# Notes/Questions (To Be Deleted) I

- Still unsure how to tie in PrimeKG paper
- Methods for edge selection/identification? Some instances we only want to preserve structure, but sometimes we want to predict/fit edges, how does that fit into message-passing/GCN methods or other extensions?
- Diffpool article as extension of general GNN, hierarchical pooling over global readout functions? https://papers.nips.cc/paper\_files/paper/2018/file/

```
e77dbaf6759253c7c6d0efc5690369c7-Paper.pdf
```

### **Graphical Neural Networks**

Dominic DiSanto

Department of Biostatistics, Harvard University

December 5, 2023

### Outline

- Set-Up and Motivation 5ish minutes
- Quantification General Construction 10-20ish minutes
- Applications and Extensions 20-25ish minutes
  - Multimodal Graph Learning (MGL)
  - Knowledge-Graph Data

Dominic DiSanto

- Structure-Based Drug Design (SBDD)
- Structure-Induced Pre-Training



### Goals

- Provide a useful overview of Graphical Neural Networks (GNN)
  - Motivation for necessity of GNN's
  - Provide a general framework of fitting
- Describe applications and extensions of the general GNN model
  - Multimodal Physiological/Biomedical Data
  - Integration of Knowledge-Graph and EHR Data



# **KG** Application

Image here. Or maybe drop, 4 might be overkill





### Multi-modal Biomedical Data

Multimodal knowledge graph of 17,080 disease phenotypes

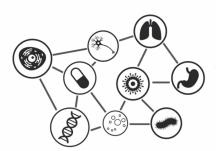
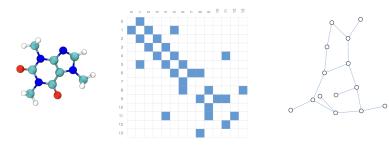


Image courtesy of partial figure from McDermott et al. *Structure-inducing* pre-training [11]

Downloadable Slides

# Molecular/Biochemical



(Left) 3d representation of the Caffeine molecule (Center) Adjacency matrix of the bonds in the molecule (Right) Graph representation of the molecule.

Image courtesy of https://distill.pub/2021/gnn-intro/ [12]

Downloadable Slide

## Protein Representation

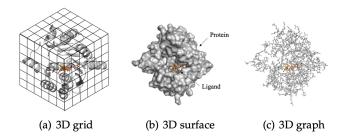


Fig. 2. 3D representations of proteins used for geometric deep learning: (a) 3D grid, (b) 3D surface, and (c) 3D graph, illustrated for PDB ID 2avd.

Fig 2. of Zhang (2023) Geometric Deep Learning for Structure-Based Drug Design: A Survey [17]

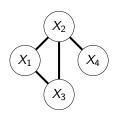
### Motivation

- Want to utilize the input structure of the graph
  - Respect/Maintain
  - Update/Estimate
- "Flattening" graphical data for DNN, CNN, etc. omits useful topology from our data
- Early methods attempting to retain topological info included recursive neural networks and random walk models, which GNN methodology extended [14]

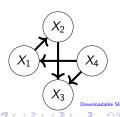
## Notation/Set-Up

- Consider the graph  $\mathcal{G} = (V, E), E \subseteq V \times V$ , where any node v has a related "feature vector"  $x_v \in \mathbb{R}^d$ 
  - Let N = |V|
- Let  $\mathcal{N}_s(v)$  represent the s-hop neighborhood of any node v (and implicitly  $\mathcal{N}(v) \equiv \mathcal{N}_1(v)$ )
- Can construct adjacency matrix  $\mathbf{A} \in \mathbb{R}^{N \times N}$  to capture structure of edge set E
  - $\mathbf{A}_{ij} = w_{ij} \mathbb{1}\{(i,j) \in E\}$  for scalar weight  $w_{ii} \in \mathbb{R}$

Undirected Graph



Directed Graph



# Topology Representations

- Simplest/Naïve method is to use A
- Consider also the Laplacian matrix  $\mathbf{L} = \mathbf{D} \mathbf{A}$ 
  - $D = diag(A1_N)$
- Can use an eigenvalue-normalized Laplacian

$$\widetilde{\mathbf{L}} = \mathbf{I} - \mathbf{D}^{-1/2} \mathbf{A} \mathbf{D}^{-1/2} = \mathbf{D}^{-1/2} \mathbf{L} \mathbf{D}^{-1/2}$$

 Note that a given graph topology is represented equivalently by any permutation of its A

### Outline

- Set-Up and Motivation 5ish minutes
- Quantification 20 General Construction 10-20ish minutes
- 3 Applications and Extensions 20-25ish minutes
  - Multimodal Graph Learning (MGL)
  - Knowledge-Graph Data
  - Structure-Based Drug Design (SBDD)
  - Structure-Induced Pre-Training

### What do we estimate about graph structure?

GNN learning can be 
$$\begin{cases} \mathsf{Node\text{-}wise}\ \Phi(\mathcal{G},v) : (v\in V) \to \mathbb{R}^m \\ \\ \mathsf{Edge\text{-}wise}\ \Phi(\mathcal{G},e) : (e\in E) \to \mathbb{R}^m \end{cases}$$
 Graph-level characteristics  $\Phi(\mathcal{G})$ 

## What do we estimate about graph structure?

### General Framework<sup>1</sup>

We begin with the general Message Passing Neural Networks (MPNN) structure of a GNN:

```
1: Initialize h^{(0)} \leftarrow x_v, \forall v \in V
2: for \kappa = 0, ..., K do:
3.
             for v \in \mathcal{G} do:
                   m_{u}^{(\kappa+1)} \leftarrow \mathsf{Message}(h_{v}^{(\kappa)}, h_{u}^{(\kappa)}, e_{vu}), \forall u \in \mathcal{N}_{v}
4:
                  h_{\mathsf{agg}}^{(\kappa+1)} \leftarrow \mathsf{Aggregate}(\{m_u^{(\kappa)} \mid u \in \mathcal{N}_v\})
    h^{(\kappa+1)} \leftarrow \mathsf{Update}(h^{(\kappa)}, h^{(\kappa)}_{\mathsf{agg}})
7: \hat{\mathbf{v}} \leftarrow \mathsf{Transform}(\{h_{v}^{K}|v \in \mathcal{G}\})
                                                                    or Readout(\cdot)
```

### General Framework

Can succinctly represent the  $\kappa$ th layer as:

$$\textit{h}_{v}^{(\kappa+1)} = \textit{Up}\left\{\textit{h}_{v}^{(\kappa)}, \textit{Agg}\left[\textit{Msg}\left(\textit{h}_{v}^{(\kappa)}, \textit{x}_{u}^{(\kappa)}, \textit{e}_{u,v}^{(\kappa)}\right)\right]\right\}$$

Choices of (differentiable) functions for Aggregate, Update, and Readout determine the architecture of your GNN

Trained end-to-end via backpropagation for problem-specific Transform function

# Aggregate & Update

- Aggregate(·) produces a representation of information from a node's neighborhood via permutation invariant function
- Can include weights (edge-wise or learned)
- Over later iterations, this includes information from further and further distant nodes to any one target node
- We then **Update**(·) our current state using this aggregated neighborhood-level information

# Transform/Readout

- Transform(·) translates our learned node representations to some desired outcome
  - Regression
  - Binary/Multi-class classification
  - MLP/DNN's
  - Readout(·) is common term for translating node-level output to graph-level
  - Global Pooling Methods applied over entire graph (e.g. averaging, fitting "regular" deep neural network, etc.)

## Graph Convolutional Network

 Proposed in 2017 by Thomas Kipf, Max Welling [10], can consider one example of "Laplacian-based methods" [6]

$$\mathbf{H}^{(\kappa+1)} = \mathsf{ReLu}\left(\widetilde{\mathbf{D}}^{-1/2}\widetilde{\mathbf{A}}\widetilde{\mathbf{D}}^{-1/2}\mathbf{H}^{(\kappa)}\mathbf{\Theta}\right)$$

- Motivated by considering the graph convolution  $x \star g = UgU^Tx$  as the message passing function
- Learned weight/parameter matrix Θ



## Graph Convolutional Network

Intuitive "derivation":

$$\begin{split} \mathbf{H}^{(\kappa+1)} &= \sigma \left( \mathbf{A} \mathbf{H}^{(\kappa)} \Theta \right) \\ \mathbf{H}^{(\kappa+1)} &= \sigma \left( \mathbf{D}^{-1} \mathbf{A} \mathbf{H}^{(\kappa)} \Theta \right) \qquad \text{Normalizing by degree} \\ \mathbf{H}^{(\kappa+1)} &= \sigma \left( \mathbf{D}^{-1/2} \mathbf{A} \mathbf{D}^{-1/2} \mathbf{H}^{(\kappa)} \Theta \right) \qquad \text{Symmetric normalization} \\ \mathbf{H}^{(\kappa+1)} &= \sigma \left( \widetilde{\mathbf{D}}^{-1/2} \widetilde{\mathbf{A}} \widetilde{\mathbf{D}}^{-1/2} \mathbf{H}^{(\kappa)} \Theta \right) \qquad \text{Adding self-loop} \end{split}$$

where  $\mathbf{A} = \mathbf{A} + \mathbf{I}$ ,  $\mathbf{D}_{ii} = \sum_{i} \mathbf{A}_{ij}$ ,  $\sigma$  is any activation function,  $\mathbf{H}$  is simply the matrix of  $\mathbf{h}_{\nu}$  for all nodes

## **Graph Convolutional Network**

 Proposed in 2017 by Thomas Kipf, Max Welling [10], can consider one example of "Laplacian-based methods" [6]

$$\mathbf{H}^{(\kappa+1)} = \underbrace{\underbrace{\mathsf{ReLu}}_{\mathsf{Update}} \underbrace{\left(\widetilde{\mathbf{D}}^{-1/2} \widetilde{\mathbf{A}} \widetilde{\mathbf{D}}^{-1/2} \mathbf{H}^{(\kappa)} \mathbf{\Theta}\right)}_{\mathsf{Aggregate}/\mathsf{Message}}$$

- Motivated by considering the graph convolution  $x \star g = UgU^Tx$  as the message passing function
- Learned weight/parameter matrix Θ

# General Framework (Revisited)

#### Input

- Node conceptualization
- Node embeddings

#### Architecture

- Message Passing Neural Network (MPNN)
- $\mathbf{H}^{(\kappa+1)} = \mathsf{ReLu}\left(\widetilde{\mathbf{D}}^{-1/2}\widetilde{\mathbf{A}}\widetilde{\mathbf{D}}^{-1/2}\mathbf{H}^{(\kappa)}\mathbf{\Theta}\right)$

### Output

- Target output (Readout, Transform functions)
- Loss function

### Outline

- Set-Up and Motivation 5ish minutes
- Quantification 20 General Construction 10-20ish minutes
- 3 Applications and Extensions 20-25ish minutes
  - Multimodal Graph Learning (MGL)
  - Knowledge-Graph Data
  - Structure-Based Drug Design (SBDD)
  - Structure-Induced Pre-Training

# Multimodal Graph Learning (MGL)

# Multimodal Graph Learning (MGL)

- Ektefaie (2023) Multimodal learning with graphs [3]
- Cite 14-16 in multimodal paper for multi improvement over uni VAE
- Topology is complicated by multimodality of input data
  - Modal collapse [9]
  - Differential data availability
  - Can mention Kipf algorithm does well in semi-supervised setting (even with limited labels available within a given "cluster"), so if we have some gold standard data (biomarker/strong proxy, etc.) that is difficult to obtain, can be VERY useful to include for MGL and lead to good performance, no bullet point here just mention

Downloadable Slides



December 5, 2023

### Mutimodal

#### Clinical Data

- Clinical text
- -omics data
- Laboratory measurements
- Clinical imaging

#### Protein Structures

- 1° AA Sequence
- 2° Helix interactions
- 3° Folding, bridges



### Framework

Authors propose a four component "blueprint"

- Identifying entitites (i.e. modalities)
- Uncovering topology
  - A priori
  - Adaptively learned
- Propagating information
- Mixing representation



### Framework

Authors propose a four component "blueprint"

- Identifying entitites (i.e. modalities) Structure Learning Uncovering topology
- Propagating information
- Mixing representation

### Structure Learning

- Consider patients as nodes
- Consider modalities as entities (colored nodes)
  - Clinical text/narrative data
  - Laboratory/Physiological measurements
  - Image/Video data
  - Patient reported measurements/symptoms
  - etc.

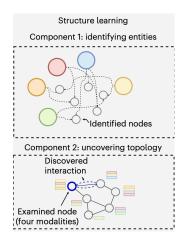
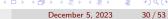


Figure: Subset of Fig 2c [3]

Downloadable Slides

December 5, 2023

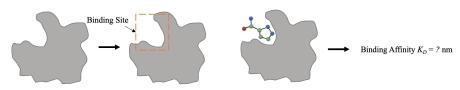
# Learning on Structure



# Proteins and Structure-Based Drug Design (SBDD)

# Structure-Based Drug Design (SBDD)

- Zhang (2023) Geometric Deep Learning for Structure-Based Drug Design: A Survey [17]
- SBDD aims to improve drug-discovery by understanding 3D protein structures and predicting drug efficacy/behavior
- Problems of note for GNN's include binding site prediction and binding affinity prediction



Images from Fig. 1 of Zhang (2023) [17]

### Output

- Binding site prediction is binary categorization at the (surface) amino acid level
- Binding affinity prediction is a continuous measure of protein-ligand interaction strength
- Protein Databank (PDB), PDBBind, Dockground, CSAR-HiQ are existing data sets used to train most GNN's in these contexts
- Other characteristics are important for drug design and protein-ligand interactions but without current GNN methods to my knowledge
  - Binding pose
  - Ligand generation
  - Linker design

### Input

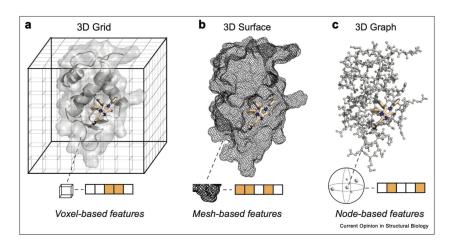
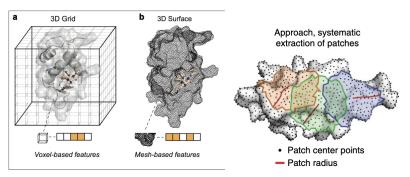


Figure from Isert (2023) [8]

### CNN Input

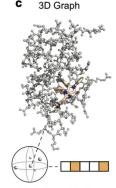
 Nodes and edges defined by radial patches about a discretization of the protein surface



Left: Fig 2(ab) from Isert (2023); Right: Fig 1a. Gainza (2020) [8, 5]

## **GNN** Input

- Nodes v include 3-dimensional coordinate data
  - Atomic structure in Euclidean space
  - Amino acid (also "residue") structure
- Maintain invariance for translations, rotations but not necessarily reflections



Node-based features

Current Opinion in Structural Biology

Figure: Figure 1c from Isert (2023) [8]

### Architecture

Consider some transformations T, T' (e.g. reflection, rotation, etc.) within the same symmetry group:

Invariance: 
$$f(T(x)) = T'(f(x)) = f(x)$$

Equivariance: 
$$\forall T, \exists T' : f(T(x)) = T'(f(x))$$

## Architecture(s)

Forgoing the iteration supercripts, one message pass can be represented as such:

$$\begin{aligned} & m_{ij} = \textit{Msg}_{m}(\mathbf{v_{i}}, \mathbf{v_{j}}, h_{i}, h_{j}, e_{ij}) \\ & \mathbf{m}_{ij} = \textit{Msg}_{m}(\mathbf{v_{i}}, \mathbf{v_{j}}, h_{i}, h_{j}, e_{ij}) \\ & h'_{i} = \textit{Update}_{h} \left[ h_{i}, \textit{Agg}_{h}(\{m_{ij}\}_{j \in \mathcal{N}(v_{i})}) \right] \\ & \mathbf{v_{i}'} = \textit{Update}_{\mathbf{v}} \left[ \mathbf{v}_{i}, \textit{Agg}_{\mathbf{v}} \left( \{\mathbf{m}_{ij}\}_{j \in \mathcal{N}(v_{i})} \right) \right] \end{aligned}$$

where  $Msg_m$ ,  $Update_h$  are geometrically **invariant**, scalar functions and  $Msg_m$ ,  $Update_v$  are geometrically **equivariant**, vector functions Here  $\mathbf{v} \in \mathbb{R}^3$  are 3-D coordinates (e.g. atom or amino acid location) EDIT Clarify invariate/equivariant to what transformations



## Architecture(s)

May also consider the proposed Equivariant Graphical Neural Network (EGNN) from Satorras (2021) [13]. Again, let  $\mathbf{v}_i$  represent a node's coordinate embeddings:

$$m_{ij} = Msg_m(h_i, h_j, ||\mathbf{v}_i^{(\kappa)} - \mathbf{v}_j^{(\kappa)}||^2, e_{ij})$$
 $\mathbf{v}_i^{(\kappa+1)} = \mathbf{v}_i^{(\kappa)} + C \sum_{j \neq 1} \left(\mathbf{v}_i^{(\kappa)} - \mathbf{v}_i^{(\kappa)}\right) \phi_v(m_{ij})$ 
 $m_i = Agg(m_{ij}) = \sum_{j \neq i} m_{ij}$ 
 $h^{(\kappa+1)} = Update(h^{(\kappa+1)}, m_i)$ 

### NodeCoder

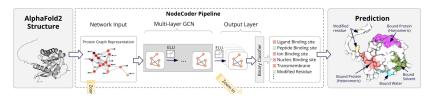


Figure: Subst of Fig. 1 from Abdollahi (2023) NodeCoder [1]

With a given layer updated using a slight adaptation:

$$\begin{split} \mathbf{H}^{(\kappa+1)} &= \mathsf{ELu}\left(\widetilde{\mathbf{D}}^{-1/2}\widetilde{\mathbf{A}}\widetilde{\mathbf{D}}^{-1/2}\mathbf{H}^{(\kappa)}\mathbf{\Theta}\right) \\ \mathbf{H}^{(K)} &= \mathit{LogSoftMax}\left\{\widetilde{\mathbf{D}}^{-1/2}\widetilde{\mathbf{A}}\widetilde{\mathbf{D}}^{-1/2}\mathsf{ELu}\left(\widetilde{\mathbf{D}}^{-1/2}\widetilde{\mathbf{A}}\widetilde{\mathbf{D}}^{-1/2}\mathbf{H}^{(\kappa)}\mathbf{\Theta}\right)\mathbf{\Theta}_{t}\right\} \end{split}$$

Downloadable Slides

Dominic DiSanto

## EquiPocket

Time pending add https://arxiv.org/pdf/2302.12177.pdf

## **Conclusion**





### References I

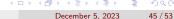
- Some diagrams generated in conjunction with ChatGPT 3.5
- [1]Nasim Abdollahi et al. NodeCoder: a graph-based machine learning platform to predict active sites of modeled protein structures. arXiv:2302.03590 [g-bio]. Feb. 2023.
- [2] David Duvenaud et al. Convolutional Networks on Graphs for Learning Molecular Fingerprints. arXiv:1509.09292 [cs, stat]. Nov. 2015.
- [3] Yasha Ektefaie et al. "Multimodal learning with graphs". en. In: Nature Machine Intelligence 5.4 (Apr. 2023). Number: 4 Publisher: Nature Publishing Group, pp. 340–350.
- [4] Oleksandr Ferludin et al. TF-GNN: Graph Neural Networks in TensorFlow. arXiv:2207.03522 [physics, stat]. July 2023.

### References II

- [5] P. Gainza et al. "Deciphering interaction fingerprints from protein molecular surfaces using geometric deep learning". en. In: Nature Methods 17.2 (Feb. 2020). Number: 2 Publisher: Nature Publishing Group, pp. 184–192.
- [6] Justin Gilmer et al. Neural Message Passing for Quantum Chemistry. arXiv:1704.01212 [cs]. June 2017.
- [7] M. Gori, G. Monfardini, and F. Scarselli. "A new model for learning in graph domains". In: Proceedings. 2005 IEEE International Joint Conference on Neural Networks, 2005. Vol. 2. ISSN: 2161-4407. July 2005. 729-734 vol. 2.
- [8] Clemens Isert, Kenneth Atz, and Gisbert Schneider. "Structure-based drug design with geometric deep learning". en. In: Current Opinion in Structural Biology 79 (Apr. 2023), p. 102548.

### References III

- [9] Adrián Javaloy, Maryam Meghdadi, and Isabel Valera. Mitigating Modality Collapse in Multimodal VAEs via Impartial Optimization. en. arXiv:2206.04496 [cs]. June 2022.
- Thomas N. Kipf and Max Welling. Semi-Supervised Classification [10]with Graph Convolutional Networks. arXiv:1609.02907 [cs, stat]. Feb. 2017.
- Matthew B. A. McDermott et al. "Structure-inducing pre-training". [11]en. In: Nature Machine Intelligence 5.6 (June 2023). Number: 6 Publisher: Nature Publishing Group, pp. 612–621.
- |12| Benjamin Sanchez-Lengeling et al. "A Gentle Introduction to Graph Neural Networks". en. In: Distill 6.9 (Sept. 2021), e33.



### References IV

- [13]Victor Garcia Satorras, Emiel Hoogeboom, and Max Welling. E(n)Equivariant Graph Neural Networks. arXiv:2102.09844 [cs, stat]. Feb. 2022.
- F. Scarselli et al. "The Graph Neural Network Model". en. In: IEEE [14] Transactions on Neural Networks 20.1 (Jan. 2009), pp. 61–80.
- [15] Keyulu Xu et al. How Powerful are Graph Neural Networks? arXiv:1810.00826 [cs, stat]. Feb. 2019.
- [16] Zhitao Ying et al. "Hierarchical Graph Representation Learning with Differentiable Pooling". In: Advances in Neural Information Processing Systems. Vol. 31. Curran Associates, Inc., 2018.
- Zaixi Zhang et al. A Systematic Survey in Geometric Deep Learning [17] for Structure-based Drug Design. arXiv:2306.11768 [cs, q-bio]. Oct. 2023.

## **Appendix Slides**



## **Implementations**

- PyTorch Geometric with directed extension PyTorch Geometric Signed Directed
- TensorFlow GNN [4]
- GraphNeuralNetworks.jl
- Spektral, Keras-based Pythhon package
- Limited but some implementation in R
  - scapGNN, package GNN implementation but specific/narrow for single-cell -omics data



## Abbreviated History

- Graph Neural Network first(?) coined in Gori (2005) [7] and subgenently in Scarselli (2009) The Graph Neural Network Model [14]
- Graph Convolutional Network by Kipf (2017) [10] but with similar convolutional message-passing algorithms (within GNN's) proposed in at least 2015 [2]
- Message passing GNN proposed in Gilmer (2017), applications in molecular chemistry [6]



## Additional Applications, Interesting Papers I

- Applications in travel time prediction, 2021 (https://arxiv.org/pdf/2108.11482.pdf)
- Someone has compiled graph-/GNN-relevant talks for NeurIPS 2023 at https:

```
//github.com/XiaoxinHe/neurips2023_learning_on_graphs
```



### **DiffPool**

# Figure 1 from Ying (2018) Hierarchical Graph Representation Learning with Differentiable Pooling [16]

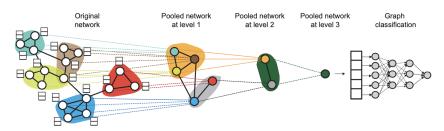


Figure 1: High-level illustration of our proposed method DIFFPOOL. At each hierarchical layer, we run a GNN model to obtain embeddings of nodes. We then use these learned embeddings to cluster nodes together and run another GNN layer on this coarsened graph. This whole process is repeated for L layers and we use the final output representation to classify the graph.

Downloadable Slides

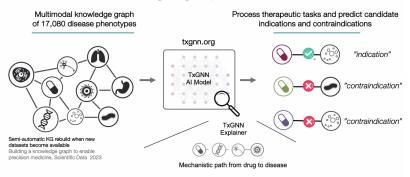
51 / 53

Graphical Neural Networks December 5, 2023

### KG AI Models

Full figure from McDermott et al. [11], cropped and presented in Introduction:

## Knowledge graph AI models



Structure-inducing pre-training, Nature Machine Intelligence 2023; Multimodal learning with graphs, Nature Machine Intelligence 2023; Zero-shot prediction of therapeutic use with geometric deep learning and clinician centered design, medRxiv, 2023

4 □ ▶ 4 □ ▶ 4 □ ▶ 4 □ ▶ 3 □ ✓ Q ○



### Protein Data Bank File

```
HEADER
         EXTRACELLULAR MATRIX
                                                 22-JAN-98
                                                             1A3I
TITLE
         X-RAY CRYSTALLOGRAPHIC DETERMINATION OF A COLLAGEN-LIKE
TITLE
         2 PEPTIDE WITH THE REPEATING SEQUENCE (PRO-PRO-GLY)
. . .
EXPDTA
        X-RAY DIFFRACTION
AUTHOR
        R.Z.KRAMER.L.VITAGLIANO, J.BELLA, R.BERISIO, L.MAZZARELLA,
AUTHOR
         2 B.BRODSKY.A.ZAGARI.H.M.BERMAN
REMARK 350 BIOMOLECULE: 1
REMARK 350 APPLY THE FOLLOWING TO CHAINS: A. B. C
REMARK 350
            BIOMT1
                     1 1.000000
                                  0.000000 0.000000
                                                            0.00000
REMARK 350
            BIOMT2
                     1 0.000000 1.000000 0.000000
                                                            0.00000
. . .
SEORES.
        1 A
                9 PRO PRO GLY PRO PRO GLY PRO PRO GLY
SEORES.
        1 B
               6 PRO PRO GLY PRO PRO GLY
SEORES.
        1 C
               6 PRO PRO GLY PRO PRO GLY
. . .
ATOM
                PRO A
                                      21,206 21,530 1,00 17,44
         1 N
                                8.316
                                                                            N
         2 CA
                PRO A
                                       20.729
                                               20.336 1.00 17.44
ATOM
                                7.608
ATOM
         3 C
                PRO A
                                8.487
                                       20.707 19.092 1.00 17.44
ATOM
         4
            0
                PRO A
                        1
                                9.466
                                       21.457 19.005
                                                      1.00 17.44
ATOM
          5 CB
                PRO A
                        1
                                6.460
                                       21.723
                                               20.211
                                                      1.00 22.26
HETATM
       130 C
                ACY
                                      22.541 11.236 1.00 21.19
                                                                            C
                      401
                                3.682
HETATM
       131 0
                ACY
                      401
                                2.807
                                       23.097 10.553 1.00 21.19
                                                                            0
HETATM 132 OXT ACY
                                4.306 23.101 12.291 1.00 21.19
                      401
. . .
```