaraštį (skirtingas pamainos laikas, su arba be pertraukų)
- kiekvienas taškas gali turėti (skirtingas) veikimo valandas (galimai su pietų pertraukom, etc...)
- kiekvienas taškas gali turėti (skirtingas) service time
- kiekvienas taškui gali būti arba nebūti griežtas reikalavimas jį aplankyti
- apmokėjimo constraints:
  - ▶ per tašką
  - ▶ per atstumą
  - ▶ etc...

## Metodai

- Matematinis modeliavimas (google or-tools)
- Heuristic – A problem-specific rule or method to quickly find a good (not necessarily optimal) solution. <https://chatgpt.com/share/68b3151a-85a8-800e-9cc6-3558041fe679>
- Metaheuristic – A higher-level strategy/framework that guides heuristics to explore solutions more effectively. <https://chatgpt.com/share/68b3151a-85a8-800e-9cc6-3558041fe679>
  - ▶ Adaptive Large Neighborhood Search
    - ▶  <https://reinterpretcat.github.io/vrp/>
    - ▶ Hybrid Adaptive Large Neighborhood Search
  - ▶ Hybrid Genetic Search (HGS)
    - ▶  <https://pyvrp.org/>

### Konkursai ir sprendimų/įrankių? palyginimai

- DIMACS [DIM22]
- the Amazon Last Mile Routing Research Challenge (Amazon last mile routing, 2021), where a specific problem was tackled, namely, the challenge of embedding driver knowledge into route optimisation;

## Įrankiai

- Matrix
  - ▶ OSMR
  - ▶ GraphHopper

- ▶ Valhalla
- ▶ BRouter
- Routing
  - ▶ <https://pgrouting.org/>
  - ▶ PyVRP
    - supports CVRP, VRPTW
  - ▶ RouteOpt
    - RouteOpt: An Open-Source Modular Exact Solver for Vehicle Routing Problems (2025)
- Simulation <https://roadsimulator3.fr/these/chapters/chapitre00.html>

Hibridinis genetinis paieškos (HGS) algoritmas yra vienas iš efektyviausių būdų spręsti transporto maršrutų optimizavimo uždavinius.

Pirma aprašytas "A Hybrid Genetic Algorithm for Multidepot and Periodic Vehicle Routing Problems" [Vid+12] (2012).

- **„HGSADC“.**

We propose a metaheuristic that combines the exploration breadth of population-based evolutionary search, the aggressive-improvement capabilities of neighborhood-based metaheuristics, and advanced population-diversity management schemes. The method that we name *Hybrid Genetic Search with Adaptive Diversity Control (HGSADC)*.

— Thibaut Vidal, Teodor Gabriel Crainic, Michel Gendreau, Nadia Lahrichi, Walter Rei  
[Vid+12]
- *HGSADC proves to be extremely competitive CVRP.*

— Thibaut Vidal, Teodor Gabriel Crainic, Michel Gendreau, Nadia Lahrichi, Walter Rei  
[Vid+12]
- maintains diversity in search -> avoids local minima ir dar aukštesnės kokybės sprendimai ir reduced computational time.

Esminis patogulinimas – [Vid22].

ivadas

## Tikslas ir uždaviniai

**Tikslas** – Išlygiagretinti hibridinio genetinio paieškos algoritmą, skirto transporto maršrutų optimizavimo uždaviniams spręsti.

**Uždavinai:**

1. Išsirinkti duomenų rinkinį pagal, kurį galima būtų testuoti/analizuoti sprendimus, pvz.:
  - Solomon
  - CVRPLIB repository (repository of BKSSs – Best Known Solutions)
  - Neural Combinatorial Optimization for Real-World Routing (2025)
  - Test-data generation and integration for long-distance e-vehicle routing (2023)
  - "New benchmark instances for the Capacitated Vehicle Routing Problem" [Uch+17] (2017)
2. Išanalizuoti, kaip veikia HGS algoritmas
3. Atrinkti paralelizujamas dalis, ar dalis, kurias galima pakeisti paralelizujamomis
3. Palyginti rezultatus su kitais state-of-the-art algoritmais

## Abbreviations

- VRP – Vechicle Routing Problem.
- **CVRP** – Capacitated Vehicle Routing Problem.
- VRPTW – VRP with Time Windows.
- MVRP – multidepot VRP
- PVRP – periodic VRP

*In classical VRPs, typically the planning period is a single day. In the case of the Period Vehicle Routing Problem (PVRP), the classical VRP is generalized by extending the planning period to  $M$  days.*

— <https://neo.lcc.uma.es/vrp/vrp-flavors/periodic-vrp/>

- MDVRP – multidepot periodic MDPVRP
- **CVRP with Backhauls**

## Matematinis formulavimas

TODO: matematikai aprašyti problemą ir siekiamą tikslą.

## Notes

- VRPTW  $\in$  CVRP
- Specializuota optimizacija specializuotam uždavinui  
"The vehicle routing problem with service level constraints" [Bul+18] (2018)

- depots and periods. A second general observation is that most methodological developments target a particular problem variant, the capacitated VRP (*CVRP*) or the VRP with time windows (*VRPTW*), for example, very few contributions aiming to address a broader set of problem settings.

## Literatūros apžvalgos

- "A Detailed Review of the Capacitated Vehicle Routing Problem: Model, Computational Complexity, Solutions, and Practical Applications" [Ham+25] (2025)  
tl;dr: aprašo logistikos problemų kriterijus ir tipus, tada šias priskiria tam tikriem VRP tipams (e.g. VRPPD, VRPTW, etc...)
- "A review of recent advances in time-dependent vehicle routing" [Ada+24] (2024)  
tl;dr: pagrinde pristato ir aprašo CVRP. Išskiria metodų grupes (tikslūs; apytikslūs - heuristiniai ir metaheuristiniai). Iš metaheuristinių algoritmų grupių išskiria tris grupes:
  - Evolutionary such as "Genetic Algorithm (GA)"*;
  - Physic - Based such as "Simulated Annealing Algorithm (SAA)"*; and
  - Swarm Intelligence like "Ant colony optimization (ACO)"*.

— Tommaso Adamo, Michel Gendreau, Gianpaolo Ghiani, Emanuela Guerriero [Ada+24]

pasirinkti ACO grįsti algoritmai ir palyginti tarpusavyje.
- "Operational Research: methods and applications" [Pet+23] (2023)  
tl;dr: apiebia visą *Operations Research* iš 200 psl. 2 skirta VRP. Pateikia įvairius naujus metaheuristinius algoritmus, išskiria HGS kaip vieną iš geresnių.

*An up-to-date survey on recent trends can be found in Vidal et al. (2020) [[VLM20]]*

*Clear standards have been set by the CVRP community around which benchmark instances should be used for testing the performance of an algorithm, and which are ways of testing a computer code for a fair comparison with other previously proposed algorithms. Uchoa et al. (2017) discuss the most widely used instances and provides a link to the repository, in which the input data, as well as the best known solutions, are provided and kept up-to-date by the authors. A more recent set of instances and best known solutions is available in Queiroga et al. (2022), where the authors provide data enabling the use of machine learning approaches to solve the CVRP. Accorsi et al. (2022) present the standard practices to test CVRP algorithms: how to determine computing time (typically on a single thread), common ways of tuning parameters, and providing best and average solutions on a specified number of executions, among others.*

- TODO: "A concise guide to existing and emerging vehicle routing problem variants" [VLM20] (2020)

## **Research areas**

Related research:

- „A Parallel Hybrid Genetic Search for the Capacitated VRP with Pickup and Delivery“ (2023)
- „Effective Parallelization of the Vehicle Routing Problem“ (2023)
- "A hybrid genetic search based approach for the generalized vehicle routing problem" [Lat25] (2025)

## Šaltiniai

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